

Module 2 R Activity

Zahlen Zbinden

1. Create the vector [1 4 9 12] using the c() function, and name it newVec1

```
newVec1 <- c(1, 4, 9, 12)
```

2. Create another object:

```
newVec2 <- (1:4)^2
```

```
newVec1 == newVec2
```

```
[1] TRUE TRUE TRUE FALSE
```

3. Use the cbind() command to creat the following matrix and name it newMat1

```
newMat1 <- matrix(c(1, 4, 2, 0, 7, -3, 5, 2, 1), ncol = 3)
```

4. Use the rbind command to create the following matrix

```
newMat2 <- rbind(c(1, 1, 2), c(4, 7, 2), c(5, -3, -1))
```

5. Companre newMat1 and newMat2 to identify which positions are not equal

```
newMat1 == newMat2
```

```
      [,1] [,2] [,3]  
[1,] TRUE FALSE FALSE  
[2,] TRUE TRUE TRUE  
[3,] FALSE TRUE FALSE
```

6. Use the matrix() command to create the following matrix and name it newMat3

```
newMat3 <- matrix(c(1, 4, 2, 5, 3, 6), byrow = T, nrow = 3)
```

7. Compare newMat1 to the transpose of newMat2 to identify which positions are not equal

```
newMat1 == newMat2
```

```
      [,1] [,2] [,3]
[1,]  TRUE FALSE FALSE
[2,]  TRUE  TRUE  TRUE
[3,] FALSE  TRUE FALSE
```

8. How could you use R to check whether a matrix is symmetric? Give code for checking whether newMat2 is symmetric

```
symetric <- function(matrix) {
  return (all(t(matrix) == matrix))
}
```

9. Create a diagonal matrix named diagMat1 with diagonal entries equal to the diagonal entries of newMat1

```
diagMat1 <- diag(newMat1)
```

10. Create the 5x5 identity matrix and name it ident5

```
ident5 <- diag(5)
```

11. Calculate the sum of newMat1 and newMat2

```
newMat1 + newMat2
```

```
      [,1] [,2] [,3]
[1,]     2     1     7
[2,]     8    14     4
[3,]     7    -6     0
```

12. Multiply newMat3 by 7

```
newMat3 * 7
```

```

      [,1] [,2]
[1,]    7   28
[2,]   14   35
[3,]   21   42

```

13. Create a 3x3 identity matrix, and name it `ident3`. Perform matrix multiplication to find the product of `ident3` and `newmat3`

```

ident3 <- diag(3)

ident3 %*% newMat3

```

```

      [,1] [,2]
[1,]    1    4
[2,]    2    5
[3,]    3    6

```

14. What happens when you try to perform the matrix multiplication to find the product of `newMat3` and `ident3`. “Error in ...: non-conformable arguments”. This is because `newMat3` is a 3X2 matrix and, `ident3` is a 3X3 matrix, the dim of each matrix makes it impossible for the multiplication to happen in this form `newMat3 * ident3`.

15. Find the matrix inverse of `newMat1`, name this matrix `newMat1.inv` and report its value

```

newMat1.inv <- solve(newMat1)
newMat1

```

```

      [,1] [,2] [,3]
[1,]    1    0    5
[2,]    4    7    2
[3,]    2   -3    1

```

16. Demonstrate that the matrix product of `newMat1` and `newMat1.inv` is the 3X3 identity matrix, no matter which order you perform the multiplication. Because of “computer” there multiplications don’t end up perfect, therefore it doesn’t recognize new inverse matrix acquired from `solve()` to be a true inverse, although the matrix that it presents are very close. if you round the result to the nearest integer than you get the true identity matrix

```

all(ident3 == round(newMat1 %*% newMat1.inv))

```

```

[1] TRUE

```

```
all(ident3 == round(newMat1.inv %*% newMat1))
```

[1] TRUE

17. What happens if you try to find the determinant of a matrix that is not square? Demonstrate an example. “Error in determinant.matrix...: ‘x’ must be a square matrix

```
tryCatch(  
  {  
    det(newMat3)  
  },  
  error = function(e) {  
    print(e)  
  }  
)
```

<simpleError in determinant.matrix(x, logarithm = TRUE, ...): 'x' must be a square matrix>

18. What happens if you try to find the trace of a matrix that is not square? Demonstrate an example. It returns a number.

```
sum(diag(newMat3))
```

[1] 6

19. Calculate the determinant of newMat2

```
det(newMat2)
```

[1] -81

20. Calculate the trace of newMat2

```
sum(diag(newMat2))
```

[1] 7

21. Create the following matrix and name it newMat2. Find the eigen decomposition of this matrix. What is the eigenvector corresponding to the smallest eigenvalue? The smallest eigenvalue is 0.5 and the vector corresponding to it is:

$$\begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

```
newMat2 <- matrix(c(6.8, 2.4, 0, 2.4, 8.2, 0, 0, 0, .5), ncol = 3)
eigen(newMat2)
```

```
eigen() decomposition
```

```
$values
```

```
[1] 10.0  5.0  0.5
```

```
$vectors
```

```
      [,1] [,2] [,3]
[1,]  0.6 -0.8   0
[2,]  0.8  0.6   0
[3,]  0.0  0.0   1
```