



University  
of Glasgow

# Digital Control 4/M

ENG4042-ENG5022

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**WORLD  
CHANGERS  
WELCOME**

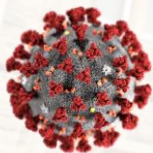




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# Digital Control

- Welcome!
- Another (mostly) online academic year



# What's your **biggest concern** for this semester (online learning)?

☐

Quality of online classes

☐

Technology issues (Zoom, internet connection not working, etc.)

☐

Lack of campus experience and social interactions

☐

Falling behind / Not keeping up with class pace

☐

Other: .....



# What's the biggest **advantage/opportunity** of online learning?

☐

Can do it from my home/where I am

☐

Can (re-)play recorded lectures/classes at my own pace

☐

Can use technology (online resources, electronic notes, etc.)

☐

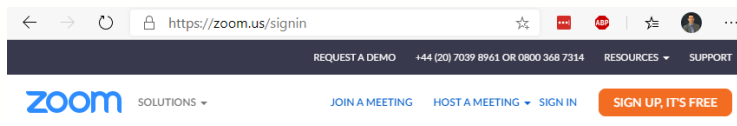
Other: .....

# Zoom etiquette

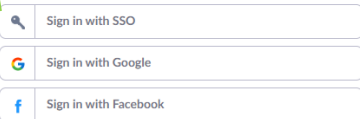
- Mute yourself when not talking
  - Limit background noise
- Turn on your webcam if you have one
- Use the “raise your hand” function
- Use the chat for non-urgent questions and general discussion
  - Keep it in English and be polite: everyone can read



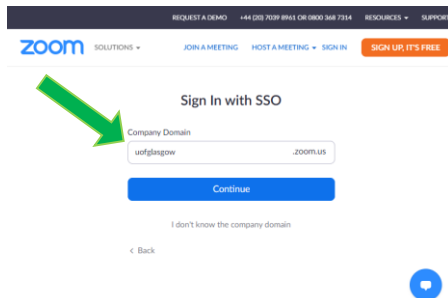
# Zoom UofG login



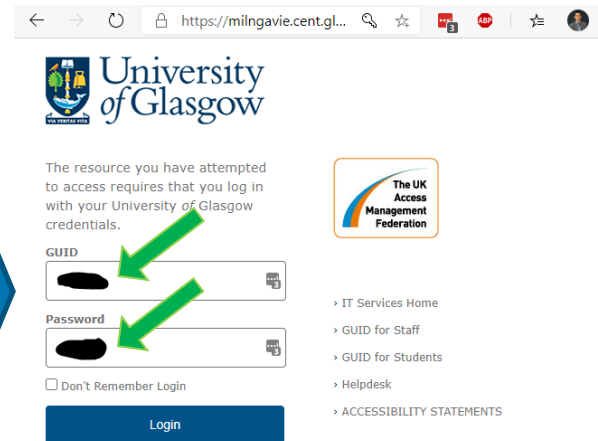
Sign In

The image shows the standard Zoom sign-in form with fields for 'Email Address', 'Password', and 'Captcha Code'. A large red 'X' is drawn over the entire form, indicating that this method is not the correct one for University of Glasgow users. Below the form is a blue 'Sign In' button. At the bottom, there is a checkbox for 'Stay signed in' and a link for 'New to Zoom? Sign Up Free'.A green arrow points from the bottom left of the Zoom sign-in page to this section. It contains three buttons: 'Sign in with SSO' (with a magnifying glass icon), 'Sign in with Google' (with the Google logo), and 'Sign in with Facebook' (with the Facebook logo).

Sign in with SSO

The image shows the 'Sign in with SSO' page. It has a 'Company Domain' field with 'uofglasgow' entered and '.zoom.us' in the dropdown. A blue 'Continue' button is below the field. A link 'I don't know the company domain' is at the bottom. A green arrow points from the 'Sign in with SSO' button on the previous page to this field.

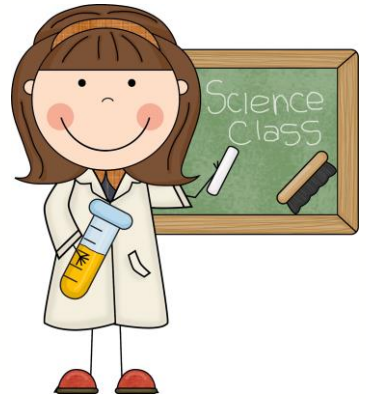
Domain: uofglasgow

The image shows the University of Glasgow login page. It features the university's crest and name. A message states: 'The resource you have attempted to access requires that you log in with your University of Glasgow credentials.' Below this are fields for 'GUID' and 'Password', each with a green arrow pointing to it. There is a 'Don't Remember Login' checkbox and a blue 'Login' button. On the right, there is a logo for 'The UK Access Management Federation' and a list of links: 'IT Services Home', 'GUID for Staff', 'GUID for Students', 'Helpdesk', and 'ACCESSIBILITY STATEMENTS'. A green arrow points from the 'Continue' button on the Zoom page to the 'GUID' field.

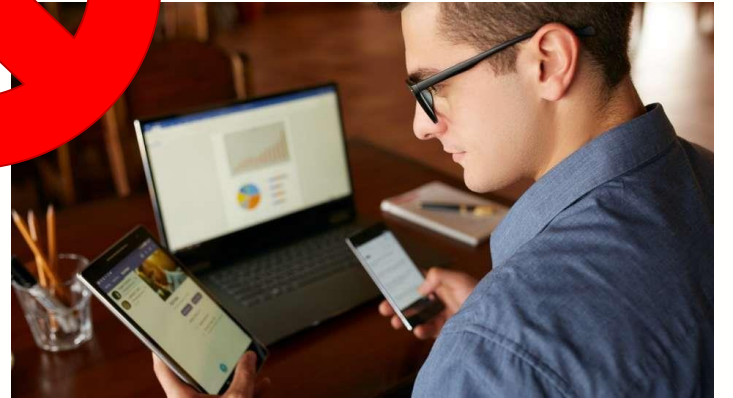
GUID & password

# Format of teaching

- **Recorded lectures**
  - Cover all course, theoretical background, lecture notes
- +
- **Live sessions (Zoom)**
  - Q&A, examples, numerical exercises, tutorials, past exam papers, etc.
  - Flexible
- **2 Live tutorial sessions (Zoom)**
  - Weeks 9~10
  - Past exam papers, Q&A, etc.
- + Experimental laboratory for ENG5022
- Feedback welcome



# How should I watch pre-recorded lectures?





# How should I watch pre-recorded lectures?

- Allocate time for watching lecture videos
- Focus on the lecture only, video in full-screen, notifications off
- Other online devices (phone) out of reach
- Take notes, as if you were in a lecture
- Take a break when you need to
  - Do not carry watching if you can't focus
  - You do not have to watch a whole section at once
- Do it at a time that is convenient for you



# Why pre-recorded lectures?

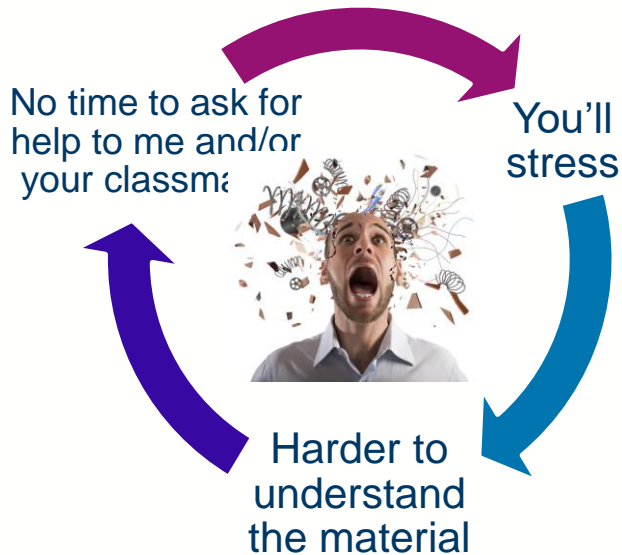
- Fail-safe solution, in these uncertain times
  - Internet connection fail, illness, ...
- Teaching via Zoom takes longer
- In my experience (8+ years), I have received very few questions while lecturing
  - Most questions were due to my own mistake explaining!
- You can (re-)watch & learn at a time convenient for **you**
- Frees live class time (Zoom) for Q&A, interactive activities, numerical examples, solutions of tutorial questions, past exam papers, ...
- Cover entire lecture notes



# The warning

- **Do not procrastinate**
- Pre-recorded video lectures will be available until the end of term but:
  - The interactive live classes will be meaningless if you have not followed the video lectures beforehand

• If you cram during revision week:



Therefore, you should **promise to yourself now** that  
you'll watch the lectures week by week



“Sign” here



# Resources: Moodle

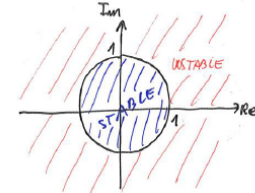
<https://moodle.gla.ac.uk/course/view.php?id=21118>

- Full lecture notes
- Forum
  - Please use it for any course-related question – I will answer there
- Reading list (core textbook available in PDF through library)
- Practice exercises (will go live later)
- Past exam papers
- Feedback form: let me know anonymously



# Lecture notes

- Available on Moodle in full right now
- Cover all theoretical material of the course
- Exercises showing applications to real-world problems and practice for exam
  - Do try them by yourself or with your mates (adhere to COVID restrictions)!
- References to related textbook sections



The equation found substituting  $u_k \rightarrow z^k$  is called the characteristic equation, and is a polynomial in  $z$ :

$$u_k = u_{k-1} + u_{k-2}$$
$$\Downarrow$$
$$z^k = z^{k-1} + z^{k-2} \quad \text{Characteristic Equation}$$

The roots of this equation determine the stability of the  $\Delta E$ . If the magnitude of all roots  $< 1$ ,  $\Delta E$  is stable.

### Exercise 8 Stability of autonomous difference equation

Determine the stability of  $u_k = 0.9u_{k-1} - 0.2u_{k-2}$ .

- [1] 4.1
- [2] 2.2

### 2.4 Difference equations with input: Numerical Integration

We now move on to difference equations with an input,  $e$ . As an example, let us consider the case of numerical integration.

Given a continuous signal  $e(t)$ , we want to approximate with a  $\Delta E$ :

$$I = \int_0^t e(t) dt$$

Using only the values  $e(0), e(t_1), \dots, e(t_{k-1}), e(t_k)$ .

$$e(k)$$



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# Assessment

## ENG5022

- **Coursework (10%)**
  - Design a controller for servo-motor
  - Remote-controlled (TBC)
  - Quiz on Moodle + Report
  - 3 groups with different timing, check your timetable/Moodle
- **Final (90%)**
  - Online (timed (?) 2 hours)
  - Theory + Numerical exercises

## ENG4042

- **Final (100%):**
  - Online (timed (?) 2 hours)
  - Theory + Numerical exercises

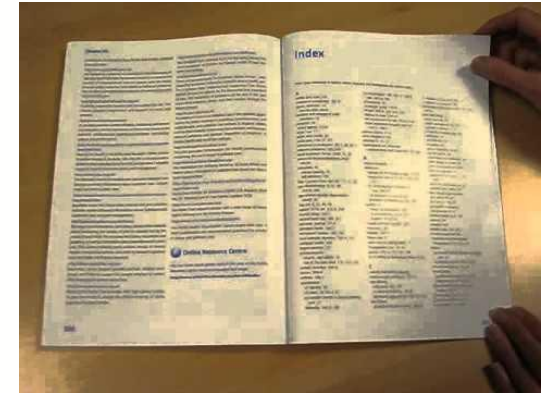
# Prerequisites

- Basics of continuous-time dynamical systems
- Laplace transform, frequency domain
- Meaning of Transfer Function, Poles, Zeros, etc.
- Continuous-time control system theory
  - Basics of feedback control design: root locus, Nyquist plot
- Fundamentals of MATLAB/Simulink
  - Optional for ENG4042 (but highly advised)
  - Compulsory ENG5022 (due to experimental coursework)
    - “On ramp” courses with certificate



# Contents of the course

1. Review of Continuous/Analogue Systems and Control
2. Introduction to Digital Control
3. Z-transform and Discrete Transfer Function
4. Signal Analysis and Dynamic Response
5. Modelling of Systems with Digital Control
6. Stability
7. Design of digital controllers
8. Sampled-data systems

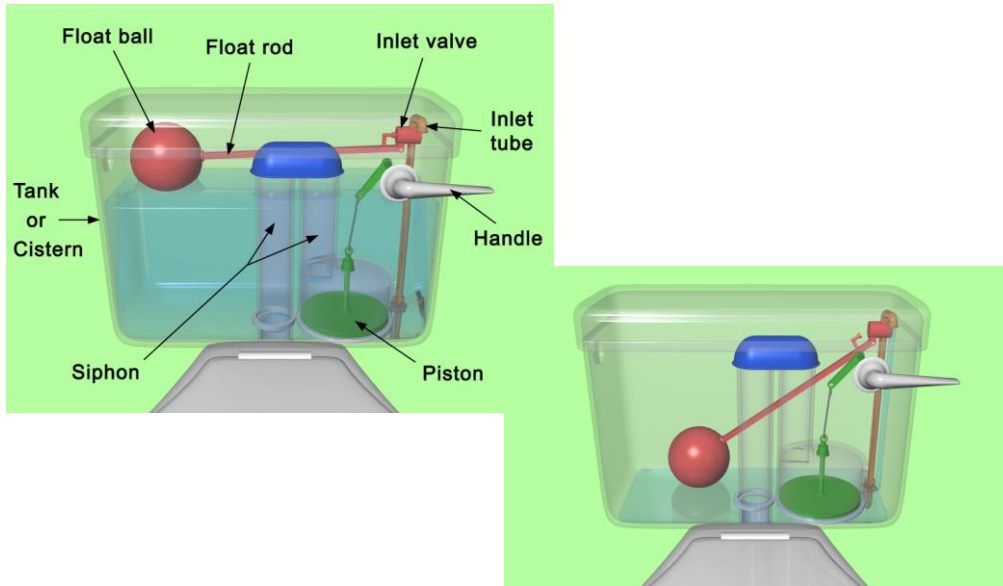


# Analogue control systems

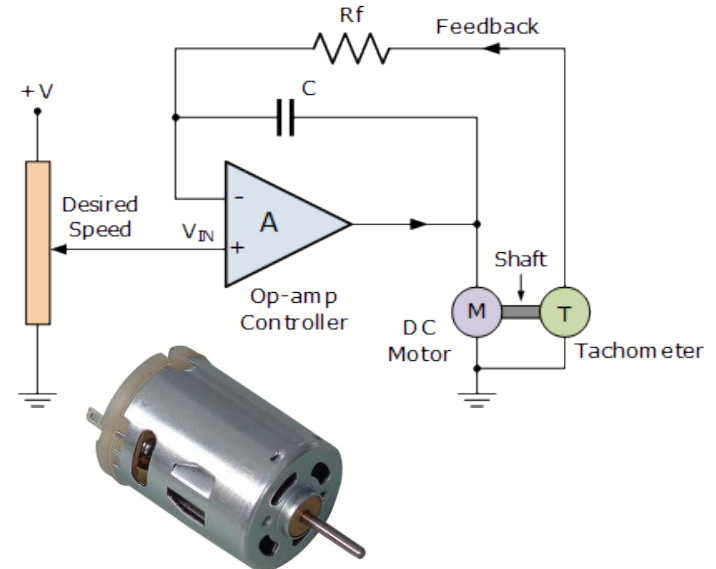
All signals are real-valued and continuous in time



## Mechanical

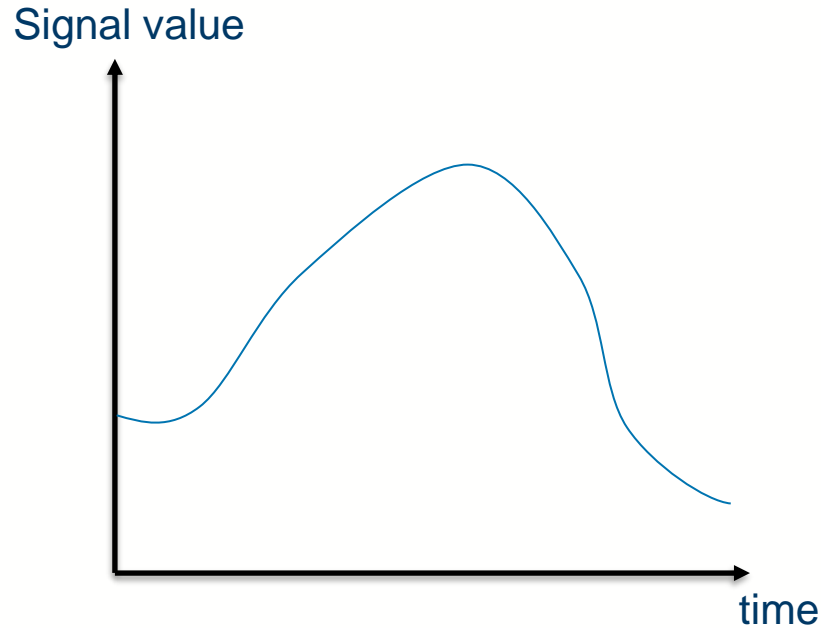


## Electric/electronic

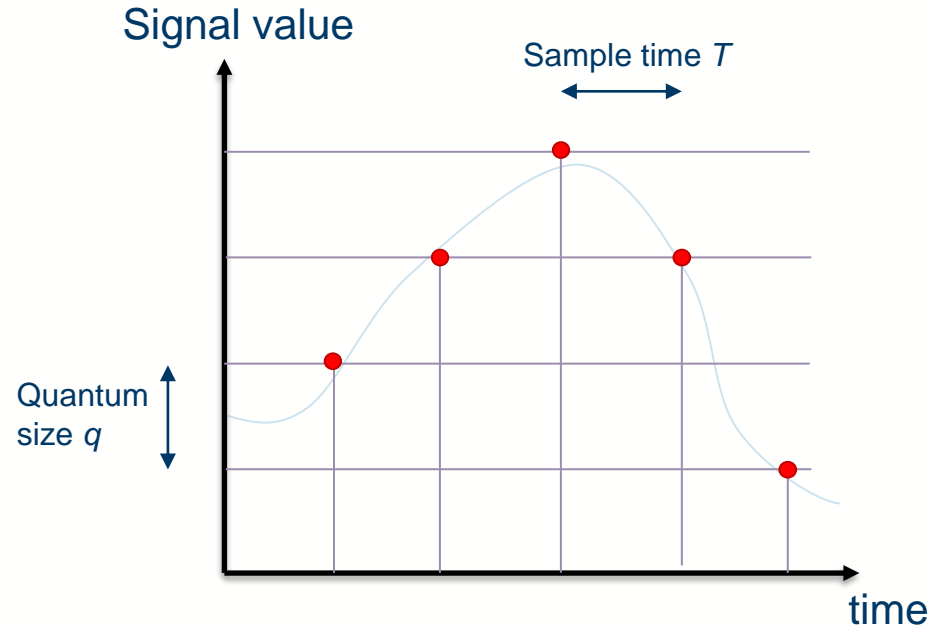




## Continuous (analogue)



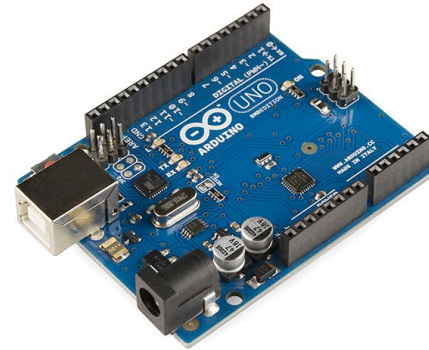
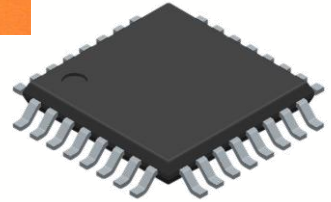
## Digital (discrete and quantised)



# Why digital control (-lers)?

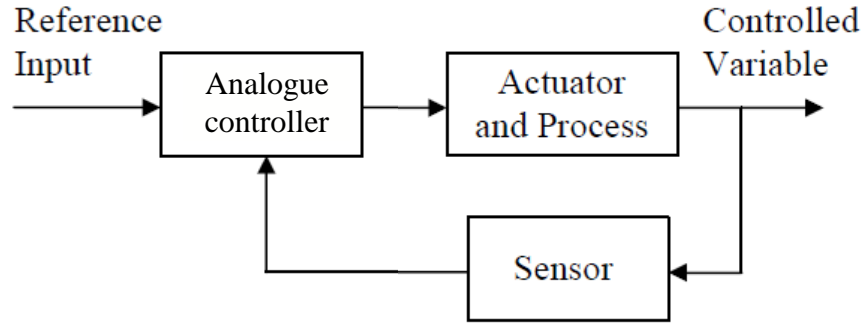
## Advantages

- Flexibility
- Multi-tasking
- Resilience to noise
- Cost
- Volume/Mass
- Depending on hardware:
  - Accuracy
  - Implementation errors
  - Speed

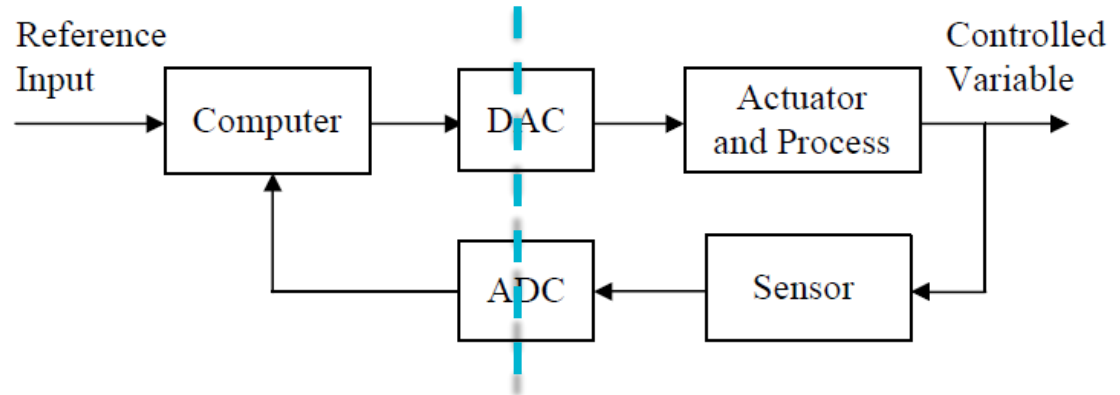


# Feedback control systems

**Analogue:**

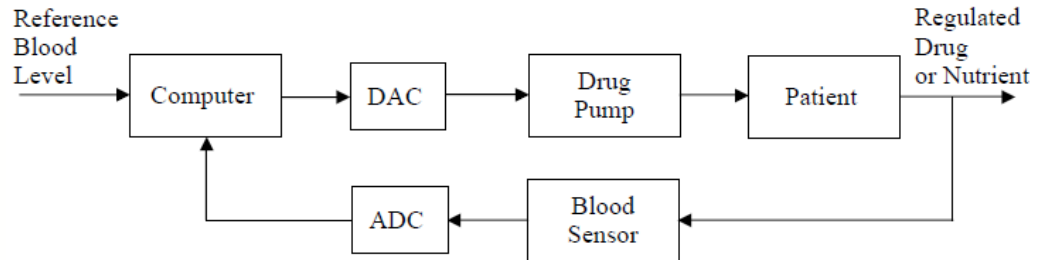
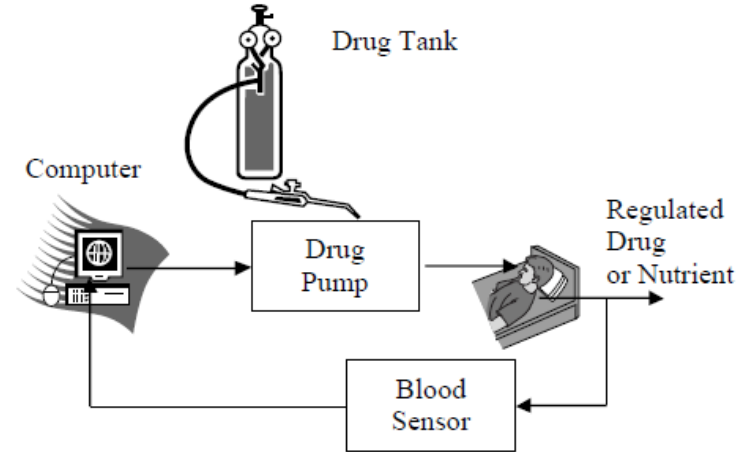


**Digital:**



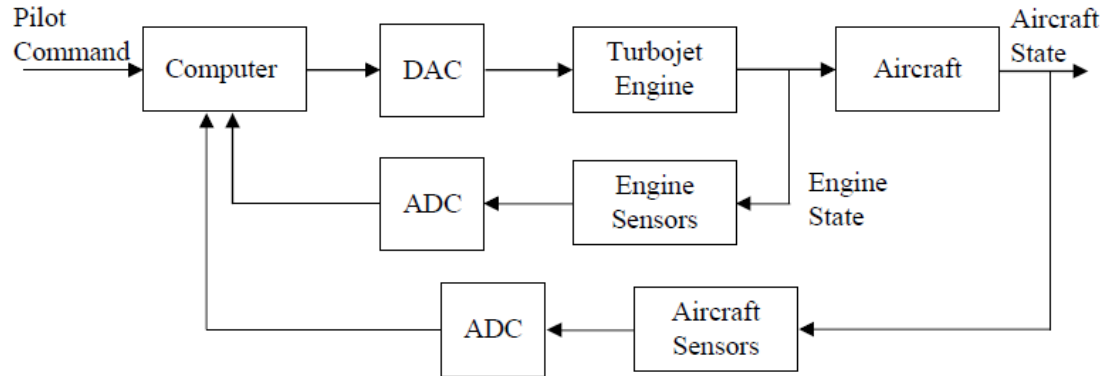
# Examples of digital controllers

## Drug-delivery devices (e.g. insulin)



# Examples of digital controllers

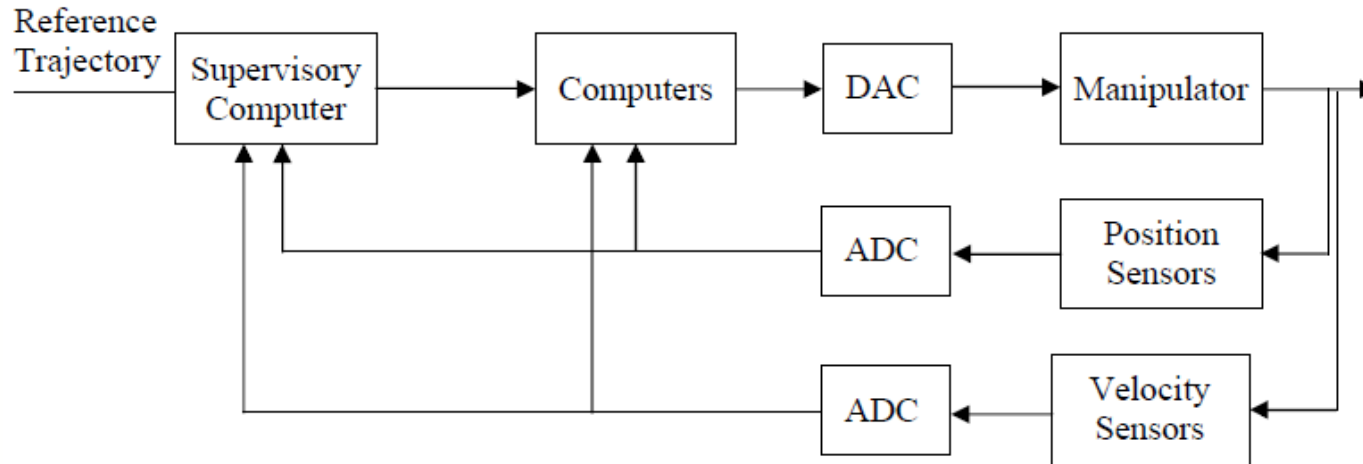
## Aircraft turbojet engine control system





# Examples of digital controllers

## Robotic manipulator



# Homework

- Watch pre-recorded video lectures:
- **00 – Introduction**
- **01 – Review of continuous systems**
- **02 – Introduction to digital control**
- Take your own notes
- Write down questions/issues/sticky points
  - Discuss on these next week





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## Digital Control

- I have done our best for delivering the usual UofG teaching experience
- Feedback on online learning welcome

**I hope that you'll enjoy this course  
and the rest of your studies!**

**STAY SAFE!**





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# Thank you and good luck!

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