

## Array

### **Algorithm to search a particular element from a list**

1. Input: A set of data in array a, and variable x. i.e., the target element

a[1...n], x;

2. found=0

3. for (i=1; i<=n; i++)

{

    if (a[i]==x)

        location=i;

        found= 1;

        break;

}

4. Output: if (found==1)

    print"FOUND" message and location.

    else print "NOT FOUND" message

### **Algorithm to find out the summations of even and odd numbers**

1. Input: An array and variable (to store the results of summations)

A[1...n], sum\_odd=0, sum\_even=0;

2. for (i=1; i<=n; i++)

{

    if(A[i]%2==0), sum\_even=sum\_even+A[i];

    else sum\_odd=sum\_odd+A[i];

}

3. Output: Summation of odd numbers (print sum\_odd) and

Summation of even numbers (print sum\_even)

### **Algorithm to find out the summations of even and odd indexed numbers**

1. Input: An array and variable (to store the results of summations)

$A[1 \dots n]$ , sum\_odd=0, sum\_even=0;

2. for (i=1; i<=n; i++)

{

if(i%2==0), sum\_even=sum\_even+A[i];

else sum\_odd=sum\_odd+A[i];

}

3. Output: Summation of numbers in odd indices (print sum\_odd) and

Summation of numbers in even indices (print sum\_even)

### **Algorithm to insert an element into an array**

1. Input: An array  $A[1 \dots n]$ , the position of insertion m and the data x.

2. Increase the size of the array,  $A[1 \dots n+1]$

3. for (i=n; i>=m; i--)

$A[i+1]=A[i]$ ;

4.  $A[m]=x$ ;

5. Output: The array, A with size n+1

### **Algorithm to delete an element from an array**

1. Input: An array  $A[1 \dots n]$ , the position of deletion m.

2. for (i=m; i<n; i++)

$A[i]=A[i+1]$ ;

3. Output: The updated array, A

## Two Dimensional Array

### Definition

Two dimensional array is an array that has two dimensions, such as row and column. Total number of elements in a two dimensional array can be calculated by multiplication of the numbers of rows and the number of columns. If there are m rows and n columns then the total number of elements is mxn, and mxn is called the size of the array. Of course, the data elements of the array will be same type.

In mathematics, the two dimensional array can be expressed as follows:

$A_{ij}$  or  $A[I,j]$  for  $1 \leq i \leq m$  and  $1 \leq j \leq n$  (where m and n are the number of rows and columns respectively)

$$\begin{array}{c} A[1 \dots m, 1 \dots n] \\ \begin{array}{cc} \longleftrightarrow & \longleftrightarrow \\ \text{m rows} & \text{n columns} \end{array} \end{array}$$

Fig 1: Symbolic representation of two dimensional array

Array B		1	2	3	4	5	6	7	
	1	0	10	12	13	19	20	18	Size=6x7
	2	23	5	63	72	79	80	65	
	3	-	-	-	-	-	-	-	Cell B[5][5]
	4	-	-	-	-	-	-	-	
	5	-	-	-	-	75	-	-	
	6	20	31	32	33	39	40	33	

Fig 2: Graphical representation of two dimensional array

### Store and retrieve values in and from array

```
for(i=0; i<2; i++) {  
    for(j=0; j<3; j++)  
        scanf("%d", &B[i][j]);  
}  
  
for(i=0; i<2; i++) {  
    for(j=0; j<3; j++)  
        printf("%d ", B[i][j]);  
}
```

## Two dimensional array representation in memory

The elements of a two dimensional array are stored in computers memory row by row or column by column. If the array is stored as row by row, it is called row-major order and if the array is stored as column by column, it is called column-major order.

In row-major order, elements of a two dimensional array are stored as-

$[A_{11}, A_{12}, A_{13}, A_{14}, A_{15}, A_{16}], [A_{21}, A_{22}, A_{23}, A_{24}, A_{25}, A_{26}], \dots, [A_{51}, A_{52}, \dots, A_{56}]$

←
→

←
→

←
→

row 1                      row 2                      row 5

And in column-major order, elements are ordered as-

$[A_{11}, A_{21}, A_{31}, A_{41}, A_{51}, A_{61}], [A_{12}, A_{22}, A_{32}, A_{42}, A_{52}, A_{62}], \dots, [A_{16}, A_{26}, \dots, A_{56}]$

←
→

←
→

←
→

column 1                      column 2                      column 6

	1 <sup>st</sup>	2 <sup>nd</sup>	3 <sup>rd</sup>	4 <sup>th</sup>	5 <sup>th</sup>	6 <sup>th</sup>	
	A <sub>11</sub>	A <sub>12</sub>	A <sub>13</sub>	A <sub>14</sub>	A <sub>15</sub>	A <sub>16</sub>	
7 <sup>th</sup>	A <sub>21</sub>	A <sub>22</sub>	A <sub>23</sub>	A <sub>24</sub>	A <sub>25</sub>	A <sub>26</sub>	
13 <sup>th</sup>							
						A <sub>46</sub>	24 <sup>th</sup>
25 <sup>th</sup>	A <sub>51</sub>	A <sub>52</sub>	A <sub>53</sub>	A <sub>54</sub>	A <sub>55</sub>	A <sub>56</sub>	
	26 <sup>th</sup>	27 <sup>th</sup>	28 <sup>th</sup>	29 <sup>th</sup>	30 <sup>th</sup>		

(a) Row-major order

	1 <sup>st</sup>	6 <sup>th</sup>	11 <sup>th</sup>				
	A <sub>11</sub>	A <sub>12</sub>	A <sub>13</sub>	-	-	A <sub>16</sub>	26 <sup>th</sup>
2 <sup>nd</sup>	A <sub>21</sub>	A <sub>22</sub>	-	-	-	A <sub>26</sub>	27 <sup>th</sup>
3 <sup>rd</sup>	A <sub>31</sub>	A <sub>32</sub>	-	-	-	A <sub>36</sub>	28 <sup>th</sup>
4 <sup>th</sup>	A <sub>41</sub>	A <sub>42</sub>	-	-		A <sub>46</sub>	29 <sup>th</sup>
5 <sup>th</sup>	A <sub>51</sub>	A <sub>52</sub>	-	-	A <sub>55</sub>	A <sub>56</sub>	30 <sup>th</sup>
					25 <sup>th</sup>		

(b) Column-major order

Fig. 3: Pictorial view of two dimensional array representation in memory.

## Location of an element of a two-dimensional array

### Row-major Order

If LOC(A[i,j]) denotes the location in the memory of the element A[i,j] or A<sub>ij</sub>, the in row-major order-

$$\text{LOC}(A[i,j]) = \text{Base}(A) + (n(i-1) + (j-1)) * w;$$

Here Base(A) is the starting or base address of the array A, n is the number of columns and w is the width of the cell, i.e., number bytes per cell.

### *Column-major Order*

In column-major order,

$$\text{LOC}(A[i,j]) = \text{Base}(A) + (m(j-1) + (i-1)) * w;$$

Here  $\text{Base}(A)$  is the starting or base address of the array  $A$ ,  $m$  is the number of rows and  $w$  is the cell width.

### *Example*

Base address,  $\text{Base}(A) = 100$ , Size of the array  $= 5 \times 6$ . If the type of array is integer then find out  $\text{LOC}(A[4,3])$ .

### *Solution:*

If the array is stored in row-major order:

$$\begin{aligned}\text{LOC}(A[4,3]) &= \text{Base}(A) + (n(i-1) + (j-1)) * 2 && \text{(2 bytes for each integer cell in C/C++)} \\ &= 100 + (6(4-1) + (3-1)) * 2 \\ &= 100 + (6 \times 3 + 2) * 2 \\ &= 100 + (18 + 2) * 2 \\ &= 100 + (20) * 2 \\ &= 100 + 40 \\ &= 140\end{aligned}$$

If the array is stored in column-major order:

$$\begin{aligned}\text{LOC}(A[4,3]) &= \text{Base}(A) + (m(j-1) + (i-1)) * 2 \\ &= 100 + (5(3-1) + (4-1)) * 2 \\ &= 100 + (5 \times 2 + 3) * 2 \\ &= 100 + (10 + 3) * 2 \\ &= 100 + (13) * 2 \\ &= 100 + 26 \\ &= 126\end{aligned}$$

### **Algorithm to find out the summation of boundary elements**

1. Input: a two-dimensional array

$A[1 \dots m, 1 \dots n]$

Sum=0;

2. Find each boundary element

for( $i = 1$ ;  $i \leq m$ ;  $i++$ )

for( $j = 1$ ;  $j \leq n$ ;  $j++$ )

if( $i = 1 \parallel j = 1 \parallel i = m \parallel j = n$ ), sum=sum+A[i,j],

3. Output: Print sum as the result of summation of boundary elements

### **Algorithm to find out the summation of diagonal elements**

1. Input: a two-dimensional array

$B[1 \dots n, 1 \dots n]$

Sum=0;

2. Find each diagonal element and add them with sum

for( $i = 1$ ;  $i \leq n$ ;  $i++$ )

for( $j = 1$ ;  $j \leq n$ ;  $j++$ )

if( $i = j \parallel i+j = n+1$ ), sum=sum+B[i,j],

3. Output: Print sum as the result of summation of diagonal elements