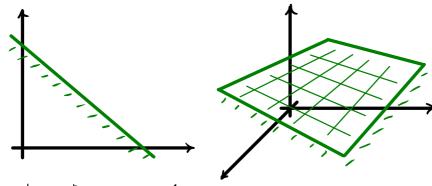
Simplex Method

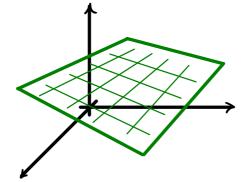
Affine Holf-Space: {xeR" | xxxx.}

if do = 0, then it's on half-space

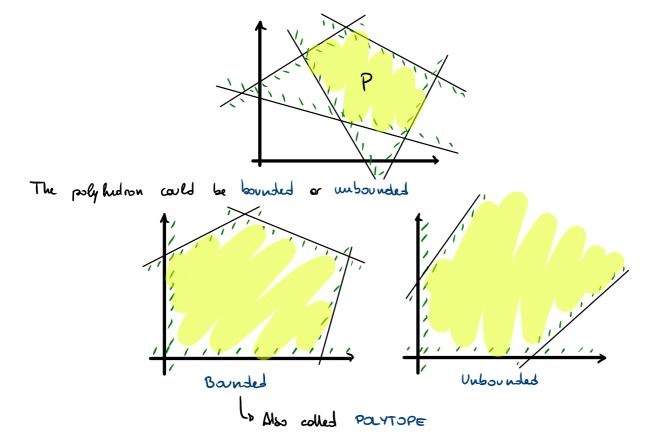


Hyperplane: { X & R" | x x = do {

Generalization of a plane (in R3)



Polyhedron: The intersection of a finite amount of affine holf-spaces and hyperplanes creates a polyhedron

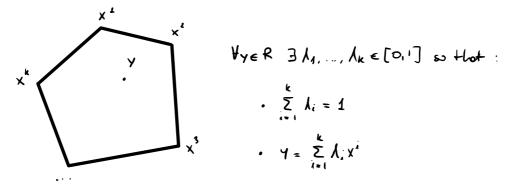


When we consider a polyhedron, given a z ∈ P ⊆ R", z = 1× + (1-1)y, L ∈ [0,1], x,y ∈ P Since 2 is the convex combination of x and y, min 1x,71 < 2

Vetex: A point x EP is said to be a vertex of P if it count be expressed on the STRICT convex combination of two DISTINCT points Y, 2 EP

Theorem of Minkowski- Weyl

Given a polytope P, and it's vertices $x', x', ..., x' \in P$, we can obtain every point inside the polytope as a convex combination of the wetices



The Given a polytope P, on aphinizohou problem min ctx has on aphinal solution away the vertices of P

Proof: Let
$$x^i, ..., x^k$$
 be the webices of P and compute $z^k = \min \{C^i x^i \mid i=1,...,k\}$

Where $A = [0,1]^k = 1$

$$C^{T}Y = C^{T} \left(\sum_{i=1}^{k} \lambda_{i} X^{i} \right)$$

$$= \sum_{j=1}^{k} \lambda_{j} C^{T} X^{i} \Rightarrow \sum_{j=1}^{k} \lambda_{j} Z^{*} = Z^{*}$$

$$C^{T}Y \geqslant Z^{*} \quad \forall y \in P$$

Consider en optimization problem in stonderd form Ax = b and suppose A is an $m \times n$ matrix (n > m) with rank (A) = m.

We can obtain a basis of A | x + of m lines independent columns of A) by picking them orbitrarily (as long they are independent)

$$A = \begin{bmatrix} 1 & 1 & 1 \\ A_1 & A_2 & \dots & A_N \\ \frac{1}{2} & \frac{1}{2} & \dots & \frac{1}{2} \end{bmatrix} = \begin{bmatrix} B & | F \\ J & M \times M \times (N-N) \end{bmatrix}$$

$$\in B \quad \Rightarrow \quad b \notin B$$

$$Ax = A_1 \times_1 + ... + A_n \times_n$$

$$A_1 \times_1 + A_2 \times_2 + ... + A_n \times_n$$

$$B \mid F \mid \left[\frac{x_0}{x_F} \right] \quad \text{(change now and column order mon't change the result)}$$

For a given B, we can rewrite the witid equation as follows:

Since B is made of m line or independent columns, det (B) \$0, so:

We thu set XF = 0 to find the solution of the equation (view example to understand the intrition)

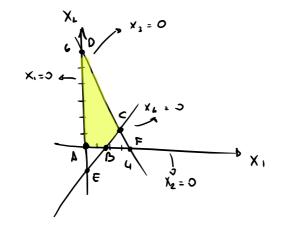
$$X_F = 0$$
 $X_0 = B^{-1}b$
 $X = \begin{bmatrix} B^{-1}b \\ 0 \end{bmatrix}$
 $X = \begin{bmatrix} B^{-1}b \\ 0 \end{bmatrix}$
 $X = \begin{bmatrix} B^{-1}b \\ 0 \end{bmatrix}$
 $(feasible if B^{-1}b \ge 0)$

To get all the artices I will have to compute all the (" borns.

 F_s :

min
$$-1, -1 = 0$$

 $6x_1 + 6x_2 \le 26 = 0$
 $3x_1 - 2x_2 \le 6 = 0$
 $3x_1 - 2x_2 \le 6 = 0$
 $3x_1 + 6x_2 + 0$
 $3x_1 + 0$
 $3x_1$



$$A \rightarrow X_1, X_2 = 0$$

$$B \rightarrow X_2, X_4 = 0$$

$$C \rightarrow X_3, X_4 = 0$$

$$P \rightarrow X_1, X_3 = 0$$

$$X_4 < 0$$

$$X_4 < 0$$

H may hoppen to have two porallel contraints as no solutions of whiteen