Stat Econ 2 Assignment 1

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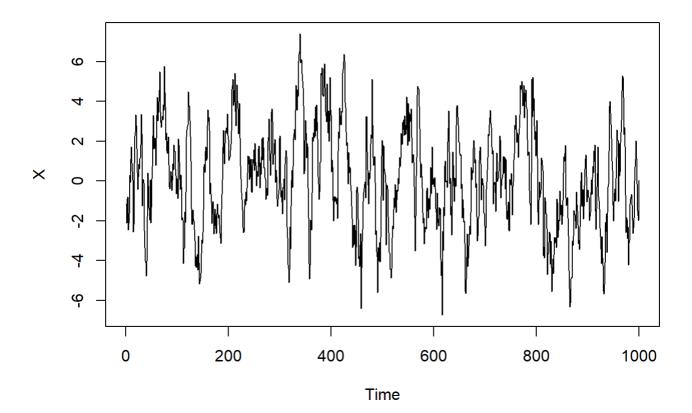
Exercise 1

We might note that we are dealing with an AR(1) process with slope 0.9 and, assuming a central requirement, central t -distributed noise with ten degrees of freedom. We simulate noise terms Z_t for $t=1,\ldots,1000$

```
set.seed(314)
desiredlag <- 20
phi <- 0.9
n <- 10^3
Z <- rt(df = 10, n=n)</pre>
```

As such we may simulate the AR(1) process using the update scheme defining the 'stopped' AR(1) process

```
X <- rep(NA,n)
X[1] <- Z[1]
for (j in 2:n) {
    X[j] <- phi*X[j-1]+Z[j]
}
ts.plot(X)</pre>
```

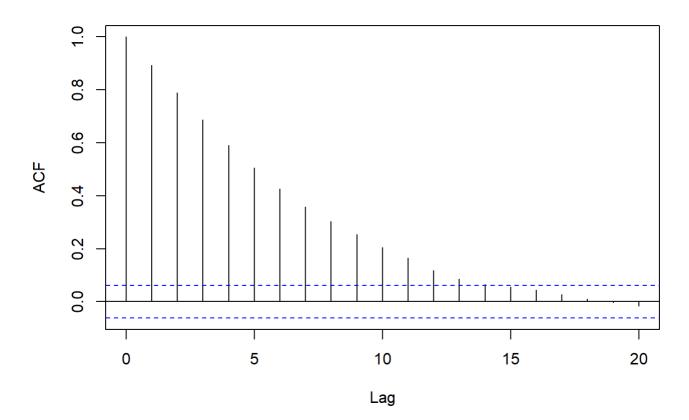


a)

We plot the acf confidence bands:

```
acf(X, lag.max = desiredlag, plot = T)
```

Series X



```
#acf(X, lag.max = desiredlag, plot = F)
```

Assuming the requirement to sample from X, and not from Z which would be more in line with the theoretical foundation for permutations of data, which are in and of themselves understood here, to be a random reordering of all data points. We may create a matrix containing 10^3 rows, each a permutation of the X data as such:

```
m <- 10^3
M <- matrix(NA, nrow = m, ncol = n)
for (i in 1:m) {
    M[i,] <- sample(X)
}</pre>
```

For each of these 'permuted' data sets, we will use acf to calculate sample autocorrelations for lags once again up to desired = 20, and then the 95% quantiles for each of the lags:

```
AutM <- apply(M,1,acf,lag.max=desiredlag, plot = F)
temp <- matrix(NA,nrow = m, ncol = desiredlag+1)
for (i in 1:1000) {
   temp[i,] <- AutM[[i]][[1]]
}
quanties <- apply(temp,2,quantile, prob=c(0.025,0.975))</pre>
```

We may then also plot the resulting quantiles:

```
#ggplot(quanties) + geom_line(aes())
#groupby?
```

We note that our AR(1) model is causal as $|\phi| < 1$. Following example 4.25, we will need to calculate the sample autocovariance function:

$$\gamma_{n,X}(h) := rac{1}{n} \sum_{t=1}^{n-h} \Big(X_t - \overline{X}_n \Big) \Big(X_{t+h} - \overline{X}_n \Big)$$

and autocorrelation function:

$$ho_{n,X}(h) := rac{\gamma_{n,X}(h)}{\gamma_{n,X}(0)}$$

Note thus in particular that we may calculate $\gamma_{n,X}(1),\ \gamma_{n,X}(0)$ in ${\Bbb R}$ with the following homemade function

```
gammaf <- function(X,h) {
    n <- length(X)
    gamt <- 0
    for (t in 1:(n-h)) {
        tempt <- (X[t]-mean(X))*(X[t+h]-mean(X))
        gamt <- gamt + tempt
    }
    1/n*gamt
}</pre>
```

Yielding

```
gammaf(X,1)
```

[1] 5.640264

gammaf(X,0)

[1] 6.317588

Such that for

$$\hat{\phi}_n = rac{\gamma_{n,X}(1)}{\gamma_{n,X}(0)} \equiv
ho_{n,X}(1)$$

$$\hat{\sigma}_n^2 = \gamma_{n,X}(0) \Big(1-
ho_{n,X}^2(1)\Big)$$

```
(rho1 <- gammaf(X,1)/gammaf(X,0))</pre>
```

[1] 0.8927876

(phih <- rho1)

[1] 0.8927876

```
(sigmah2 <- gammaf(X,0)*(1-rho1^2))
```

Let $\nu=10$ be the degrees of freedom of our student-t distributed random noise Z_t . As is surmised on page 47-48 in the lecture notes, in dealing with a causal AR(1) process driven by iid noise Z_t with variance $\sigma^2=\frac{\nu}{\nu-2}=\frac{10}{8}=\frac{5}{4}$, we have asymptotic normality of $\hat{\phi}$ with corresponding asymptotic mean ϕ and asymptotic variance $\frac{\sigma^2\Gamma_p^{-1}}{n}$ i.e.

$$\hat{\phi}_n \overset{as}{\sim} \mathcal{N} \Bigg(\phi, rac{\sigma^2 \Gamma_{p=1}^{-1}}{n} \Bigg)$$

or equivalently

$$\sqrt{n} \Big(\hat{\phi} - \phi \Big) \stackrel{d}{
ightarrow} \mathcal{N} ig(0, \sigma^2 \Gamma_1^{-1} ig).$$

With this we may for our fixed n=1000 determine that $\left(\phi-\frac{1.96}{\sqrt{n}}\sqrt{\sigma^2\Gamma_1^{-1}},\ \phi+\frac{1.96}{\sqrt{n}}\sqrt{\sigma^2\Gamma_1^{-1}}\right)$ will be an asymptotic 95% confidence interval for ϕ . Estimating Γ_1 via the sample autocovariance function, we find:

$$ilde{\Gamma}_1 := \gamma_{n,X}(1-1) = \gamma_{n,X}(0) = 6.3175881$$

such that

$$ilde{\Gamma}_1^{-1} = rac{1}{ ilde{\Gamma}_1} = 0.1582883
eq 0$$

such that we may rewrite the confidence bands as

$$\left(\phi - rac{1.96}{\sqrt{n}}\sqrt{\sigma^2 0.1582883}, \ \phi + rac{1.96}{\sqrt{n}}\sqrt{\sigma^2 0.1582883}
ight)$$

Inserting the other estimates and n=1000 we get

$$\begin{pmatrix} \hat{\phi} - \frac{1.96}{\sqrt{10^3}} \sqrt{\hat{\sigma}^2 0.1582883}, \ \hat{\phi} + \frac{1.96}{\sqrt{10^3}} \sqrt{\hat{\sigma}^2 0.1582883} \end{pmatrix}$$

$$= \begin{pmatrix} 0.8927876 - \frac{1.96}{\sqrt{10^3}} \sqrt{0.2029302}, \ 0.8927876 + \frac{1.96}{\sqrt{10^3}} \sqrt{0.2029302} \end{pmatrix}$$

$$= (0.8648667, 0.9207085)$$

c)

i+ii)

We calculate the residuals:

```
Zh <- rep(NA,n)
Zh[1] <- X[1]
for (j in 2:n) {
    Zh[j] <- X[j]+phih*X[j-1]
}</pre>
```

We do a reordering of these in the requested fashion using sample:

```
Zhs<-sample(Zh)</pre>
```

We define a new sample:

```
Xhs <- rep(NA,n)
Xhs[1] <- Zhs[1]
for (j in 2:n) {
    Xhs[j] <- phih*Xhs[j-1]+Zhs[j]
}</pre>
```

```
iii)
```

part1)

As in b)

```
(hsrho1 <- gammaf(Xhs,1)/gammaf(Xhs,0))</pre>
```

```
## [1] 0.8541978
```

```
(hsphih <- hsrho1)
```

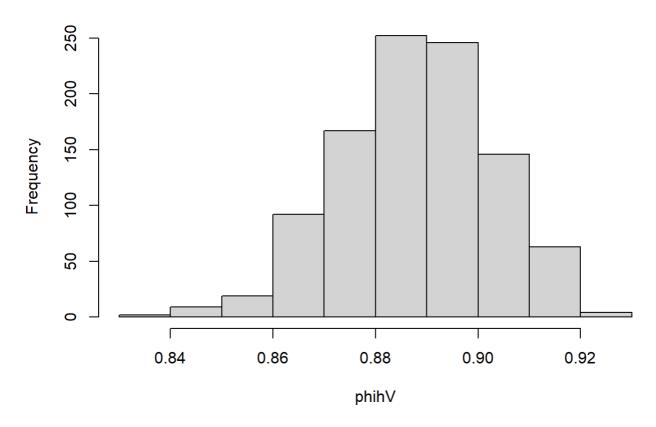
```
## [1] 0.8541978
```

part2)

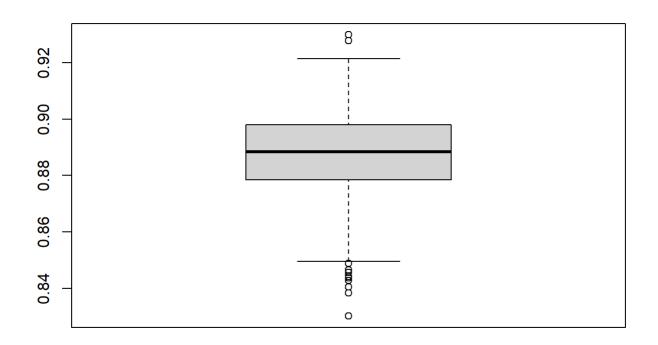
We repeat the tasks done in the previous exercises by writing a function to do so

```
boots <- function(Zh,n) { #Simulating the Bootstrap data
   q <- length(Zh)
   XhsM <- matrix(NA,nrow=n,ncol=q)</pre>
   for (i in 1:n) {
      Zhsi <- sample(Zh)</pre>
      XhsM[i,1] <- Zhsi[1]</pre>
      for (j in 2:q) {
         XhsM[i,j] <- phih*XhsM[i,j-1]+Zhsi[j]</pre>
      }
   }
   XhsM
}
dat <- boots(Zh,1000)</pre>
YW <- function(Zh,n) { #Calculating the YW's
   q <- length(Zh)
   dat <- boots(Zh,n)</pre>
   phihV <- rep(NA,n)</pre>
   for (i in 1:n) {
      phihV[i] <- gammaf(dat[i,],1)/gammaf(dat[i,],0)</pre>
   }
   phihV
}
phihV <- YW(Zh,n)</pre>
hist(phihV)
```

Histogram of phihV



boxplot(phihV)



```
## 2.5% 97.5%
## 0.8587749 0.9149991
```

Comparing this confidence interval to the asymptotic one achieved in b):

```
rbind(quantile(phihV, c(0.025, 0.975)), c(phih - 1.96/(sqrt(n))*sqrt(sigmah2*1/gammaf(X,0)), phih + 1.96/(sqrt(n))*sqrt(sigmah2*1/gammaf(X,0))))\\
```

```
## 2.5% 97.5%
## [1,] 0.8587749 0.9149991
## [2,] 0.8648667 0.9207085
```

we notice a great similarity, though the asymptotic confidence interval seems shifted approximately $\cong 0.007$ in comparison to the bootstrap interval.

Exercise 2

We may import the data

```
## Warning: One or more parsing issues, call `problems()` on your data frame for details,
## e.g.:
## dat <- vroom(...)
## problems(dat)</pre>
```

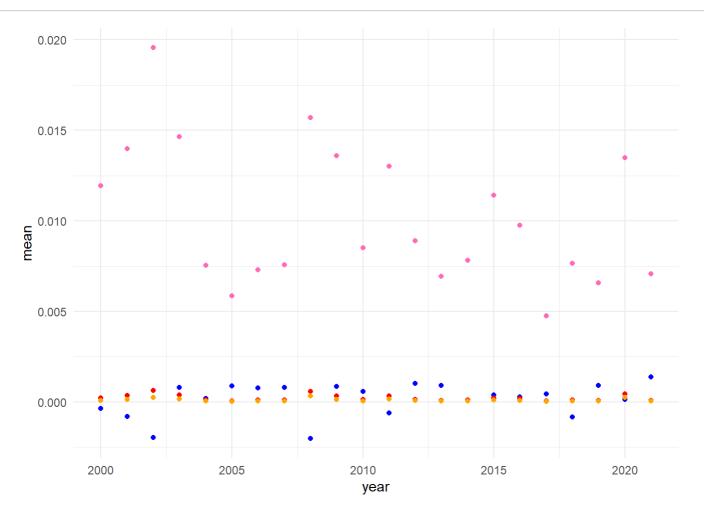
```
head(Data, 10)
```

```
## # A tibble: 10 × 7
##
                   Open High
                                 Low Close `Adj Close` Volume
      Date
                  <dbl> <dbl> <dbl> <dbl> <dbl>
                                                         <int>
      <date>
                                                  <dbl>
##
    1 1990-03-01 1796. 1796. 1796. 1796.
                                                  1796.
                                                              0
##
    2 1990-03-02 1805. 1805. 1805. 1805.
                                                  1805.
                                                              a
##
    3 1990-03-05 1838. 1838. 1838. 1838.
##
                                                  1838.
                                                              0
##
    4 1990-03-06 1820. 1820. 1820. 1820.
                                                  1820.
                                                              0
    5 1990-03-07 1842. 1842. 1842. 1842.
##
                                                  1842.
                                                              a
##
    6 1990-03-08 1862. 1862. 1862. 1862.
                                                  1862.
                                                              0
##
    7 1990-03-09 1859. 1859. 1859. 1859.
                                                  1859.
                                                              0
    8 1990-03-12 1844. 1844. 1844. 1844.
                                                              0
##
                                                  1844.
##
    9 1990-03-13 1867. 1867. 1867. 1867.
                                                  1867.
                                                              0
## 10 1990-03-14 1877. 1877. 1877. 1877.
                                                  1877.
                                                              0
```

We may create a yearly data set, and filter for data after 2000 and remove NA's

We plot these:

```
ggplot(Data_new_new) + geom_point(aes(x=year, y=mean), colour = 'blue') + geom_point(aes(x=year, y=var), colour = 'red') + geom_point(aes(x=year, y=absmean), colour = 'hotpink') + geom_point(aes(x=year, y=absvar), colour = 'orange')
```



None of the requested quantiles vary a lot, so we cannot reject the possibility of underlying ergodicity.

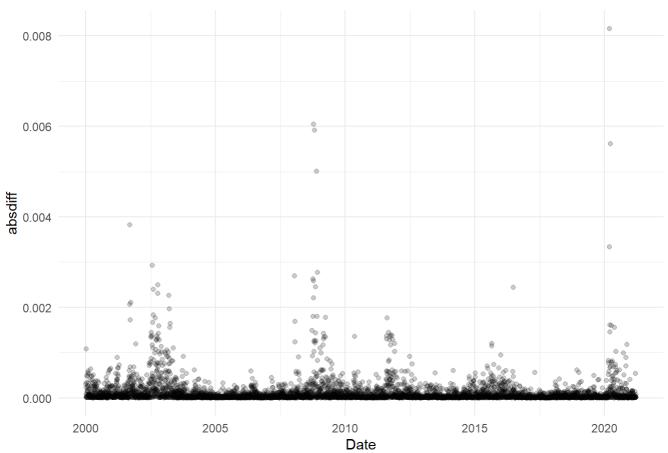
Exercise 3

a)

We might plot the absolute differences:

```
ggplot(Data_new_clean, aes(x=Date, y=absdiff)) + geom_point(alpha = 0.2) + ggtitle("Absolute difference
s over time")
```

Absolute differences over time



and calculate the maximum of the absolute difference between returns and logreturns:

```
max(Data_new_clean$absdiff)
```

[1] 0.008162438

b)

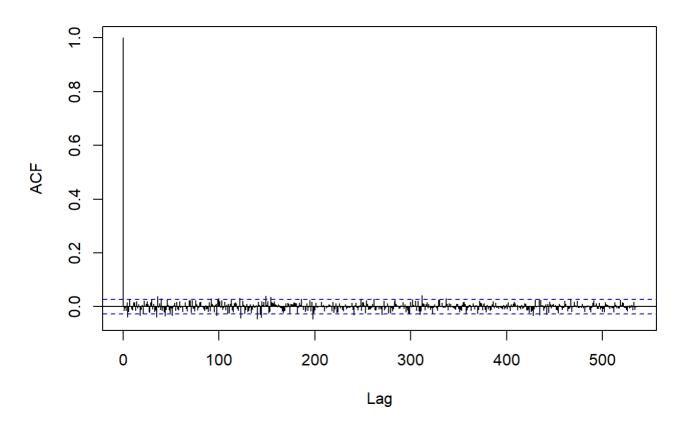
We note that the dataset <code>Data_new_clean</code> has <code>nrow(Data_new_clean) =5353</code> data points, such that 10% of the sample size of the log return time series will be of the size <code>floor(nrow(Data_new_clean)/10) =535</code>. We may use <code>acf</code> to calculate this many lags for the sample autocorrelation function for the log-return time series, its absolute value, and its square:

autocorLogRet <- acf(Data_new_clean\$logreturns, lag.max = floor(nrow(Data_new_clean)/10), plot=F)
autocorLogRetAbs <- acf(Data_new_clean\$abslogreturn, lag.max = floor(nrow(Data_new_clean)/10), plot=F)
autocorLogRetSquared <- acf((Data_new_clean\$logreturns)^2, lag.max = floor(nrow(Data_new_clean)/10), pl
ot=F)</pre>

We may also choose to plot each of these:

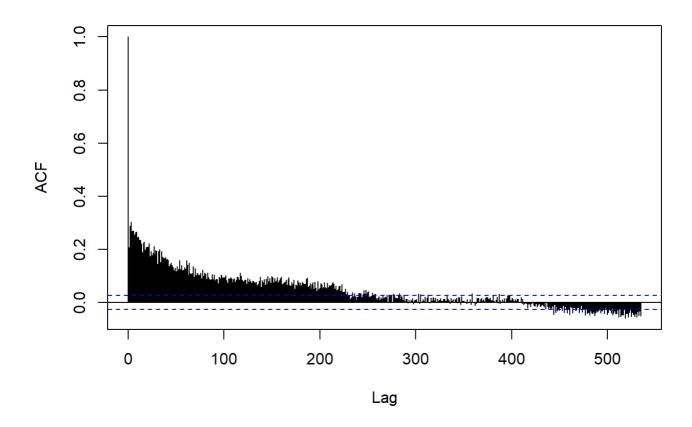
```
acf(Data_new_clean$logreturns, lag.max = floor(nrow(Data_new_clean)/10), plot=T)
```

Series Data_new_clean\$logreturns

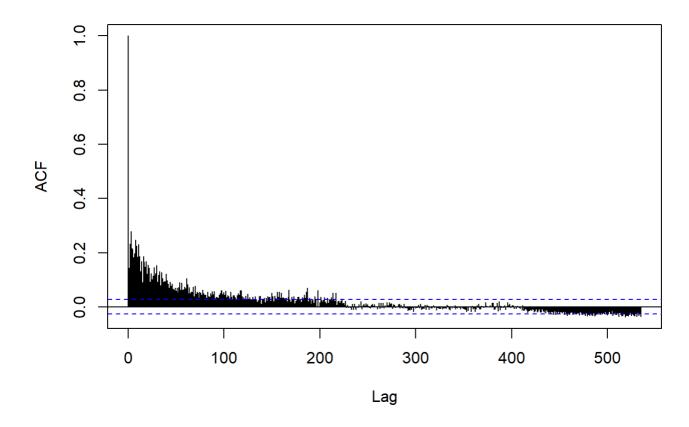


acf(Data_new_clean\$abslogreturn, lag.max = floor(nrow(Data_new_clean)/10), plot=T)

Series Data_new_clean\$abslogreturn



Series (Data_new_clean\$logreturns)^2



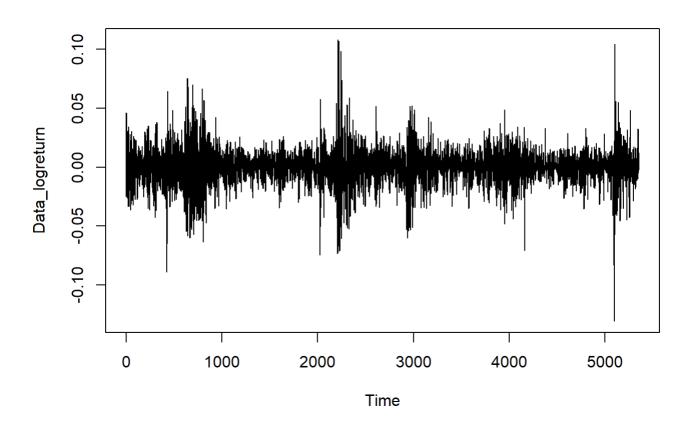
c)

We will fit the AR model using ar.yw

```
Data_logreturn <- Data_new_clean[,9][[1]]
head(Data_logreturn)
```

```
## [1] -0.024564608 -0.012969888 -0.004184320 0.046182439 0.021094463
## [6] -0.004960651
```

```
ts.plot(Data_logreturn)
```



```
modellr <- ar.yw(Data_logreturn, aic = T)</pre>
```

We may see a summary of the model:

```
print(modellr)
```

```
##
## Call:
## ar.yw.default(x = Data_logreturn, aic = T)
##
## Coefficients:
##
         1
                  2
                           3
                                              5
                                                       6
                                                                7
  -0.0132 -0.0030
                    -0.0145
                               0.0156
                                       -0.0385
                                                -0.0183
                                                           0.0289
##
##
## Order selected 7 sigma^2 estimated as
                                           0.0002197
```

```
summary(modellr)
```

```
##
                Length Class Mode
## order
                       -none- numeric
## ar
                   7
                       -none- numeric
## var.pred
                   1
                       -none- numeric
## x.mean
                   1
                       -none- numeric
## aic
                  38
                       -none- numeric
## n.used
                   1
                       -none- numeric
## n.obs
                       -none- numeric
                   1
## order.max
                   1
                       -none- numeric
## partialacf
                  37
                       -none- numeric
## resid
               5353
                       -none- numeric
## method
                       -none- character
                   1
## series
                   1
                       -none- character
## frequency
                       -none- numeric
                   1
## call
                   3
                       -none- call
## asy.var.coef
                 49
                       -none- numeric
```

d)

We may simulate based on the built up model:

```
modellr$ar
```

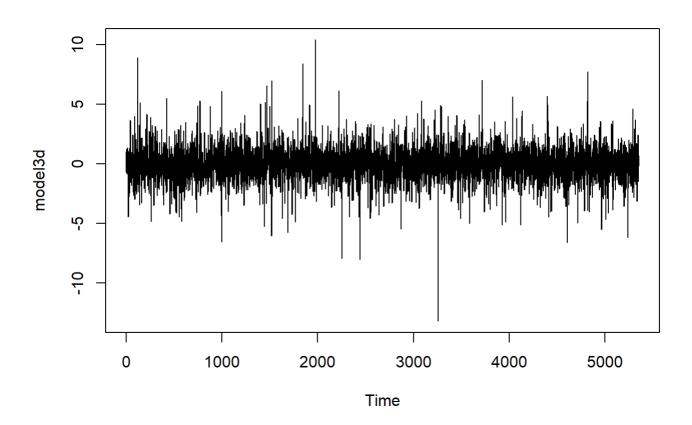
```
## [1] -0.013222942 -0.003024756 -0.014527039 0.015641328 -0.038478367
## [6] -0.018285413 0.028921894
```

```
model3d <- arima.sim(model = list(ar = modellr$ar), n = length(Data_logreturn), rand.gen = function
(n,...) rt(n,df=4))
summary(model3d)</pre>
```

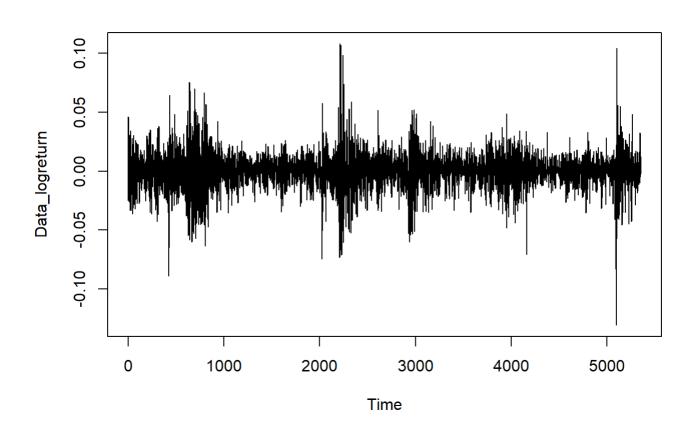
```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## -13.198054 -0.729220 -0.010417 -0.007745 0.730539 10.396367
```

We may plot the series, together with the original log-returns:

```
plot(model3d)
```

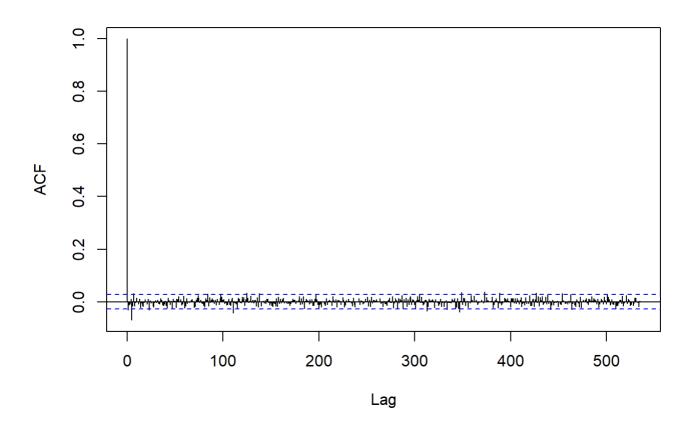


ts.plot(Data_logreturn)



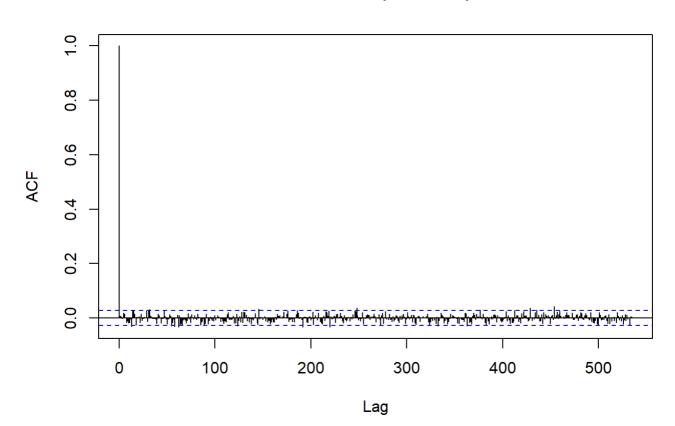
acf(model3d,lag.max = floor(nrow(Data_new_clean)/10), plot=T)

Series model3d



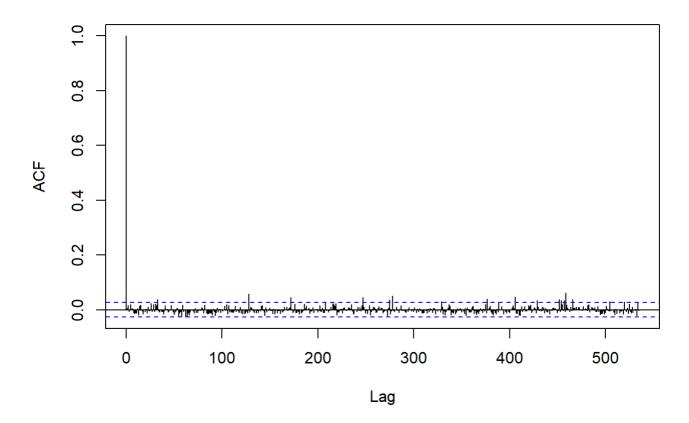
acf(abs(model3d), lag.max = floor(nrow(Data_new_clean)/10), plot=T)

Series abs(model3d)



acf(model3d^2, lag.max = floor(nrow(Data_new_clean)/10), plot=T)

Series model3d^2



We might note that comparing the plot of <code>model3d</code> to the log-return series, a striking difference appears, in that the model seems to attain values orders of magnitude higher, than there is in the original log-returns time series:

We may also note that while the autocorrelation function of the untransformed <code>model3d</code> looks rather similar to that of untransformed log-return series, the transformations appear dissimilar, possibly hinting at another problem. It seems that <code>model3d</code> as a model does not perform adequately in these circumstances, such that a different model, or a different choice of noise term might be needed.

Exercise 4

a)

Noting that $ho_X(h)=\phi^{|h|}$ we may compute

$$\begin{split} w_{hh} &= \sum_{k=1}^{\infty} \left(\rho_X(k+h) + \rho_X(k-h) - 2\rho_X(h)\rho_X(k) \right)^2 \\ &= \sum_{k=1}^{\infty} \left(\phi^{|k+h|} + \phi^{|k-h|} - \phi^{|k|}\phi^{|h|} \right)^2 \\ &= \sum_{k=1}^{\infty} \left(\phi^{|k-h|} - \phi^{|k+h|} \right)^2 \\ &= \sum_{k=1}^{h} \left(\phi^{h-k} - \phi^{k+h} \right)^2 + \sum_{k=h+1}^{\infty} \left(\phi^{k-h} - \phi^{k+h} \right)^2 \\ &= \sum_{k=1}^{h} \phi^{2h} (\phi^{-k} - \phi^k)^2 + \sum_{k=h+1}^{\infty} \phi^{2k} (\phi^{-h} - \phi^h)^2 \\ &= \phi^{2h} \sum_{k=1}^{h} \left(\phi^{-k} - \phi^k \right)^2 + \left(\phi^{-h} - \phi^h \right)^2 \sum_{k=h+1}^{\infty} \phi^{2k} \\ &= -\frac{\phi^{2h} (1 + 2h - \phi^2 - 2h\phi^2 - \phi^{-2h} + \phi^{2+2h})}{1 - \phi^2} + \frac{\phi^{2h+2} (\phi^{-h} - \phi^h)^2}{1 - \phi^2} \end{split}$$

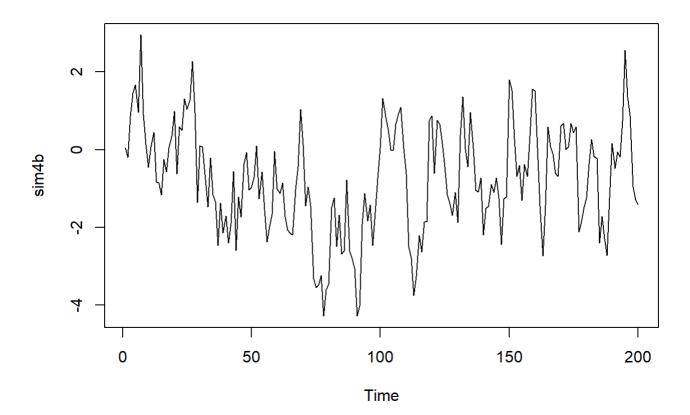
such that for $0<\phi<1$ we may conclude that for $h\to\infty$

$$w_{hh}
ightarrow rac{1}{1-\phi^2} + rac{\phi^2}{1-\phi^2}.$$

b)

We will simulate a size 200 sample from the AR(1) process as follows:

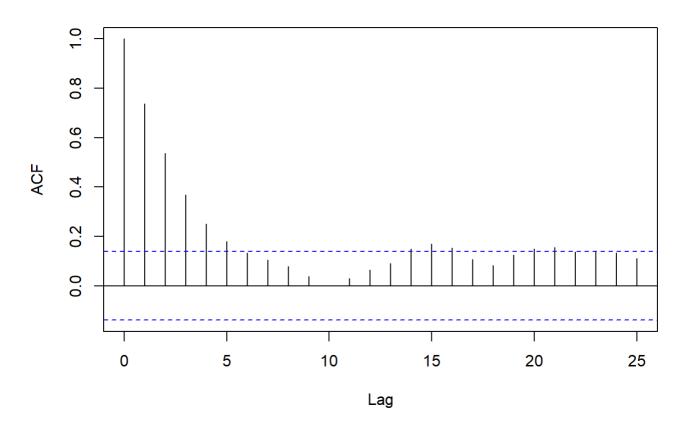
```
sim4b <- arima.sim(model = list(ar = 0.8), n=200)
ts.plot(sim4b)</pre>
```



We may draw the sample auotcorrelations, along with the confidence band for the iid white noise for a $25\ \text{lag}$:

acf(sim4b, lag.max = 25)

Series sim4b

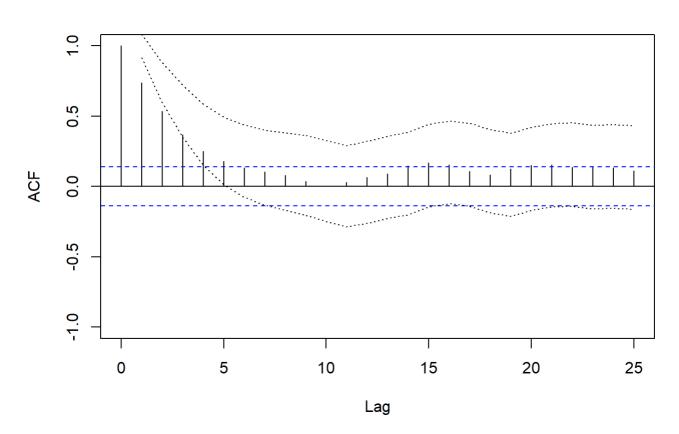


```
n4b <- 200
phi4b <- 0.8
rhonX4b <- as.numeric(acf(sim4b, lag.max = 25, plot=F)[[1]])
w <- 1:25
autocorconfp <- 1:25
autocorconfm <- 1:25
for (h in w) {
    w[h] <- -((phi4b^(2*h))*(1+2*h-phi4b^2-2*h*phi4b^2-phi4b^(-2*h)+phi4b^(2+2*h)))/(1-phi4b^2)+(phi4b^(2*h+2)*(phi4b^(-h)-phi4b^h)^2)/(1-phi4b^2)
    autocorconfp[h] <- rhonX4b[h]+qnorm(0.975)*sqrt(w[h]/n4b)
    autocorconfm[h] <- rhonX4b[h]-qnorm(0.975)*sqrt(w[h]/n4b)
}
autocorconf <- rbind(autocorconfp, autocorconfm)</pre>
```

We may plot the asymptotic correlation confidence bands together with the previous sample auto correlation function

```
acf(sim4b, lag.max = 25, ylim = c(-1,1)); lines(1:25, autocorconfp, lty = 3); lines(1:25, autocorconfm, lty = 3)
```

Series sim4b



Exercise 5

We may import the dataset, convert it to xts and calculate last day of each year

```
ss <- as.xts(sunspots)
ep <- ss %>% endpoints("years")
```

With this, we will aggregate the data averaging over each year:

```
ssy <- ss %>% period.apply(INDEX = ep, FUN = mean)
```

```
## NOTE: `period.apply(..., FUN = mean)` operates by column, unlike other math
## functions (e.g. median, sum, var, sd). Please use `FUN = colMeans` instead,
## and use `FUN = function(x) mean(x)` to take the mean of all columns. Set
## `options(xts.message.period.apply.mean = FALSE)` to suppress this message.
```

head(ssy)

```
## Dec 1749 80.92500

## Dec 1750 83.39167

## Dec 1751 47.65833

## Dec 1752 47.80000

## Dec 1753 30.69167

## Dec 1754 12.21667
```

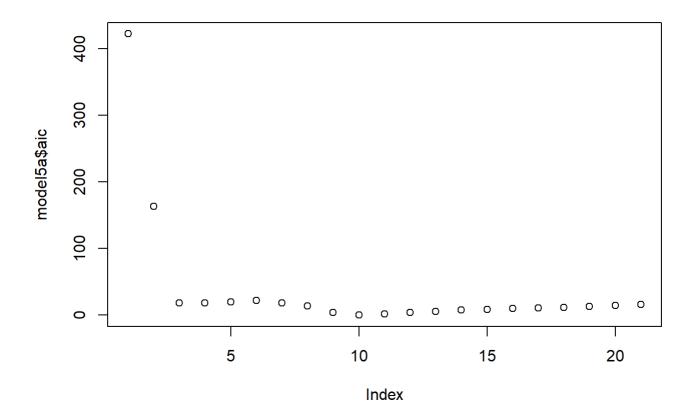
a)

We may calculate AIC using the ar.yw command:

```
model5a <- ar.yw(ssy, order.max= 20)
model5a$aic
```

```
##
                                    2
                                                3
                                                           4
                                                                       5
                                                                                   6
  422.180447 162.851001
                           18.446755
                                       18.064145
                                                   19.704643
                                                               21.684112
                                                                          17.947992
##
            7
                        8
                                    9
                                               10
                                                          11
                                                                      12
    13.778283
                 4.123101
                            0.000000
                                        1.836597
                                                    3.759563
                                                                5.598154
                                                                            7.522672
##
##
           14
                       15
                                   16
                                               17
                                                          18
                                                                      19
                                                                                  20
##
     8.578587
                 9.886723
                           10.866008
                                       11.055926 12.595664 14.138207
                                                                          16.136743
```

```
plot(model5a$aic)
```



b)

We may let ar.yw choose the order of the AR model that minimizes the AIC over ssy:

```
model5b <- ar.yw(ssy, aic = T)
print(model5b)</pre>
```

```
##
## Call:
## ar.yw.default(x = ssy, aic = T)
##
  Coefficients:
##
##
         1
                  2
                           3
                                    4
                                             5
                                                      6
            -0.4644 -0.1339
                             0.1351 -0.1133
                                                 0.0730 -0.0450
##
##
##
   0.1604
##
## Order selected 9 sigma^2 estimated as 264.2
```

```
summary(model5b)
```

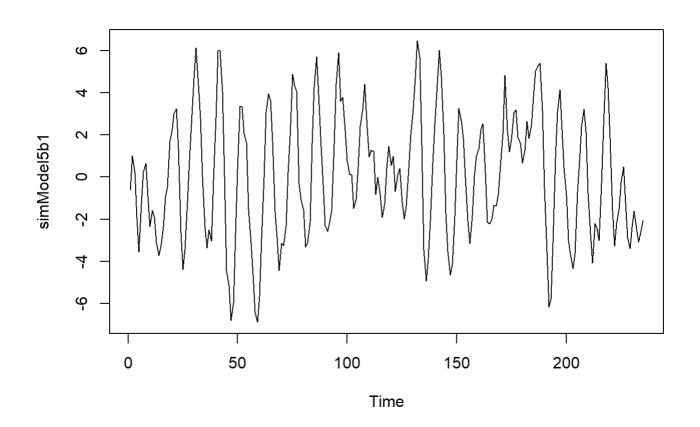
```
##
                 Length Class Mode
## order
                        -none- numeric
## ar
                   9
                        -none- numeric
## var.pred
                   1
                        -none- numeric
## x.mean
                   1
                        -none- numeric
## aic
                  24
                        -none- numeric
## n.used
                   1
                        -none- numeric
## n.obs
                   1
                        -none- numeric
                   1
                        -none- numeric
## order.max
## partialacf
                  23
                        -none- numeric
                 235
                        -none- numeric
## resid
## method
                   1
                        -none- character
## series
                   1
                        -none- character
                   1
                        -none- numeric
## frequency
                   3
## call
                        -none- call
                        -none- numeric
## asy.var.coef
                  81
```

We may then simulate from the model

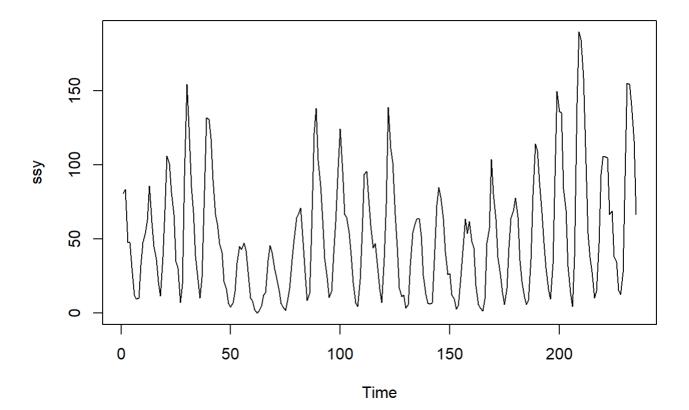
```
simModel5b1 <- arima.sim(model = list(ar = model5b$ar), n = length(ssy))</pre>
```

And provide the respective plots:

```
ts.plot(simModel5b1)
```



ts.plot(ssy)



It seems that the noise terms in the simModel5b1 that by default are chosen by arima.sim to be iid standard normally distributed have one major problem: simModel5b1 attains the wrong range of values, than required in order to model ssy

We will attempt to solve these problems by implementing the suggested solutions to these problems provided. Staying within iid normal noise, we may take a look at the residuals of <code>model5b</code> attain their mean and standard deviation, in order to attempt a non-standard normal noise term model

```
head(model5b$resid,15)
```

```
NA
##
    [1]
                  NA
                              NA
                                                      NA
                                                                   NA
                                                                               NA
                                                           -9.609204
                                          NA
                                               -7.691004
                                                                        7.470140
##
    [7]
                 NA
                              NA
##
  [13]
          21.343604 -22.998983
                                   5.214451
```

```
mean(model5b$resid, na.rm = T)
```

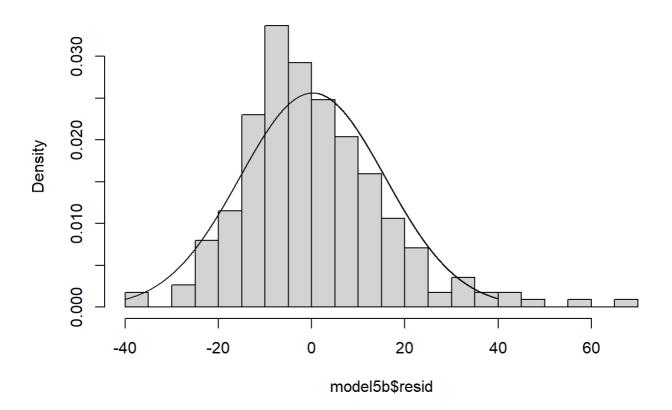
```
## [1] 0.2039417
```

```
sd(model5b$resid, na.rm = T)
```

```
## [1] 15.58728
```

```
\label{eq:model5b} $\text{resid, prob} = T$, $\text{breaks} = 20$; $\text{lines}(\text{seq}(-40,40,\text{by}=0.01), $\text{dnorm}(\text{seq}(-40,40,\text{by}=0.01), $\text{mean} = mean(\text{model5b}\text{resid, na.rm} = T)$, $\text{sd} = \text{sd}(\text{model5b}\text{resid, na.rm} = T)$)}
```

Histogram of model5b\$resid

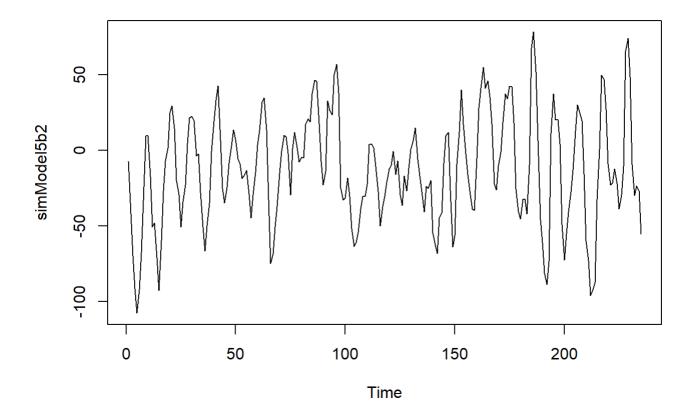


We note from the simple histogram plot above that the fit is adequate, but with resolution lost in the center, probably caused by a few larger values dragging out the summary statistics.

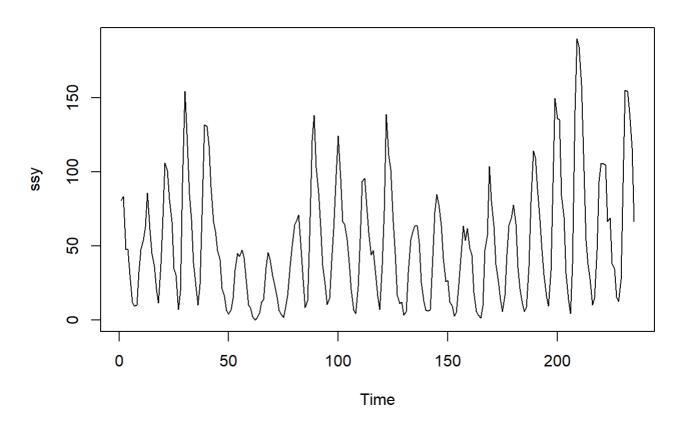
```
simModel5b2 <- arima.sim(model = list(ar = model5b$ar), n = length(ssy), rand.gen = function(n,...) rno
rm(n,mean(model5b$resid, na.rm = T),sd(model5b$resid, na.rm = T)))</pre>
```

And provide the respective plots:

```
ts.plot(simModel5b2)
```



ts.plot(ssy)

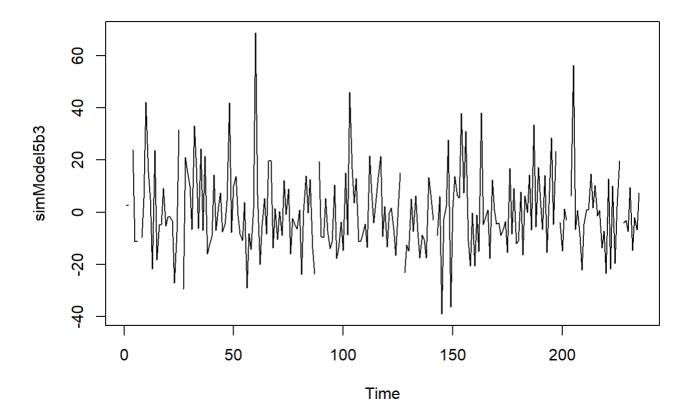


we see that the variability of simMode15b2 is now appropriate, though still attaining negative values thus requiring further investigation.

```
simModel5b2new <- arima.sim(model = list(ar = model5b$ar), n = length(ssy), rand.gen = function(n,...)
rcauchy(n,mean(model5b$resid, na.rm = T),sd(model5b$resid, na.rm = T)))</pre>
```

Permuting the residuals, we get the following model

```
sRes <- sample(model5b$resid)
simModel5b3 <- arima.sim(model = list(ar = model5b$coefficients), n = length(ssy), rand.gen = function
(...) sRes)
ts.plot(simModel5b3)</pre>
```



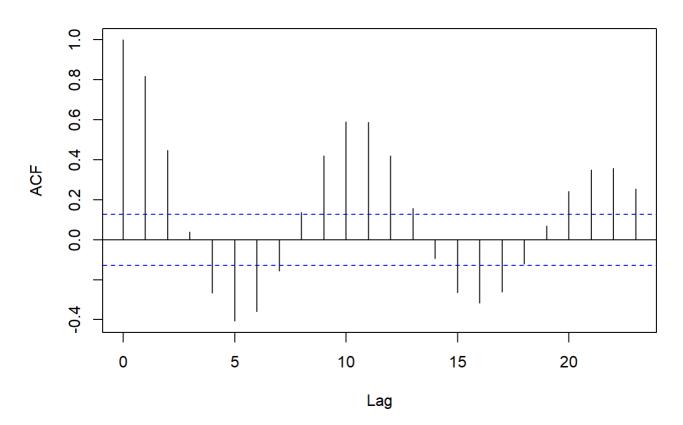
this however seems to attain too large a degree of variability, than what is 'required' for the data.

c)

We note that the simulated model attains the same kind of oscillatory autocorrelation behaviour as ssy, if not slightly less pronounced.

```
acf(ssy)
```

Series ssy



acf(simModel5b2)

Series simModel5b2

