

Graph theory

Course Outline

1. Basic Concept of Graph

- 1.1 Basic concepts of Graphs
- 1.2 Directed and Undirected graphs
- 1.3 Basic terminologies
- 1.4 Degree of a vertex
- 1.5 Isolated and pendent vertices
- 1.6 Handshaking Theorem
- 1.7 Types of graphs
- 1.8 Subgraphs
- 1.9 Graphs isomorphism

2. Connected and disconnected Graph

- 2.1 Connected and disconnected graphs
- 2.2 Path and cycle graphs
- 2.3 Rank and Nullity
- 2.4 Walk, Path and Circuits

3. Matrix Representation of Graph (Matrix Notation of Graph)

- 3.1 Adjacency Matrices
- 3.2 Reachability Matrices

4. Euler Diagram and Hamilton Diagram

- 4.1 Euler Diagram
- 4.2 Hamilton Diagram

5. Trees and Spanning Trees (with applications)

- 5.1 Undirected Trees
- 5.3 Directed Trees
- 5.2 Spanning Trees and Minimal Spanning Trees

6. Shortest Path Problems

- 6.1 Two Shortest Path Algorithm
- 6.2 The Steiner Network Problem

Modern Algebra

1. Binary Operations and Their Properties

- 1.1 Binary operations
- 1.2 Properties of operations
- 1.3 Special elements in a set with one binary operation

2. Groups and Subgroups

- 2.1 The concept of group
- 2.2 The properties of groups
- 2.3 Subgroups

3. Algebraic systems

4. Euler's theorem & Lagrange's Theorem

5. Abelian (commutative) groups and cyclic groups

- 5.1 Abelian (Commutative) Groups
- 5.2 Cyclic Groups
- 5.3 Permutation group

6. Homomorphism and Isomorphism of Algebraic Systems

7. Rings and Fields

- 7.1 Rings
- 7.2 Fields

Recommended Books:

1. Graph Theory with Applications to Engineering and Computer Science by Narsingh Deo, 1st Edition.
2. Graphs and Matrices by Ravindra B. Bapat, 2nd Edition.
3. Modern Algebra: An Introduction by John R. Durbin, 6th Edition.