How effective are different configurations of a neural network reinforcement learning in playing space invaders?

Introduction

Artificial intelligence (AI) is any computer performing tasks typically requiring a human to operate. These tasks can vary from a wide range of difficulties and goals. Similarly, AI comes in many forms; in this experiment, the focus is on Machine learning. Machine learning is a branch of AI that primarily deals with building models to predict patterns within data. Machine learning, which is a subdomain of artificial intelligence, relies on a multitude of statistical techniques to find patterns and predict outcomes (Portilla, 2023a).

Reinforcement Learning

Reinforcement learning is a subset of machine learning. There are multiple types of machine learning, with reinforcement learning being one of them. Unlike other types of machine learning, reinforcement learning does not rely on large amounts of previously labeled data to make the model (Mnih et al., 2013). Instead, the model, or "agent," learns in a given environment through observations and rewards. The learning process starts with the agent in an "environment" where the agent gets trained. The agent performs an action and then takes in an "observation" and a "reward" value. The observation gives the state of the environment (such as an image of what is happening), and the reward allows the agent to determine how good (or bad)

it is doing. This process works in a cycle: the agent performs an action, the agent takes in an observation and reward, and then the agent updates its policy, or way of thinking. With enough repetitions of this cycle, one can hope the agent becomes competent enough to achieve desirable results (Portilla, 2023c).

There are many models to run this reinforcement learning cycle, such as Q-learning. The main idea of Q-learning is that in an environment with a set number of conditions and a set number of actions, theoretically all of the state/action combinations are able to be mapped onto a data table, such as in the game of tic-tac-toe. In each of the cells of a table, there is a Q-Value. The Q-Value is the expected sum of all future rewards, with higher Q-Values meaning an action is more desirable to take. For each state the agent comes across, it could just look up the state in the table and take the action with the best Q value. As the agent experiments with the environment, it adjusts the Q values using its policy. By training the agent, said Q table can be filled out, and the environment could be considered "solved," with all possible states already having optimal actions that would lead to the highest reward (Portilla 2023c). In the initial training process with the table being empty, the initial actions would have to be chosen purely randomly. As the table gets filled out, the agent starts getting the choice between choosing random actions and choosing actions that it thinks would lead to the best outcome. This problem is called exploration vs exploitation. There are pros and cons for both exploration (randomly chosen action) and exploitation (optimal known action). If an agent solely explored, it would never be able to apply what it is learning and end up with very bad results. On the flip side, if an agent only exploited, it would only use one solution to a problem, without any chance to find a

better solution. This balance between exploration and exploitation is determined by a value called "epsilon", the probability that the agent will take a random action. Epsilon can have a value between 1 and 0, with 1 being a 100% chance of the action taken being random, and 0 meaning the actions will always be what the agent decides. By slowly decreasing epsilon throughout the training period, the agent will start to take less random actions as time goes on. This is part of the learning process, with the agent gradually using what it has learned over making random actions. (Portilla, 2023b).

In this experiment, Deep Q-Learning is used for the reinforcement learning agent. Deep Q-Learning, or DQN, is a combination of both Q-Learning and an artificial neural network.

Instead of using a table-based method to make decisions, a DQN agent utilizes neural networks to analyze and make decisions about the environment around it.

Artificial Neural Network

An artificial neural network can be thought of as a human brain. In a human brain, there are millions of interconnected cells, called neurons. Each neuron has an input and an output, which are connected to other neurons. Through this connected network, the neurons send signals to each other, and the brain can make decisions. Though this is an oversimplification of how the brain works, it models out basically what a neural network is in terms of machine learning.

Instead of cells, the computer uses a series of equations, each of which feed into each other.

Through the process of machine learning, the computer adjusts the values within the equations

and the connections between the neurons. As the computer is training, it adjusts these parameters so that the network will output desirable numbers, or decisions.

Experiment

Neural Network

The experiment is set up to test 25 different neural network models. There are 5 different shapes, with 5 different numbers of layers. The shapes, arbitrarily named, are as follows: Line, Cone, Inverse Cone, Hourglass, and Inverse Hourglass. Each shape describes the formation of the neurons in the neural network. The line shape is the simplest one, with a constant number of neurons in each layer. The cone has an increasing increment of neurons in each layer, creating a cone shape. Inversely, the inverse cone has a decreasing number of neurons in each layer. The hourglass, much akin to an hourglass, starts out with a wider layer, then it shrinks in the middle, and then the layer widens again. Following this convention, the inverse hourglass starts out with a smaller layer, widens, and then shrinks again. The number of neurons per layer is easier visualized the following table:

		3 Layers	S		4 La	yers				5 Layer	S				6 La	yers						7 Layers	\$		
Line	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128	128
Cone	8	16	32	8	16	32	64	8	16	32	64	128	8	16	32	64	128	256	8	16	32	64	128	256	512
Inverse Cone	32	16	8	64	32	16	8	128	64	32	16	8	256	128	64	32	16	8	512	256	128	64	32	16	8
HourGlass	64	32	64	64	32	32	64	128	64	32	64	128	128	64	32	32	64	128	256	128	64	32	64	128	256
Inverse Hourglass	32	64	32	32	64	64	32	32	64	128	64	32	32	64	128	128	64	32	32	64	128	256	128	64	32

Table 1: Number of neurons per in each layer of the neural network (left to right).

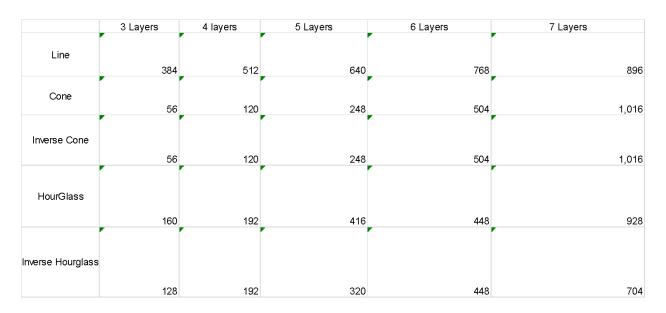


Table 2: Total number of neurons per neural network shape

This assortment of neural networks enables the testing of multiple aspects: the shape of a neural network, the number of layers in a neural network, and the number of neurons in a network. Neurons on each layer are a multiple of two for optimization. Each shape was made to have about the same number of neurons as possible, but some shapes end up having more due to their shape.

Environment

The environment in which the agents will be trained on is the Space Invaders environment. In Space Invaders, the player controls a laser cannon, which has 3 actions: move left, move right, and fire. The goal of the game is to gain as many points as possible by firing the laser cannon at descending alien invaders. Each invader destroyed awards the player with points ranging from 5 to 30, increasing depending on the row that they are in. There is an additional

seventh type of invader, which occasionally flies across the top of the screen and awards a bonus 200 points. The aliens come in waves, each wave consisting of 6 rows with 6 aliens. Each time a wave of invaders is wiped, a new one will spawn. The player loses a life if either the aliens reach the bottom of the screen or if the player gets hit by one of the bombs dropped by the aliens. The game ends if the player loses all 3 lives.

Agent and Policy

Each of the DQN agents are trained for 1,000,000 steps, or frames. On each step of a Space Invaders game, the agent has 6 possible actions, including doing nothing. The first 100,000 are treated as a warm-up. In this warm-up phase, the epsilon value for the agent will not decrease. This allows for the agent to have some data of how its environment works, without the agent starting its learning process. Every episode the epsilon value is multiplied by 0.99, until it reaches the minimum value of 0.1, from a starting value of 1.

Software and Hardware

To set up the experiment between the different shapes of neural networks, multiple python libraries were used, all of them using python version 3.7. A python library contains modules, each made to complete a smaller sub-task. This makes it much easier to make a reinforcement learning agent, or any other goal. Rather than making a system for a reinforcement learning agent from scratch, instead it is much easier to build off of existing libraries.

The primary library used in the experiment was Tensorflow and Keras. Both of these libraries handle the creation of the neural network and the reinforcement learning agent.

OpenAI Gym library was used to create the environment for the reinforcement learning agent. The gym library utilizes ROMs for atari games, found at atarimania.com.

The program runs on Windows 10, using Visual Studio Code. It uses Jupyter Notebooks, allowing for the code to be run piece by piece. All of this was run on a personal computer with an IntelCore i5-9600K CPU @ 3.70GHz.

Results

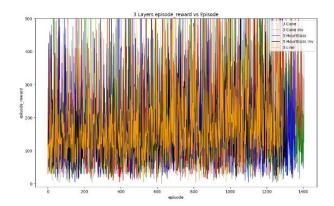
After each episode, the program returns a lot of metrics, which are as follows: loss, mean absolute error, mean_q, mean_eps, episode_reward, nb_episode_steps, nb_steps, episode, and duration. Of these, the ones that really matter are the mean Q and episode reward.

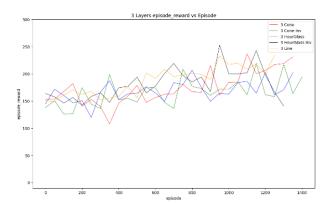
The mean Q, as mentioned in the introduction, is the average expected reward the model will obtain in a with the actions it is taking. This makes it possible to determine how well the model is doing in terms of maximizing future reward potential.

The reward is similar to this; however, it is the actual number of points that the agent obtained. Unlike the mean_q value, this value fluctuates greatly, due to exploration by the agent. If the agent was constantly exploiting, the mean_q value would be similar, if not the same as the reward value. However, the exploration that the agent does isn't always optimal, often resulting in games where the agent completely fails to gain any points. This in turn creates massive spikes in the original reward graphs, shooting up and down from 0 to 100 every other episode. To

mitigate this problem and make the graph more stable and readable, the reward data for each 50th cell is equal to the average reward of the next 50 cells. For example, the reward value for episode 500 would be the average value of the rewards from episodes 500 to 549. This turns the unreadable graph in *Figure 2* to a cleaner and legible version of the data in *Figure 1*.

Each of these metrics is measured per episode. The "episode" is each full game of space invaders that the agent plays. Each episode has a varying number of steps, which depends on how long the agent plays. Longer games would naturally lead to more steps. The only limit to how long a game can be is the number of steps that the agent is training for.





3 Layers

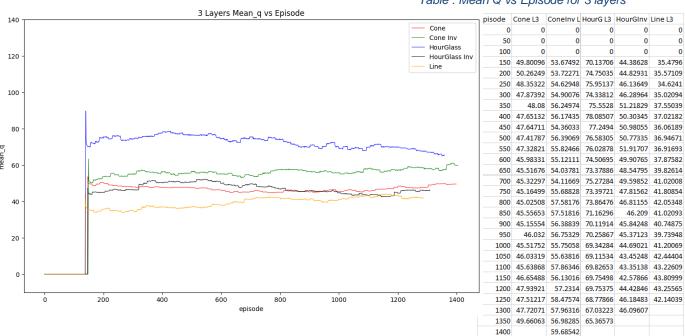
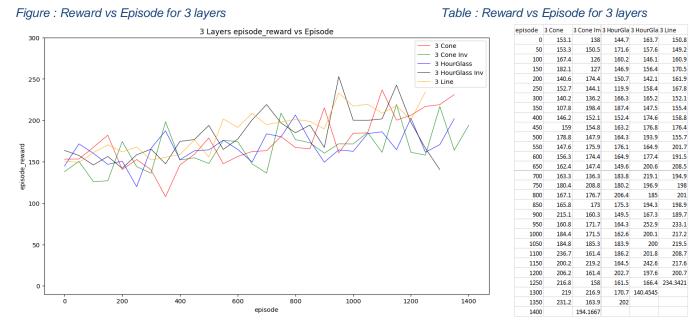


Table: Mean Q vs Episode for 3 layers

In the trial with 3 layers, all of the layers had a mean_q value within the range of about 40-70, a range of 30 mean_q points. There isn't much variance in the mean_q values, with the ranking of highest to lowest being: Hourglass, Cone Inverse, Cone, Hourglass Inverse, and Line.

The reward values vary wildly, due to the epsilon randomness as mentioned previously. By episode 1250, there was a range of about 70 points, from 234 to 158. The shape with the highest reward was the Line, with 234.3 points. After that, the next highest is the Cone, with 216.8 points total. Following it is Hourglass Inverse, with 166.4 points and Hourglass, with



161.5 points. Cone

Inverse is in last place with 158 points. The rankings for points were: Line, Cone, Hourglass Inverse, Hourglass, and Cone Inverse.

4 Layers

4 Layers Mean_q vs Episode 140 Cone Inv 0 HourGlass 50 120 HourGlass Inv 100 0 150 0 132.8967 112.7839 79.3189 100.9918 200 13.27792 127.9435 106.5162 81.59983 101.0178 100 13.67948 127.3267 104.7838 81.94883 250 300 14.67626 124,9718 102.3568 83.05201 350 15.56244 123.9103 100.8359 81.28409 96.73761 400 16.23098 121.6693 99.66191 78.9544 95.11283 450 17.42373 119,7251 98.37873 77.5714 98.90981 500 18.57258 115.3805 96.45022 76.09059 98.85583 550 19.30232 111.3351 94.53222 77.10629 98.17405 60 600 20.07859 109.384 93.84384 75.07297 96.36163 650 21.20098 105.7822 91.4998 71.44739 96.47832 21.36285 105.056 90.87684 70.50069 40 750 21.96216 88.02268 102.9692 23.84226 98.50131 86.46761 66.90276 850 24.12611 95.47411 83.44232 65.80533 85.26221 25.35414 95.69492 81.46557 63.23215 83.57449 20 25.10349 93.79899 80.49031 62.70362 950 1000 25.03151 89.12784 80.62026 60.38181 81.03654 79.45175 1050 24.84282 85.82601 80.07104 60.90616 1100 26.32839 83.50413 80.00714 58.4 78.54123 1150 26.95342 81.26017 77.39605 58.64081 77.03039 200 400 1000 1200 1400 600 800 1200 27.00879 82.78471 77.24337 55.23132 75.83159 1250 28.80532 81.91178 76.42851 56.24861 76.86696 1300 29.76252 81.1354 75.84217 55.98946 76.00033 1350 30.69794 80.78181 74.40258

Table · Mean Q vs Episode for 4 layers

In the 4 layer trials, there was more variance between the mean_q values, with the cone at the bottom. By episode 1250, the cone only had a mean_q value a little under 29. This is really small, in comparison to the other shapes, ranging from 56 to 81. Overall, there is a range of 50, including the outlier, and a range of 30, when disregarding the cone shape. Past about episode 375, the Hourglass and Line follow similar trends, within 10 mean_q of each other. Towards the end, the Line shape had about 0.2 more mean_q than the Hourglass, a 76.4 versus a 76.8. The ranking of the shapes, from highest to lowest is: Cone Inverse, Line, Hourglass, Hourglass Inverse, and Cone.

The final reward values are quite spread out. At episode 1250, the highest reward value is 242.2 points by Hourglass Inverse. The lowest reward value is 167 points, by Cone Inverse. This

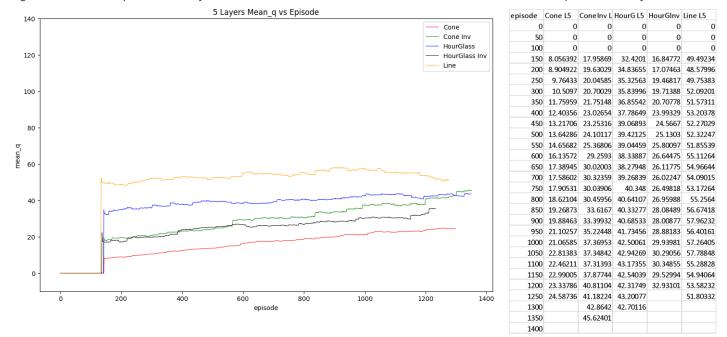
Figure: Reward vs Episode for 4 layers Table: Reward vs Episode for 4 layers episode 4 Cone 4 Layers episode reward vs Episode 4 Cone Inv4 HourGla 4 HourGla 4 Line 126.7 149 139.2 146.2 134.8 4 Cone 170.2 172.3 149.2 50 151.5 188.9 4 Cone Inv 144.2 148.8 100 174.7 156.4 165.8 4 HourGlass 169 152.7 173 150 196.8 181.2 4 HourGlass Inv 139.8 142.1 176.3 122.5 139.4 200 250 4 Line 250 152.4 153.9 144.4 142.7 154.7 300 154.9 143.3 176.9 141.6 118.7 350 153.5 154.1 183.9 149.5 168.5 400 189.4 169.9 194.1 142.8 143.9 200 450 202.6 147.5 172.8 160.8 500 212.1 167.3 177.5 200.4 550 189.9 152.7 177.9 184.8 162 600 186.3 130.2 166.3 167.5 182.1 650 215.8 157.2 146.6 228.7 182 700 233.2 148.7 163.6 167.1 177.5 750 183.4 146.7 149.9 215.4 206.4 800 162.2 155.9 212.9 192.1 214 100 850 185.9 182.8 169.7 219.4 177.6 185.4 900 223.5 182.1 132.8 196 179.4 185.8 950 172.3 161.9 169.4 1000 207.9 159.5 198.5 212.6 221.7 1050 174.2 215.4 204.1 165.8 216.7 50 1100 193.7 176 218.5 171.9 169.9 1150 215.6 175.9 172.5 213.3 229.5 1200 206.6 184.9 200.3 225.9 223.1 1250 181.2 167 226.6 242.2 173 1300 215.8 177.7 209.7 218.3333 210.2857 1200 1350 197.5 206.9512 233.4615 200 1000 1400 400 600

results in a range of 75 points between all the shapes. The final ranking for the shapes was:

Hourglass Inverse, Hourglass, Cone, Line, and lastly Cone Inverse.

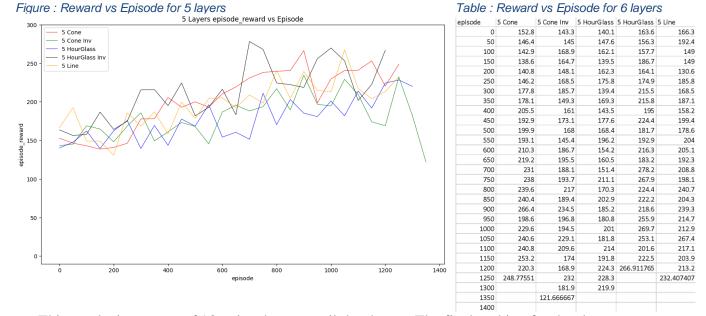
5 Layers
Figure : Mean Q vs Episode for 5 layers

Table: Mean Q vs Episode for 5 layers



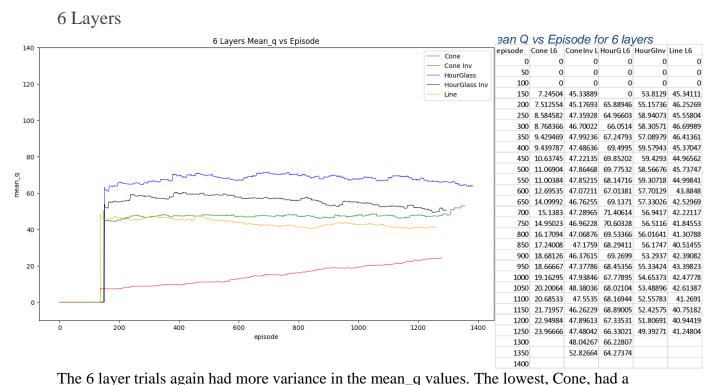
The 5 layer trials had more distinct and clear separation between the shapes. By episode 1250, the mean_q values ranged from 24 to 50, a range of 25 between the mean_q values. However, the Hourglass Inverse never made it to 1250 episodes, possibly due to longer games in general. The Cone Inverse started around the same as the Hourglass Inverse, but then climbed to the level of the Hourglass. Every other shape had a much slower increase in mean_q. The final rankings of the shapes are (from highest to lowest): Cone, Cone Inverse, Hourglass, Hourglass Inverse, and Line.

The final reward values are quite spread out. The only shape that didn't make it to episode 1250 was Hourglass Inverse. This isn't necessarily a bad thing; it just means that it had longer games that took up more frames. Interestingly, by episode 1200, the highest reward value is 266.9 points by Hourglass Inverse. The lowest reward value is 168.9 points, by Cone Inverse.



This results in a range of 98 points between all the shapes. The final ranking for the shapes was:

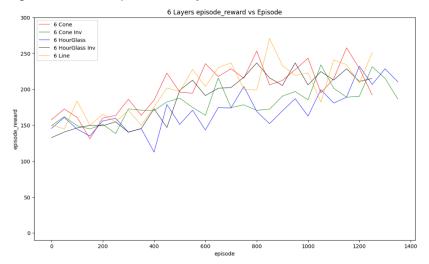
Hourglass Inverse, Hourglass, Cone, Line, and lastly Cone Inverse.



mean_q value of 24, and the highest, Hourglass, had a mean_q value of 66. This results in a range of 40 between all of the shapes. Excluding the outlier, cone, there is a range of 25 between all of the shapes. The ranking of the shapes is as follows: Hourglass, Cone Inverse, Hourglass Inverse, Line, and Cone.

For the 6 layers, the reward values are more consistent with each other. Most of the shapes stopped by episode 1250. By then, the highest reward value is 251 points by Line. The lowest reward value is 192 points, by Cone. This results in a range of 59 points between all the





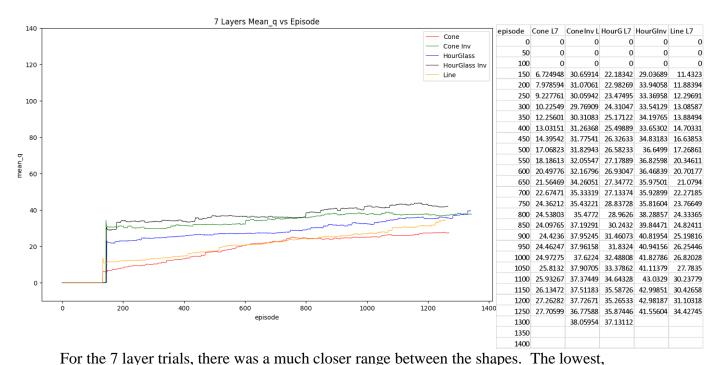
episode	6 Cone	6 Cone Inv	6 HourGlass	6 HourGlass	6 Line
0	157.4	149.3	145.4	132.6	150.1
50	172.5	161.8	160.7	140.4	144.8
100	160.8	149.2	144.5	146.2	183.6
150	131.1	144.7	134.9	149.6	150
200	160	151.2	155.9	149.2	165
250	163.4	138.3	159.5	154.6	154.6
300	186	172.6	140.3	140.2	170.8
350	163.8	170.9	145.1	145.3	149.9
400	184.7	170.4	112.5	172.9	175.5
450	222.5	182.3	178.8	146.7	201.6
500	195.9	187.5	151	198.6	196.9
550	194.4	174.7	170.8	212.5	227.4
600	235.6	163.8	143.2	191.1	203.7
650	217.7	215.7	174.5	201.3	230.1
700	228.4	174.4	174	202.4	236.6
750	215.2	178.3	203.8	216.7	200
800	253.2	170.6	169.1	236.5	198.9
850	206	172.3	152.1	215.8	270.5
900	212.1	190.3	169.9	205.2	232.9
950	227.3	196.8	186.8	236.6	219
1000	243.1	185.1	162.6	206	222.7
1050	195	233.9	199.3	224.5	181.9
1100	214.5	201.4	180.8	212.7	240.7
1150	257.6	188.9	188.8	228.4	234.1
1200	228.9	190.1	232	210.8	208.3
1250	192	231.2	206.6	215	251
1300		215.2	228.4		
1350		186.25	210.285714		
1400					

shapes. The final ranking for the shapes was: Line, Cone Inverse, Hourglass Inverse, Hourglass, and finally Cone.

Figure : Mean Q vs Episode for 7 layers

Table : Mean Q vs Episode for 7 layers

7 Layers



Cone, has a mean_q value of 27, and the highest, Hourglass Inverse has a mean_q value of 41. This results in a range of about 14. The final ranking of the shapes are as follows: Hourglass Inverse, Cone Inverse, Hourglass, Line, and Cone. It is notable that towards the end The Cone Inverse and Hourglass had about the same Q values, 38 and 37 respectively.

For the 7 layers, the reward values are all close to each other. Similar to the 6 layer shapes, most shapes stopped by episode 1250. By then, the highest reward value is 255.8 points by Hourglass. The lowest reward value is 204.7 points, by Cone. This results in a range of 51

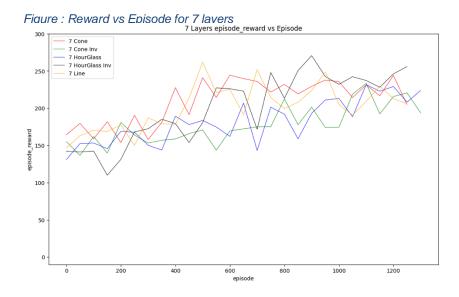


Table : Reward vs Episode for 7 layers

episode	7 Cone	7 Cone Inv	7 HourGlass	7 HourGlass	7 Line
0	164.3	155.1	130.9	142	146.8
50	179.6	136.5	152.5	141.2	163
100	158.8	161.9	153.2	142.3	170.3
150	181.8	139.7	145.6	109.9	168.6
200	153.8	180.9	169	131.2	177.6
250	190.5	163.9	167.7	168.1	149.9
300	157.8	153.1	150.1	172.4	187
350	180.9	156.9	143.7	185	178.9
400	227.6	158.6	189.3	179.3	178.3
450	191.3	165.8	177.9	153.9	213.7
500	241	170.7	183.5	180.4	261.8
550	214.3	143.7	174.7	227.2	221
600	244.4	169.4	162.1	226.1	225.3
650	239.7	172.2	206.9	222.8	191.4
700	235.9	174.9	143.2	171.6	251.8
750	221.6	175.1	201.3	247.9	214.3
800	232	212.5	191.9	213.2	199.5
850	219.1	177.8	158.8	250.5	208
900	229.3	201.4	193.1	270.6	223.8
950	237.8	174.1	211	242.5	248.6
1000	235.7	174.3	213.1	232	204.9
1050	214.3	218.7	188.5	242.3	190.6
1100	231.1	233.3	231.5	237.2	209.1
1150	216.7	192.3	222.8	228.1	229.4
1200	244	215.6	229.1	246.1	212.9
1250	204.75	220.6	208.1	255.882353	206
1300		193.666667	223.902439		
1350					
1400					

points between all the shapes. The final ranking for the shapes was: Hourglass Inverse, Cone Inverse, Hourglass, Line, and lastly Cone.

Discussion

Based on these results, the effectiveness of each of the shapes can be analyzed.

Ranking	3 Layer	4 Layer	5 Layer	6 Layer	7 Layer
1	HourGlass	Cone Inv	Cone	HourGlass	HourGlass Inv
2	Cone Inv	Line	Cone Inv	Cone Inv	Cone Inv
3	Cone	HourGlass	HourGlass	HourGlass Inv	HourGlass
4	HourGlass Inv	HourGlass Inv	Hourglass Inv	Line	Line
5	Line	Cone	Line	Cone	Cone

Table: Q Value rankings of each shape by number of layers

The most straight forward analysis would be of the placements that each shape placed in terms of Q values.

Rankings	Cone	Cone Inv	HourGlass	HourGlass Inv	Line	First
1	1	1	2	1	0	HourGlass
2	0	4	0	0	1	Cone Inv
3	1	0	3	1	0	HourGlass
4	0	0	0	3	2	HourGlass Inv
5	3	0	0	0	2	Cone

Looking at how many times each shape placed, it can be possible to determine what shape consistently ranks above the others. If a ranking consistently has one shape, it can be determined that the shape is really ranked that place against the other shapes. Alternatively, if a rank has multiple shapes evenly, that rank is likely to be up to chance.

In the number one spot, each shape took it at least once, except for line. This would lead to the conclusion that first place is mostly up to chance, and can't lead to any meaningful result.

For second place, there is a more conclusive result. Cone Inverse placed in second place 4 times. The only other shape in rank 2 is Line. This would mean that Cone Inverse is second overall.

For third rank the majority shape is Hourglass, placing 3 times. The other two shapes that placed in 3rd are Cone and Hourglass Inverse. Though not as certain of a placement as the 2nd place, Hourglass can be placed as 3rd rank overall.

For rank 4, Hourglass Inverse placed 3 times and line placed twice. This would place Hourglass as rank 4. Rank 5 is similar, with Cone placing 3 times and Line placing twice.

The only shape that hasn't consistently placed in a rank is Line. On average, it was in multiple ranks, scattered across the board. This would point to the success of Line being more based on the randomness of exploration, rather than actually being a more effective shape. Due to this, Line would most appropriately be placed in last place.

From this, the rankings for the shapes can be in the following descending order: Cone Inverse, Hourglass, Hourglass Inverse, Cone, and lastly, Line.

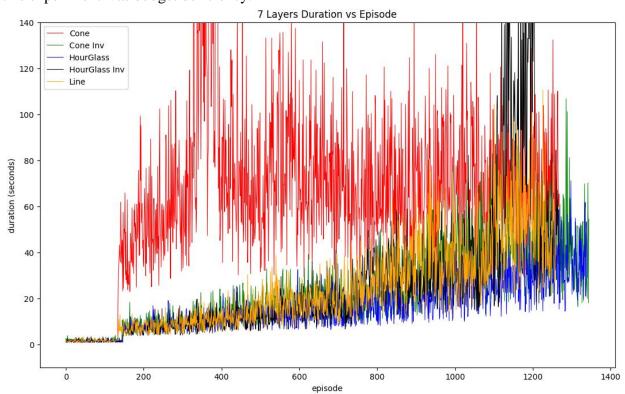
Limitations and Improvements

One of the biggest flaws in this experiment was the number of episodes that the agents played of space invaders. Though 1,000,000 frames might sound like a lot, for a reinforcement learning agent it simply isn't enough for it to play at a proficient level. Even though the game seems relatively simple for a human to play, the agent requires tens of millions of episodes to begin to recognize the gameplay patterns and play decently. At minimum, it would require about 10,000,000 frames or even 25,000,000 to 50,000,000 frames to really get it great at the game. The solution to not having enough episodes is, obviously, to tell the agent to run for a couple million more episodes. However, there are two problems with this: processing power and time.

Training the reinforcement learning agent is a very CPU demanding task. It needs to run both the agent and the game. Training one agent for 1,000,000 episodes can take from 10 hours upwards of around 24 hours. Multiplying this number by at least 10 for 10,000,000 episodes results in a very unreasonable length for testing one model, let alone 25. The increase isn't linear either. The less random actions the agent takes (as epsilon gets lower and lower), the more thinking the computer needs to calculate, and the longer the agent takes. This means that a game from episode 900,000 with 0.2 epsilon would take significantly longer than a game from episode 50,000, where all the actions are random. As demonstrated in figure 3, the first couple hundred episodes take a significantly shorter amount of time before it increases exponentially. So, the increase in time depends on the epsilon value of the model, meaning that as epsilon decreases,

the training time increases. Note that the outlier for cone is due to other processes running on the computer and taking up processing power.

This problem with time can be solved with more processing power, with either multiple computers (which would divide the total training time significantly, as multiple computers can train multiple models simultaneously) or with faster CPUs (which would train each model faster). This is easiest achieved with cloud computing, which rents processing power by the hour. However, the cost to rent computing power for 25 models, for a model with 1,000,000 frames, can be at least \$250 with AWS. Adding another couple million would increase the time, and cost, to train the models significantly, possibly with the lower end CPUs being about \$300 for 2 weeks, and the higher end CPUs going up to possibly \$500. In the end, the biggest limitation to this experiment was budget deficiency.



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