# Tracing the refractive index profile of a multiplering two-mode fiber by analyzing modal interference feedback

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Abstract—We present a methodology to trace the refractive index profile of a multiple-ring two-mode fiber by analyzing modal interference, serving for exploring specialized applications in the optical communication area.

Keywords—few-mode fiber, modal interference, fiber modes

## I. INTRODUCTION

Few-mode fiber (FMF) plays an important role in the area of large capacity optical transmission, optical fiber sensing, optical imaging, and signal processing [1]-[4]. FMF, which can provide several independent channels by the use of guide modes in a single optical fiber, has been explored to support several times of the transmission capacity comparing with a standard single-mode fiber (SMF) via the mode division multiplexing (MDM) technology [5]. In an MDM system, optical components, such as mode multiplexers [6], mode converters [7], and mode filters [8], are building blocks of the MDM transmission frame. However, the accurate parameters of an FMF are essential to be known to predict and analyze its behavior or characteristics. By knowing the detailed information of an unknown FMF, we can further develop the FMF to work as an all-fiber functional optical device [9].

In this paper, we propose a methodology to deduce the refractive index profile of a multiple-ring two-mode fiber (TMF). According to the experimental results, we reproduce the parameters of the multiple-ring TMF by using modal interference and finite element method (FEM)-based calculation. The approach can be developed to serve as inline fiber quality qualification system, and offers key proofs of special fibers before they are utilized to develop as functional components.

#### II. METHODOLOGY AND OPERATION PRINCIPLE

There are many instruments that can test a special fiber by measuring the material compositions, profiles, and defects. However, the cost of the instruments is usually expensive. Here, we present a simple optical method to search the refractive index profile of a multiple-ring TMF by the use of modal interference and FEM-based calculation.

The modal interference is achieved via the lateral-offset aligning of a multiple-ring TMF with two SMFs. A schematic diagram of lateral-offset aligning is shown in Fig.1, where a segment of multiple-ring TMF is sandwiched between two SMFs with the same lateral-offset direction of the fiber ends.

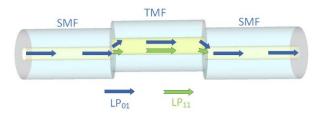


Fig. 1. Schematic diagram of the proposed lateral-offset aligning of a segment of multiple-ring TMF with two SMFs.

When broadband light is launched into the multiple-ring TMF from one end of SMF (labels as the first lateral-offset point), part of the LP $_{01}$  mode is excited and converted to be the LP $_{11}$  mode in the multiple-ring TMF. Then the LP $_{01}$  mode and the LP $_{11}$  mode arrive at the entrance of the other SMF (labels as the second lateral-offset point). Interference fringes that contribute by the LP $_{01}$  mode and the LP $_{11}$  mode occur. Output light intensity ( $\it{I}$ ) against the wavelength can be express as

$$I = I_{LP_{01}} + I_{LP_{11}} - 2\sqrt{I_{LP_{01}}I_{LP_{11}}}cos(\Delta\varphi)$$
 (1)

where  $I_{LP_{01}}$  and  $I_{LP_{11}}$  are the light intensities of the LP<sub>01</sub> mode and the LP<sub>11</sub> mode;  $\Delta \varphi$  is the phase difference, which can be given as:

$$\Delta \varphi = \frac{2\pi}{3} \Delta n_{eff} L \tag{2}$$

where  $\lambda$  is the central wavelength,  $\Delta n_{eff}$  is the effective refractive index difference of the LP<sub>01</sub> mode and the LP<sub>11</sub> mode, L is the length of the multiple-ring TMF. When the phase difference satisfies the condition of  $\Delta \varphi = (2m+1)\pi$  with m of an integer, minimum output light intensity is achieved,

which is defined as resonant dip at specific wavelength. The wavelength range between the adjacent resonant dips is called free spectra range (FSR), which can be approximately expressed as

$$FSR = \frac{\lambda^2}{\Delta n_{eff}L} \tag{3}$$

It is obvious in Eq. (3) that the longer the length of multiple-ring TMF, the smaller FSR will be. As a result, more accurate effective index difference between the LP<sub>01</sub> mode and the LP<sub>11</sub> mode will be obtained with a longer multiple-ring TMF. By knowing the accurate effective index difference between the LP<sub>01</sub> mode and the LP<sub>11</sub> mode, we can reproduce or prove the refractive index profile of the multiple-ring TMF. We both carry out the experiment and simulation to support this point in the following sections.

#### III. RESULTS AND DISCUSSION

First, we captured the cross-section of the multiple-ring TMF by using optical microscope, which is shown in Fig. 2. Here, the radius of core is labeled as R1, the radius of the ring 1 and ring 2 are labeled as R2 and R3, respectively, and the radius of cladding is labeled as R4.

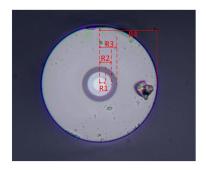


Fig. 2. The cross-section of the multiple-ring TMF captured by an optical microscope.

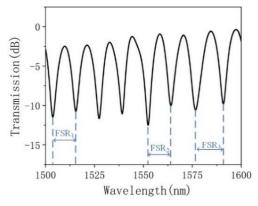


Fig. 3. Transmission spectrum generated by lateral-offset aligning a 35.4cm-length multiple-ring TMF with two SMFs.

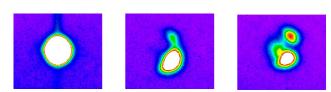


Fig. 4. Near field patterns captured by infrared CCD with the lateral-offset value increasing to confirm the modal interference of the  $LP_{01}$  mode and the  $LP_{11}$  mode.

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We use a segment of the multiple-ring TMF with a length of 35.4 cm in the experimental study. We build an experimental setup to support the generation of modal interference fringes with the multiple-ring TMF, two SMFs, broadband light source, and optical spectrum analyzer (OSA). The measured transmission spectrum is shown in Fig. 3. The FSR increases when the resonant dip of the wavelength operates at the infrared area. Three FSRs are labeled in the figure, which are FSR<sub>1</sub>, FSR<sub>2</sub> and FSR<sub>3</sub>. The values of the FSR<sub>1</sub>, FSR<sub>2</sub> and FSR<sub>3</sub> are about 11.81 nm, 13.12 nm, and 13.84 nm, respectively.  $\Delta n_{\rm eff}$  is deduced to be about 5.792 X  $10^{-4}$  at the wavelength of 1558 nm.

To confirm the interference fringes is generated by the modal interference of the  $LP_{01}$  mode and the  $LP_{11}$  mode. Near filed pattern from the output end of the multiple-ring TMF is captured by an infrared CCD. As shown in Fig. 4, with the lateral-offset value increasing, the mode filed of the  $LP_{11}$  mode becomes clearer at the wavelength of the resonant dip.

To study the model of such kind of fiber, we use finiteelement method (FEM)-based commercial software COMSOL to analyze the modal dispersion of the multiplering TMF. The initial parameters of the multiple-ring TMF are given in the follow, where the core radius (R1), the ring 1 radius (R2), the ring 2 radius(R3) and the cladding radius(R4) are about 7.0  $\mu$ m, 13.0  $\mu$ m, 19.0  $\mu$ m and 62.5  $\mu$ m, respectively, and the refractive index of core, ring 1, ring 2, and the cladding are 1.4485, 1.444, 1.435336 and 1.444, respectively. In the simulation, the modal dispersion curve is shown in Fig. 5(a), where the effective index difference of the LP<sub>01</sub> mode and the LP<sub>11</sub> mode is calculated to be about  $1.99 \times 10^{-3}$  at the wavelength of 1550 nm, which is shown in Fig. 5(b). The simulation is far from the experimental one, and there should be some deviations among the fiber parameters above.

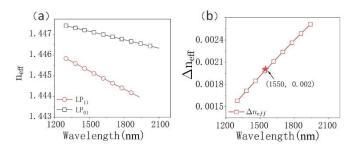


Fig. 5. (a) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the wavelength; (b) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode.

To figure out which parameter that affect the modal dispersion of the multiple-ring TMF, we use elimination process to find out the key parameter of the fiber. In the fiber structure, we learn that the core radius and core refractive index, and the ring 1 radius and the ring 1 refractive index would be the key factors.

According to the provided fiber parameters, firstly, we fix other parameters of the multiple-ring TMF and only change the core refractive index. As shown in Fig. 6(a), the effective index of the  $LP_{01}$  mode and the  $LP_{11}$  mode increases with the core refractive index at the wavelength of 1550 nm. The increasing of the effective index of the  $LP_{01}$  mode is faster than the  $LP_{11}$  mode, which is shown in the

effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode in Fig. 6(b). Then we fix other parameters of the multiple-ring TMF and only change the core radius. As shown in Fig. 6(c), the effective index of the  $LP_{01}$  mode and the  $LP_{11}$  mode increases with the core radius at the wavelength of 1550 nm. However, the increasing of the effective index of the  $LP_{11}$  mode is faster than the  $LP_{01}$  mode, which is shown in the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode in Fig. 6(d).

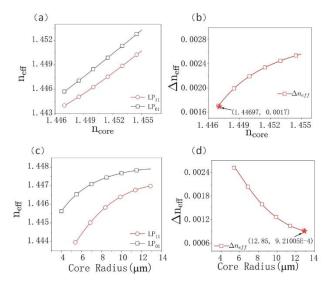


Fig. 6. (a) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the core refractive index; (b) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode. (c) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the core radius; (d) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode.

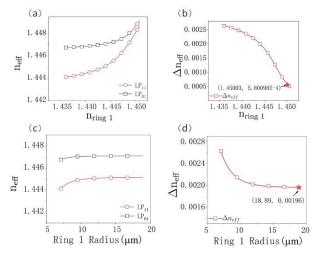


Fig. 7. (a) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the ring 1 refractive index; (b) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode. (c) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the ring 1 radius; (d) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode.

Later, we fix other parameters of the multiple-ring TMF and only change the ring 1 refractive index. As shown in Fig. 7(a), the effective index of the  $LP_{01}$  mode and the  $LP_{11}$  mode increases with the ring 1 refractive index at the wavelength of 1550 nm. However, the increasing of the effective index of the  $LP_{11}$  mode is faster than the  $LP_{01}$  mode, which is shown in the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode in Fig. 7(b). Finally, we fix other parameters

of the multiple-ring TMF and only change the ring 1 radius. As shown in Fig. 7(c), the effective index of the  $LP_{01}$  mode and the  $LP_{11}$  mode increases with the ring 1 radius at the wavelength of 1550 nm. However, the increasing of the effective index of the  $LP_{11}$  mode is faster than the  $LP_{01}$  mode, which is shown in the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode in Fig. 7(d).

By systematically analyzing the fiber parameters variation characteristics, we select a group of fiber parameters that matches the trend of the experimental results. The combination of the parameters of the multiple-ring TMF are settled as follow. The core radius, the ring 1 radius, the ring 2 radius, and the cladding radius are about 8  $\mu m$ , 16  $\mu m$ , 21  $\mu m$  and 62.5  $\mu m$ , respectively, and the refractive index of core, ring 1, ring 2, and the cladding are 1.4485, 1.44867, 1.435336 and 1.444, respectively. In the simulation, the modal dispersion curve is shown in Fig. 8(a), where the effective index difference of the LP01 mode and the LP11 mode is calculated to be about 5.8044  $\chi$  10<sup>-4</sup> at the wavelength of 1550 nm, which is shown in Fig. 8(b). The simulation results are well fitting with the experimental one.

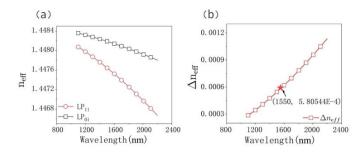


Fig. 8. (a) Effective indices of the  $LP_{01}$  mode and the  $LP_{11}$  mode against the wavelength; (b) the effective index difference of the  $LP_{01}$  mode and the  $LP_{11}$  mode.

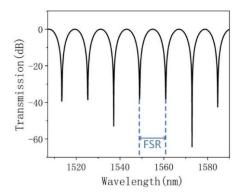


Fig. 9. Transmission spectrum generated by lateral-offset aligning a 35.4cm-length multiple-ring TMF with two SMFs in the simulation.

Finally, we simulate the transmission spectrum by using Eq. (1). As shown in Fig. 9, the transmission spectrum of the two-mode interference by the multiple-ring TMF length with a fiber length of 35.4 cm. The effective index difference of the LP<sub>01</sub> mode and the LP<sub>11</sub> mode is  $5.753 \times 10^{-4}$  at the wavelength of 1548nm with the FSR = 12 nm, which agrees with the experiment result of  $5.792 \times 10^{-4}$ .

# IV. CONCLUSION

We demonstrate a method to trace the refractive index profile of a multiple-ring TMF by using modal interference feedback, which can be extended to analyze all types of TMF and FMF. The method is simple and easily to carry out, which can be developed as an algorithm in the fiber analysis system.

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