

zalshaye_5_Q2

Maximize $Z = P - 6C - 3D$

P = total (discounted) profit over the life of the new products, C = change (in either direction) in the current level of employment, D = decrease (if any) in next year's earnings from the current year's level.

Profit_Goal: Max $P = 20x_1 + 15x_2 + 25x_3$ Emp_level goal: $6x_1 + 4x_2 + 5x_3 = 50$

Earning_next_year goal: $8x_1 + 7x_2 + 5x_3 \geq 75$

Part 1) Model_Formulation:

$$y_1 = 6x_1 + 4x_2 + 5x_3 - 50$$

$$y_2 = 8x_1 + 7x_2 + 5x_3 - 75$$

Substitute the information into the original constraints

For employment level goal $y_1 = y_1^+ - y_1^-$ $y_1^+ - y_1^- = 6x_1 + 4x_2 + 5x_3 - 50$

For the goal regarding earnings next year $y_2 = y_2^+ - y_2^-$ $y_2^+ - y_2^- = 8x_1 + 7x_2 + 5x_3 - 75$

Final Formulation Max $P = 20x_1 + 15x_2 + 25x_3$ $6x_1 + 4x_2 + 5x_3 - (y_1^+ - y_1^-) = 50$

$8x_1 + 7x_2 + 5x_3 - (y_2^+ - y_2^-) = 75$ $x_j \geq 0, y_i^+ \geq 0, y_i^- \geq 0$

Part 2)

Objective Function: Maximize $Z = P - 6C - 3D$

Objective function in terms of $x_1, x_2, x_3, y_1^+, y_1^-, y_2^+$ and y_2^- Maximize $Z = 20x_1 + 15x_2 + 25x_3 - 6y_1^+ - 6y_1^- - 3y_2^+ - 3y_2^-$

Part 3) Objective Function: max: $20x_1 + 15x_2 + 25x_3 - 6y_1^m - 6y_1^p - 3y_2^m - 3y_2^p$;

Constraints: $x_j \geq 0, y_i^+ \geq 0, y_i^- \geq 0$ $6x_1 + 4x_2 + 5x_3 - y_1^p + y_1^m = 50$; $8x_1 + 7x_2 + 5x_3 - y_2^p + y_2^m = 75$;

```
library(lpSolveAPI)
GoalProg <- read.lp("C:\\Users\\Z\\Desktop\\Emax.lp")
GoalProg

## Model name:
##          x1      x2      x3      y1m      y1p      y2m      y2p
## Maximize    20     15     25      -6      -6      -3       0
## R1           6      4      5       1      -1       0       0 = 50
## R2           8      7      5       0       0       1      -1 = 75
## Kind        Std     Std     Std     Std     Std     Std     Std
## Type        Real    Real    Real    Real    Real    Real    Real
## Upper       Inf     Inf     Inf     Inf     Inf     Inf     Inf
## Lower        0      0      0      0      0      0      0
```

```
solve(GoalProg)
## [1] 0
get.objective(GoalProg)
## [1] 225
get.constraints(GoalProg)
## [1] 50 75
get.variables(GoalProg)
## [1] 0 0 15 0 25 0 0
```