

Computer Vision

Assignment -1

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1. Given:

- a. $f = [1 \ 2 \ 1]$, $X = [0 \ 1 \ 2 \ 3 \ 4 \ 4 \ 1 \ 5 \ 6]$
 - i. Using zero padding
 $X' = [0 \ 0 \ 1 \ 2 \ 3 \ 4 \ 4 \ 1 \ 5 \ 6 \ 0]$
 $\Rightarrow f * X' = [1 \ 4 \ 8 \ 12 \ 15 \ 13 \ 11 \ 17 \ 17]$
 - ii. Using boundary replication
 $X' = [0 \ 0 \ 1 \ 2 \ 3 \ 4 \ 4 \ 1 \ 5 \ 6 \ 6]$
 $\Rightarrow f * X' = [1 \ 4 \ 8 \ 12 \ 15 \ 13 \ 11 \ 17 \ 23]$
- b. $f = [1 \ 0; 0 \ 1]$, $X = [1 \ 0 \ 0; 0 \ 0 \ 1; 0 \ 0 \ -1]$
 - i. Using zero padding
 $X' = [0 \ 0 \ 0 \ 0; 0 \ 1 \ 0 \ 0; 0 \ 0 \ 0 \ 1; 0 \ 0 \ 0 \ -1]$
 $\Rightarrow f * X' = [1 \ 0 \ 0; 0 \ 1 \ 1; 0 \ 0 \ -1]$
 - ii. Using boundary replication
 $X' = [1 \ 1 \ 0 \ 0; 1 \ 1 \ 0 \ 0; 0 \ 0 \ 0 \ 1; 0 \ 0 \ 0 \ -1]$
 $\Rightarrow f * X' = [2 \ 1 \ 0; 1 \ 1 \ 1; 0 \ 0 \ -1]$

2. **No effect** on swapping the two operations as convolution operation is commutative. The result will remain the same. The reason to do smoothening before the image gradient was to remove the noises(salt-pepper like noise) from the gradients as they affect the result and are not a part of edges.

3. Canny edge detection is composed of:

- a. **Noise reduction**
- b. **Gradient calculation**
- c. **Non-maximum suppression**
- d. **Double threshold**
- e. **Edge tracking**

Mathematically for noise reduction smooth it with a Gaussian filter

$$g(m, n) = G_{\sigma}(m, n) * f(m, n)$$

G_{σ} is Gaussian function

After this compute the gradient of $g(m, n)$ using Sobel filter to get

$$M(m, n) = \sqrt{g_m^2(m, n) + g_n^2(m, n)}$$

$$\Theta(m, n) = \tan^{-1} |g_n(m, n) / g_m(m, n)|$$

Threshold M:

$$M_T(m, n) = \{M(m, n) \text{ if } M(m, n) > T; 0 \text{ otherwise}\}$$

Where T is chosen to suppress noise most of the noise.

Suppress non-maxima pixels in the edges in M_T

$$M_T(m, n) = \{M_T(m, n) \text{ if } M_T(m, n) > \text{two neighbours along } \Theta(m, n); 0 \text{ otherwise}\}$$

Threshold the result by two different thresholds (T_1, T_2) where $T_1 < T_2$ to obtain two binary images. Image with T_2 has less noise and fewer false edges but greater gaps between edge segments.

Link edge segment in M_{T_2} to form continuous edges. I.e. trace each segment in M_{T_2} to its end and then search its neighbor in M_{T_1} to find any edge segment to bridge the gap until reaching another edge segment in M_{T_2} .

4. The question is missing.
5. There is a **trade-off** between **intensity** and **blurriness**. To get a clear image we require small-sized pinhole, but reducing the pinhole size also decreases the intensity of light falling on the image plane. So we kept decreasing the size until we get a visually clear image. **Advantage** of having small-sized pinhole: The image will be less blurred or more clear. **Disadvantage**: The intensity will decrease which might cause the image to not be detected.
6. Affine matrix for scaling followed by translation =
 $[[s_x \cos \Theta - s_y \sin \Theta \ 0], [s_y \sin \Theta \ s_x \cos \Theta \ 0], [0 \ 0 \ 1]]$ as given in the problem it is equal to
 $[[1 \ 1 \ 0], [-1 \ 1 \ 0], [0 \ 0 \ 1]]$
 \Rightarrow on solving we get $s_y = s_x = \sqrt{2}$ and $\Theta = 45 \text{ degree clockwise or } 315 \text{ anticlockwise}$.