Instrumental Variables

Introduction

MIXTAPE SESSIONS

Roadmap

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Groos Family Assistant Professor of Economics, Brown University

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- Quasi-experimental evaluations of healthcare quality

  (Hull 2020; Abaluck et al. 2021, 2022)

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A constant student of IV (and econometrics more generally)

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- I will be live-coding in Stata, but R code will also be available
- Goal: demonstrate both methods & how I think about applying them

Schedule

9:00-10:00am	Lecture 1: Regression Review; Regression Endogeneity; Introduction to IV
10:00-10:10am	*Break*
10:10-11:10am	Lecture 2: Understanding Instrument Validity; 2SLS Mechanics; Applications
11:10-11:15am	*Break*
11:15am-12:30pm	Coding Lab 1: Angrist and Krueger (1991)
12:30-1:30pm	*Lunch*
1:30-2:30pm	Lecture 3: Heterogeneous Treatment Effects; Characterizing Compliers; MTEs
2:30-2:40pm	*Break*
2:40pm-3:40pm	Lecture 4: Judge Leniency Designs; Shift-Share IV; New IV Frontiers
3:40-3:45pm	*Break*
3:45-5:00pm	Coding Lab 2: Stevenson (2018)
5:00-5:15pm	Closing Remarks

Roadmap

Models vs. Estimands vs. Estimators

Three distinct objects (though not always clearly distinguished)

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- Parameters come from models of how observed data are generated
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- **Estimators** are functions of the observed data itself (the "sample")

  - $\rightarrow$ E.g. a difference in sample means or ratio of OLS coefficients
  - $\rightarrow$ Since data are random, so are estimators. Each has a distribution
  - $\rightarrow$ Use knowledge of estimator distributions to make learn about estimands ("inference") and—hopefully—identified parameters

The IV Solution
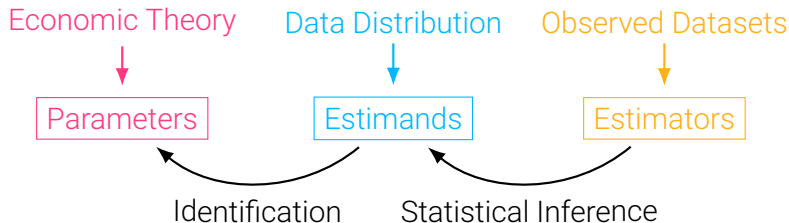
This course will mostly focus on identification, but we'll cover some IV estimation / inference issues as well

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- Parameter: returns to taking this class β, measured in some outcome Y_i (e.g. lifetime top-5 pubs / earnings / twitter followers)
- Simple causal/structural model: $Y_i = \alpha + \beta D_i + \varepsilon_i$, where $D_i \in \{0, 1\}$ indicates taking this class

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We see a sample of Y_i, D_i, and some other covariates $W_{1i}, \dots, W_{Ki}$

- We fire up Stata and type `reg y d w1-wk, r`. How do we interpret the output?

Population Regression

The OLS *estimator* $\widehat{\beta}^{OLS}$ consistently estimates the regression *estimand* β^{OLS} under relatively weak conditions (e.g. *i.i.d.* data)

- Stata tells us $\widehat{\beta}^{OLS}$ and what we can infer about β^{OLS} from it
- It *doesn't* directly tell us about the relationship between β^{OLS} and β

Population Regression

The population regression of Y_i on $\mathbf{X}_i = [1, D_i, W_{1i}, \ldots, W_{Ki}]'$ is given by $Y_i = \mathbf{X}_i' \beta^{OLS} + U_i$ where $E[\mathbf{X}_i U_i] = 0$

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- Equivalently, $\beta^{OLS} = E[\mathbf{X}_i \mathbf{X}_i']^{-1} E[\mathbf{X}_i Y_i]$ and $U_i = Y_i - \mathbf{X}_i'\beta^{OLS}$

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Key point: we can always define β^{OLS} for any Y_i and $\mathbf{X}_i$ (assuming no perfect collinearity); this is what Stata estimates

- Specifically it computes $\widehat{\beta}^{OLS} = (\frac{1}{N} \sum_i \mathbf{X}_i \mathbf{X}_i')^{-1} (\frac{1}{N} \sum_i \mathbf{X}_i Y_i)$ and uses large-sample asymptotics (LLN/CLT) to get a standard error

You Can't Always Get What you Want…

But what if this *estimand* is not what we want?

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- What if β^{OLS} fails to coincide with our economic parameter of interest (e.g. returns to mixtape workshops)?

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The model parameter in $Y_i = \alpha + \beta D_i + \varepsilon_i$ need not coincide with the regression coefficient in $Y_i = \alpha^{OLS} + \beta^{OLS} D_i + U_i$

- I.e. we may not have $Cov(D_i, \varepsilon_i) = 0$ (always have $Cov(D_i, U_i) = 0$)

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Selection bias (a.k.a. omitted variables bias): students with higher latent earnings potential ε_i are more likely to take this class D_i
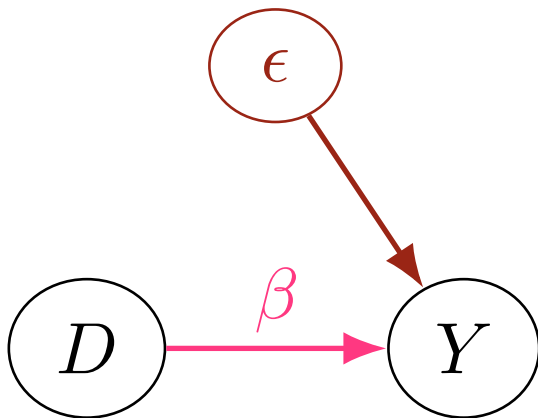
- $Cov(D_i, \varepsilon_i) > 0$ means $\beta^{OLS} > \beta$: overstate the returns-to-mixtape

Can I just Control My Way Out of This?

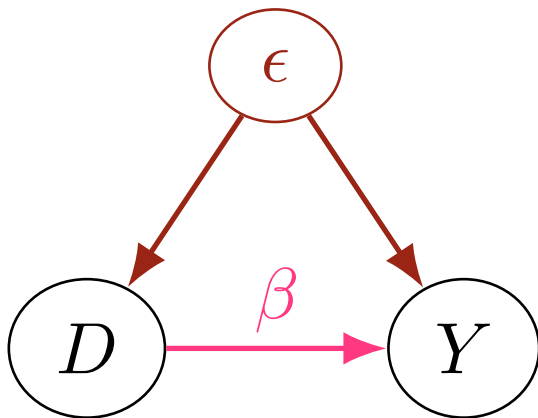Adding more controls (e.g. demographics) may or may not help

- Projecting ε_i on X_i, we get $Y_i = \alpha + \beta D_i + \gamma X_i + \tilde{\varepsilon}_i$, $Cov(X_i, \tilde{\varepsilon}_i) = 0$
- Whether or not $Cov(D_i, \tilde{\varepsilon}_i) = 0$ depends on whether X_i sufficiently accounts for the confounding relationship $Cov(D_i, \varepsilon_i) \neq 0$

Regression "Exogeneity"

Regression "Endogeneity"

...But Sometimes, You Get What you Need

Imagine this course was "oversubscribed," and admission was determined by lottery

- Among those interested in taking the course, a random sample denoted by $Z_i = 1$ was given access
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- Affects D_i, so relevant to the "treatment" of interest
- Randomly assigned, so unconfounded by selection (unlike D_i)

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Indeed, this leads us to IV estimands (and estimators)

The IV Solution
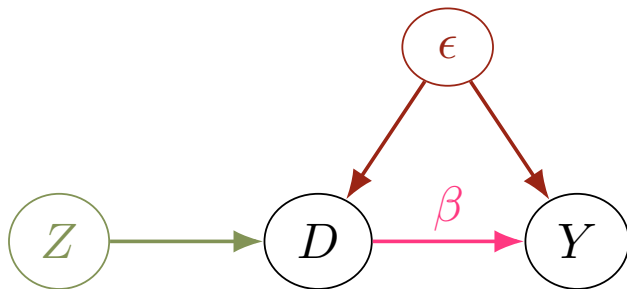
Roadmap

Instrument Validity and Relevance

Causal/structural model $Y_i = \alpha + \beta D_i + \varepsilon_i$ and a candidate IV Z_i

- Single D_i and Z_i and no further controls, for now

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- Compare to the OLS estimand: $\beta^{OLS} = \frac{Cov(D_i, Y_i)}{Var(D_i)}$

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IV estimand as the "Second Stage"

Sometimes we refer to the IV estimand as the "second stage":

$$Y_i = \alpha^{IV} + \beta^{IV} D_i + U_i$$

where now $Cov(Z_i, U_i) = 0$. Thus "IV=RF/FS" ($\beta^{IV} = \rho^{OLS}/\pi^{OLS}$)

The 2SLS Estimator

As with OLS, we estimate IV by sample analog:

$$\hat{\beta}^{IV} = \frac{\widehat{Cov}(Z_i, Y_i)}{\widehat{Cov}(Z_i, D_i)} = \frac{\hat{\rho}^{OLS}}{\hat{\pi}^{OLS}}$$

where $\widehat{Cov}(X_i, W_i) = \frac{1}{N}\sum_i X_i W_i - \left(\frac{1}{N}\sum_i X_i\right)\left(\frac{1}{N}\sum_i W_i\right)$,
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We will soon consider extensions of all of this, with controls / multiple instruments / etc

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- First stage $E[D_i \mid Z_i = 1] - E[D_i \mid Z_i = 0]$: effect of eligibility on the *probability* of military service (b/c D_i is binary)

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IV interprets the latter causal effect in terms of the former

IV Estimates of the Effects of Military Service on the Earnings of White Men born in 1950

Earnings year	Earnings		Veteran Status		Wald Estimate of Veteran Effect
	Mean	Eligibility Effect	Mean	Eligibility Effect	
	(1)	(2)	(3)	(4)	(5)
1981	16,461	-435.8 (210.5)	.267	.159 (.040)	-2,741 (1,324)
1971	3,338	-325.9 (46.6)			-2050 (293)
1969	2,299	-2.0 (34.5)			

Note: Adapted from Table 5 in Angrist and Krueger (1999) and author tabulations. Standard errors are shown in parentheses. Earnings data are from Social Security administrative records. Figures are in nominal dollars. Veteran status data are from the Survey of Program Participation. There are about 13,500 individuals in the sample.
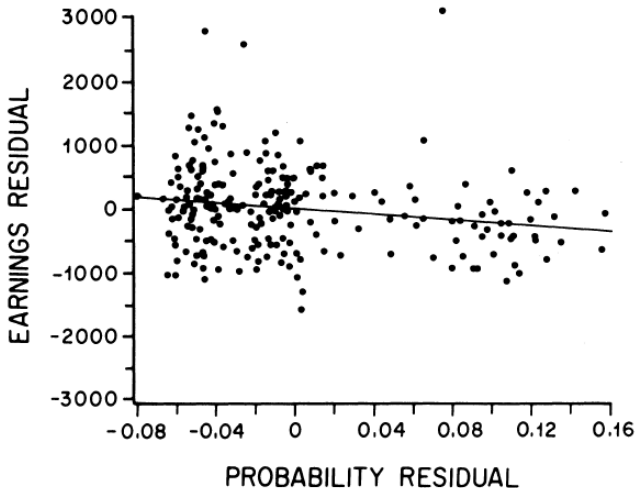
FIGURE 3. EARNINGS AND THE PROBABILITY OF VETERAN STATUS BY
LOTTERY NUMBER

Notes: The figure plots mean W-2 compensation in 1981–4 against probabilities of
veteran status by cohort and groups of five consecutive lottery numbers for white men
born 1950–3. Plotted points consist of the average residuals (over four years of
earnings) from regressions on period and cohort effects. The slope of the least-squares
regression line drawn through the points is −2,384, with a standard error of 778, and
is an estimate of α in the equation

$$\bar{y}_{ctj} = \beta_c + \delta_t + \hat{p}_{cj}\alpha + \bar{u}_{ctj}.$$