

# Chapter 10

## And, Finally...

## The Stack

# Stack: An Abstract Data Type

An important abstraction that you will encounter in many applications.

We will describe three uses:

## Interrupt-Driven I/O

- The rest of the story...

## Evaluating arithmetic expressions

- Store intermediate results on stack instead of in registers

## Data type conversion

- 2's comp binary to ASCII strings

# Stacks

**A LIFO (last-in first-out) storage structure.**

- The **first** thing you put in is the **last** thing you take out.
- The **last** thing you put in is the **first** thing you take out.

**This means of access is what defines a stack, not the specific implementation.**

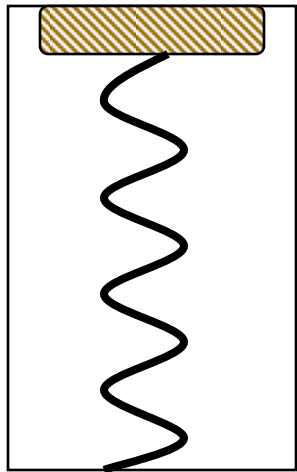
**Two main operations:**

**PUSH:** add an item to the stack

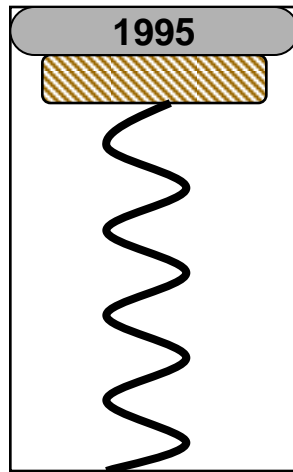
**POP:** remove an item from the stack

## A Physical Stack

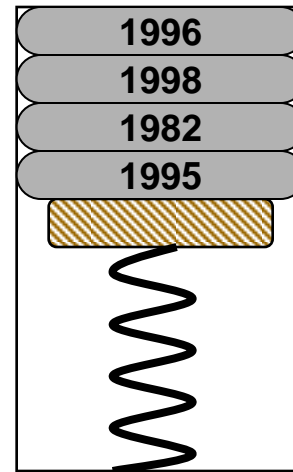
### Coin holder in the armrest of an automobile



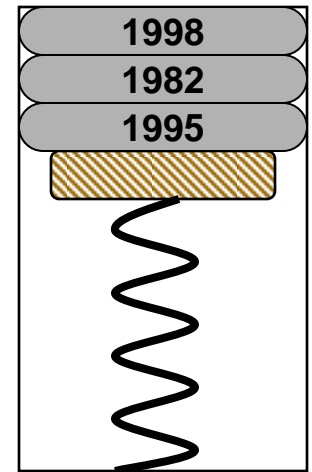
Initial State



After  
One Push



After Three  
More Pushes

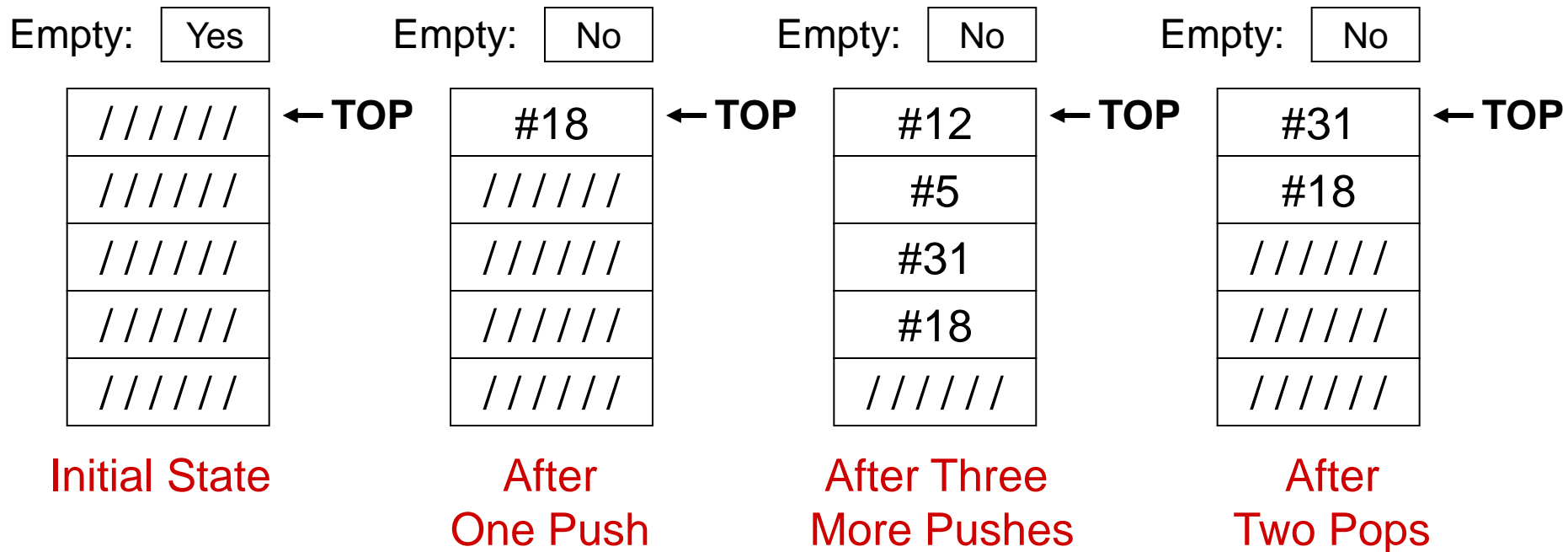


After  
One Pop

**First quarter out is the last quarter in.**

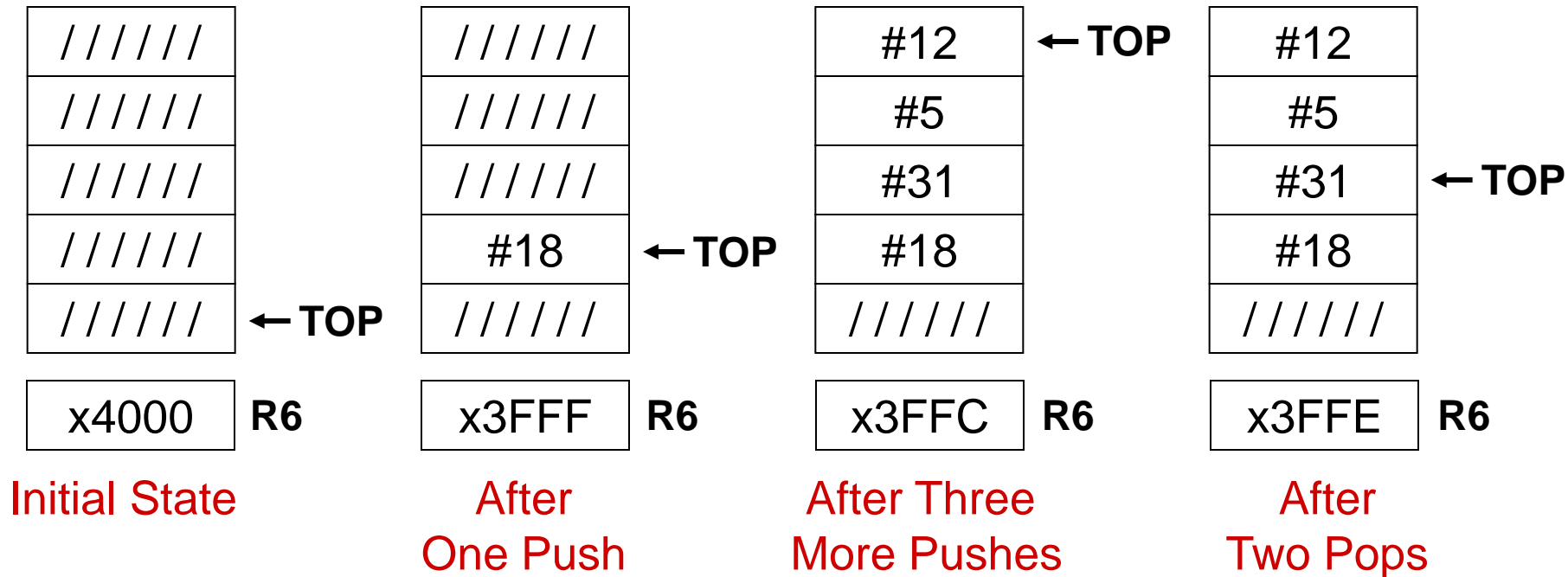
# A Hardware Implementation

## Data items move between registers



## A Software Implementation

Data items don't move in memory,  
just our idea about where the TOP of the stack is.



By convention, R6 holds the Top of Stack (TOS) pointer.

## Basic Push and Pop Code

For our implementation, stack grows downward  
(when item added, TOS moves closer to 0)

### Push

```
ADD    R6, R6, #-1    ; decrement stack ptr
STR    R0, R6, #0     ; store data (R0)
```

### Pop

```
LDR    R0, R6, #0     ; load data from TOS
ADD    R6, R6, #1     ; increment stack ptr
```

## Pop with Underflow Detection

If we try to pop too many items off the stack, an **underflow** condition occurs.

- Check for underflow by checking TOS before removing data.
- Return status code in R5 (0 for success, 1 for underflow)

```
POP      LD    R1, EMPTY    ; EMPTY = -x4000
          ADD  R2, R6, R1    ; Compare stack pointer
          BRz  FAIL          ; with x4000
          LDR  R0, R6, #0
          ADD  R6, R6, #1
          AND  R5, R5, #0    ; SUCCESS: R5 = 0
          RET
FAIL     AND  R5, R5, #0    ; FAIL: R5 = 1
          ADD  R5, R5, #1
          RET
EMPTY    .FILL xC000
```



## Push with Overflow Detection

If we try to push too many items onto the stack, an **overflow** condition occurs.

- Check for underflow by checking TOS before adding data.
- Return status code in R5 (0 for success, 1 for overflow)

```
PUSH  LD  R1, MAX      ; MAX = -x3FFB
      ADD R2, R6, R1    ; Compare stack pointer
      BRz FAIL         ; with x3FFB
      ADD R6, R6, #-1
      STR R0, R6, #0
      AND R5, R5, #0    ; SUCCESS: R5 = 0
      RET
FAIL  AND R5, R5, #0    ; FAIL: R5 = 1
      ADD R5, R5, #1
      RET
MAX   .FILL xC005
```

## Interrupt-Driven I/O (Part 2)

**Interrupts were introduced in Chapter 8.**

- 1. External device signals need to be serviced.**
- 2. Processor saves state and starts service routine.**
- 3. When finished, processor restores state and resumes program.**

*Interrupt is an unscripted subroutine call, triggered by an external event.*

**Chapter 8 didn't explain how (2) and (3) occur, because it involves a **stack**.**

**Now, we're ready...**

## Processor State

What state is needed to completely capture the state of a running process?

### Processor Status Register

- Privilege [15], Priority Level [10:8], Condition Codes [2:0]



### Program Counter

- Pointer to next instruction to be executed.

### Registers

- All temporary state of the process that's not stored in memory.

## **Supervisor Stack**

**A special region of memory used as the stack for interrupt service routines.**

- **Initial Supervisor Stack Pointer (SSP) stored in Saved.SSP.**
- **Another register for storing User Stack Pointer (USP): Saved.USP.**

**Want to use R6 as stack pointer.**

- **So that our PUSH/POP routines still work.**

**When switching from User mode to Supervisor mode (as result of interrupt), save R6 to Saved.USP.**

## Invoking the Service Routine – The Details

1. If **Priv = 1** (user),  
    **Saved.USP = R6**, then **R6 = Saved.SSP**.
2. Push **PSR** and **PC** to Supervisor Stack.
3. Set **PSR[15] = 0** (supervisor mode).
4. Set **PSR[10:8]** = priority of interrupt being serviced.
5. Set **PSR[2:0] = 0**.
6. Set **MAR = x01vv**, where **vv** = 8-bit interrupt vector provided by interrupting device (e.g., keyboard = x80).
7. Load memory location (**M[x01vv]**) into **MDR**.
8. Set **PC = MDR**; now first instruction of **ISR** will be fetched.

**Note:** This all happens between the **STORE RESULT** of the last user instruction and the **FETCH** of the first **ISR** instruction.

## Returning from Interrupt

**Special instruction – RTI – that restores state.**

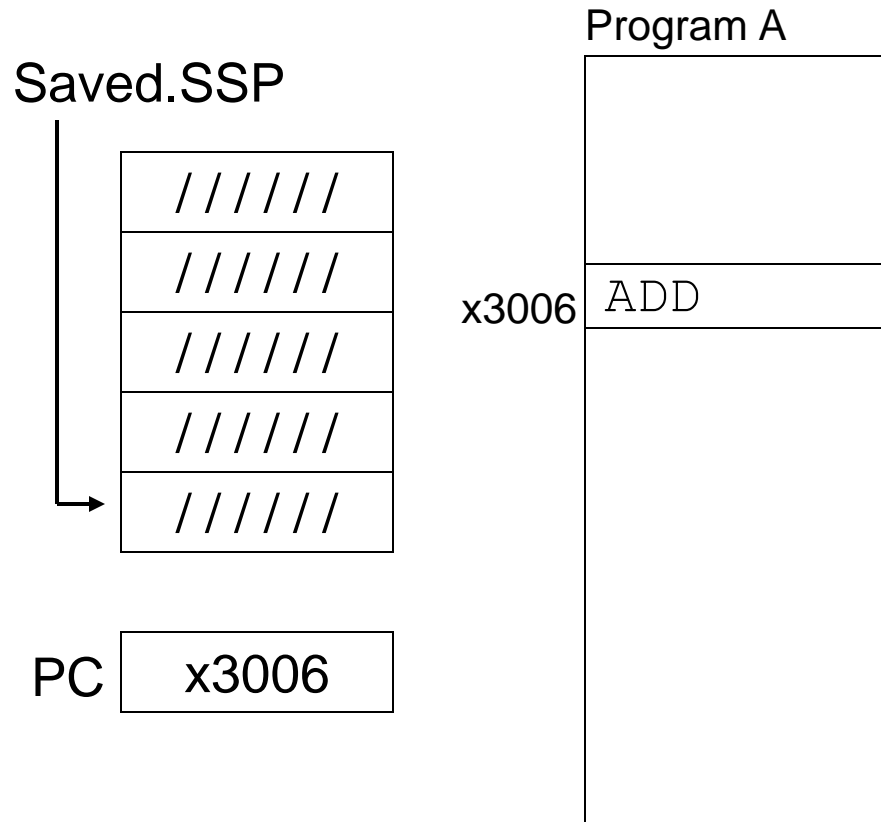
	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
<b>RTI</b>	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

1. **Pop PC from supervisor stack.** ( $PC = M[R6]; R6 = R6 + 1$ )
2. **Pop PSR from supervisor stack.** ( $PSR = M[R6]; R6 = R6 + 1$ )
3. **If  $PSR[15] = 1$ ,  $R6 = \text{Saved.USP}$ .**  
(If going back to user mode, need to restore User Stack Pointer.)

**RTI is a privileged instruction.**

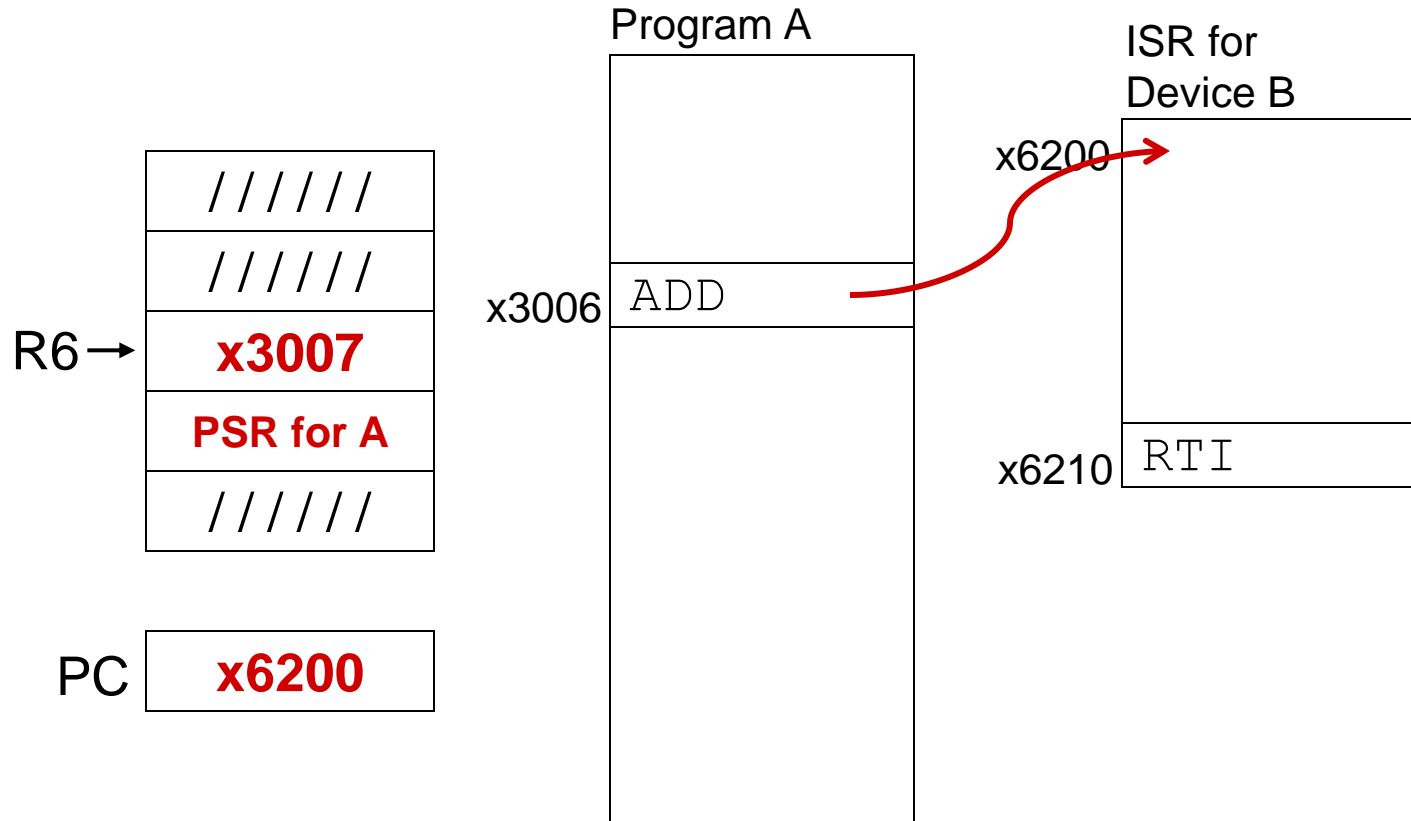
- **Can only be executed in Supervisor Mode.**
- **If executed in User Mode, causes an exception.**  
(More about that later.)

## Example (1)



Executing ADD at location x3006 when Device B interrupts.

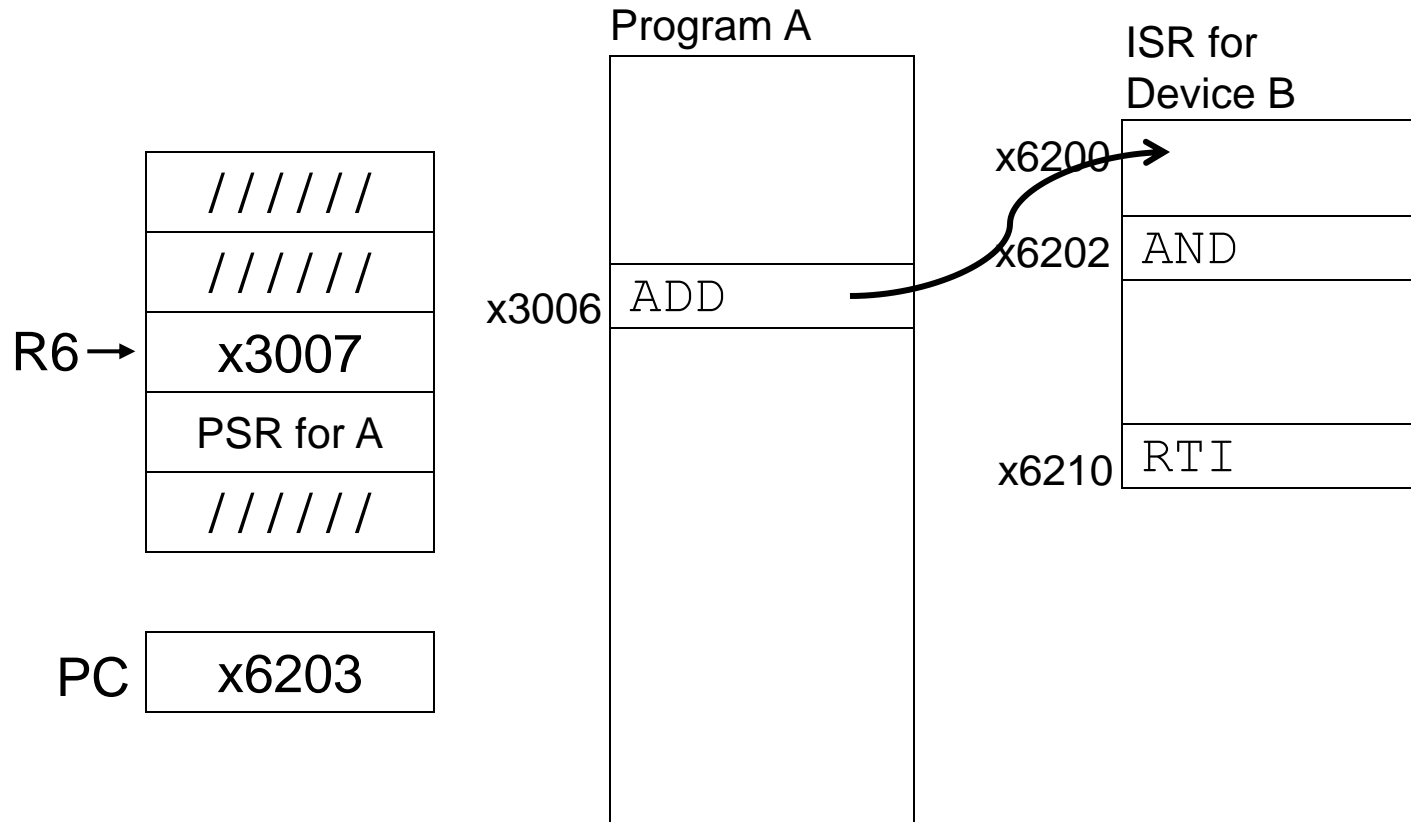
## Example (2)



Saved.USB = R6. R6 = Saved.SSP.  
Push PSR and PC onto stack, then transfer to  
Device B service routine (at x6200).

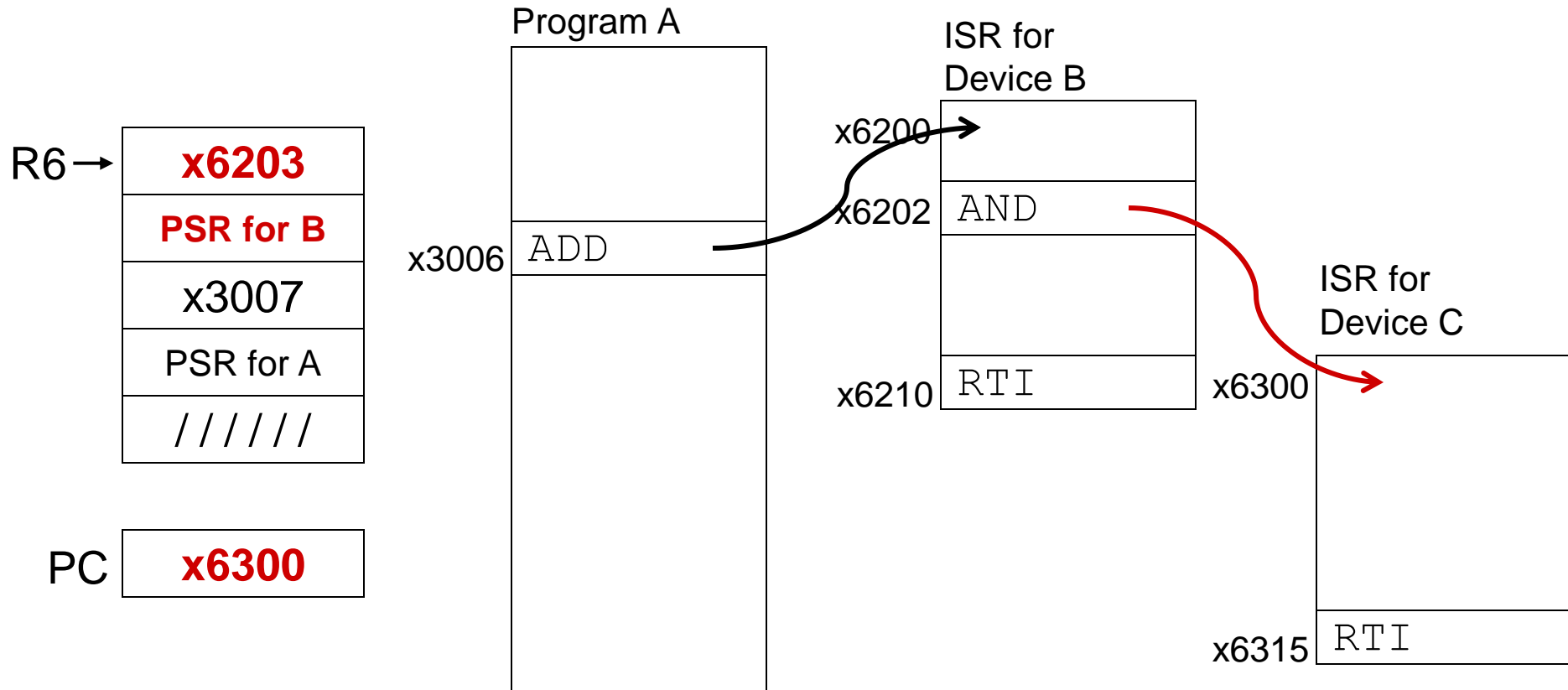


## Example (3)



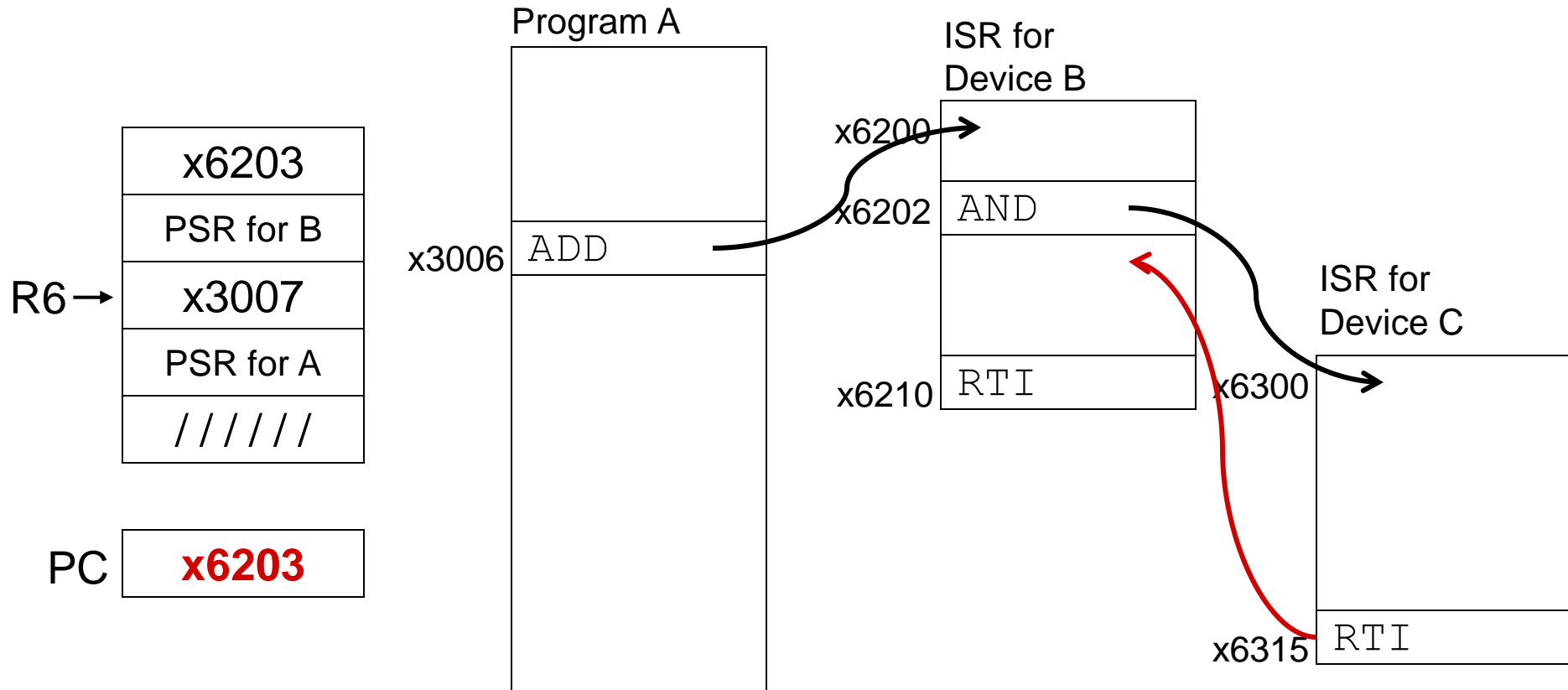
Executing AND at x6202 when Device C interrupts.

## Example (4)



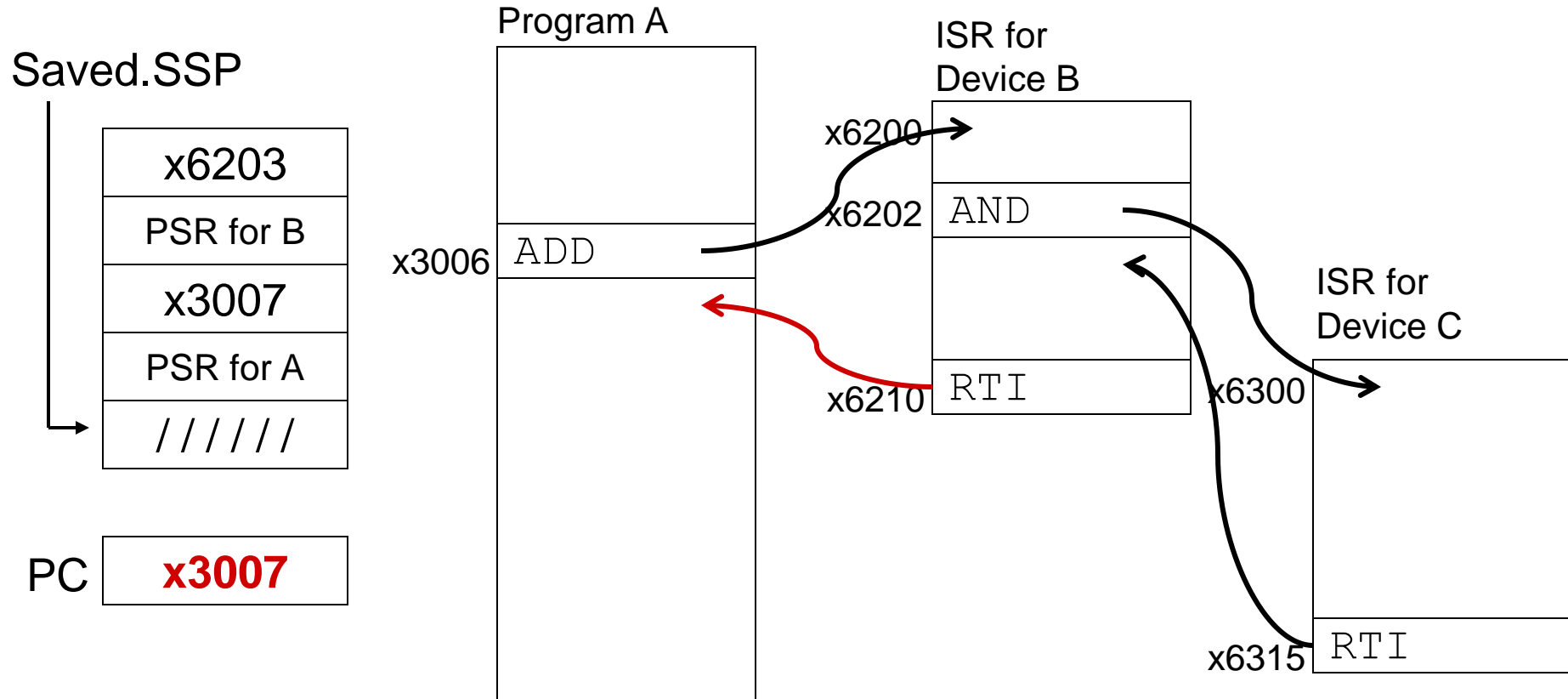
Push PSR and PC onto stack, then transfer to Device C service routine (at x6300).

## Example (5)



Execute RTI at x6315; pop PC and PSR from stack.

## Example (6)



Execute RTI at x6210; pop PSR and PC from stack.  
Restore R6. Continue Program A as if nothing happened.

## Exception: Internal Interrupt

When something unexpected happens inside the processor, it may cause an exception.

### Examples:

- Privileged operation (e.g., RTI in user mode)
- Executing an illegal opcode
- Divide by zero
- Accessing an illegal address (e.g., protected system memory)

### Handled just like an interrupt

- Vector is determined internally by type of exception
- Priority is the same as running program

## Arithmetic Using a Stack

Instead of registers, some ISA's use a stack for source and destination operations: a **zero-address** machine.

- Example:  
ADD instruction pops two numbers from the stack, adds them, and pushes the result to the stack.

Evaluating  $(A+B) \cdot (C+D)$  using a stack:

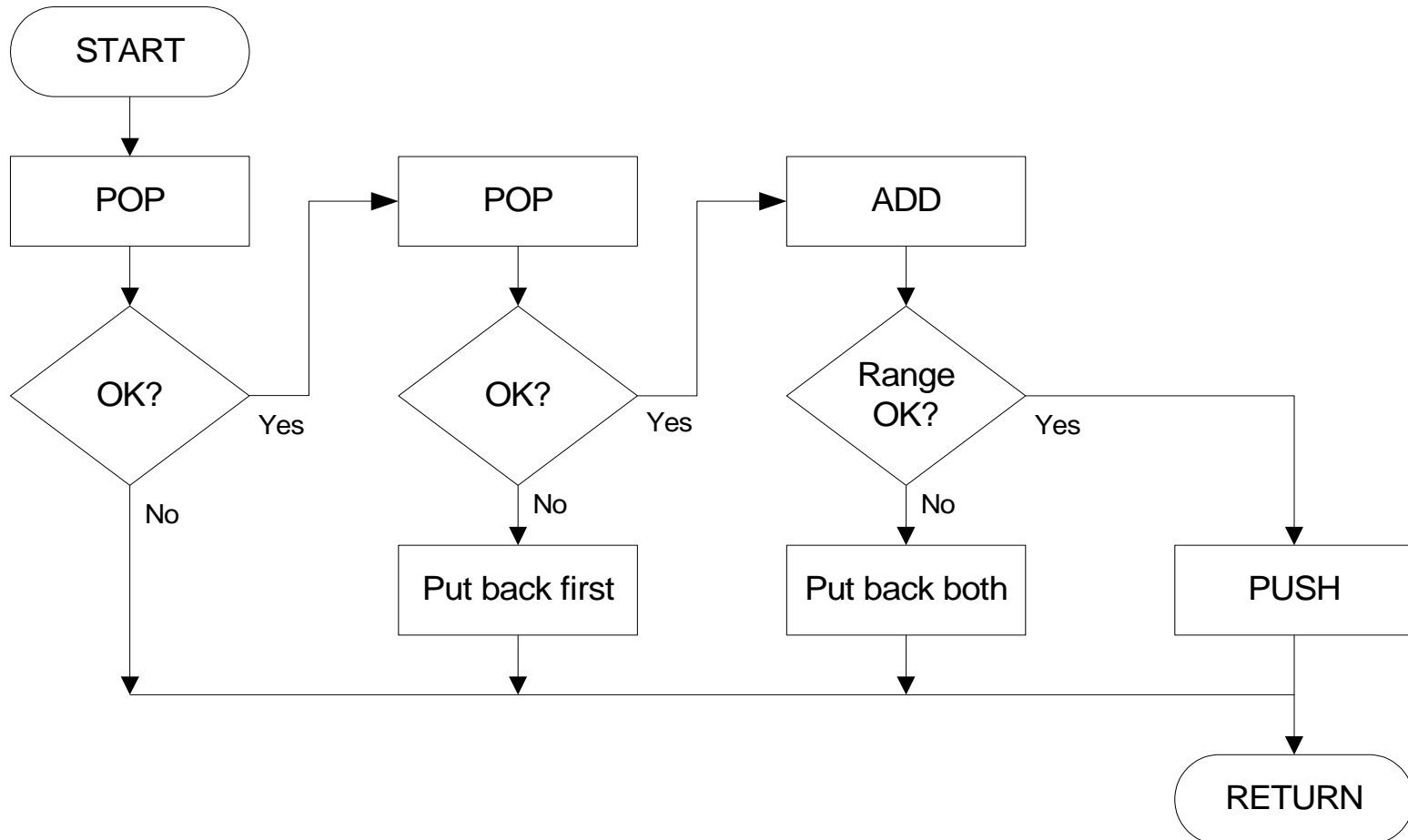
- (1) push A
- (2) push B
- (3) ADD
- (4) push C
- (5) push D
- (6) ADD
- (7) MULTIPLY
- (8) pop result

### Why use a stack?

- Limited registers.
- Convenient calling convention for subroutines.
- Algorithm naturally expressed using FIFO data structure.

## Example: OpAdd

**POP two values, ADD, then PUSH result.**



## Example: OpAdd

OpAdd	JSR POP	; Get first operand.
	ADD R5,R5,#0	; Check for POP success.
	BRp Exit	; If error, bail.
	ADD R1,R0,#0	; Make room for second.
	JSR POP	; Get second operand.
	ADD R5,R5,#0	; Check for POP success.
	BRp Restore1	; If err, restore & bail.
	ADD R0,R0,R1	; Compute sum.
	JSR RangeCheck	; Check size.
	BRp Restore2	; If err, restore & bail.
	JSR PUSH	; Push sum onto stack.
	RET	
Restore2	ADD R6,R6,#-1	; Decr stack ptr (undo POP)
Restore1	ADD R6,R6,#-1	; Decr stack ptr
Exit	RET	



## Data Type Conversion

Keyboard input routines read ASCII characters, not binary values.

Similarly, output routines write ASCII.

Consider this program:

```
TRAP    x23          ; input from keybd
ADD     R1, R0, #0    ; move to R1
TRAP    x23          ; input from keybd
ADD     R0, R1, R0    ; add two inputs
TRAP    x21          ; display result
TRAP    x25          ; HALT
```

User inputs **2** and **3** -- what happens?

Result displayed: **e**

Why? ASCII '2' (**x32**) + ASCII '3' (**x33**) = ASCII 'e' (**x65**)

## ASCII to Binary

**Useful to deal with mult-digit decimal numbers**

**Assume we've read three ASCII digits (e.g., "259") into a memory buffer.**

**How do we convert this to a number we can use?**

x32	'2'
x35	'5'
x39	'9'

- **Convert first character to digit (subtract x30) and multiply by 100.**
- **Convert second character to digit and multiply by 10.**
- **Convert third character to digit.**
- **Add the three digits together.**

## Multiplication via a Lookup Table

### How can we multiply a number by 100?

- One approach:  
Add number to itself 100 times.
- Another approach:  
Add 100 to itself <number> times. (Better if number < 100.)

Since we have a small range of numbers (0-9),  
use number as an index into a lookup table.

Entry 0:  $0 \times 100 = 0$

Entry 1:  $1 \times 100 = 100$

Entry 2:  $2 \times 100 = 200$

Entry 3:  $3 \times 100 = 300$

etc.

## Code for Lookup Table

```
; multiply R0 by 100, using lookup table  
;
```

```
    LEA    R1, Lookup100    ; R1 = table base  
    ADD    R1, R1, R0       ; add index (R0)  
    LDR    R0, R1, #0       ; load from M[R1]
```

```
    . . .
```

```
Lookup100 .FILL 0    ; entry 0  
          .FILL 100  ; entry 1  
          .FILL 200  ; entry 2  
          .FILL 300  ; entry 3  
          .FILL 400  ; entry 4  
          .FILL 500  ; entry 5  
          .FILL 600  ; entry 6  
          .FILL 700  ; entry 7  
          .FILL 800  ; entry 8  
          .FILL 900  ; entry 9
```

## Complete Conversion Routine (1 of 3)

; Three-digit buffer at ASCIIBUF.

; R1 tells how many digits to convert.

; Put resulting decimal number in R0.

ASCIItoBinary   AND   R0, R0, #0   ; clear result

                  ADD   R1, R1, #0   ; test # digits

                  BRz   DoneAtoB     ; done if no digits

;

                  LD     R3, NegZero ; R3 = -x30

                  LEA    R2, ASCIIBUF

                  ADD    R2, R2, R1

                  ADD    R2, R2, #-1 ; points to ones digit

;

                  LDR    R4, R2, #0   ; load digit

                  ADD    R4, R4, R3   ; convert to number

                  ADD    R0, R0, R4   ; add ones contrib

## Conversion Routine (2 of 3)

```
ADD    R1, R1, #-1    ; one less digit
BRz    DoneAtoB        ; done if zero
ADD    R2, R2, #-1    ; points to tens digit
```

;

```
LDR    R4, R2, #0      ; load digit
ADD    R4, R4, R3       ; convert to number
LEA    R5, Lookup10    ; multiply by 10
ADD    R5, R5, R4
LDR    R4, R5, #0
ADD    R0, R0, R4       ; adds tens contrib
```

;

```
ADD    R1, R1, #-1    ; one less digit
BRz    DoneAtoB        ; done if zero
ADD    R2, R2, #-1    ; points to hundreds
                        ; digit
```

## Conversion Routine (3 of 3)

```
LDR  R4, R2, #0    ; load digit
ADD  R4, R4, R3     ; convert to number
LEA  R5, Lookup100 ; multiply by 100
ADD  R5, R5, R4
LDR  R4, R5, #0
ADD  R0, R0, R4     ; adds 100's contrib
```

;

DoneAtoB

```
RET
```

NegZero

```
.FILL xFFD0    ; -x30
```

ASCIIBUF

```
.BLKW 4
```

Lookup10

```
.FILL 0
```

```
.FILL 10
```

```
.FILL 20
```

...

Lookup100

```
.FILL 0
```

```
.FILL 100
```

...

## Binary to ASCII Conversion

**Converting a 2's complement binary value to a three-digit decimal number**

- Resulting characters can be output using OUT

**Instead of multiplying, we need to **divide by 100** to get hundreds digit.**

- Why wouldn't we use a lookup table for this problem?
- Subtract 100 repeatedly from number to divide.

**First, check whether number is negative.**

- Write sign character (+ or -) to buffer and make positive.



## Binary to ASCII Conversion Code (part 1 of 3)

```
; R0 is between -999 and +999.  
; Put sign character in ASCIIBUF, followed by three  
; ASCII digit characters.
```

```
BinaryToASCII  LEA R1, ASCIIBUF    ; pt to result string  
                ADD R0, R0, #0      ; test sign of value  
                BRn NegSign  
                LD  R2, ASCIIplus   ; store '+'  
                STR R2, R1, #0  
                BRnzp Begin100  
NegSign        LD  R2, ASCIIneg     ; store '-'  
                STR R2, R1, #0  
                NOT R0, R0           ; convert value to pos  
                ADD R0, R0, #1
```

## Conversion (2 of 3)

```
Begin100      LD  R2, ASCIIoffset
              LD  R3, Neg100
Loop100      ADD R0, R0, R3
              BRn End100
              ADD R2, R2, #1    ; add one to digit
              BRnzp Loop100
End100      STR R2, R1, #1    ; store ASCII 100's digit
              LD  R3, Pos100
              ADD R0, R0, R3    ; restore last subtract
;
              LD  R2, ASCIIoffset
              LD  R3, Neg10
Loop100      ADD R0, R0, R3
              BRn End10
              ADD R2, R2, #1    ; add one to digit
              BRnzp Loop10
```

## Conversion Code (3 of 3)

```
End10          STR R2, R1, #2   ; store ASCII 10's digit
               ADD R0, R0, #10   ; restore last subtract
;
               LD  R2, ASCIIoffset
               ADD R2, R2, R0     ; convert one's digit
               STR R2, R1, #3    ; store one's digit
               RET

;
ASCIIplus      .FILL x2B        ; plus sign
ASCIIneg       .FILL x2D        ; neg sign
ASCIIoffset    .FILL x30        ; zero
Neg100         .FILL xFF9C      ; -100
Pos100         .FILL #100
Neg10          .FILL xFFF6      ; -10
```