

## Assignment 1 – Chapter 1.1 – Chapter 2.2

### Q1 (Chapter 1.1)

- a. There have 2 programs offered in Faculty of Computing, UTM. In this semester only 90 students out of total 150 from program 1 take discrete structure (DS) and software engineering (SE) subjects. While there have half of total 100 students from program 2 take discrete structure and programming technique 1 (PT1). All of the students from program 1 must take at least one of the subjects offered as stated either DS or SE while all of the students from program 2 must take at least one of the subjects offered as stated either DS or PT1.
- Draw a Venn diagram to represent to above use case. (2 marks)
  - How many students in total that take DS? (2 marks)
  - How many students have exactly took two subjects? (2 marks)
  - How many students took less than 2 subjects? (2 marks)
- b. Suppose,  $A = \{n \in N | n \text{ odd}, 1 < n < 20\}$ , where  $N = \{\text{natural number}\}$   
 $B = \{n \in N | n \text{ is prime}, 1 < n < 20\}$ ,  $C = \{n \in N | n \text{ divisible by } 5, 1 < n < 10\}$
- Find  $|A|$ ,  $|B|$  and  $|C|$ , (3 marks)
  - Find the number of proper subsets of A. (3 marks)
  - Find  $C \times B$  (2 marks)

### Q2 (Chapter 1.2)

- a. Formulate the symbolic expression in words using  
m : You play table tennis.  
n : You miss the midterm test.  
o : You pass the subject.
- $m \wedge n$  (2 marks)
  - $\neg(m \vee n) \vee o$  (2 marks)
- b. Show that  $(a \rightarrow b) \equiv (\neg a \vee b)$ . (6 marks)
- c. Represent the given proposition symbolically by letting  
x : You run 30 laps weekly .  
y : You are healthy.  
z : You take vegetable.
- If you run 30 laps weekly, then you will be healthy. (2 marks)
  - If you do not run 30 laps weekly or do not take vegetable, then you will not be healthy. (2 marks)
  - You will be health if and only if you run 30 laps weekly and take vegetable (2 marks)

### Q3 (Chapter 1.3)

- a. Let  $P(n)$  be the propositional function “n divides 15.” Write each proposition in words and tell whether it is true or false. The domain of discourse is  $Z^+$ .

- i)  $P(5)$  (2 marks)
- ii)  $\forall n P(n)$  (2 marks)
- iii)  $\exists n \neg P(n)$  (2 marks)

- b. Let  $P(m, n)$  be the propositional function  $m \geq n$ . The domain of discourse is  $\mathbb{Z}^+ \times \mathbb{Z}^+$ . Tell whether  $\exists m \exists n P(m, n)$  is true or false. (2 marks)  
Write the negation of the proposition above. (2 marks)

#### Q4 (Chapter 1.4)

Prove that if  $x$  and  $y$  are real numbers with  $x < y$ , there exists a rational number  $a$  satisfying  $x < a < y$ . (6 marks)  
*klv indirect x leh, try contradiction*

#### Q5 (Chapter 2.1)

- a. List the elements of relation  $R$  on the set  $\{1, 2, 3, 4, 5\}$  defined by the rule  $(m, n) \in R$  if 2 divides  $m - n$ . Afterwards, list the elements of  $R^{-1}$ . (4 marks)
- b. Repeat question **a** for relation  $R$  on the set  $\{1, 2, 3, 4, 5\}$  defined by the rule  $(m, n) \in R$  if  $m + n \leq 4$ . (4 marks)
- c. Determine either relation of question **a** and **b** are symmetric. (2 marks)
- d. Determine whether each relation below defined on the set of positive integers is reflexive, symmetric, antisymmetric, transitive, and/or a partial order. (6 marks)
  - i)  $(x, y) \in R$  if  $xy = 1$ .
  - ii)  $(x, y) \in R$  if  $x = y^2$ .
  - iii)  $(x, y) \in R$  if  $x = y$ .

#### Q6 Chapter 2.2)

- a. Determine whether each function below is one-to-one, onto, or both. Prove your answers. The domain of each function is the set of all integers. The codomain of each function is also the set of all integers.
  - i)  $f(n) = n + 1$  (3 marks)
  - ii)  $f(n) = |n|$  (3 marks)
- b. Given  $n = \{(1, b), (2, c), (3, a)\}$ , a function from  $X = \{1, 2, 3\}$  to  $Y = \{a, b, c, d\}$ , and  $m = \{(a, x), (b, x), (c, z), (d, w)\}$ , a function from  $Y$  to  $Z = \{w, x, y, z\}$ , write  $m \circ n$  as a set of ordered pairs and draw the arrow diagram of  $m \circ n$ . (5 marks)
- c. Let  $g = \{(1, a), (2, c), (3, c)\}$  be a function from  $X = \{1, 2, 3\}$  to  $Y = \{a, b, c, d\}$ . Let  $S = \{1\}$ ,  $T = \{1, 3\}$ ,  $U = \{a\}$ , and  $V = \{a, c\}$ . Find  $g(S)$ ,  $g(T)$ ,  $g^{-1}(U)$ , and  $g^{-1}(V)$ . (4 marks)