

Computation Theory Notes:

Chapter 0

Question 0:

If a programmer understands the limitations and capabilities of a computer, they can more efficiently work to solve their problems.

Question 1:

The set A consists of all numbers between (and including) 1 and 30 that are divisible by 3.

Enumerating the element:

$$A = \{e_1, \dots, e_n\}$$

Property of the element

Question 2:

$$A \cup B = \{1, 2, 3, 4, 5, 6, 10\}$$

$$A \cap B = \{10\}$$

$A \setminus B$ is the same as A minus the elements of B

Sets are unordered, but sequences have a specified order.

Sets are defined with parentheses: (7, 24, 38, 299)

Power Sets are a set of the original set and all of its subsets

Question 3:

$$P\{6, 7, 8\} = \{ \{\emptyset\} \{6\} \{7\} \{8\} \{6, 7\} \{7, 8\} \{6, 8\} \{6, 7, 8\} \}$$

Question 5:

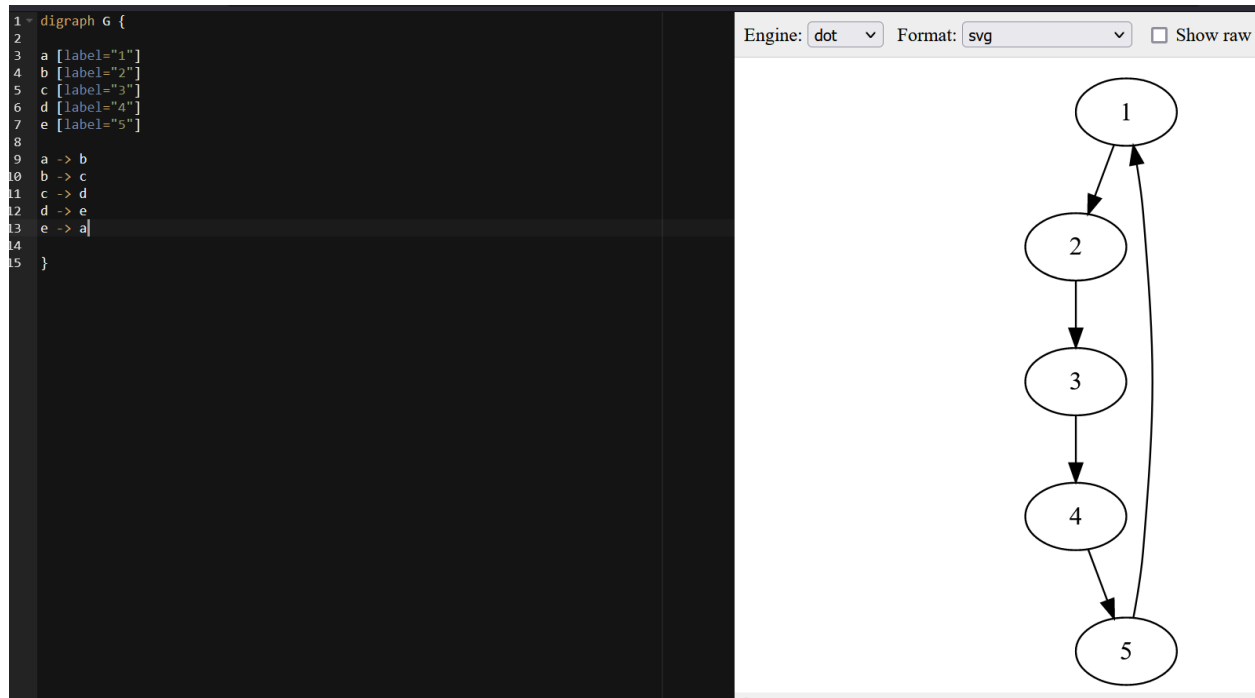
A^3 = All binary numbers from 0 to 7

Functions take an input and produce an output

Domain is the value of inputs

Range is the value of outputs

Question 6:



A graph is a tree if it is connected and has no simple cycles

Leaves are nodes with no children / they are the highest degree

Question 7:

We did it on the other assignment

Directed path: path where all arrows point in the same direction.

Alphabet: Non-empty, finite set

Symbols: Members of the alphabet

We use Greek letters to designate alphabets

Strings of characters are fundamental building blocks in CS

String(over an alphabet): finite sequences of symbols from that alphabet

Language: Set of “acceptable” strings

Assume $w = 01001$. $|w| = 5$

$|...|$ is asking for the size of the set inside

If two strings are connected via \circ , like $w \circ b$, it’s a concatenation

Concatenation: combine the strings in order

Question 8:

$(\epsilon), (0), (1), (00), (01), (10), (11), (000)$

Question 9:

$(P \wedge Q) \vee (P \wedge R)$

$(P \vee Q) \wedge (P \vee R)$

Question 10:

X cannot represent a “largest” number, as it would allow for $X + 1$ to exist and be larger.

If m and n have no common divisors, one must be odd.

Question 11:

2^0 one node / one leaf

Question 12:

n=1

$1 = 1 + 1/2$