TTK4255: Robotic Vision

# Homework 1: Image processing

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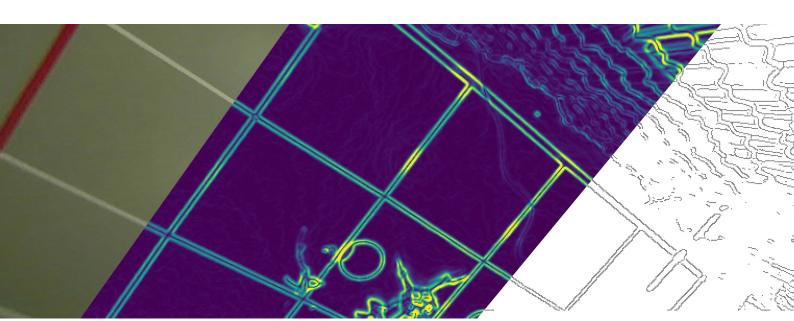


Figure 1: Intermediate stages of a simple edge detection algorithm you will implement.

### **Instructions**

First make sure to read about.pdf in the "Course work" page on Blackboard. To get your assignment approved, you need to complete any <u>60%</u>. Upload the requested answers and figures as a single PDF. You may collaborate with other students and submit the same report, but you still need to upload individually on Blackboard. Please write your collaborators' names on your report's front page. If you want detailed feedback, please indicate so on the front page.

# **Relevant reading**

The image processing theory in this assignment is presented in Szeliski (2021) §3.1 (Point operators) and §3.2 (Linear filtering). Edge detection is discussed in more detail in §7.2 (Edges and contours), but it is not necessary to read the chapter to complete the tasks. Color spaces, which are briefly mentioned in the assignment, are presented in §2.3.2 (Color), but this should not be necessary to read.

# **Getting started**

The assignments are a mix of theory and programming problems. We recommend that you use Python or Matlab. We provide reference solutions, and often starter code, for these languages. The back of this document also has some tips, useful functions and common mistakes for Python and Matlab.

**Python** While the assignments don't require a specific version, our reference solutions are written for Python 3.7. If you want to be able to run these without significant modifications, use a version from 3.0 or above. We recommend that you install Numpy (link) and Matplotlib (link), for linear algebra and plotting. You may need to install Pillow (link) to read some image formats. The Python Numpy Tutorial by Justin Johnson (link) is a good reference for various functionality we'll use.

**Matlab** You can use any version of Matlab. However, our reference solutions make use of local function definitions inside script files—a feature added in 2016b. If you have an earlier version, you may want to upgrade. The assignments will require some functions in the Image Processing Toolbox (link). If you don't have it, you can install new toolboxes to an existing Matlab installation by rerunning the installer (link). While you're at it, you may want to install the Computer Vision Toolbox (link), which will be useful later in the course. The first eight pages of the Matlab Primer (link) from ETHZ is a good reference for Matlab functionality we'll use.

# Part 1 Theory questions

**Task 1.1:** (12%) What is the effect of convolving an image with this kernel?

$$\begin{bmatrix} -0.5 & -1.0 & -0.5 \\ -1.0 & +7.0 & -1.0 \\ -0.5 & -1.0 & -0.5 \end{bmatrix}$$

Tip: Work out the result of the convolution along a straight line in an image with (a) uniform pixel values and (b) a vertical or horizontal step edge (e.g. a transition from 0 to 1).

**Task 1.2:** (8%) Several filter kernels in signal processing are based on continuous functions due to the ease of analyzing theoretical properties in the continuous domain. For example, a commonly-used function is the one-dimensional Gaussian,

$$g(x) = \frac{1}{\sqrt{2\pi} \cdot \sigma} \cdot \exp\left(\frac{-x^2}{2\sigma^2}\right),$$
 (1)

where  $\sigma$  is called the standard deviation. A corresponding discrete filter kernel can be created by evaluating the continuous function within a finite-sized window, e.g. at integer locations:

$$[g(-h), \cdots, g(-1), g(0), g(1), \cdots, g(h)].$$
 (2)

Because the Gaussian has infinite support, a finite-sized window will cause a truncation error. Thus, when creating a Gaussian filter kernel, you need to choose both the standard deviation (reflecting the desired filtering properties) and the kernel size (constrained by your computational budget).

- (a) For a given error threshold  $\epsilon$  and standard deviation  $\sigma$ , derive an expression for the half-width h such that the value of g outside the window is less than  $\epsilon$ .
- (b) Suppose the desired threshold is  $\epsilon = 1/256$  and  $\sigma = 3$ , how big should the kernel be?

# Part 2 Basics

This part will familiarize you with loading, plotting and basic image operations. There is no provided starter code, so you will have to write the code to produce the requested outputs yourself.

**Task 2.1:** (4%) An image named grass.jpg is in the provided data directory. The image is from a dataset of a sugar beet field (link). Load the image and print its width and height.

**Task 2.2:** (4%) The image has three channels: red, green and blue. A single-channel image can be extracted (in Python) using img[:,:,i],  $i \in {0,1,2}$  or (in Matlab) using img(:,:,i),  $i \in {1,2,3}$ . Can you find out which i corresponds to the green channel by plotting the three single-channel images?

Task 2.3: (4%) Thresholding is a simple technique for isolating parts of interest in an image (a problem known as segmentation). In Python and Matlab, thresholding is a one-liner operation using the syntax img > threshold. The result is a binary image of 1's and 0's, where a value of 1 is assigned to each element that satisfies the expression. Using only the green channel, can you find a threshold that isolates all the pixels belonging to the sugar beet leaves? Tip: Zoom in to ensure you are not simply segmenting their shadows.

**Task 2.4:** (4%) The issue you will encounter above is that the G component of RGB confuses the hue and luminance of the color and cannot be used in isolation to determine the "green-ness" of something. For example, pure white has a large G component, but doesn't look green. Usually we would represent the image in a different color space which disentangles the aspects of interest of the perceived color. A simple solution is to use normalized rgb coordinates:

$$r = \frac{R}{R+G+B}, \quad g = \frac{G}{R+G+B}, \quad b = \frac{B}{R+G+B},$$
 (3)

which sum up to 1. Normalized rgb coordinates are invariant to a scalar multiplicative factor, which can be somewhat useful to make an algorithm sensitive only to the hue of a color. Convert the RGB image to normalized rgb and include a figure showing the three single-channel images (r, g, b).

**Task 2.5:** (4%) Repeat the thresholding task using the normalized rgb image. Include a figure showing your segmentation result (i.e. the binary image). Are you able to achieve a result similar to that below? (You don't have to reproduce the rightmost figure.)

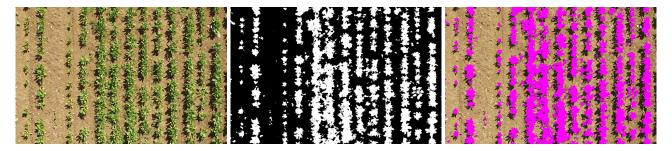


Figure 2: Segmentation obtained by thresholding normalized rgb. Left: Input. Middle: Binary image. Right: Above-threshold pixels replaced by magenta.

# Part 3 Edge detection

In this part you will implement a simple edge detection algorithm. In the tasks below, you should finish the implementation of stub functions declared in the provided code. After each task, you can run the task3 script to generate a figure visualizing each output. You only need to include this figure once. If you do not complete all the tasks, you can run the script to get a figure showing your partial results.

**Task 3.1:** (4%) Color images have three channels, but it can sometimes be more practical to work with single-channel grayscale images. There is no unique color-to-grayscale conversion, and the most appropriate one will depend on the application. A fast and simple conversion is the average of the three channels. Implement the function rgb\_to\_gray.

**Task 3.2:** (14%) To detect edges, we will look for pixels that have an abrupt change in pixel value. This can be measured by using the image gradient. Implement the function central\_difference that takes a grayscale image I and computes the horizontal and vertical gradient by convolving with the following 1-D central difference kernel:

$$\begin{bmatrix} +\frac{1}{2} & 0 & -\frac{1}{2} \end{bmatrix}. \tag{4}$$

Return the two gradient images and the gradient magnitude. To compute the horizontal gradient image  $I_x$ , convolve the kernel with each row of the input. For the vertical gradient image  $I_y$ , convolve with each column. You can use conv (Matlab) or numpy.convolve (Python) for 1-D convolution. The gradient magnitude can be computed as  $I_m = \sqrt{I_x^2 + I_y^2}$ .

Ensure that the outputs have the same size as the input. To do this you need to handle border effects (Szeliski 3.2). One solution is to pad the image row or column with zeros, which you can do easily by specifying the 'same' option in conv and numpy.convolve. However, zero-padding may produce darkening near the sides. You can alternatively pad by replicating the end element on either side.

Task 3.3: (14%) Implement gaussian which convolves a grayscale image with the 2-D Gaussian

$$\frac{1}{2\pi\sigma^2}\exp\left(-\frac{x^2+y^2}{2\sigma^2}\right) \tag{5}$$

taking the standard deviation parameter  $\sigma$  (sigma) as the blur strength. The 2-D Gaussian is separable, which means that the 2-D convolution can be computed by convolving the 1-D Gaussian with each row of I, giving an intermediate image I', followed by convolving with each column of I'. Again, ensure that the result image has the same size as the input using one of the two padding strategies above.

**Task 3.4:** (14%) Implement the function extract\_edges that identifies edges by thresholding the gradient magnitude. The function should return a list of pixel coordinates (x, y) and orientations  $\theta$ . The orientation should be computed as the angle of the image gradient vector:  $\theta = \tan 2(I_y(x, y), I_x(x, y))$ .

Tip: Use the functions np.nonzero (Python) or find (Matlab) to extract the coordinates of above-threshold pixels. In Matlab, sub2ind may be useful to obtain the  $I_x$ ,  $I_y$  values for computing the angle.

**Task 3.5:** (14%) Test your functions on the grid.jpg image and include the figure showing the blurred image, gradient images and the extracted edges. Try adjusting the blurring parameter  $\sigma$  and the edge threshold. What effect does blurring have on the detected edges?

**Notes:** Instead of convolving with the Gaussian and then convolving with a central difference kernel, you could instead convolve with the partial derivatives of a Gaussian. This is because convolution commutes with differentiation.

## Python tips (see next page for Matlab)

```
import matplotlib.pyplot as plt
                                       Import a Matlab-like interface to Matplotlib.
import numpy as np
                                       Common way to import Numpy.
from numpy import *
                                       Make all functions accessible in global namespace.
help(<name>)
                                       Print information about <name>.
np.array([x,y,z])
                                       Create a vector.
np.array([[x,y,z]])
                                       Create a row vector.
np.array([[x],[y],[z]])
                                       Create a column vector.
np.array([[a,b],[c,d]])
                                       Create a 2\times2 matrix.
np.linalg.norm(p)
                                       Calculate 2-norm of vector.
h,w = img.shape[0:2]
                                       Retrieve the height and width of an image.
plt.imread
                                       Load an image.
                                       Draw an image on the current plot.
plt.imshow
                                       Save an image to disk.
plt.imsave
                                       Make your plots actually show up on the screen.
plt.show
plt.savefig('figure.png')
                                       Save displayed figure to disk. (Call before plt.show)
plt.plot([x0,x1], [y0,y1])
                                       Draw a single line from (x_0, y_0) to (x_1, y_1).
plt.scatter(x, y)
                                       Draw a marker at (x, y).
plt.scatter(p[:,0], p[:,1])
                                       Draw a set of points stored as an n \times 2 array.
```

Unlike Matlab, the \* operator in Numpy is element-wise multiplication, not matrix multiplication. The dot function or @ operator can be used instead to compute inner products of vectors, to multiply a vector by a matrix, and to multiply matrices: e.g. A.dot(b) and A @ b both perform standard matrix multiplication between A and b. (The np.matrix class does define \* to be matrix multiplication, but it is no longer recommended to use this class, even for linear algebra. Instead use regular arrays. The class may be removed in the future).

plt.imread may store the loaded image using 8-bit unsigned integers (values 0 to 255 in each channel). Using this format later can lead to unexpected behavior or mysterious error messages due to overflow or type mismatch. You can convert an 8-bit image to floating-point by dividing it by 255. This will scale the RGB components to be in the range [0, 1], so keep that in mind when e.g. choosing thresholds.

It's very easy to accidentally swap x and y coordinates. Remember, images expressed as NumPy arrays are accessed like a matrix: e.g. image [row, column] or image [y, x]

plt.imshow will automatically rescale the pixel values. If this is undesired, you can specify a custom range using vmin and vmax; see the documentation page.

## Matlab tips (see previous page for Python)

help <function> Print information about a function.

lookfor <keyword> Get a list of functions related to a keyword.

doc <function> Documentation for a function.

doc images Documentation for the Image Processing Toolbox.

imread Load an image.

imshow Draw an image on the current plot.

imwrite Save an image to disk.

print('myfigure', '-dpng') Save displayed figure to disk.

plot(x,y) Draw lines. scatter(x,y) Draw points.

im2double Convert image in 8-bit unsigned format (values 0 to 255 in

each channel) to floating-point (values 0-1).

norm(v) Calculate the 2-norm of vector v.

vecnorm(A,p,dim) If A is a matrix, calculate the p-norm of each vector along

dimension dim.

imread may store the loaded image using 8-bit unsigned integers (values 0 to 255 in each channel). Using this format later can lead to unexpected behavior or mysterious error messages due to overflow or type mismatch. It can be useful to convert the image to floating-point using im2double. This will scale the RGB components to be in the range [0, 1], so keep that in mind when e.g. choosing thresholds.

It's very easy to accidentally swap x and y coordinates. Remember, images expressed as Matlab arrays are accessed like a matrix: e.g. image(row, column) or image(y, x).

imshow will automatically rescale the pixel values to the minimum and maximum representable values for the data type (e.g. 0 to 255 for uint8). If this is undesired, you can specify a custom range; see the documentation page.