# zalshaye\_5\_Q1

Formulate and perform DEA analysis under all DEA assumptions of FDH, CRS, VRS, IRS, DRS, and FRH.

### Facility 1

```
library(lpSolveAPI)
dmu1 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU1.lp")</pre>
dmu1
## Model name:
##
                                v1
                                       v2
                 u1
                        u2
## Maximize
             14000
                      3500
                                 0
                                        0
## R1
             14000
                      3500
                             -150
                                     -0.2
                                                0
                                            <=
## R2
             14000
                     21000
                              -400
                                     -0.7
                                            <=
                                                0
## R3
             42000
                     10500
                             -320
                                     -1.2
                                            <=
                                                0
## R4
             28000 42000
                              -520
                                       -2
                                            <=
                                                0
             19000
                     25000
                             -350
                                     -1.2
## R5
                                           <=
                                                0
## R6
             14000 15000
                             -320
                                     -0.7
                                                0
                                           <=
## R7
                  0
                         0
                              150
                                      0.2
                                                1
## Kind
               Std
                       Std
                              Std
                                      Std
## Type
              Real
                      Real
                             Real
                                     Real
                              Inf
                                      Inf
## Upper
               Inf
                       Inf
## Lower
                  0
                                 0
                                        0
                         0
solve(dmu1)
## [1] 0
get.objective(dmu1)
## [1] 1
get.variables(dmu1)
## [1] 7.142857e-05 0.000000e+00 5.172414e-03 1.120690e+00
facility 2
```

```
library(lpSolveAPI)
dmu2 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU2.1p")</pre>
dmu2
## Model name:
##
                 u1
                        u2
                                ν1
                                       v2
## Maximize
             14000
                     21000
                                 0
                                         0
## R1
              14000
                      3500
                              -150
                                     -0.2
                                            <=
                                                0
                                     -0.7
              14000
                     21000
                              -400
## R2
                                            <=
                                                0
## R3
              42000
                     10500
                              -320
                                     -1.2
                                            <=
```

```
## R4
              28000
                     42000
                              -520
                                       -2 <=
                                                0
              19000
## R5
                     25000
                              -350
                                     -1.2
                                                0
                                            <=
## R6
              14000
                     15000
                              -320
                                     -0.7
                                            <=
                                                0
## R7
                  0
                         0
                               400
                                      0.7
                                                1
                                             =
## Kind
                Std
                       Std
                               Std
                                      Std
## Type
               Real
                      Real
                              Real
                                     Real
                               Inf
                                      Inf
## Upper
                Inf
                       Inf
## Lower
                  0
                         0
                                 0
                                         0
solve(dmu2)
## [1] 0
get.objective(dmu2)
## [1] 1
get.variables(dmu2)
## [1] 0.000000e+00 4.761905e-05 1.376147e-03 6.422018e-01
facility-3
library(lpSolveAPI)
dmu3 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU3.lp")</pre>
dmu3
## Model name:
                                       v2
##
                 u1
                        u2
                                v1
## Maximize 42000
                     10500
                                 0
                                         0
## R1
              14000
                      3500
                              -150
                                     -0.2
                                                0
                                            <=
## R2
              14000
                     21000
                              -400
                                     -0.7
                                                0
                                            <=
## R3
             42000
                     10500
                              -320
                                     -1.2
                                            <=
                                                0
                     42000
                              -520
## R4
              28000
                                        -2
                                            <=
## R5
              19000
                     25000
                              -350
                                      -1.2
                                            <=
## R6
              14000
                     15000
                              -320
                                     -0.7
                                                0
                                            <=
## R7
                  0
                         0
                               320
                                      1.2
                                                1
## Kind
                Std
                       Std
                               Std
                                      Std
## Type
               Real
                      Real
                              Real
                                     Real
## Upper
                Inf
                       Inf
                               Inf
                                      Inf
## Lower
                  0
                         0
                                 0
                                         0
solve(dmu3)
## [1] 0
get.objective(dmu3)
## [1] 1
get.variables(dmu3)
## [1] 2.380952e-05 0.000000e+00 1.724138e-03 3.735632e-01
```

#### facility 4

```
library(lpSolveAPI)
dmu4 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU4.lp")</pre>
dmu4
## Model name:
##
                         u2
                                        v2
                 u1
                                ν1
## Maximize
              28000
                     42000
                                 0
                                         0
              14000
                      3500
                              -150
                                      -0.2
## R1
                                                 0
                                            <=
## R2
              14000
                     21000
                              -400
                                      -0.7
                                            <=
                                                 0
## R3
              42000
                     10500
                              -320
                                      -1.2
                                                 0
                                            <=
## R4
              28000
                     42000
                              -520
                                        -2
                                            <=
                                                 0
## R5
              19000
                     25000
                              -350
                                      -1.2
                                            <=
                                                 0
## R6
              14000
                              -320
                     15000
                                      -0.7
                                            <=
                                                 0
## R7
                  0
                          0
                               150
                                                 1
                                         2
## Kind
                Std
                        Std
                               Std
                                       Std
## Type
               Real
                      Real
                              Real
                                      Real
## Upper
                Inf
                       Inf
                               Inf
                                       Inf
## Lower
                          0
                  0
                                 0
                                         0
solve(dmu4)
## [1] 0
get.objective(dmu4)
## [1] 3.466667
get.variables(dmu4)
## [1] 0.000000e+00 8.253968e-05 6.666667e-03 0.000000e+00
facility 5
library(lpSolveAPI)
dmu5 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU5.lp")</pre>
dmu5
## Model name:
##
                 u1
                         u2
                                ٧1
                                        v2
              19000
                     25000
                                         0
## Maximize
                                 0
## R1
              14000
                      3500
                              -150
                                      -0.2
                                            <=
                                                 0
                              -400
## R2
              14000
                     21000
                                      -0.7
                                                 0
                                            <=
## R3
              42000
                     10500
                              -320
                                      -1.2
                                            <=
                                                 0
## R4
              28000
                     42000
                              -520
                                        -2
                                            <=
                                                 0
                     25000
## R5
              19000
                              -350
                                      -1.2
                                                 0
                                            <=
## R6
              14000
                     15000
                              -320
                                      -0.7
                                            <=
                                                 0
## R7
                  0
                          0
                               350
                                       1.2
                                                 1
## Kind
                Std
                        Std
                               Std
                                       Std
## Type
               Real
                      Real
                              Real
                                      Real
```

```
## Upper
               Inf
                       Inf
                              Inf
                                     Inf
## Lower
                 0
                         0
                                0
                                        0
solve(dmu5)
## [1] 0
get.objective(dmu5)
## [1] 0.9774987
get.variables(dmu5)
## [1] 0.0000115123 0.0000303506 0.0010989011 0.5128205128
facility 6
library(lpSolveAPI)
dmu6 <- read.lp("C:\\Users\\Z\\Desktop\\QMMAssignment5\\DMU6.lp")</pre>
dmu6
## Model name:
##
                u1
                        u2
                               ٧1
                                       v2
## Maximize
             14000 15000
                                0
                                        0
## R1
             14000
                      3500
                             -150
                                     -0.2
                                               0
                                           <=
## R2
             14000
                    21000
                             -400
                                     -0.7
                                               0
                                           <=
## R3
             42000
                    10500
                             -320
                                     -1.2
                                           <=
             28000 42000
## R4
                             -520
                                       -2
                                           <=
                                               0
             19000
## R5
                    25000
                             -350
                                     -1.2
                                               0
                                          <=
## R6
             14000
                    15000
                             -320
                                    -0.7
                                           <=
                                               0
## R7
                 0
                         0
                              320
                                     0.7
                                               1
## Kind
               Std
                       Std
                              Std
                                     Std
## Type
              Real
                      Real
                             Real
                                    Real
## Upper
               Inf
                       Inf
                              Inf
                                     Inf
## Lower
                 0
                         0
                                0
                                        0
solve(dmu6)
## [1] 0
get.objective(dmu6)
## [1] 0.8674521
get.variables(dmu6)
## [1] 1.620029e-05 4.270987e-05 1.546392e-03 7.216495e-01
Benchmarking
library(Benchmarking)
```

## Warning: package 'Benchmarking' was built under R version 4.0.3

```
## Loading required package: ucminf
## Warning: package 'ucminf' was built under R version 4.0.3
## Loading required package: quadprog
## Warning: package 'quadprog' was built under R version 4.0.3
x \leftarrow matrix(c(150,400,320,520,350,320,0.2,0.7,1.2,2.0,1.2,0.7),ncol=2)
y <-
matrix(c(14000,14000,42000,28000,19000,14000,3500,21000,10500,42000,25000,150
00), ncol = 2)
colnames(y) <- c("reimbursed", "privately paid")</pre>
colnames(x) <- c("staff", "supplies")</pre>
Χ
##
        staff supplies
## [1,]
          150
                   0.2
## [2,]
          400
                   0.7
## [3,] 320
                   1.2
## [4,]
          520
                   2.0
## [5,]
          350
                   1.2
          320
                   0.7
## [6,]
У
        reimbursed privately paid
## [1,]
             14000
                              3500
             14000
                             21000
## [2,]
## [3,]
             42000
                             10500
## [4,]
             28000
                             42000
## [5,]
             19000
                             25000
## [6,]
             14000
                             15000
```

#### **DEA** analysis

```
DEA <- dea(x,y,RTS = "crs")
DEA
## [1] 1.0000 1.0000 1.0000 1.0000 0.9775 0.8675

DEA1 <- dea(x,y,RTS = "fdh")
DEA1
## [1] 1 1 1 1 1 1

DEA2 <- dea(x,y,RTS = "vrs")
DEA2
## [1] 1.0000 1.0000 1.0000 1.0000 0.8963

DEA3 <- dea(x,y,RTS = "irs")
DEA3</pre>
```

```
## [1] 1.0000 1.0000 1.0000 1.0000 1.0000 0.8963
DEA4 <- dea(x,y,RTS = "drs")
DEA4
## [1] 1.0000 1.0000 1.0000 1.0000 0.9775 0.8675
DEA5 <- dea(x,y,RTS = "add")
DEA5
## [1] 1 1 1 1 1 1
DEA6 <- dea(x,y,RTS = "vrs+")
DEA6
## [1] 1 1 1 1 1 1
DEA7 <- dea(x,y,RTS = "irs2")
DEA7
## [1] 1 1 1 1 1 1
DEA8 <- dea(x,y,RTS = "fdh+")
DEA8
## [1] 1 1 1 1 1 1
Finding peers
peers(DEA)
                NA
          2
                 NA
                       NA
          3 NA
                       NA
```

```
## peer1 peer2 peer3
## [1,] 1
## [2,]
## [3,]
        4 NA
## [4,]
                   NA
## [5,]
         1
              2
                   4
## [6,]
               2
peers(DEA1)
      peer1
##
## [1,]
          1
## [2,]
          2
## [3,]
          3
## [4,]
          4
          5
## [5,]
## [6,]
peers(DEA2)
## peer1 peer2 peer3
## [1,] 1
              NA
                    NA
## [2,] 2 NA
                   NA
```

```
## [3,] 3
                NA
                     NA
                     NA
## [4,]
           4
                NA
## [5,]
           5
                NA
                     NA
## [6,]
           1
                2
                      5
peers(DEA3)
## peer1 peer2 peer3
## [1,]
           1
               NA
                     NA
## [2,]
           2
                NA
                     NA
## [3,]
           3
                     NA
                NA
## [4,]
           4
             NA
                     NA
           5
## [5,]
                NA
                     NA
          1
               2
                     5
## [6,]
peers(DEA4)
## peer1 peer2 peer3
## [1,]
         1
               NA
                     NA
           2
                NA
                     NA
## [2,]
## [3,]
          3
                NA
                     NA
## [4,]
          4
                NA
                     NA
## [5,]
           1
               2
                     4
                2
                     4
## [6,]
           1
peers(DEA5)
## peer1
## [1,]
           1
## [2,]
           2
## [3,]
           3
           4
## [4,]
## [5,]
           5
## [6,]
           6
peers(DEA6)
## peer1
## [1,]
           1
## [2,]
           2
## [3,]
           3
           4
## [4,]
## [5,]
           5
## [6,]
peers(DEA7)
## peer1
## [1,]
           1
           2
## [2,]
## [3,]
           3
## [4,]
           4
```

```
## [5,]
## [6,]
peers(DEA8)
##
       peer1
## [1,]
           2
## [2,]
           3
## [3,]
           4
## [4,]
## [5,]
           5
## [6,]
           6
Finding lambda
lambda(DEA)
##
              L1
                        L2 L3
                                     L4
## [1,] 1.0000000 0.00000000 0 0.0000000
## [2,] 0.0000000 1.00000000 0 0.0000000
## [3,] 0.0000000 0.00000000 1 0.0000000
## [4,] 0.0000000 0.00000000 0 1.0000000
## [5,] 0.2000000 0.08048142 0 0.5383307
## [6,] 0.3428571 0.39499264 0 0.1310751
lambda(DEA1)
       L1 L2 L3 L4 L5 L6
##
## [1,] 1 0 0
                 0 0 0
                 0 0 0
## [2,] 0
          1
              0
## [3,] 0 0 1 0 0 0
## [4,] 0 0 0 1 0 0
## [5,] 0 0 0 0 1 0
## [6,] 0 0 0 0 0 1
lambda(DEA2)
##
              L1
                        L2 L3 L4
                                       L5
## [1,] 1.0000000 0.0000000 0 0 0.0000000
## [2,] 0.0000000 1.0000000 0 0 0.0000000
## [3,] 0.0000000 0.0000000 1 0 0.0000000
## [4,] 0.0000000 0.0000000 0 1 0.0000000
## [5,] 0.0000000 0.0000000 0 0 1.0000000
## [6,] 0.4014399 0.3422606 0 0 0.2562995
lambda(DEA3)
              L1
                        L2 L3 L4
## [1,] 1.0000000 0.0000000 0 0 0.0000000
## [2,] 0.0000000 1.0000000 0 0 0.0000000
## [3,] 0.0000000 0.0000000 1 0 0.0000000
```

## [4,] 0.0000000 0.0000000 0 1 0.0000000

```
## [5,] 0.0000000 0.0000000 0 0 1.0000000
## [6,] 0.4014399 0.3422606 0 0 0.2562995
lambda(DEA4)
##
             L1
                      L2 L3
## [1,] 1.0000000 0.00000000 0 0.0000000
## [2,] 0.0000000 1.00000000 0 0.0000000
## [3,] 0.0000000 0.00000000 1 0.0000000
## [4,] 0.0000000 0.00000000 0 1.0000000
## [5,] 0.2000000 0.08048142 0 0.5383307
## [6,] 0.3428571 0.39499264 0 0.1310751
lambda(DEA5)
      L1 L2 L3 L4 L5 L6
##
## [1,] 1 0 0 0 0
                     0
## [2,] 0
         1 0 0 0
                     0
## [3,] 0 0 1 0 0 0
## [4,] 0 0 0 1 0 0
## [5,] 0 0 0 0 1 0
## [6,] 0 0 0 0 0 1
lambda(DEA6)
      L1 L2 L3 L4 L5 L6
##
## [1,] 1 0 0 0 0
                     0
## [2,] 0 1 0
## [3,] 0 0 1 0 0 0
## [4,] 0 0 0 1 0 0
## [5,]
      0 0 0 0 1 0
## [6,] 0 0 0 0 0 1
lambda(DEA7)
## L1 L2 L3 L4 L5 L6
## [1,] 1 0 0 0 0
## [2,]
       0
         1
             0
               0 0
                     0
## [3,] 0 0 1 0 0 0
## [4,] 0 0 0 1 0 0
## [5,] 0 0 0 0 1 0
## [6,]
      0
lambda(DEA8)
##
      L1 L2 L3 L4 L5 L6
## [1,] 1 0 0 0 0
                     0
## [2,]
       0
          1
            0
               0 0
                    0
## [3,]
       0
          0
            1
               0 0
## [4,]
       0 0 0
               1 0 0
## [5,] 0 0 0 0 1
## [6,] 0 0 0 0 0 1
```

## Compare and contrast the above results

->constant return to scale method results indicates that DMU 1,2,3,4 are efficient. ->DMU 4 is 0.9777 efficient and DMU 5 is 0.8675 efficient. ->Free Disposability Hull)—> All DMUs are efficient. VRS(variable returns to scale) —>DMU 1,2,3,4,5 are efficient and DMU 6 is 0.8963 efficient. IRS(Increasing return to scale) ->DMU 1,2,3,4,5 are efficient and DMU 6 is 0.8963 efficient. DRS(decreasing return to scale) —>DMU 1,2,3,4 are efficient ,DMU 5 is 0.9775 efficient and DMU 6 is 0.8963 efficient. FRH/Add (Free replicability hull) —> All DMUs are efficient