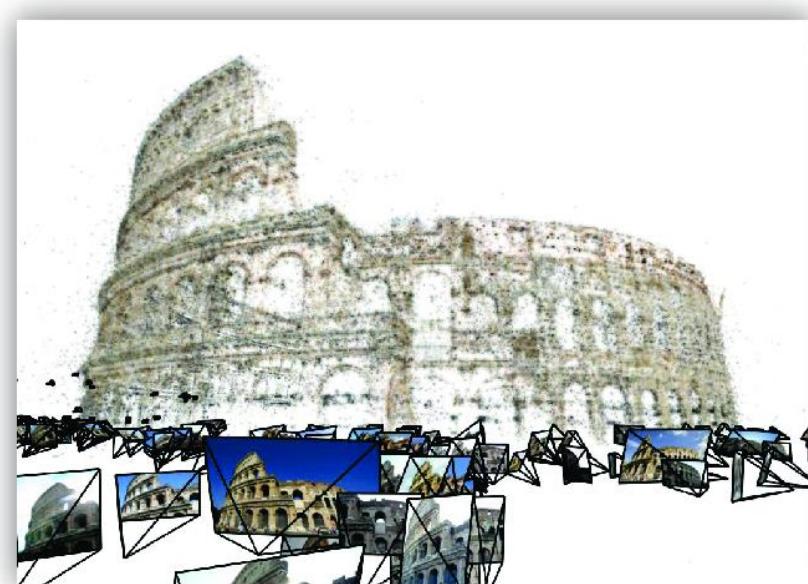


CS5670: Computer Vision

Noah Snavely / Zhengqi Li

Multi-view stereo



Recommended Reading

Szeliski Chapter 11.6

Multi-View Stereo: A Tutorial
Furukawa and Hernandez, 2015

http://www.cse.wustl.edu/~furukawa/papers/fnt_mvs.pdf

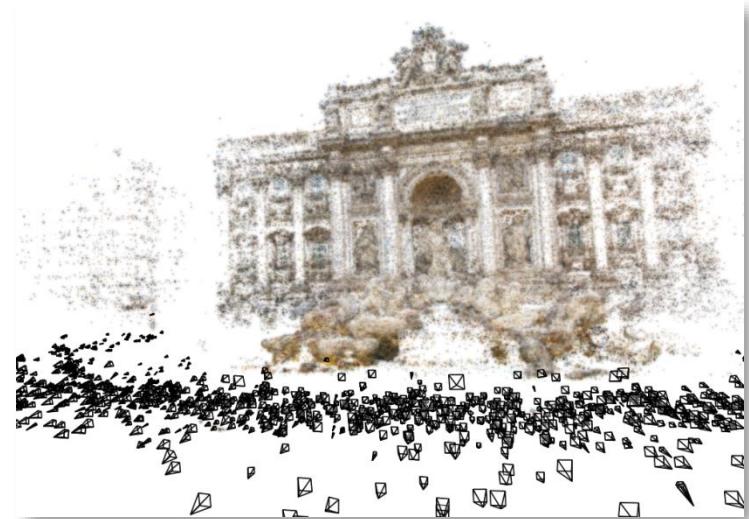
Multi-view Stereo

What is stereo vision?

Generic problem formulation: given several images of the same object or scene, compute a representation of its 3D shape



Stereo



Multi-view stereo

Multi-view Stereo



[Point Grey's Bumblebee XB3](#)



[Point Grey's ProFusion 25](#)

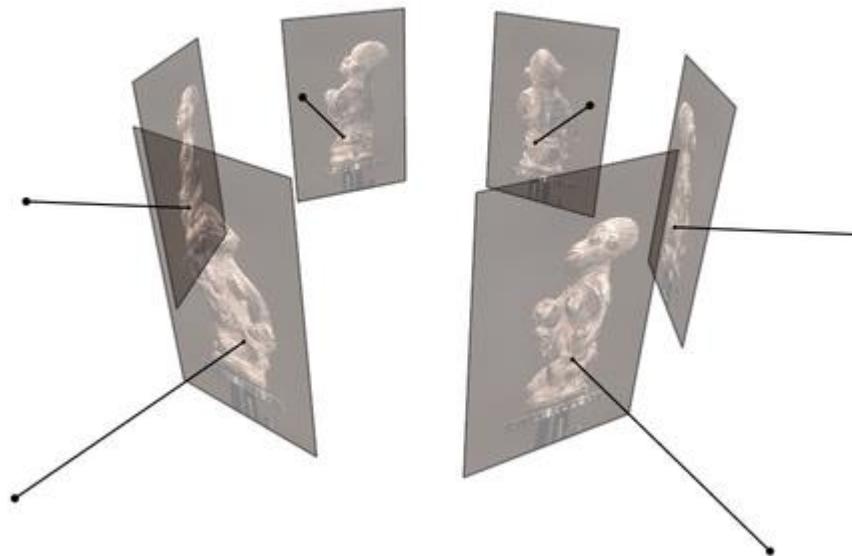


CMU's [3D Room](#)

Multi-view Stereo

Input: calibrated images from several viewpoints

Output: 3D object model



Figures by Carlos Hernandez

What is stereo vision?

- **Generic problem formulation:** given several images of the same object or scene, compute a representation of its 3D shape.
- “**Images of the same object or scene**”
 - Arbitrary number of images (from two to thousands)
 - Arbitrary camera positions (camera network or video sequence)
 - Calibration may be initially unknown
- “**Representation of 3D shape** **Representation of 3D shape** ”
 - Depth maps
 - Meshes
 - Point clouds
 - Patch clouds
 - Volumetric models
 - Layered models



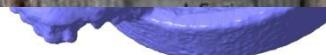
Furukawa et al., 2010



Hernandez, Schmitt
2004



Pons, Keriven, Faugeras
2005



Furukawa, Ponce
2006



Goesele et al.
2007

Towards Internet-scale Multi-view Stereo

CVPR 2010

Yasutaka Furukawa¹ Brian Curless²

Steven M. Seitz^{1,2} Richard Szeliski³

Google Inc.¹
University of Washington²
Microsoft Research³

<https://www.youtube.com/watch?v=ofHFOr2nRxU>

The Visual Turing Test for Scene Reconstruction Supplementary Video

Qi Shan⁺ Riley Adams⁺ Brian Curless⁺

Yasutaka Furukawa^{*} Steve Seitz^{++*}

⁺University of Washington ^{*}Google

<https://www.youtube.com/watch?v=NdeD4cjLI0c&t=64s>

3DV 2013

Applications



Data SIO, NOAA, U.S. Navy, NGA, GEBCO

Google earth



AUTODESK® 123D®

APPS

3D MODELS

PROJECTS

TOOLS

BLOG

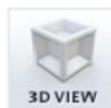


でんじろんさん

by じろう でん 266, +✉



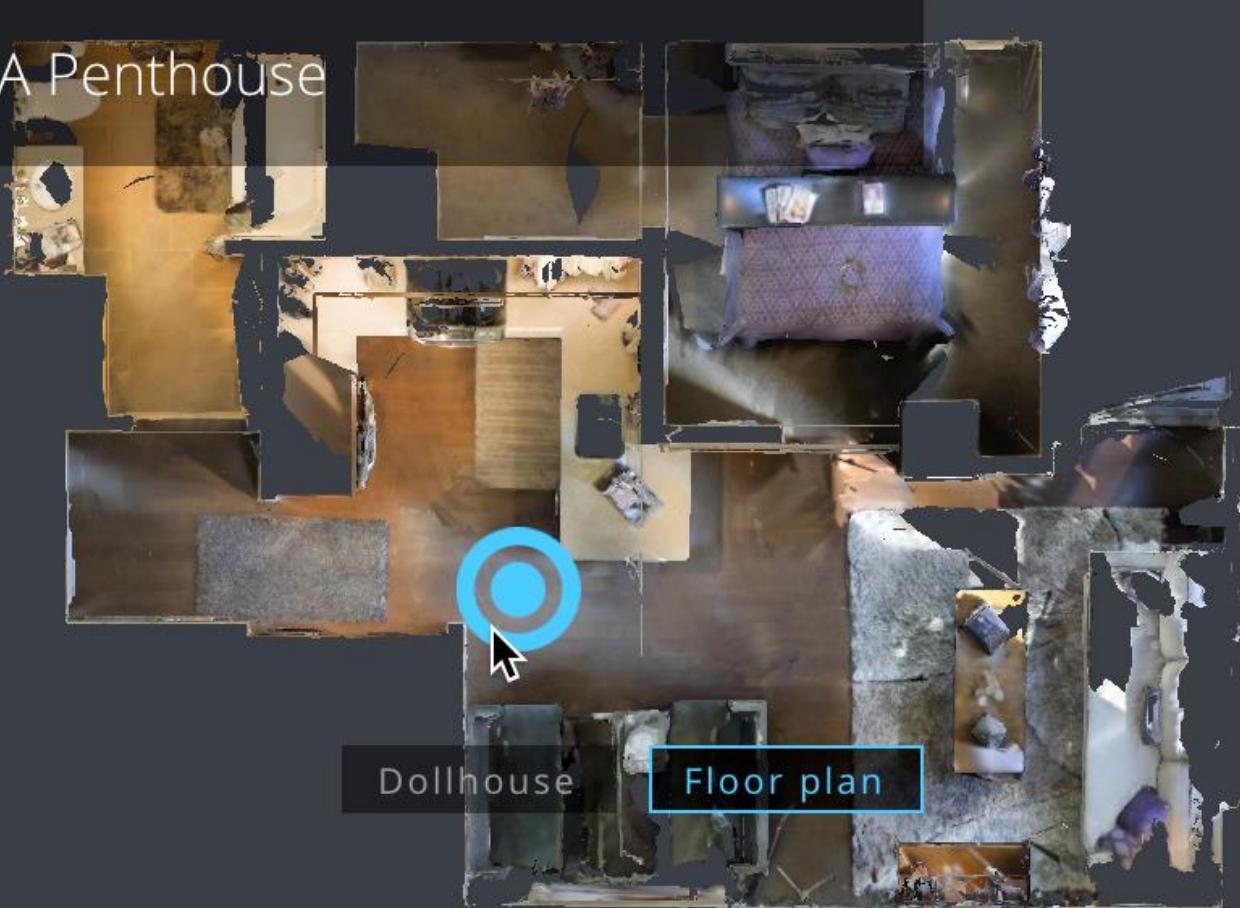
? ⌂





< 1BR, 1BA Penthouse >

Terms



Whistle in the Form of Female Figure 600 AD - 900 AD



≡

Details

Los Angeles County Museum of Art



Los Angeles County Museum of Art



Sculpture



Mexico

Share

Compare

Saved 0

Discover

Google



JUMP

Google



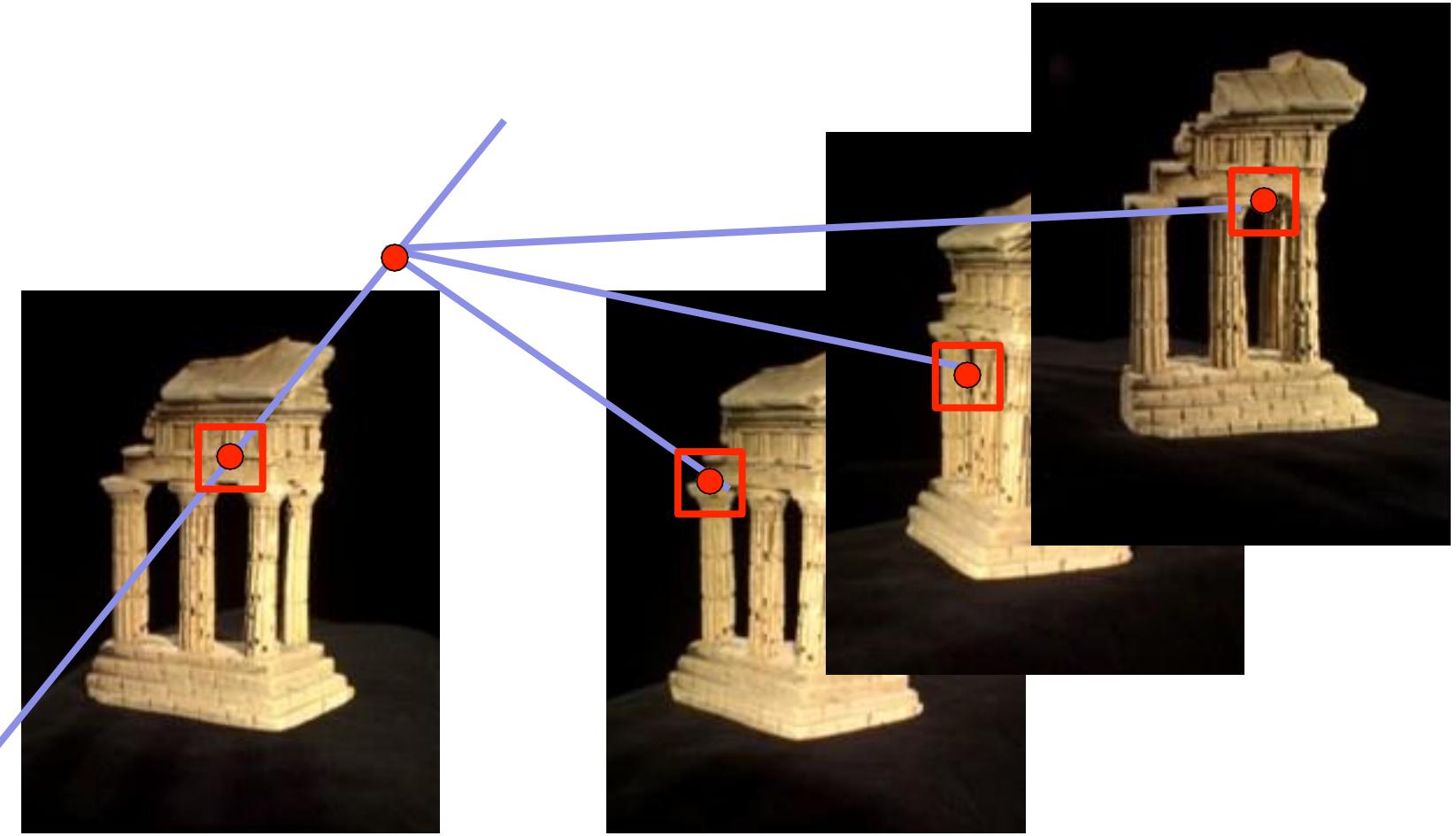




https://code.facebook.com/posts/1755691291326688/introducing-facebook-surround-360-an-open-high-quality-3d-360-video-capture-system?hc_location=ufi



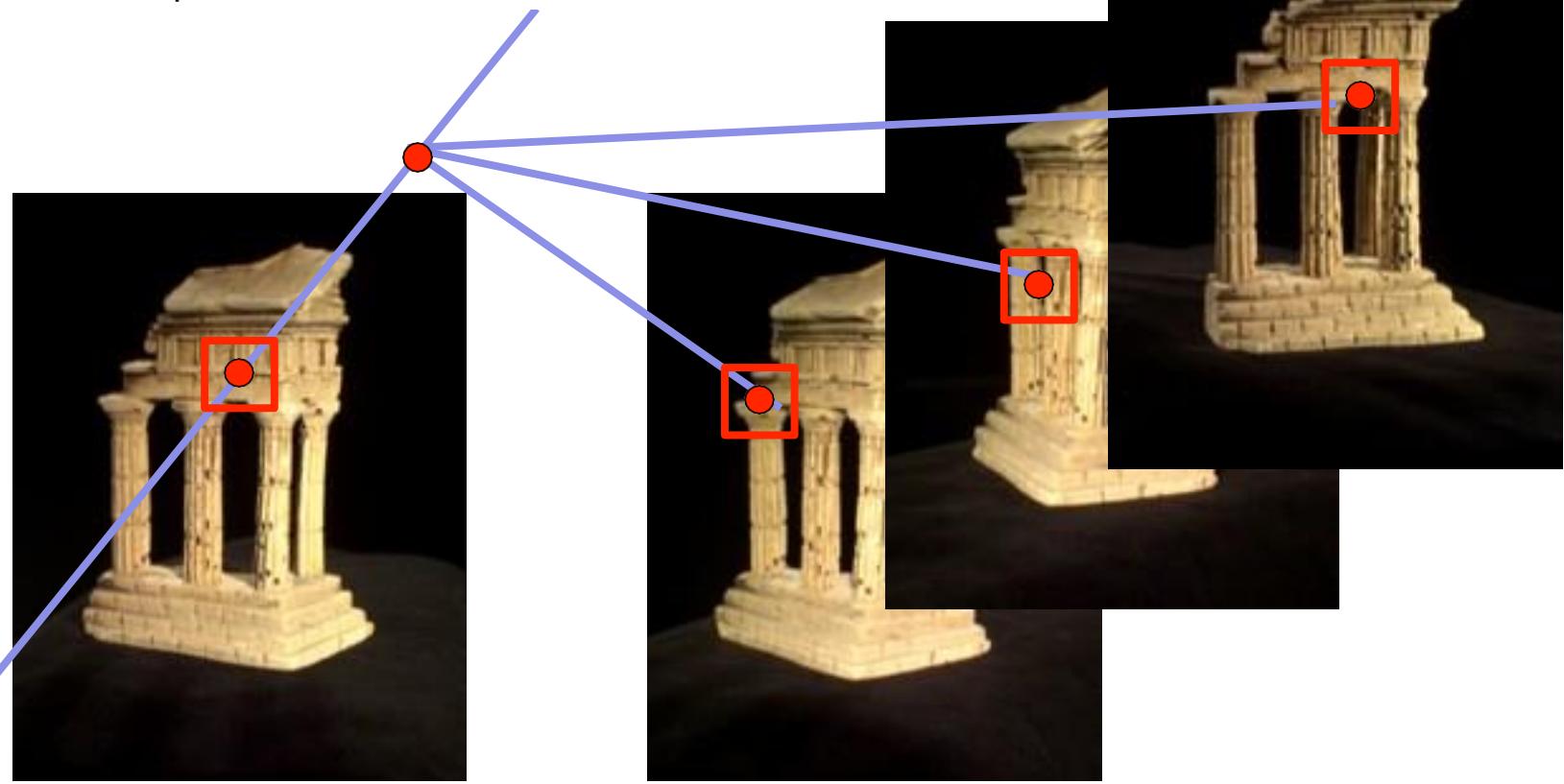
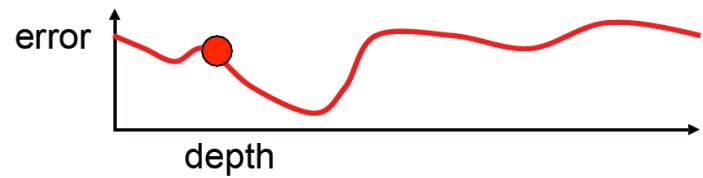
Multi-view stereo: Basic idea



Source: Y. Furukawa

Multi-view stereo:

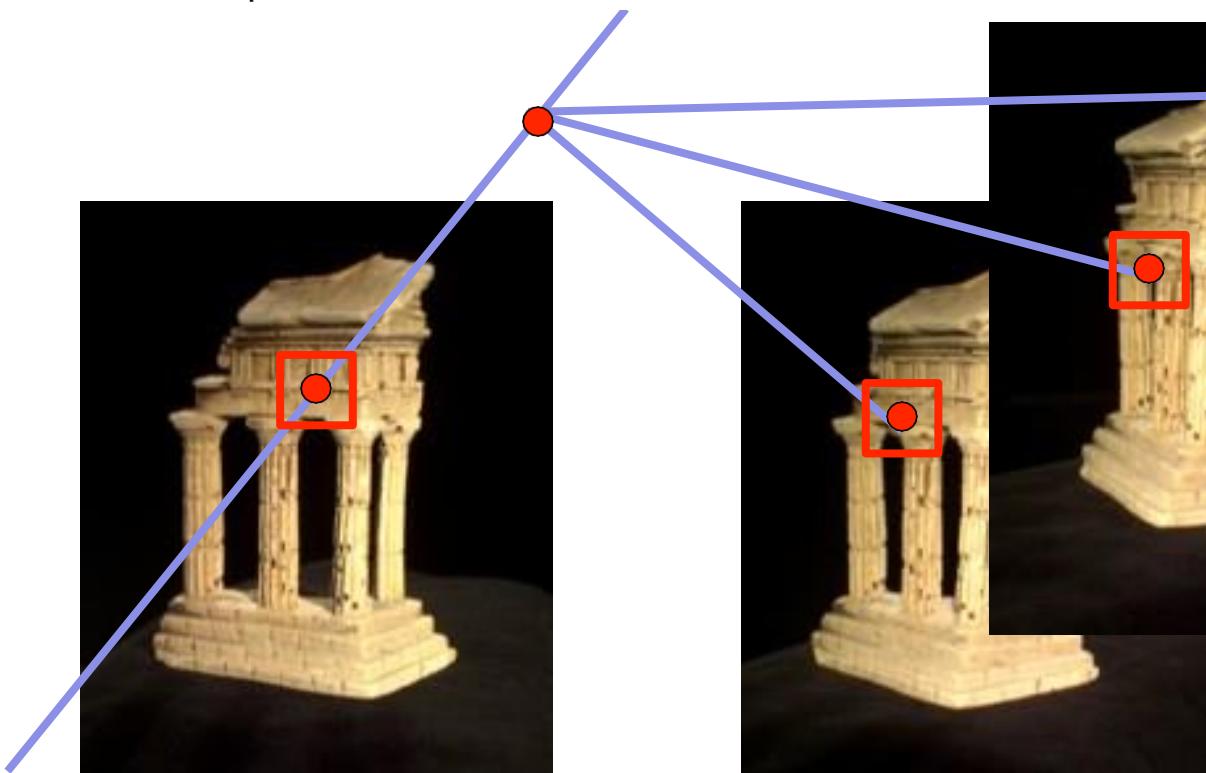
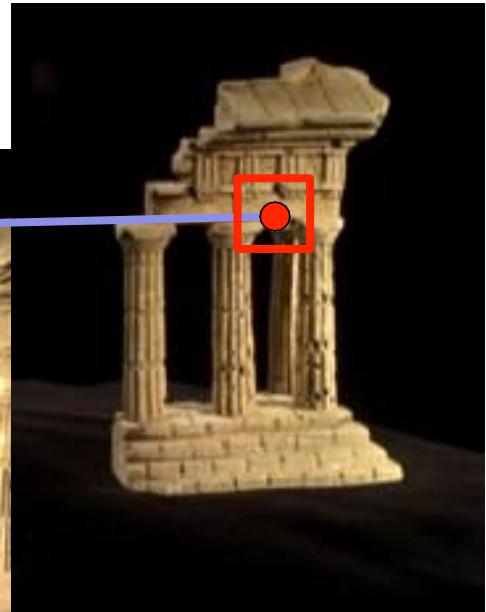
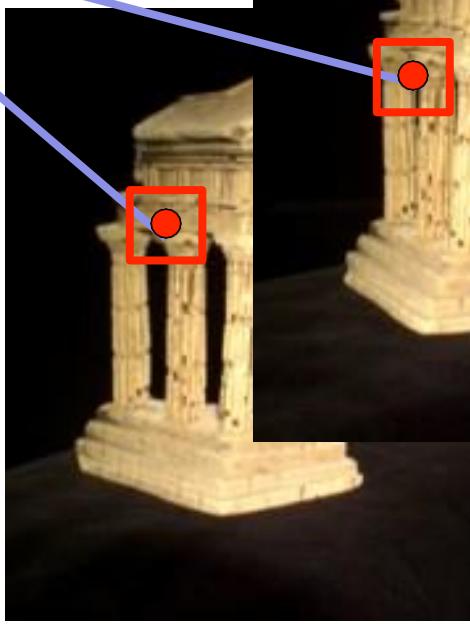
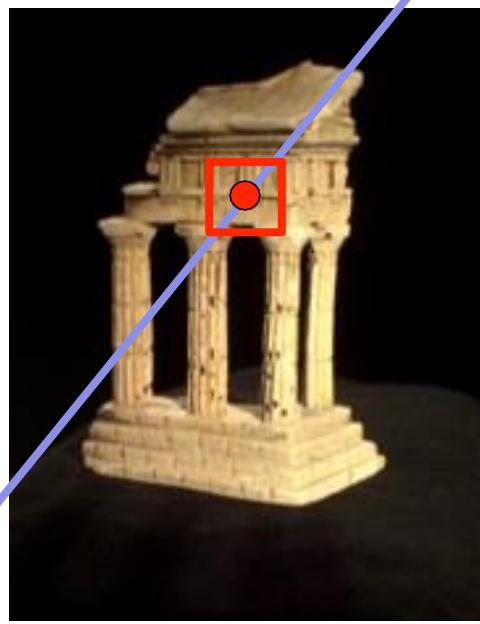
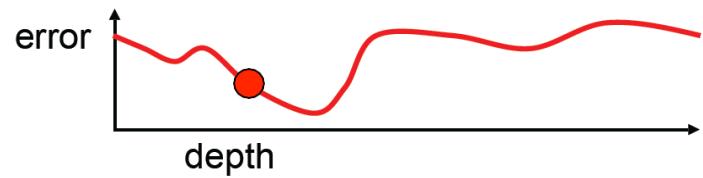
Basic idea



Source: Y. Furukawa

Multi-view stereo:

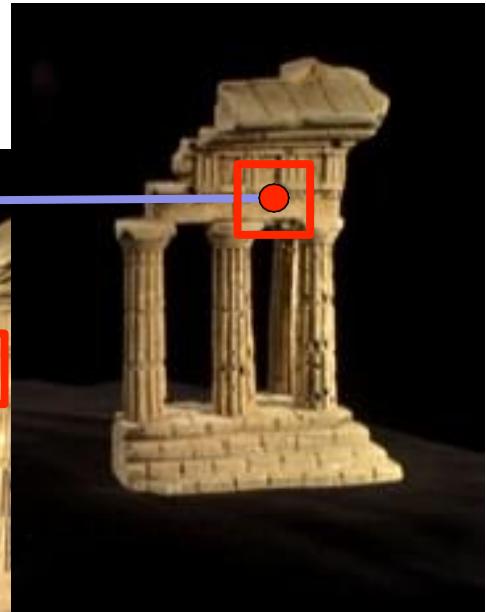
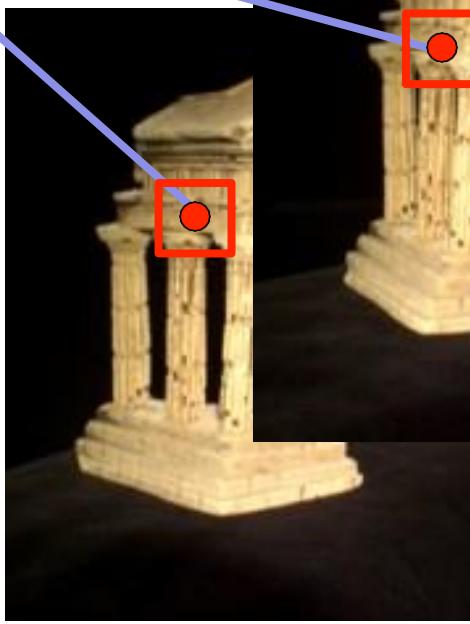
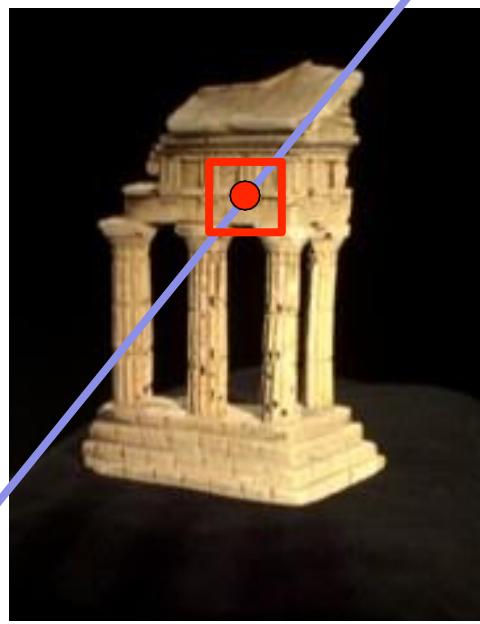
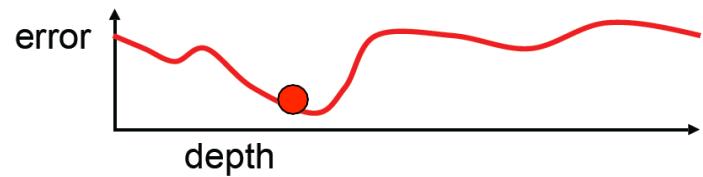
Basic idea



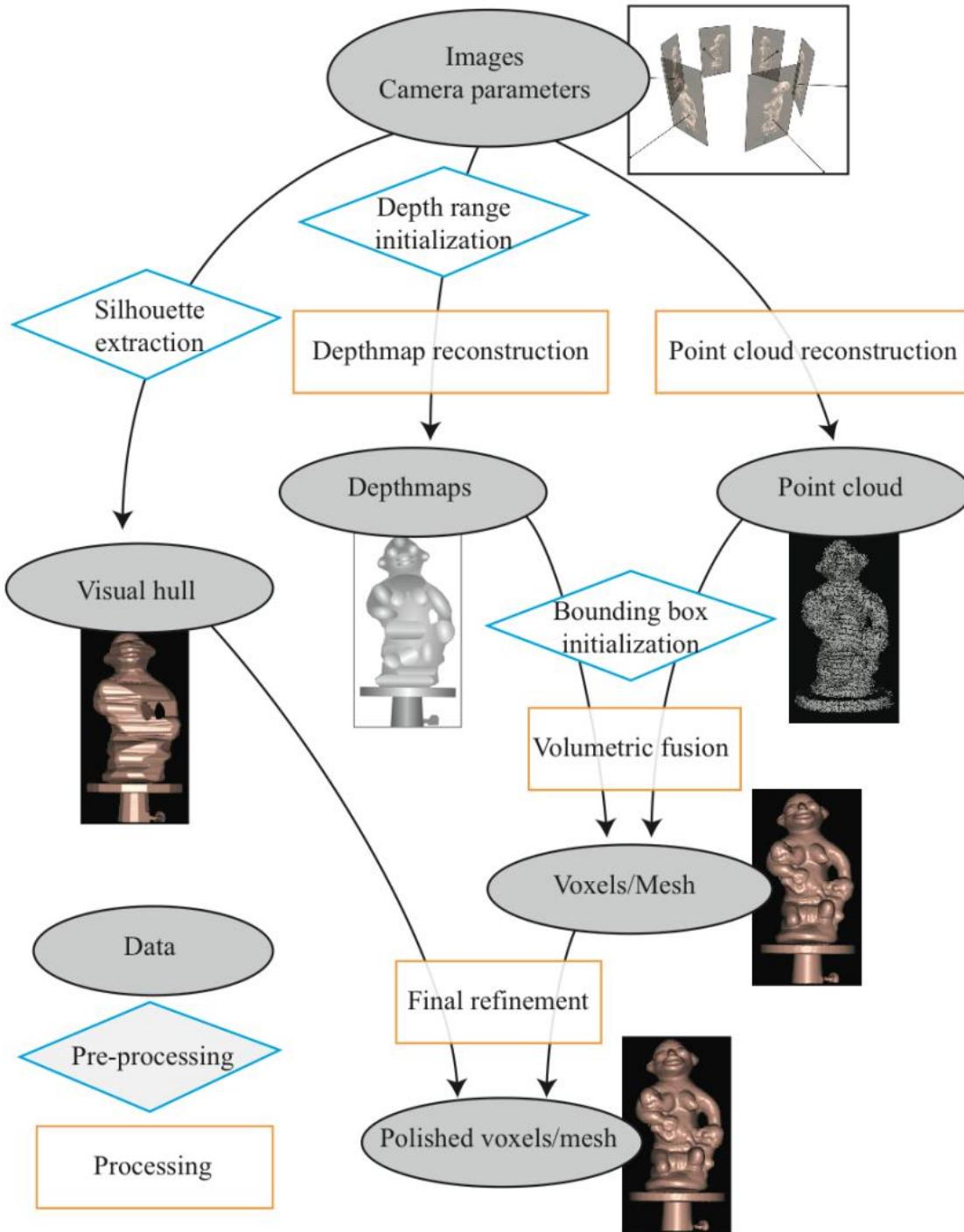
Source: Y. Furukawa

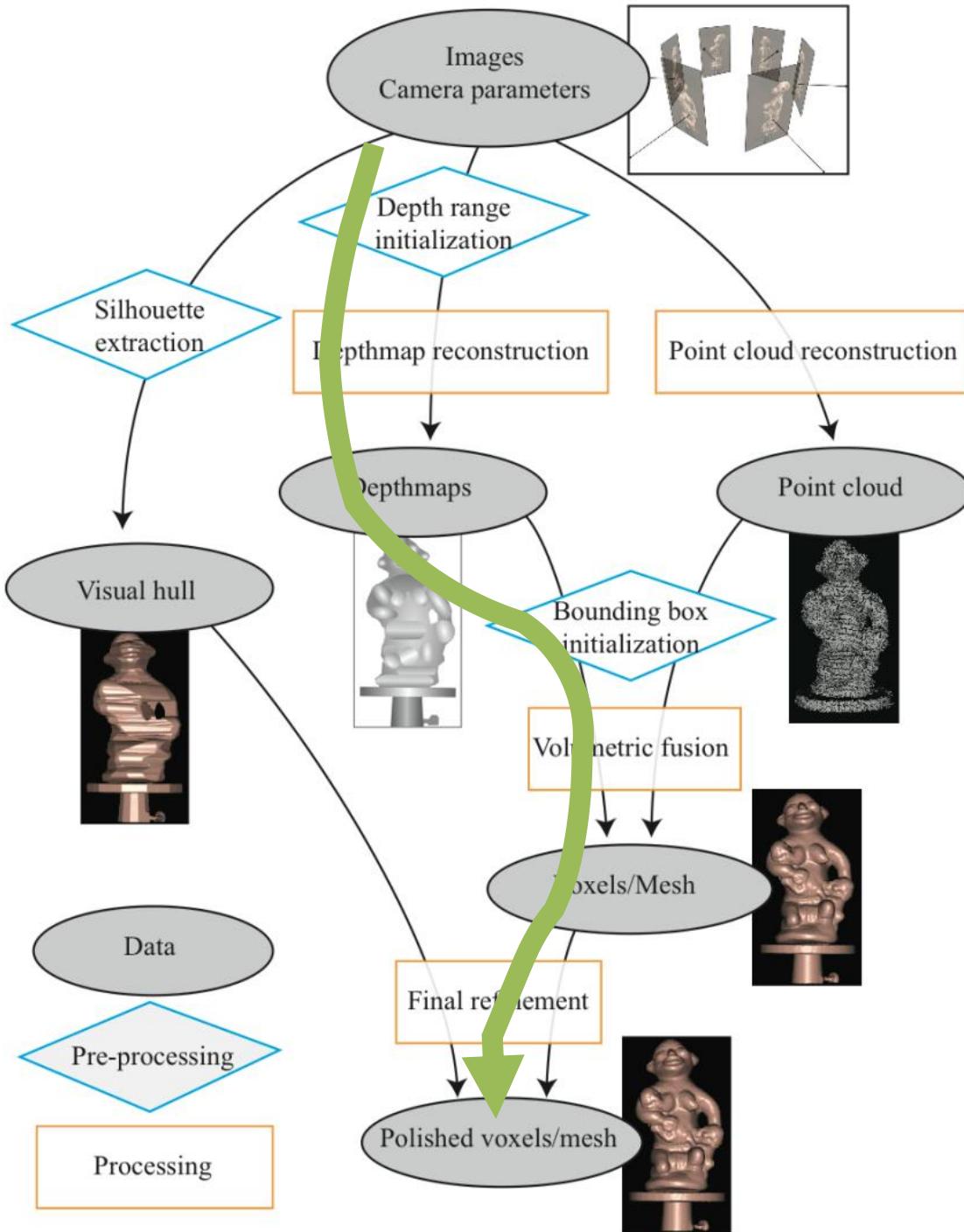
Multi-view stereo:

Basic idea

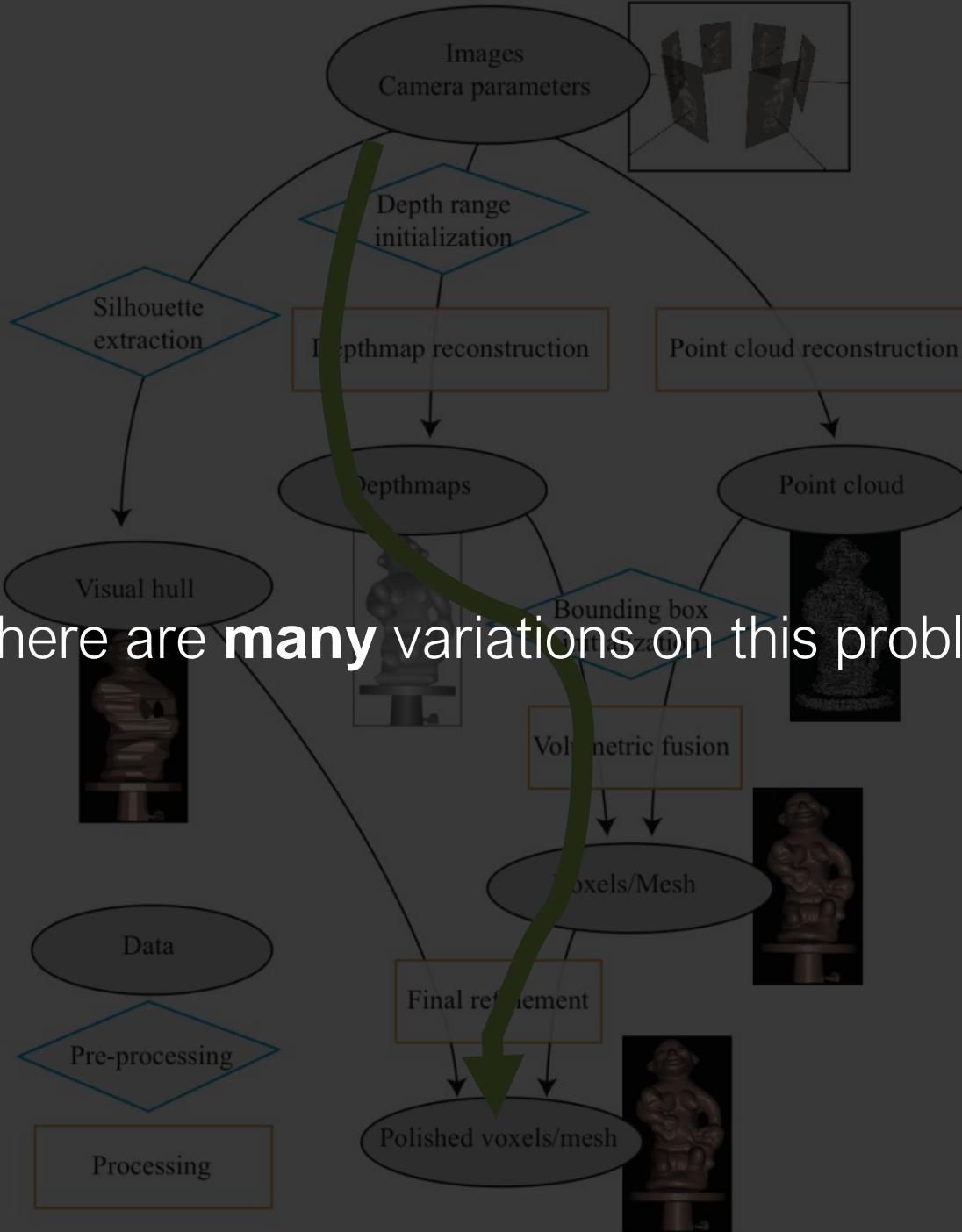


Source: Y. Furukawa



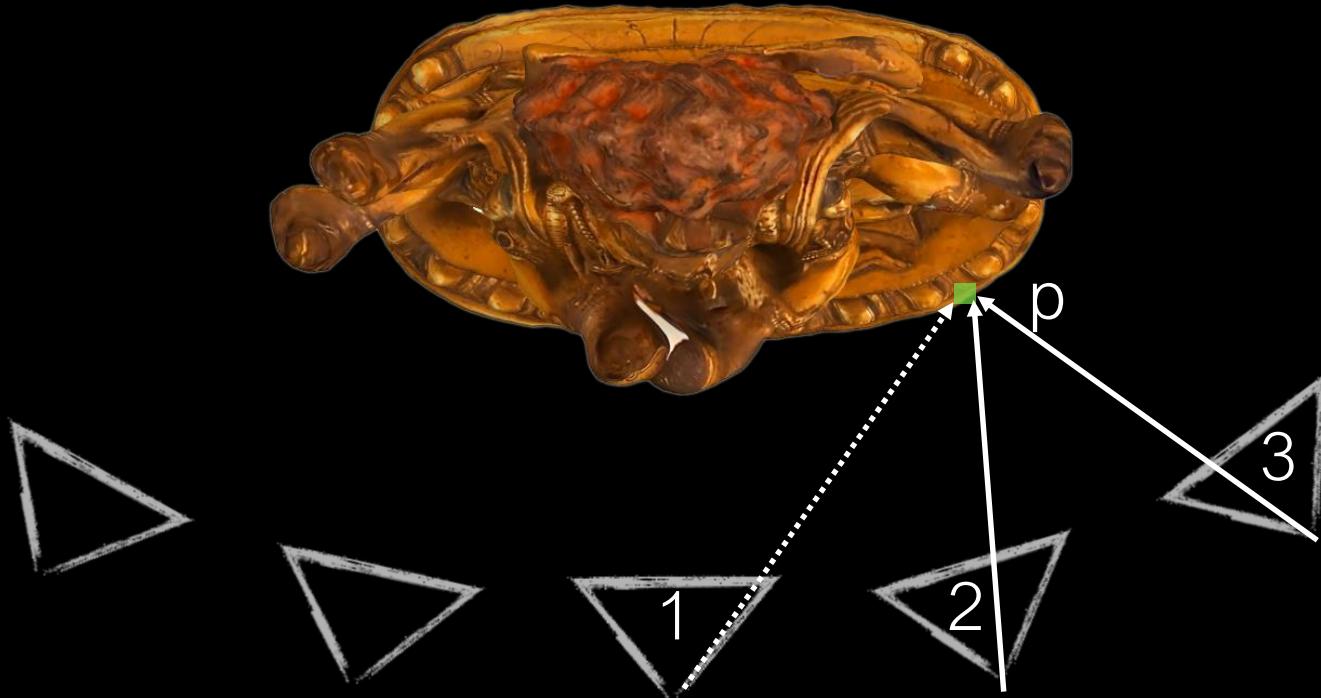


There are **many** variations on this problem.

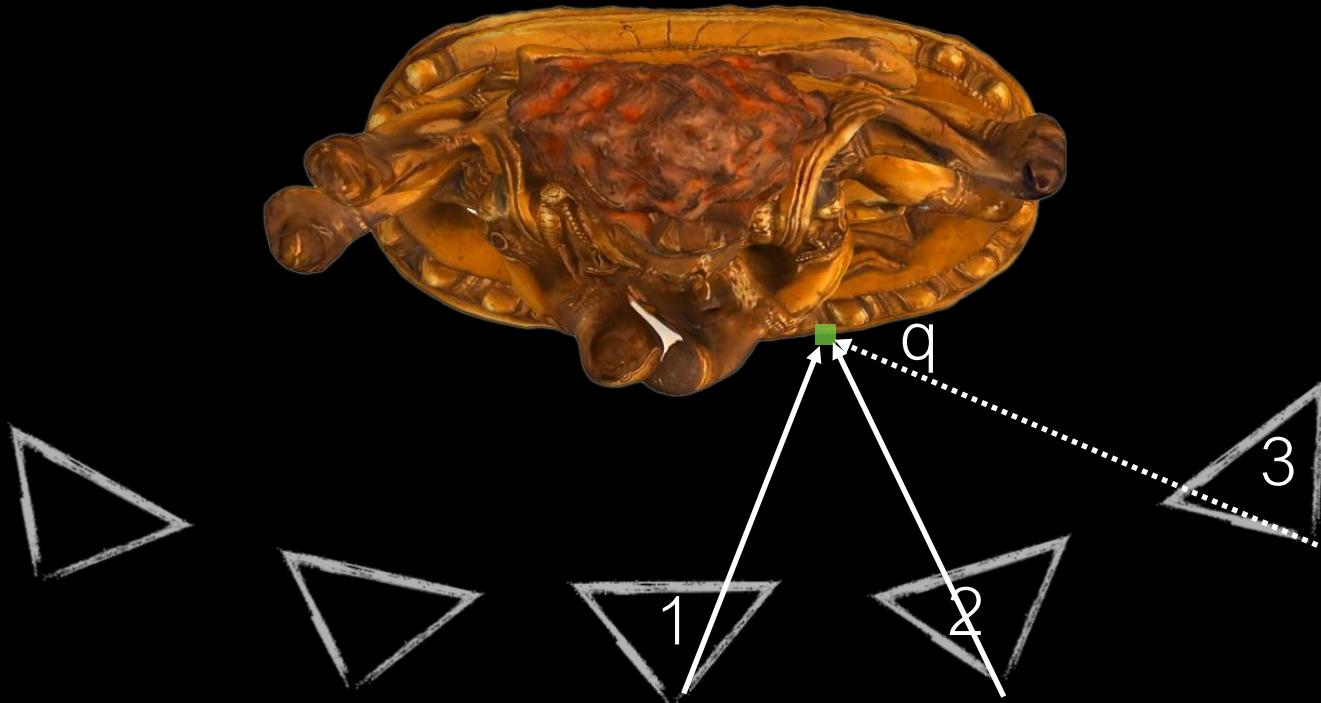


Why MVS?

- Different points on the object's surface will be more clearly visible in some subset of cameras
 - Could have high-res closeups of some regions
 - Some surfaces are foreshortened from certain views



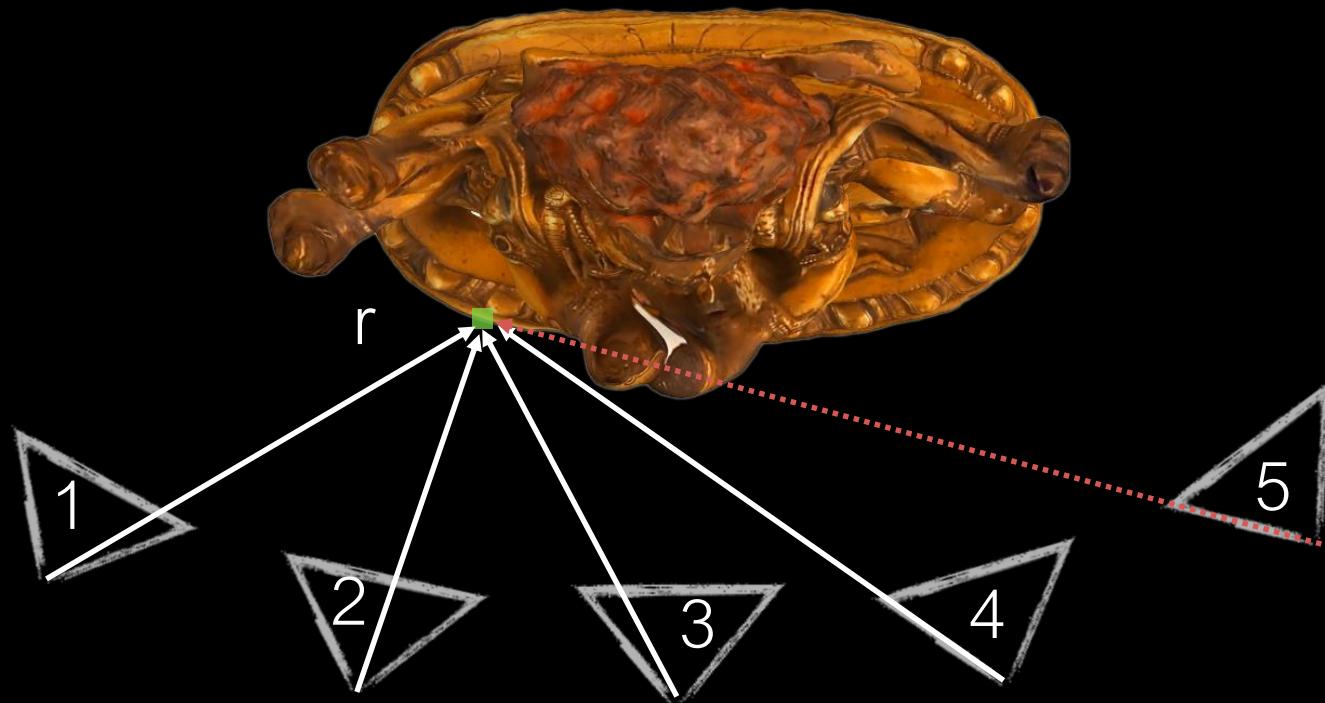
Cameras 2 and 3 can more clearly see point p.



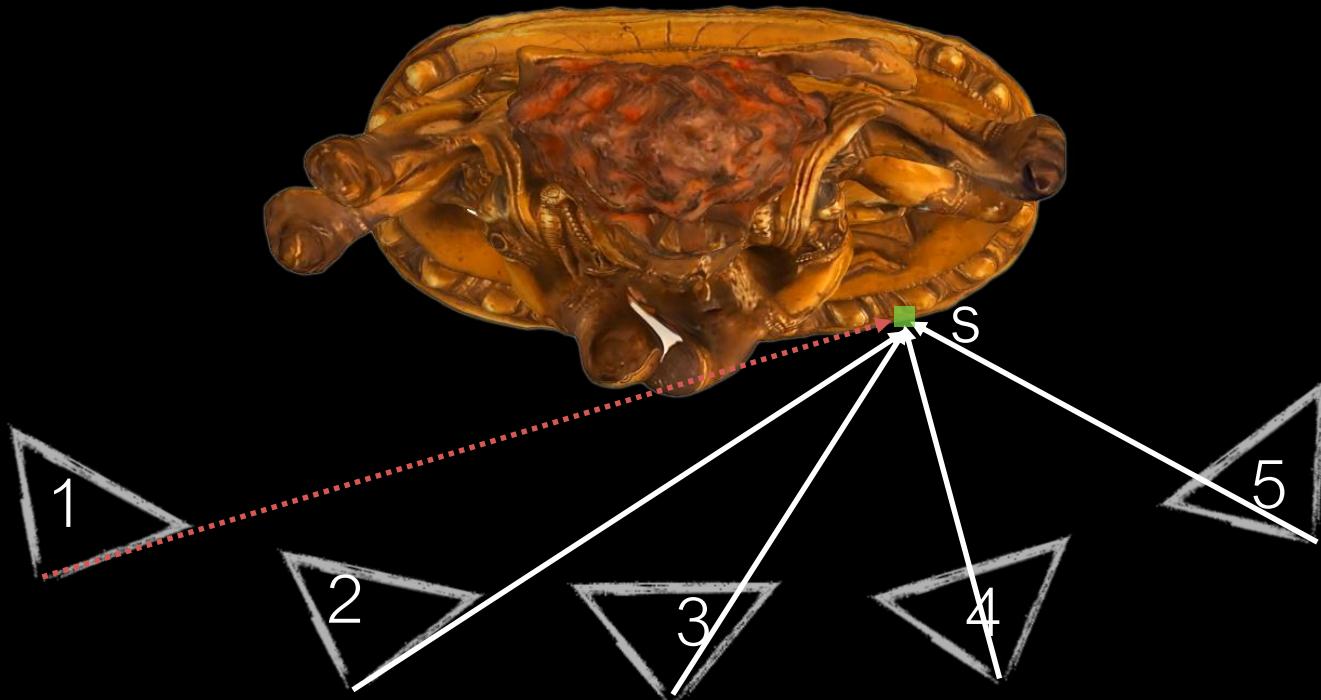
Cameras 1 and 2 can more clearly see point q.

Why MVS?

- Different points on the object's surface will be more clearly visible in some subset of cameras
 - Could have high res close-ups of some regions
 - Some surfaces are foreshortened from certain views
- Some points may be occluded entirely in certain views



Camera 5 can't see point r.



Camera 1 can't see point s.

Why MVS?

- Different points on the object's surface will be more clearly visible in some subset of cameras
 - Could have high res closeups of some regions
 - Some surfaces are foreshortened from certain views
- Some points may be occluded entirely in certain views
- More measurements per point can reduce error



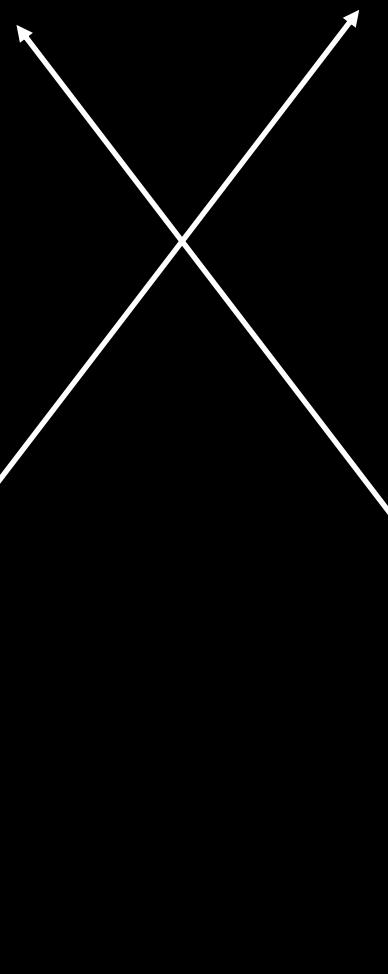
1

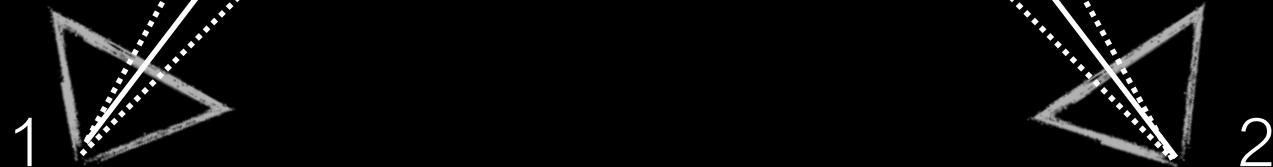
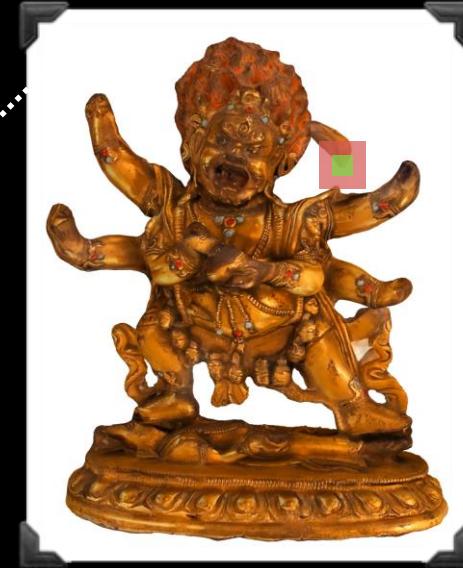
2



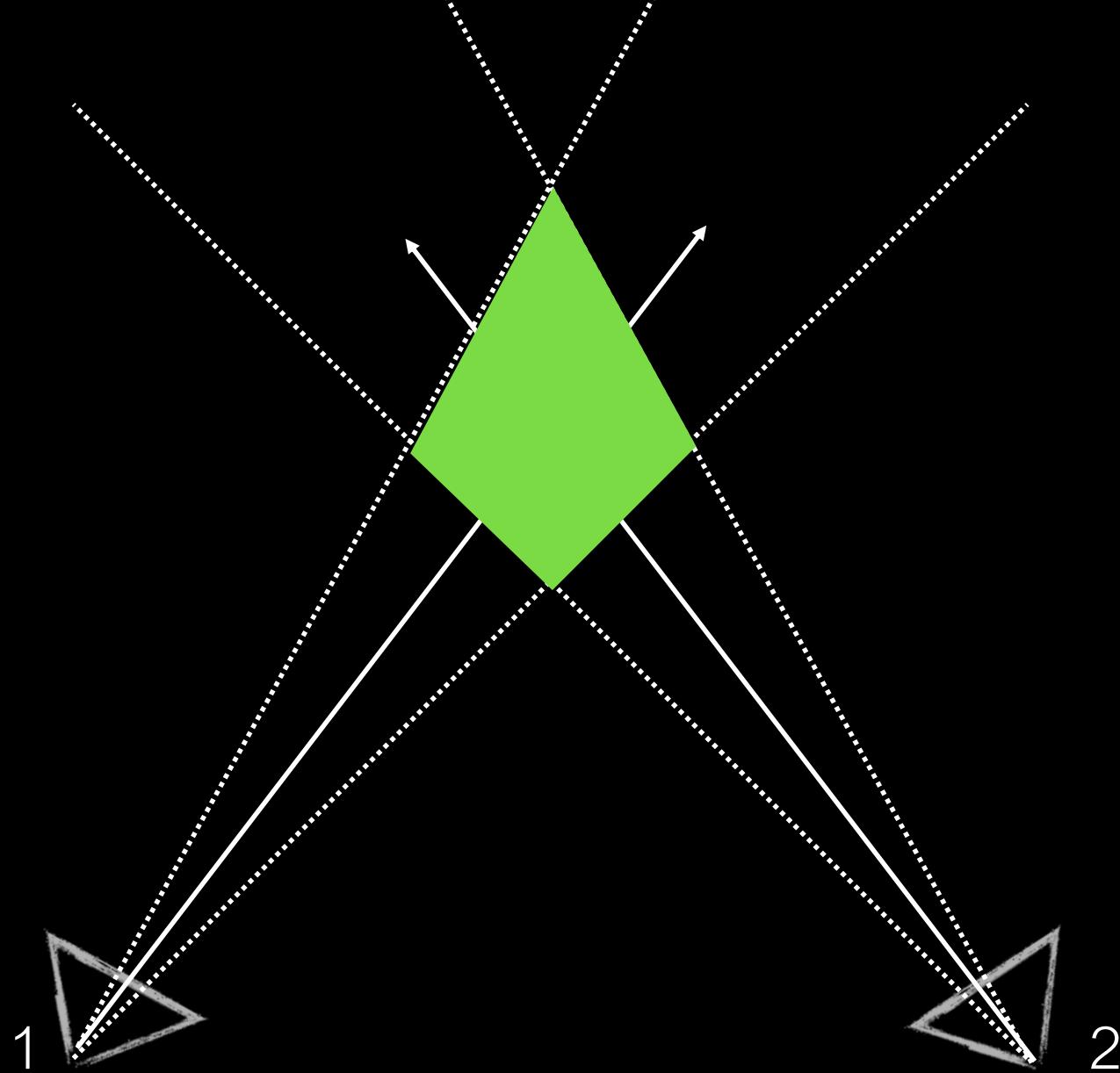
1

2

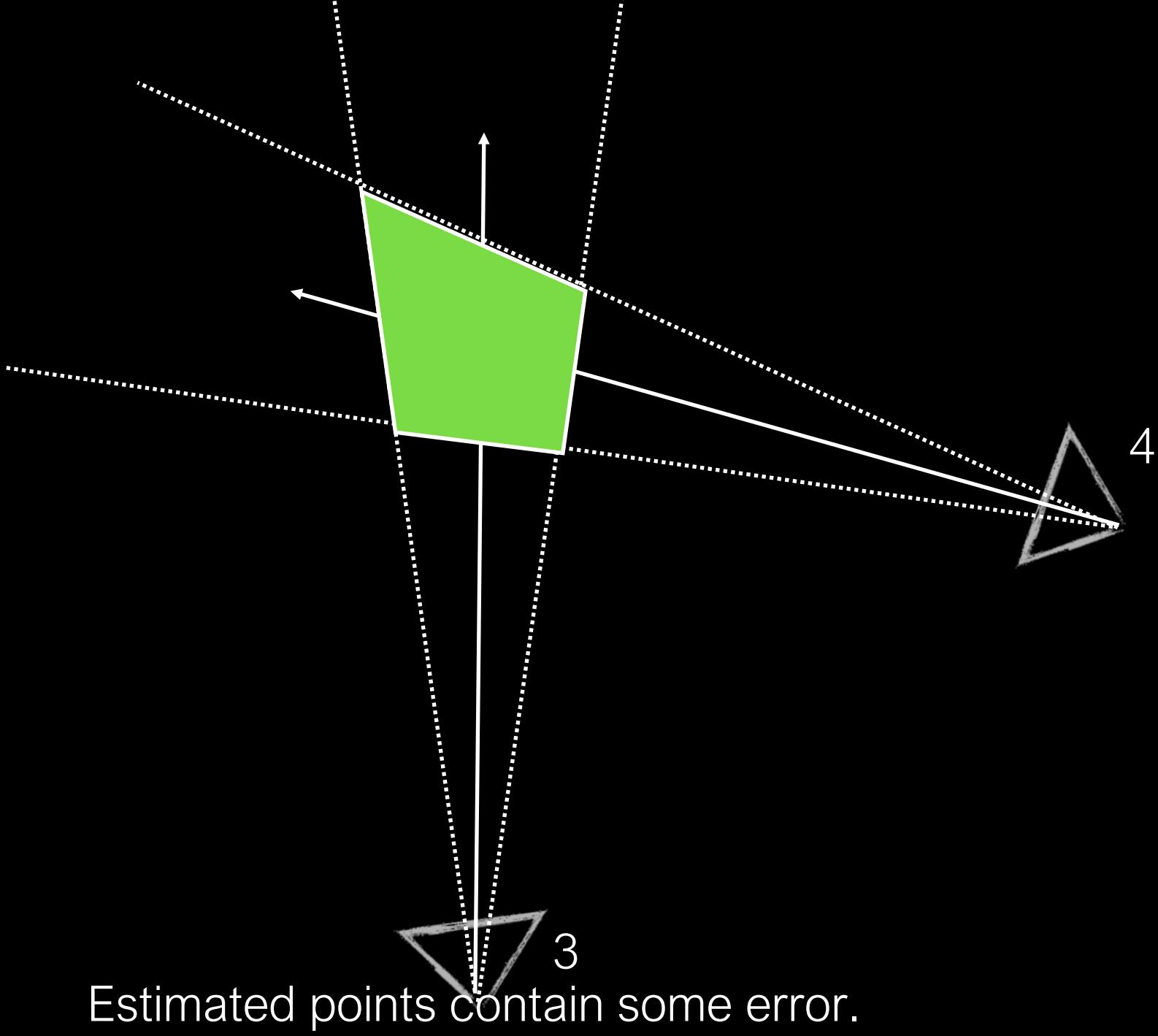


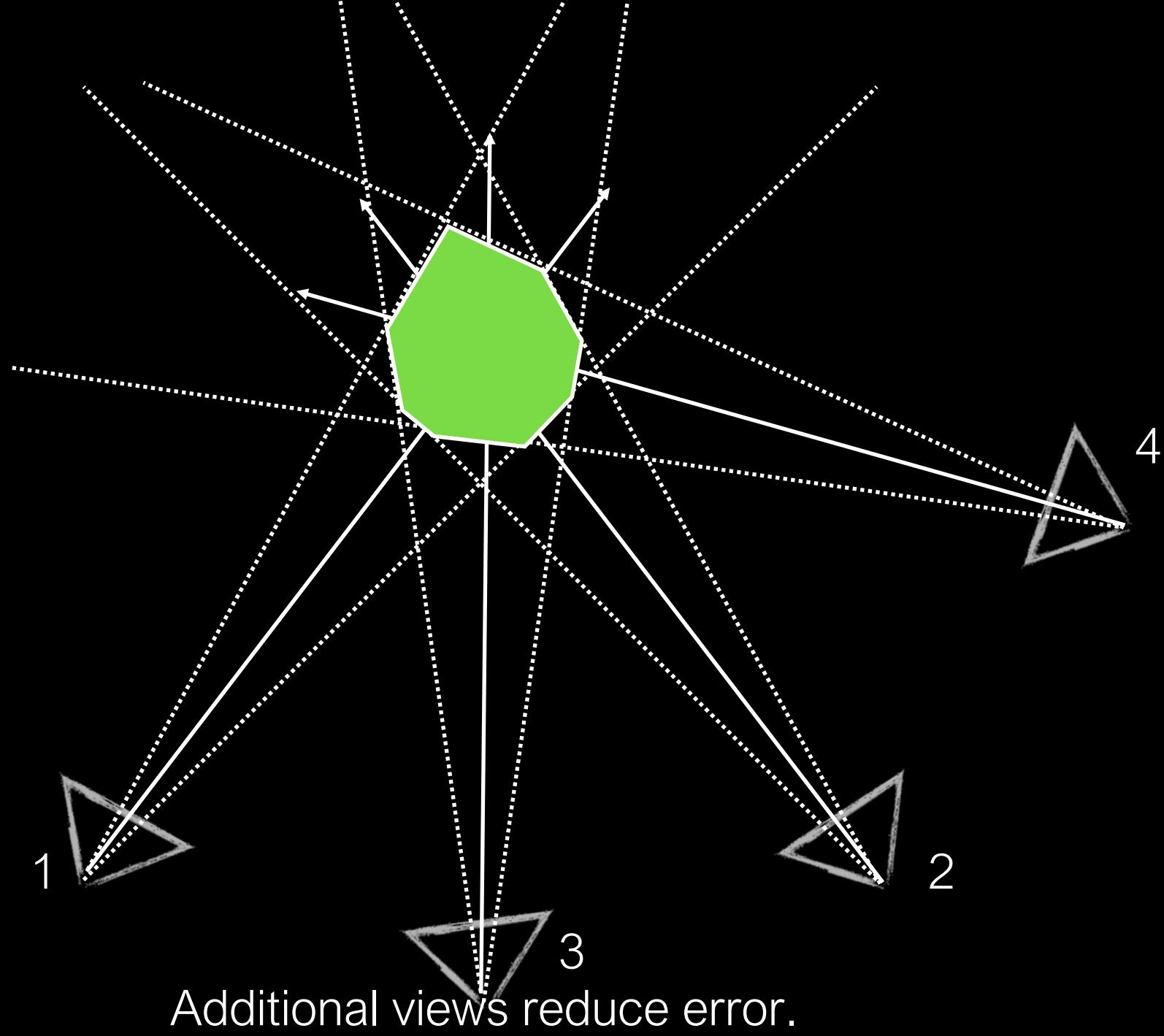


Estimated points contain some error.



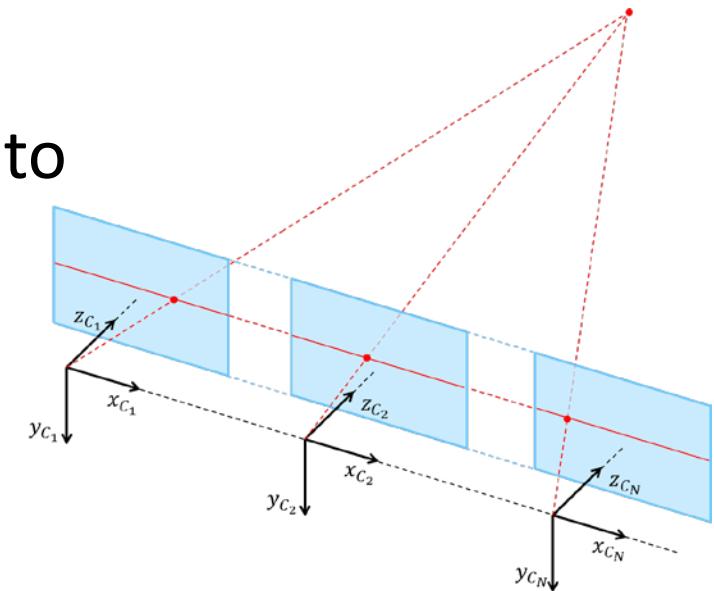
Estimated points contain some error.



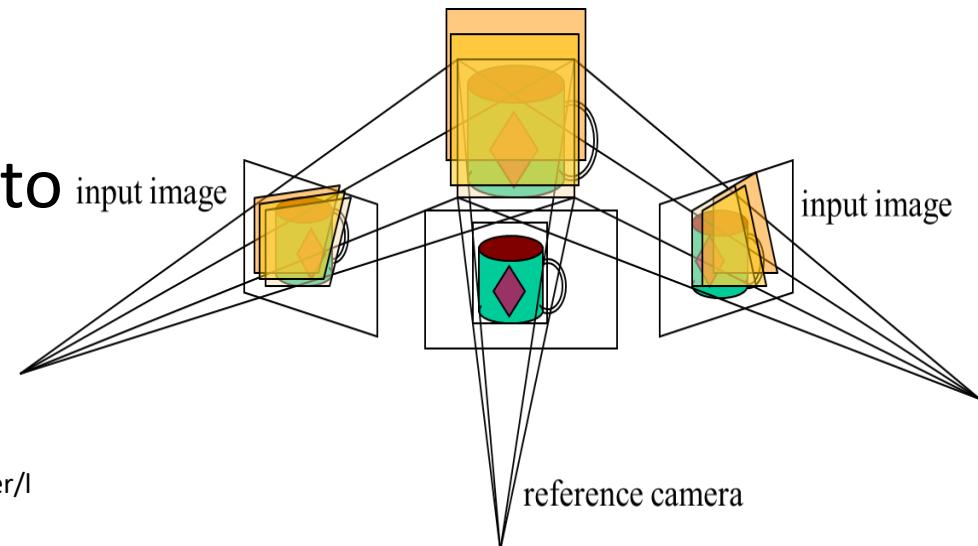


Depth maps reconstruction

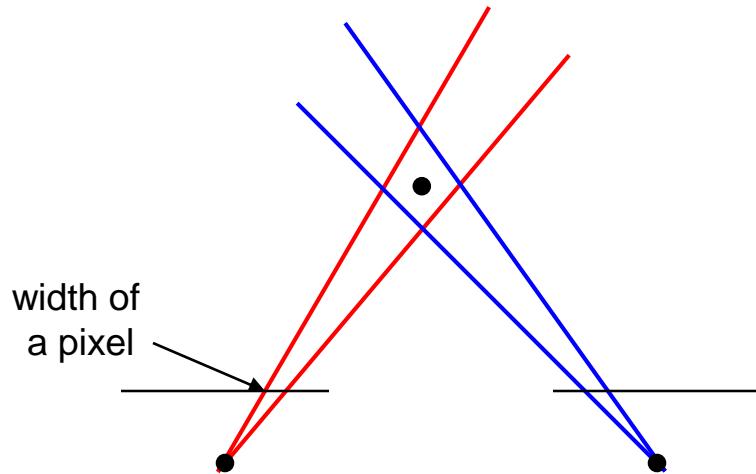
- **Multiple-baseline stereo**
 - Rectification of several cameras onto common plane
 - Problems with wide baselines and distortions after rectification



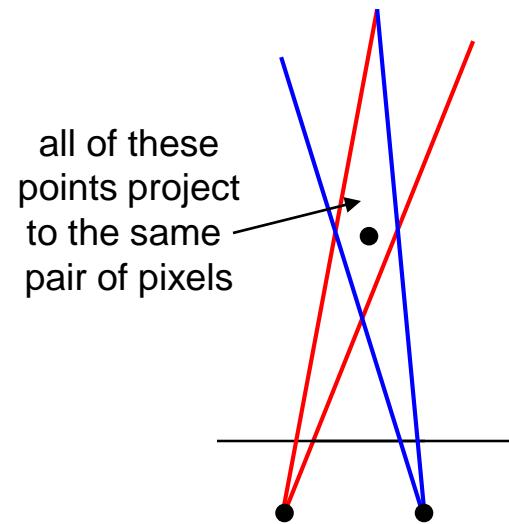
- **Plane sweep stereo**
 - Choose a reference view
 - Sweep family of planes at different depths with respect to the reference camera



Choosing the stereo baseline



Large Baseline



Small Baseline

What's the optimal baseline?

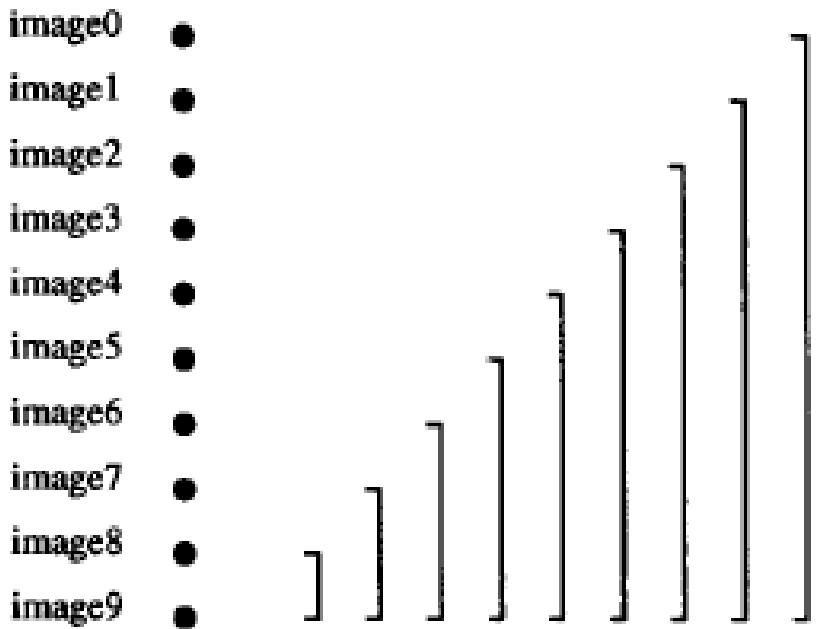
- Too small: large depth error
- Too large: difficult search problem

The Effect of Baseline on Depth Estimation

- Pick a reference image, and slide the corresponding window along the corresponding epipolar lines of all other images, using **inverse depth** relative to the first image as the search parameter

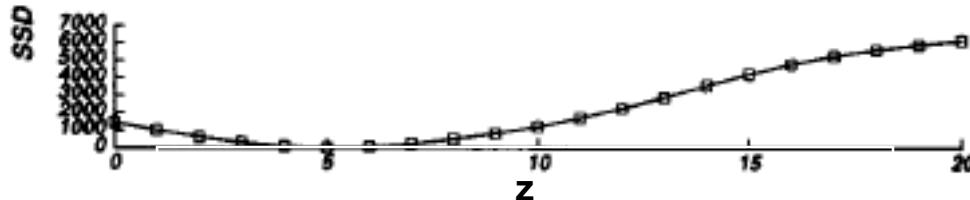


Figure 2: An example scene. The grid pattern in the background has ambiguity of matching.

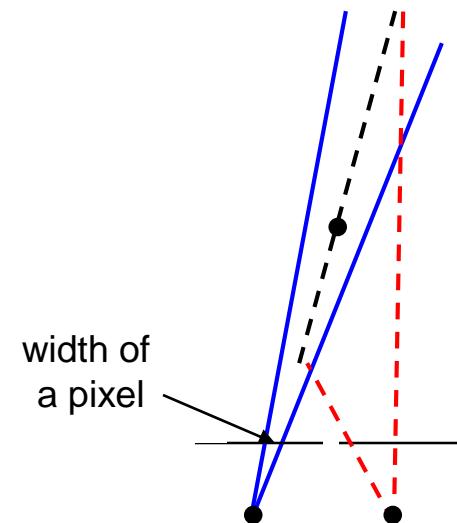


Baseline b 2b 3b 4b 5b 6b 7b 8b 9b

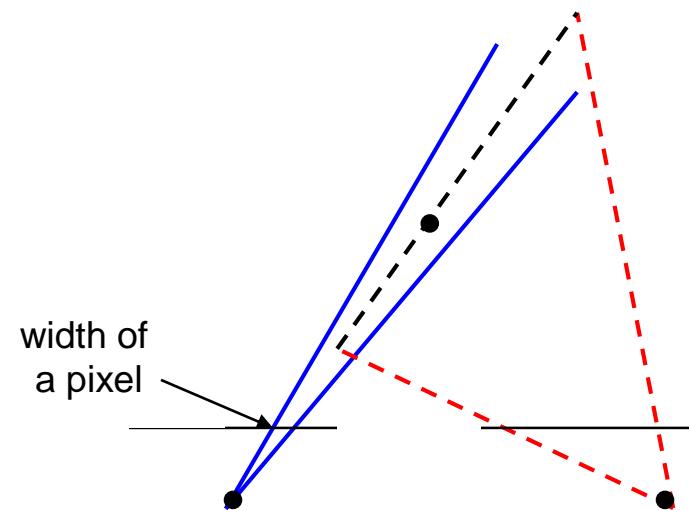
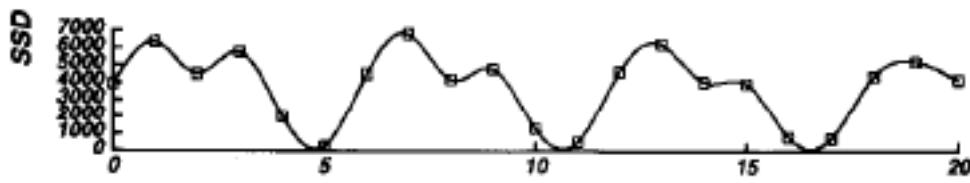
Multiple-baseline stereo



pixel matching score



- For short baselines, estimated depth will be less precise due to narrow triangulation



- For larger baselines^z, must search larger area in second image

Multiple-baseline stereo

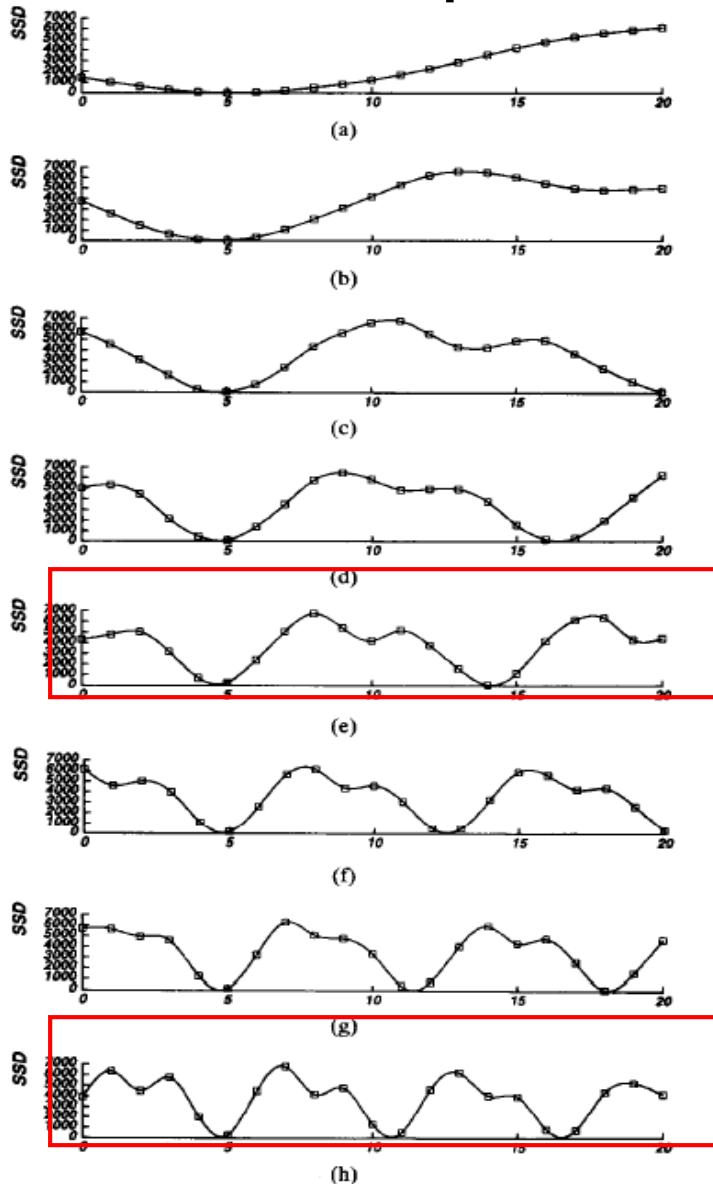


Fig. 5. SSD values versus inverse distance: (a) $B = b$; (b) $B = 2b$; (c) $B = 3b$; (d) $B = 4b$; (e) $B = 5b$; (f) $B = 6b$; (g) $B = 7b$; (h) $B = 8b$. The horizontal axis is normalized such that $8bF = 1$.

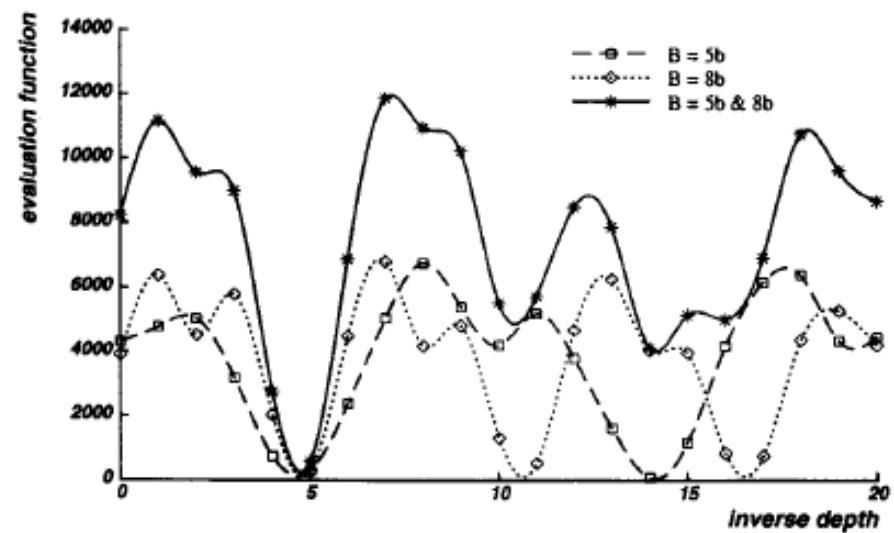


Fig. 6. Combining two stereo pairs with different baselines.

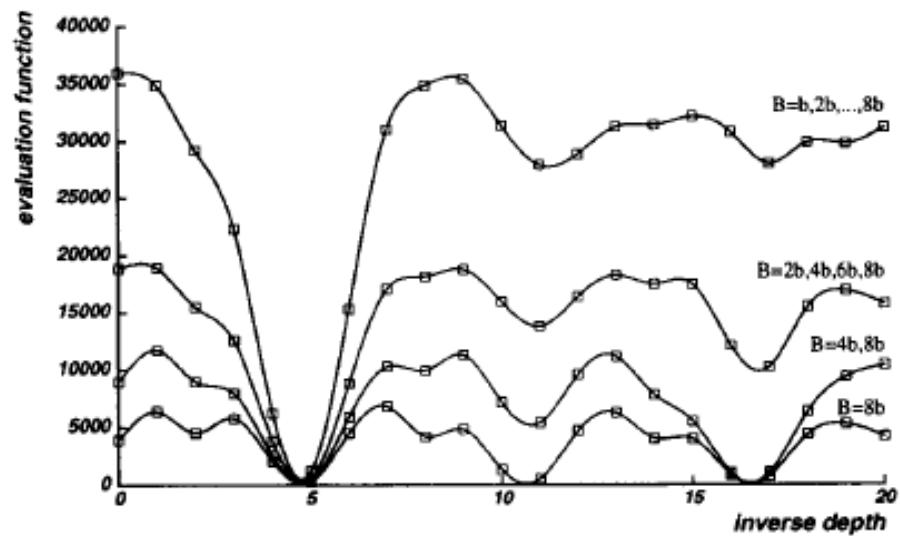
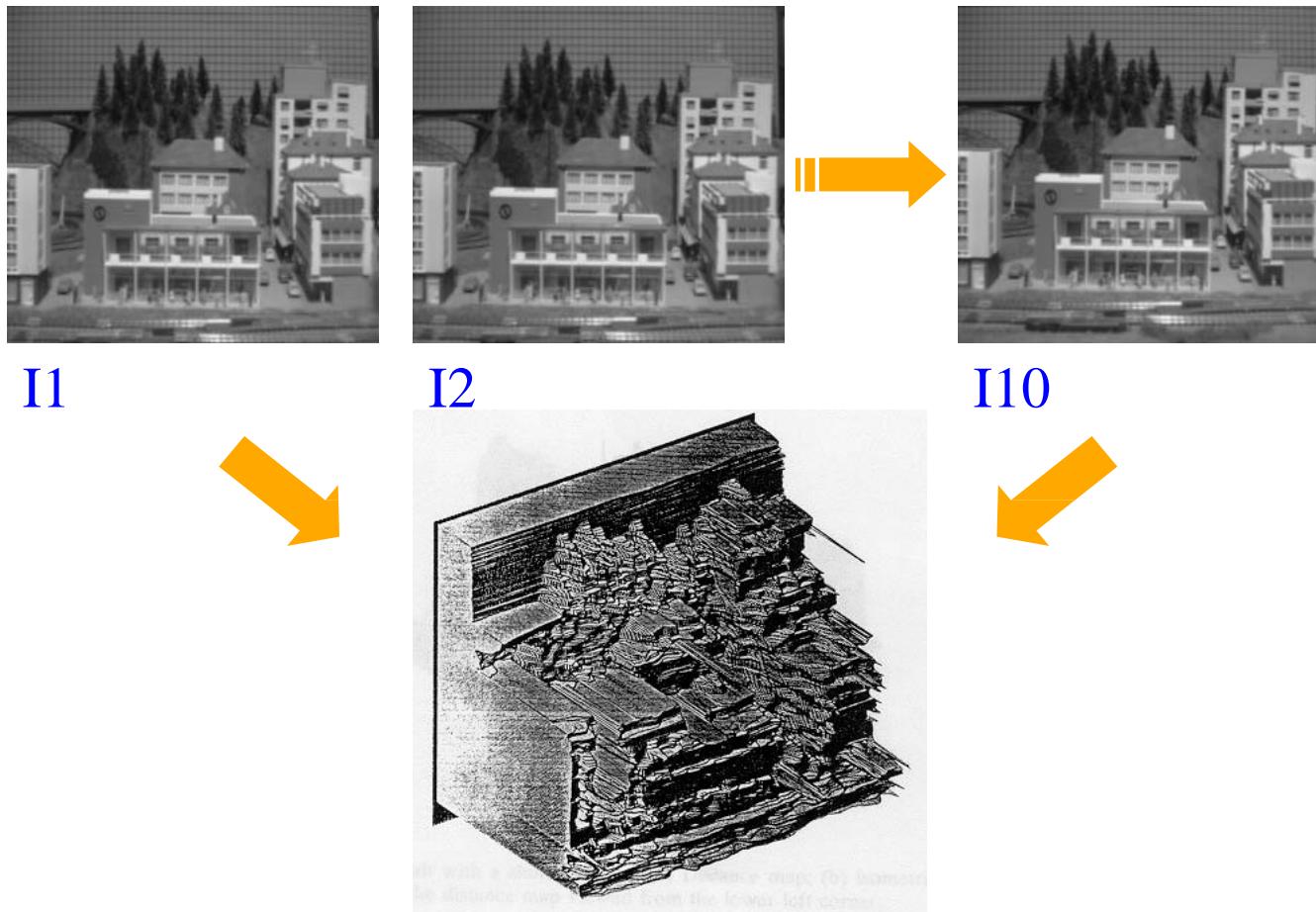


Fig. 7. Combining multiple baseline stereo pairs.

Multiple-baseline stereo results



M. Okutomi and T. Kanade, “A Multiple-Baseline Stereo System,” IEEE Trans. on Pattern Analysis and Machine Intelligence, 15(4):353-363 (1993).

Multibaseline Stereo

Basic Approach

- Choose a reference view
- Use your favorite stereo algorithm BUT
 - replace two-view SSD with **SSSD** over all baselines
 - **SSSD**: the SSD values are computed first for each pair of stereo images, and then add all together from multiple stereo pairs.

Limitations

- Only gives a depth map (not an “object model”)
- Won’t work for widely distributed views.

Problem: *visibility*

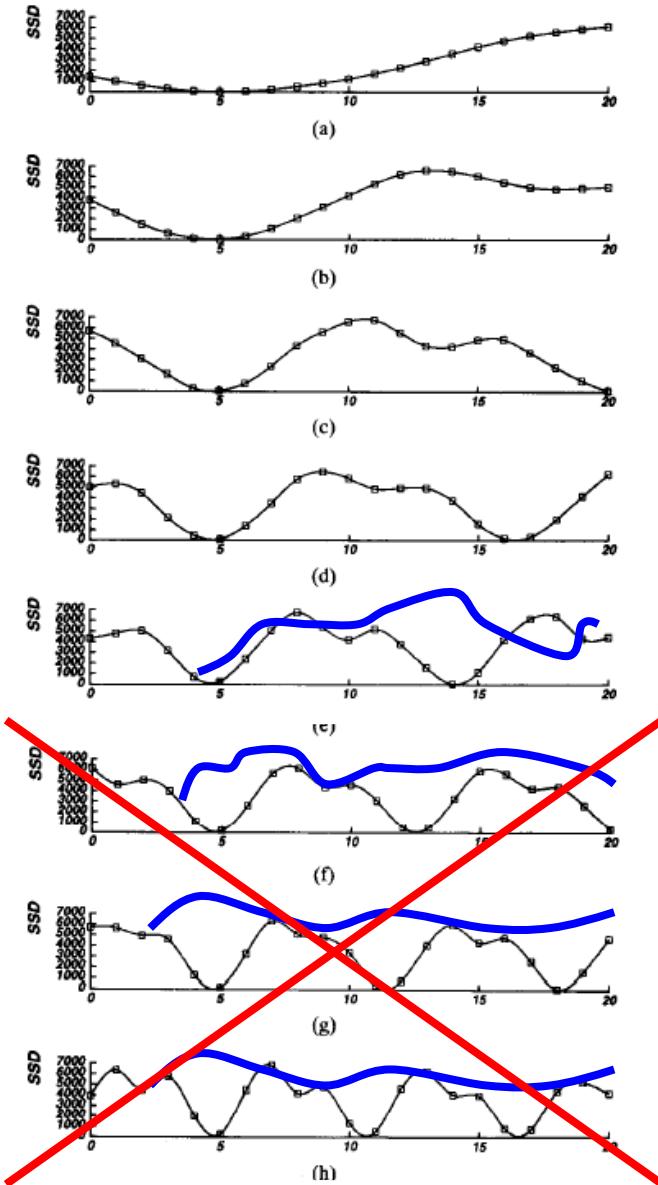


Fig. 5. SSD values versus inverse distance: (a) $B = b$; (b) $B = 2b$; (c) $B = 3b$; (d) $B = 4b$; (e) $B = 5b$; (f) $B = 6b$; (g) $B = 7b$; (h) $B = 8b$. The horizontal axis is normalized such that $8bF = 1$.

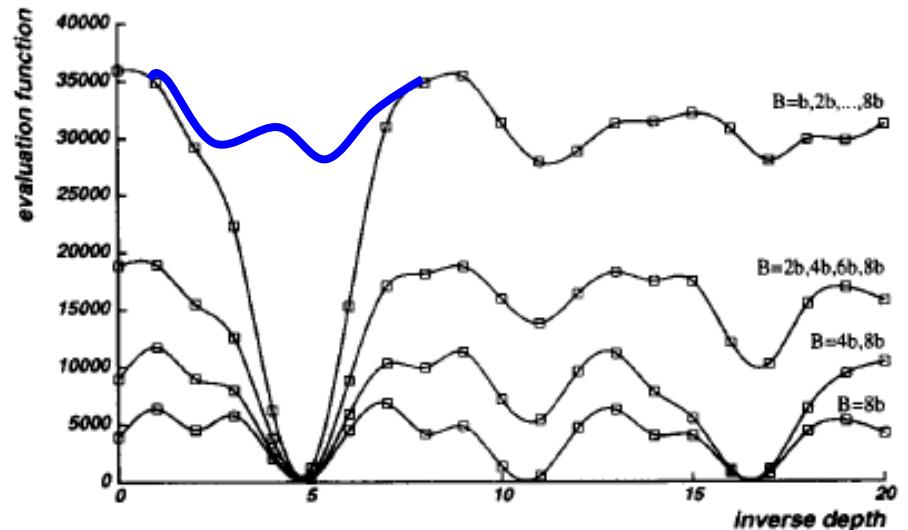


Fig. 7. Combining multiple baseline stereo pairs.

Some Solutions

- Match only nearby photos [Narayanan 98]
- Use NCC instead of SSD,
Ignore NCC values > threshold
[Hernandez & Schmitt 03]

Photo-consistency measures (matching score)

Given a set of N input images and a 3D point p seen by all the images, one can define the photo-consistency of p w.r.t. each pair of images I_i and I_j as:

$$\mathcal{C}_{ij}(p) = \rho(I_i(\Omega(\pi_i(p))), I_j(\Omega(\pi_j(p)))), \quad (2.1)$$

where $\rho(f, g)$ is a similarity measure that compares two vectors, $\pi_i(p)$ denotes the projection of p into image i , $\Omega(x)$ defines a support domain around point x , and $I_i(x)$ denotes the image intensities sampled within the domain. Every photo-consistency measure can be described as a particular choice of ρ and Ω .

Popular matching scores

- SSD (Sum Squared Distance)

$$\sum_{x,y} |W_1(x,y) - W_2(x,y)|^2$$

- SAD (Sum of Absolute Difference) $\sum_{x,y} |W_1(x,y) - W_2(x,y)|$
- ZNCC (Zero-mean Normalized Cross Correlation)

$$\frac{\sum_{x,y} (W_1(x,y) - \bar{W}_1)(W_2(x,y) - \bar{W}_2)}{\sigma_{W_1} \sigma_{W_2}}$$

– where $\bar{W}_i = \frac{1}{n} \sum_{x,y} W_i$ $\sigma_{W_i} = \sqrt{\frac{1}{n} \sum_{x,y} (W_i - \bar{W}_i)^2}$

- what advantages might NCC have?

Summary

Table 2.1: Summary table of different similarity measures used to compute photo-consistency.

Measure	required Ω	invariance
Sum of Squared Differences (SSD)	no	none
Sum of Absolute Differences (SAD)	no	none
Normalized Cross Correlation (NCC)	yes	bias/gain
Census	yes	bias/gain
Rank	yes	bias/gain/rotation
Mutual Information (MI)	yes	any bijection

Plane sweep stereo

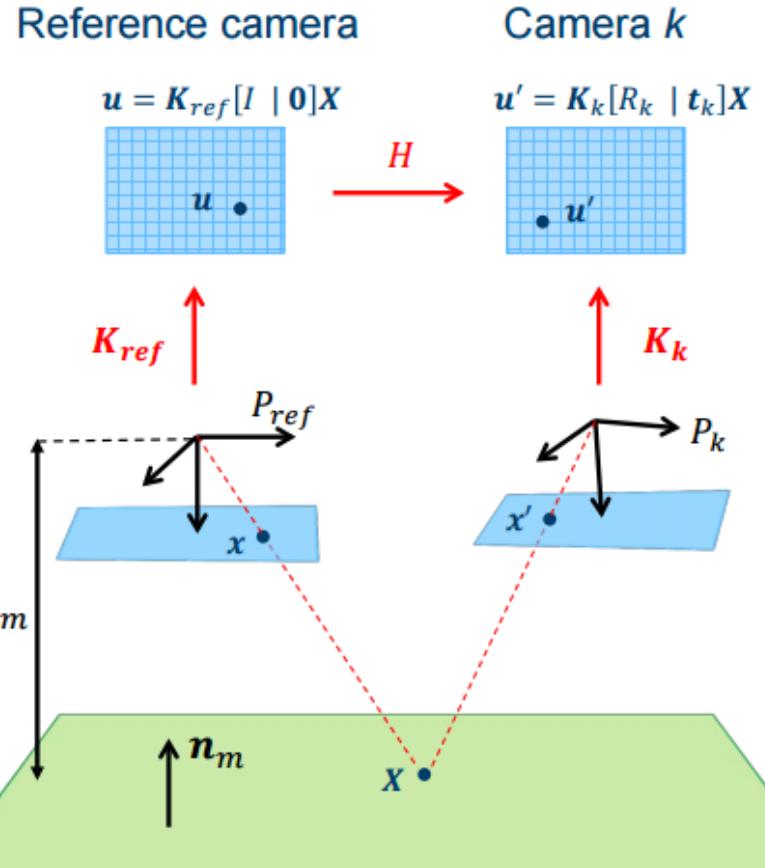
- The family of depth planes in the coordinate frame of the reference view

$$\Pi_m = \begin{bmatrix} \mathbf{n}_m^T & -d_m \end{bmatrix}$$

- The mapping from the reference camera P_{ref} onto the plane Π_m and back to camera P_k is described by the homography induced by the plane Π_m

$$H_{\Pi_m, P_k} = K_k \left(R_k - t_k \mathbf{n}_m^T / d_m \right) K_{ref}^{-1}$$

- The mapping from P_k to P_{ref} induced by Π_m is the inverse homography H_{Π_m, P_k}^{-1}



Plane sweep stereo

1. Map each target image I_k to the reference image I_{ref} for each depth plane Π_m with the homography H_{Π_m, P_k}^{-1} giving the warped images $\breve{I}_{k,m}$
2. Compute the similarity between I_{ref} and each $\breve{I}_{k,m}$
 - Zero Mean Normalized Cross Correlation (ZNCC) between small patches W around each pixel
3. Compute the figure-of-merit for each depth plane by combining the similarity measurements for each image k

$$M(u, v, \Pi_m) = \sum_k \text{ZNCC}(I_{ref}, \breve{I}_{k,m})$$

4. For each pixel, select the depth plane with best fit

$$\tilde{\Pi}(u, v) = \arg \max_m M(u, v, \Pi_m)$$

Plane sweep through oriented planes

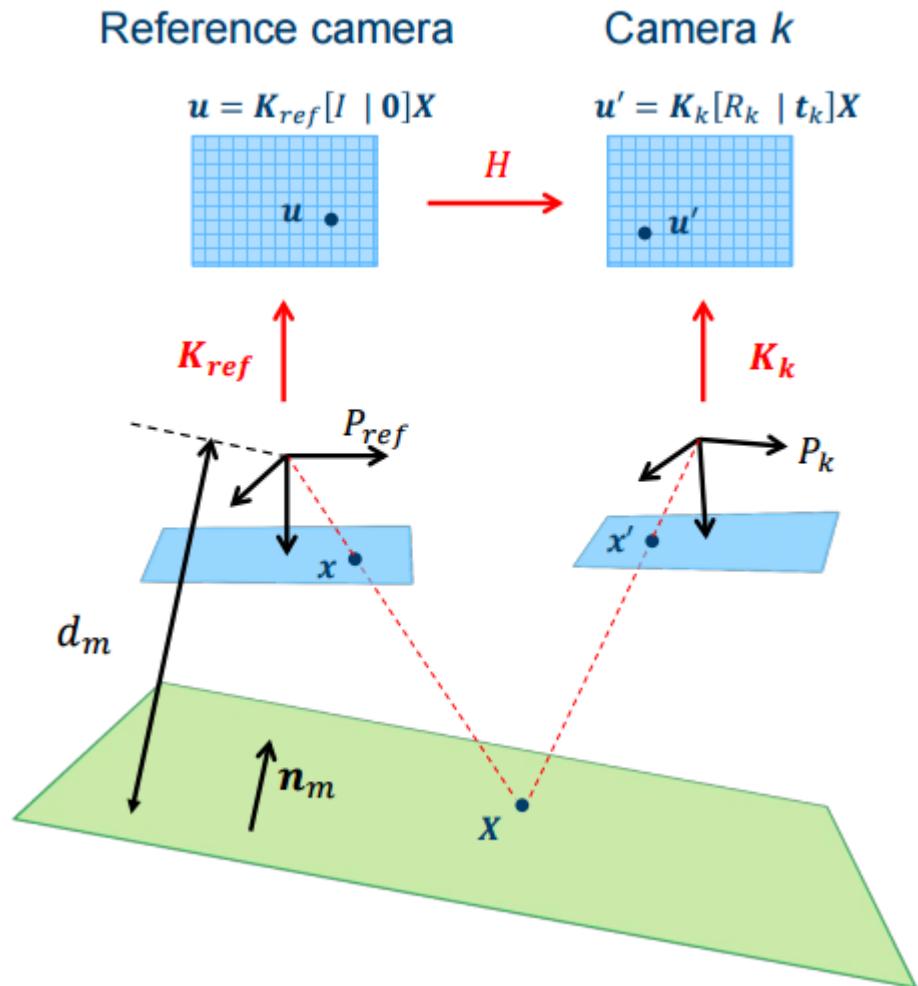
- Fronto-parallel

$$\mathbf{n}_m = [0 \ 0 \ -1]^T$$

$$Z_m(u, v) = d_m$$

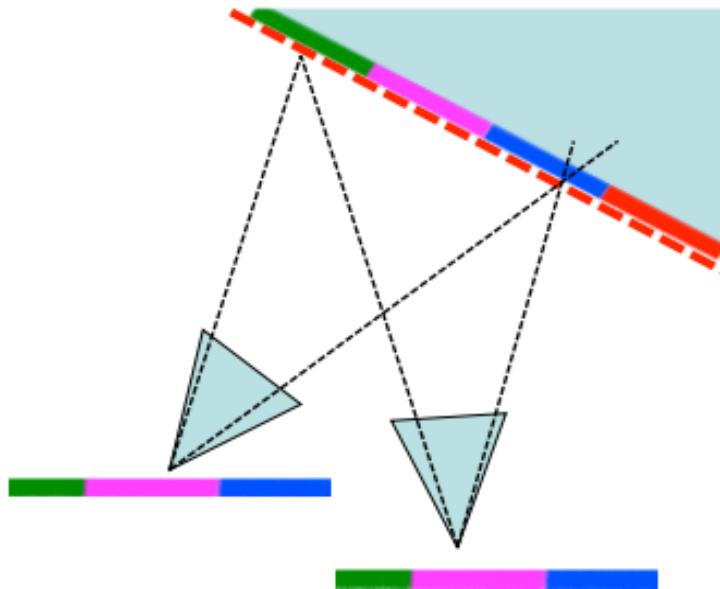
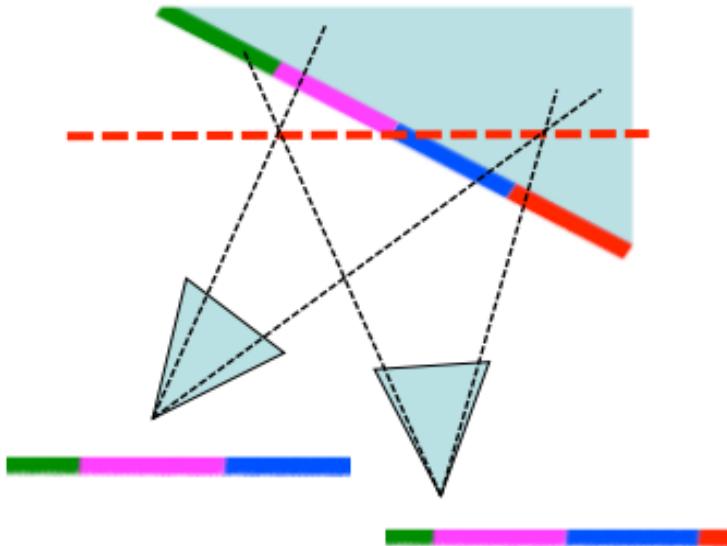
- Other plane orientations

$$Z_m(u, v) = \frac{-d_m}{[u \ v \ 1] K_{ref}^{-T} \mathbf{n}_m}$$



Plane Sweep: Enhanced Robustness through oriented planes

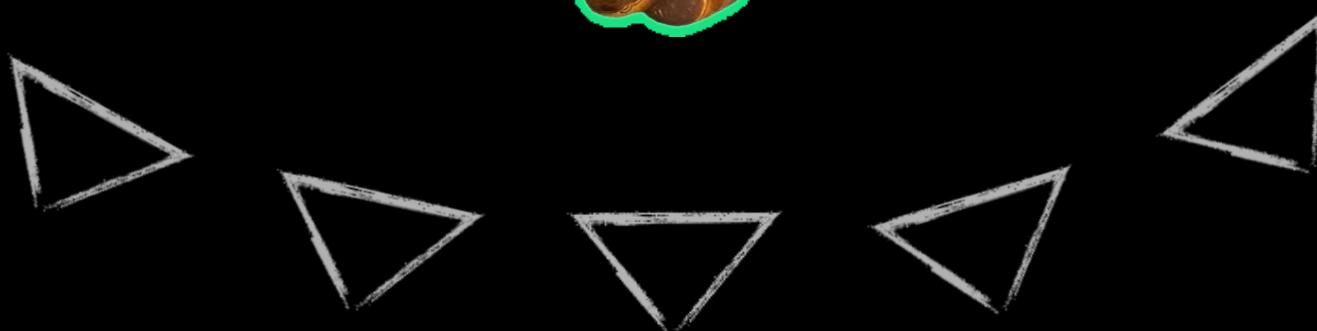
- Aligning sweeping direction to surface orientation reduces photometric inconsistencies at correct depth



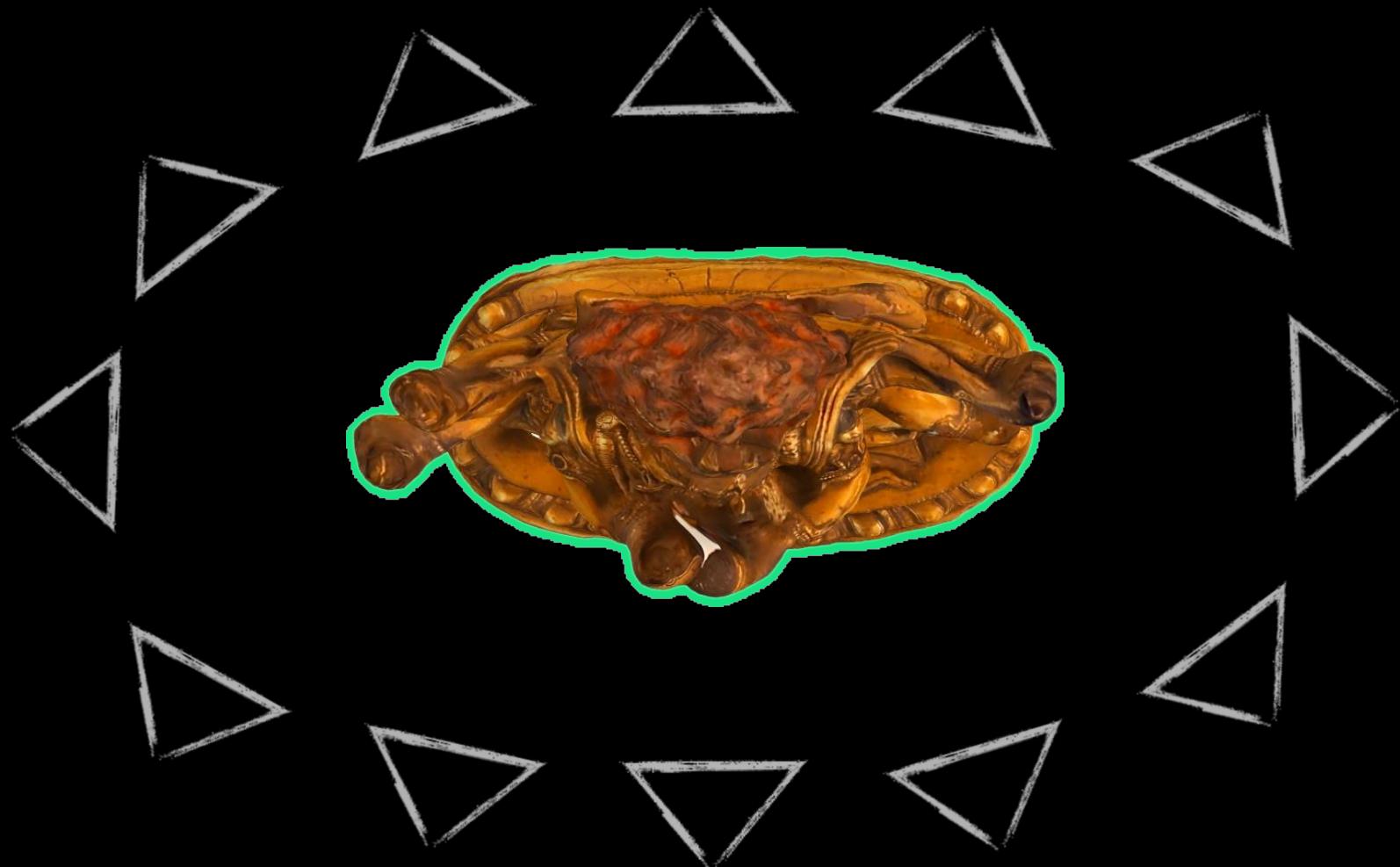
Streetside reconstructions by plane sweeping stereo



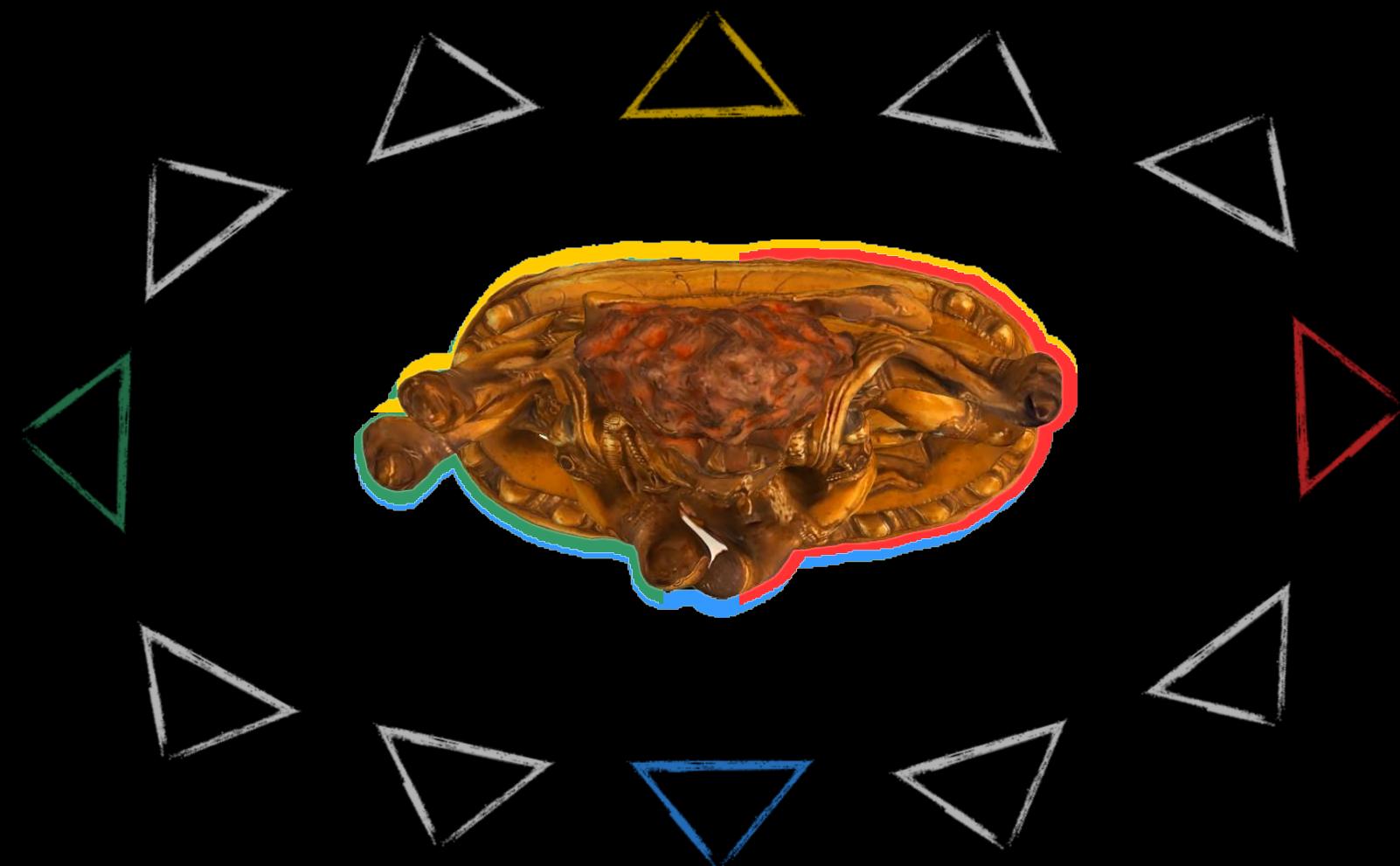
Single depth map often isn't enough



Really want full coverage



Idea: Combine many depth maps



Many depth maps, each with error. How can we fuse these?

Merging depth maps

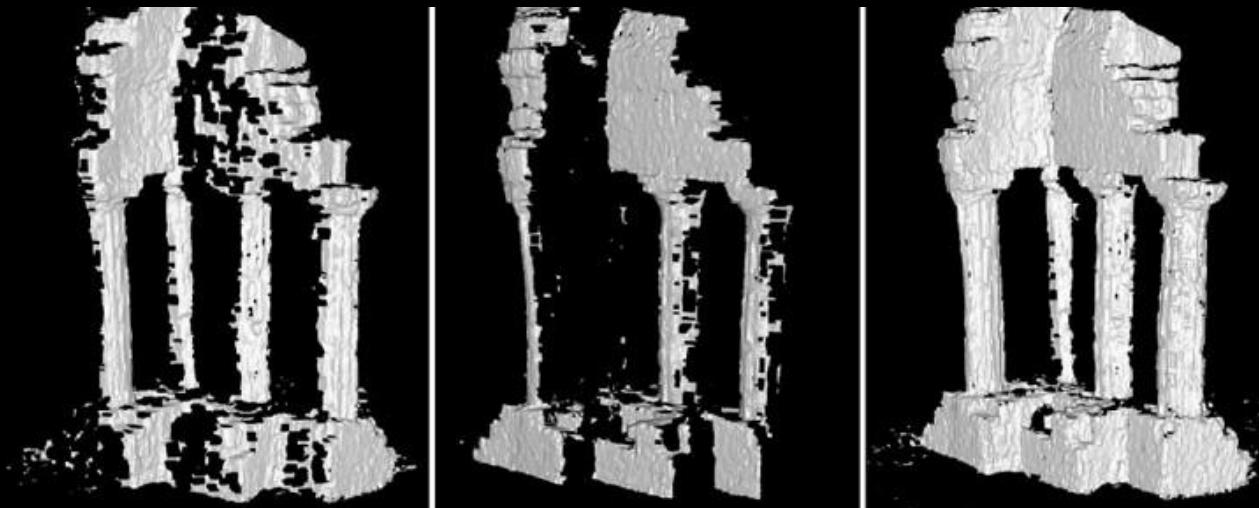
- Given a group of images, choose each one as reference and compute a depth map w.r.t. that view using a multi-baseline approach
- Merge multiple depth maps to a volume or a mesh (see, e.g., Curless and Levoy 96)



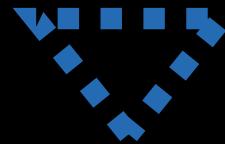
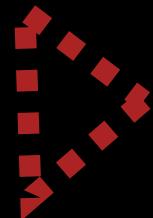
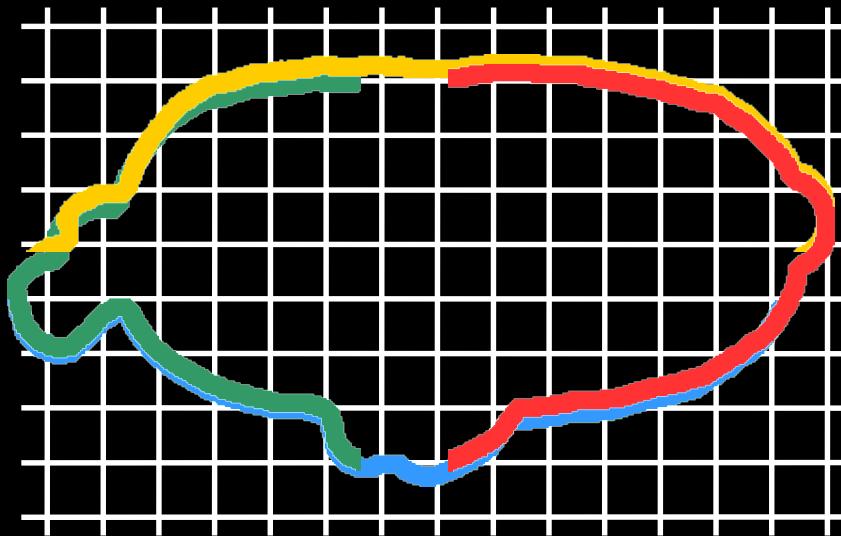
Map 1

Map 2

Merged

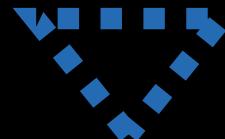
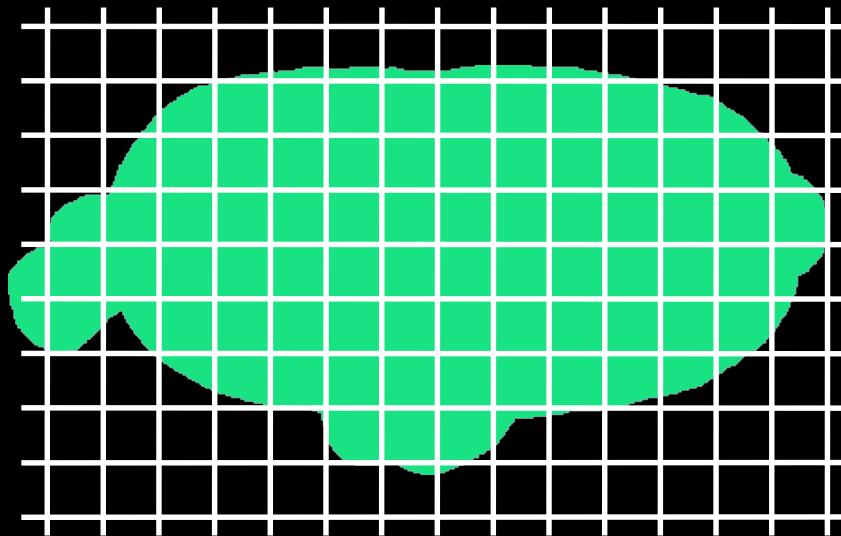


Volumetric fusion



A common world-space coordinate system.

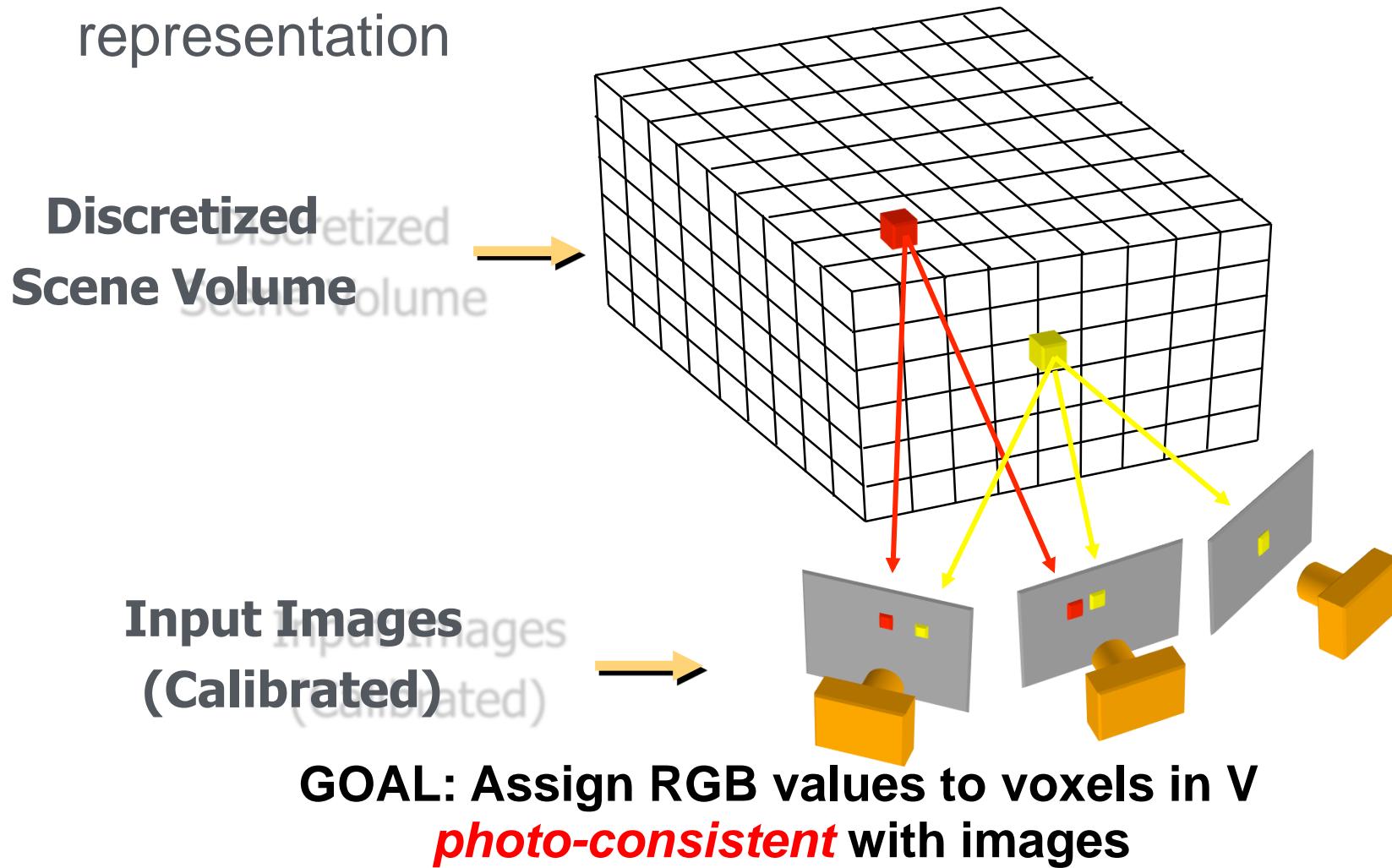
Volumetric fusion

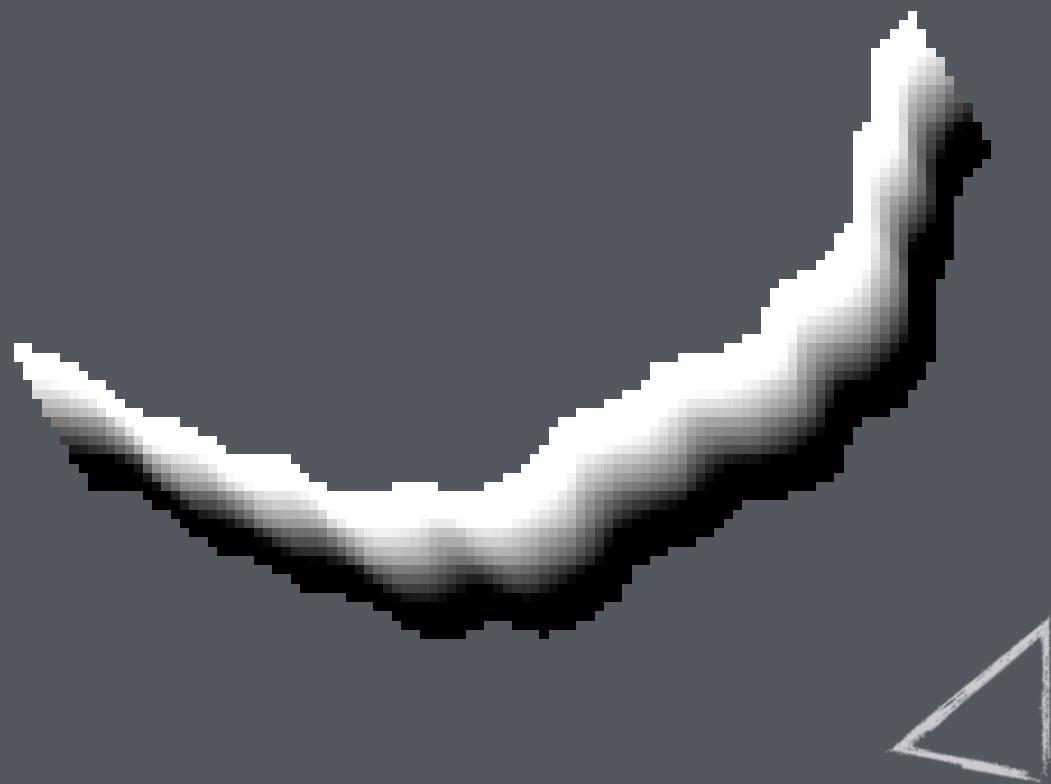


A common world-space coordinate system.

Volumetric stereo

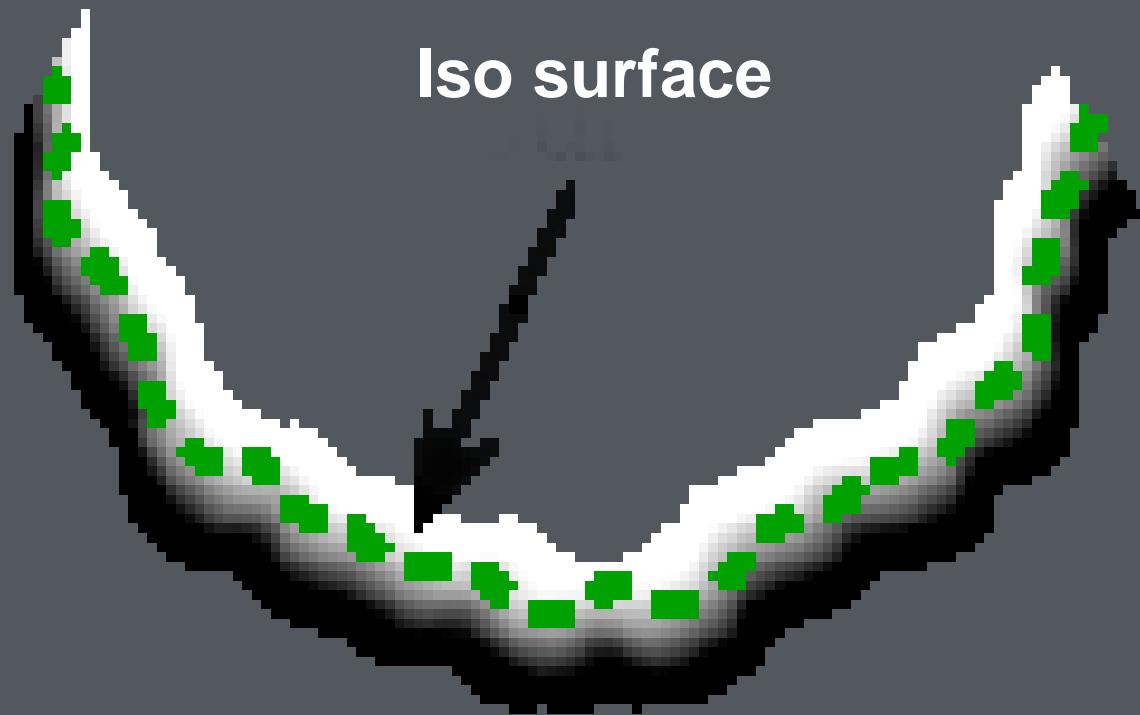
- In plane sweep stereo, the sampling of the scene depends on the reference view
- We can use a voxel volume to get a view independent representation







Iso surface



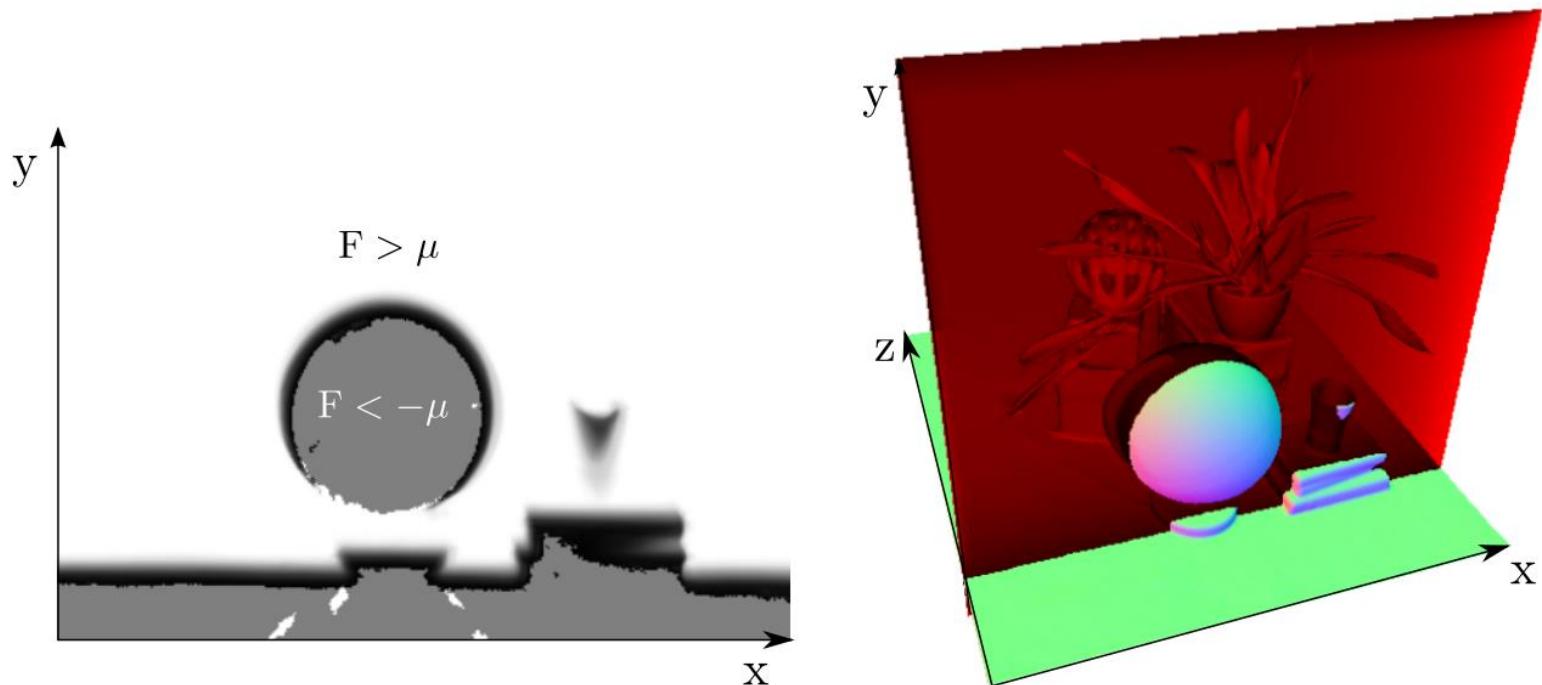


Figure 4: A slice through the truncated signed distance volume showing the truncated function $F > \mu$ (white), the smooth distance field around the surface interface $F = 0$ and voxels that have not yet had a valid measurement(grey) as detailed in eqn. 9.

KinectFusion: Real-time 3D Reconstruction and Interaction Using a Moving Depth Camera*

Shahram Izadi¹, David Kim^{1,3}, Otmar Hilliges¹, David Molyneaux^{1,4}, Richard Newcombe², Pushmeet Kohli¹, Jamie Shotton¹, Steve Hodges¹, Dustin Freeman^{1,5}, Andrew Davison², Andrew Fitzgibbon¹

¹Microsoft Research Cambridge, UK

²Imperial College London, UK

³Newcastle University, UK

⁴Lancaster University, UK

⁵University of Toronto, Canada

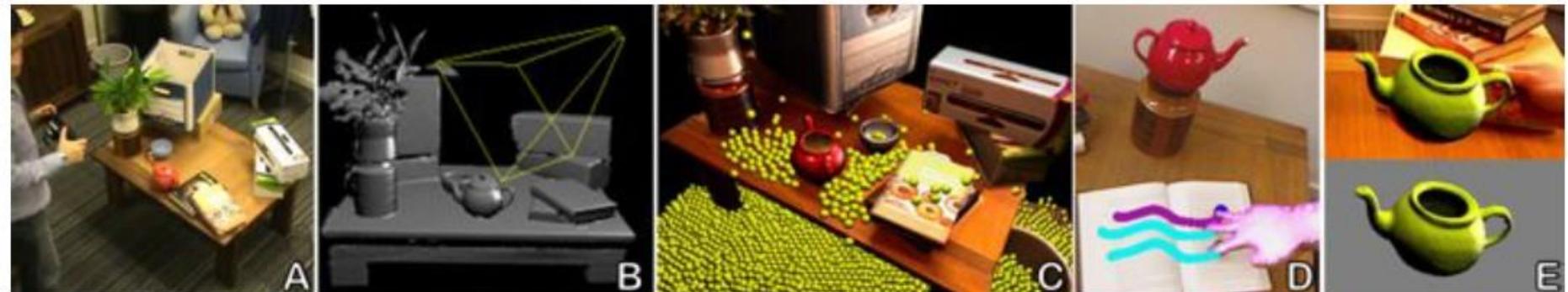


Figure 1: KinectFusion enables real-time detailed 3D reconstructions of indoor scenes using only the depth data from a standard Kinect camera. A) user points Kinect at coffee table scene. B) Phong shaded reconstructed 3D model (the wireframe frustum shows current tracked 3D pose of Kinect). C) 3D model texture mapped using Kinect RGB data with real-time particles simulated on the 3D model as reconstruction occurs. D) Multi-touch interactions performed on any reconstructed surface. E) Real-time segmentation and 3D tracking of a physical object.

Questions?

Questions?

Multi-view stereo from Internet Collections

[[Goesele, Snavely, Curless, Hoppe, Seitz, ICCV 2007](#)]

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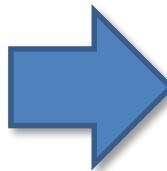
We found **80,865** results matching **statue** and **of** and **liberty**.

View: Most relevant • Most recent • Most interesting Show: Details • Thumbnails

From mbell1975 From sbcreate11 From Marion Doss From Barry Wright

From phileole From almk From sbcreate11 From sbcreate11

From sigardiner From sjgardiner From elesa.ah From nicoatridge



Stereo from community photo collections

- Need structure from motion to recover unknown camera parameters
- Need view selection to find good groups of images on which to run dense stereo

flickr® from YAHOO!

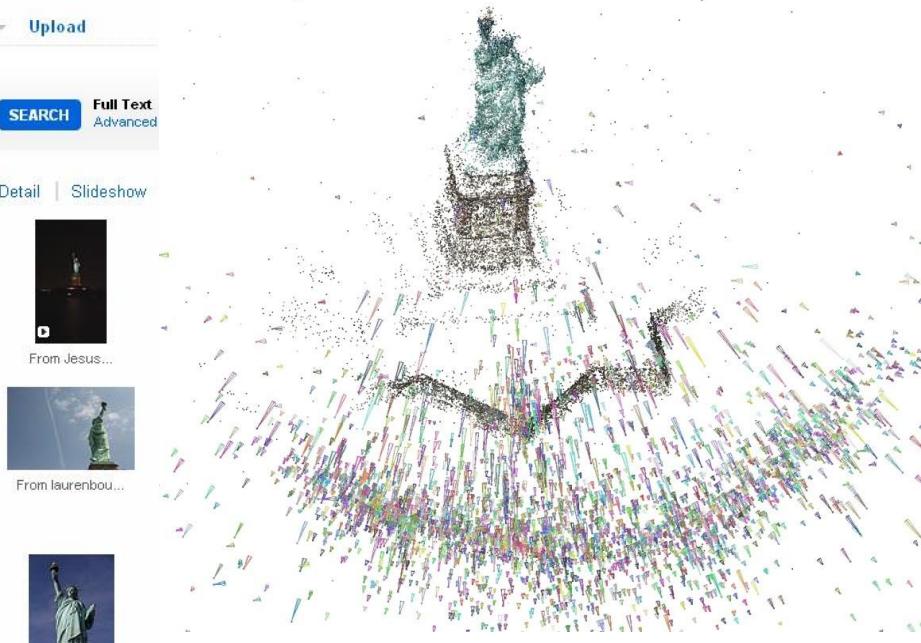
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Sort: Relevant | Recent | Interesting View: Small | Medium | Detail | Slideshow

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From Julio... From StephiGra... From alabs From BigMs.Take From laurenbou...
From dmp0309 From laverrue From Mojumbo22...



Challenges

- appearance variation

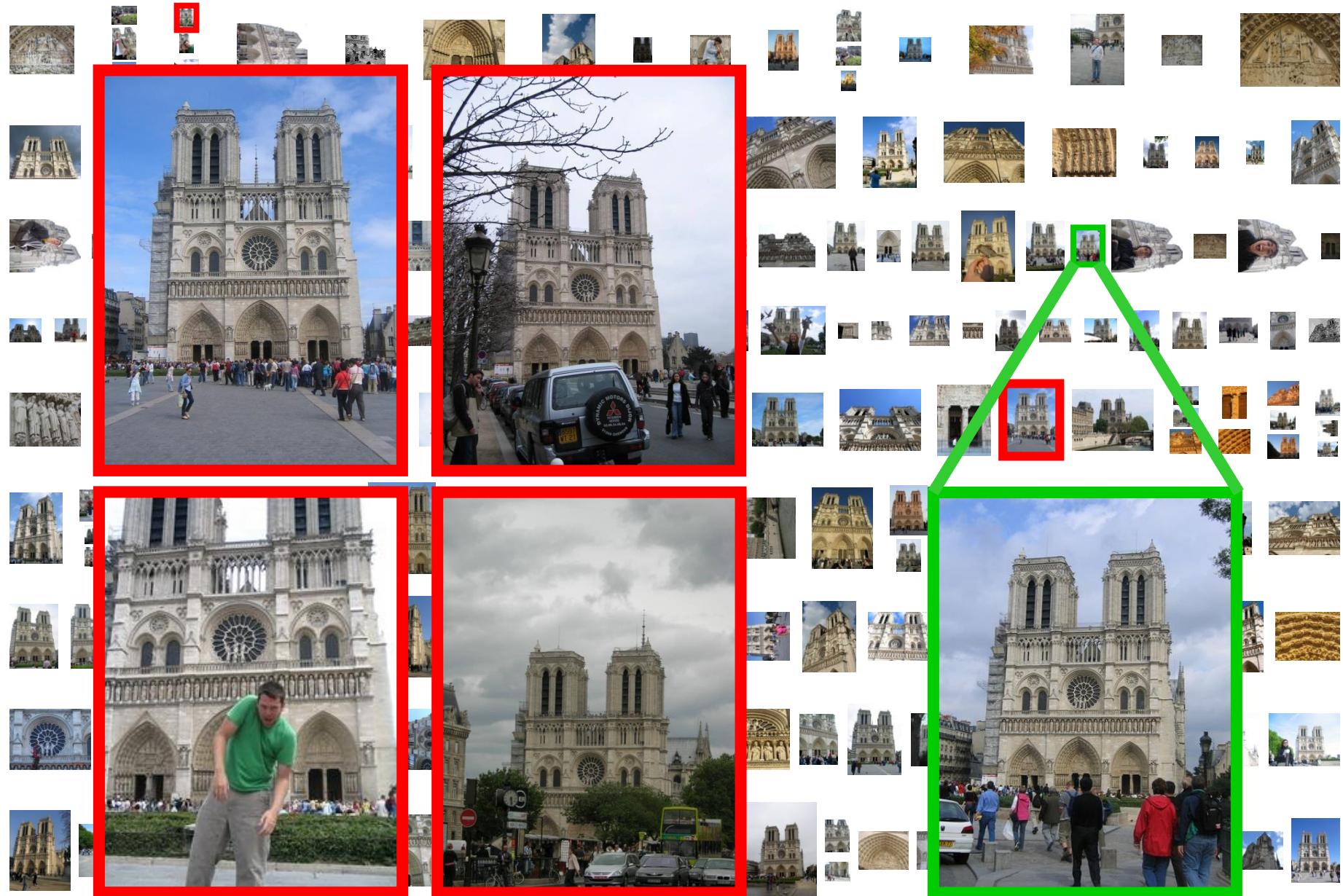


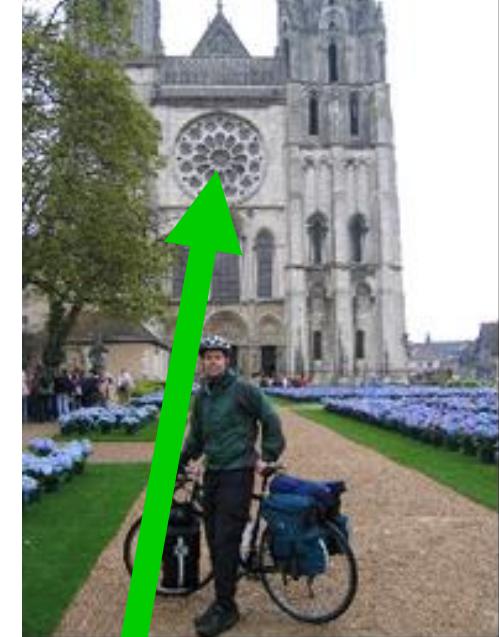
- resolution



- massive collections

82,754 results for photos matching **notre** and **dame** and **paris**.



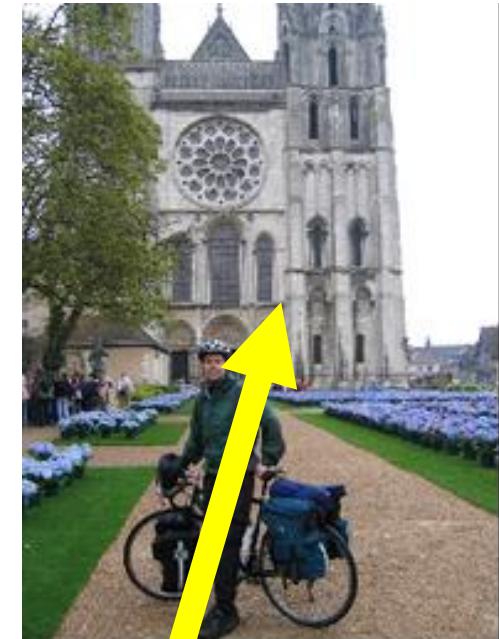
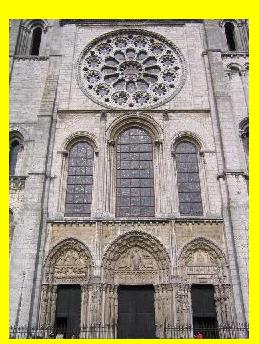


4 best neighboring views



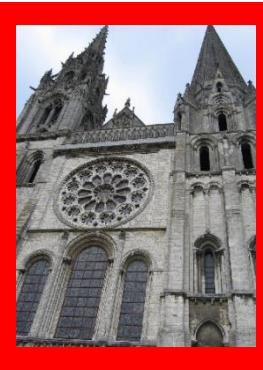
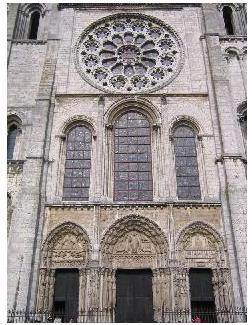
reference view

- Automatically select neighboring views for each point in the image
- Desiderata: good matches AND good baselines



reference view

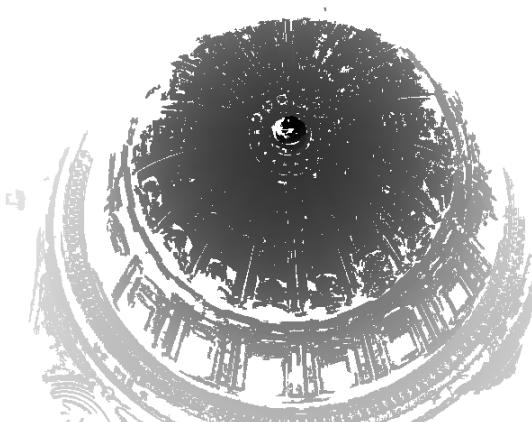
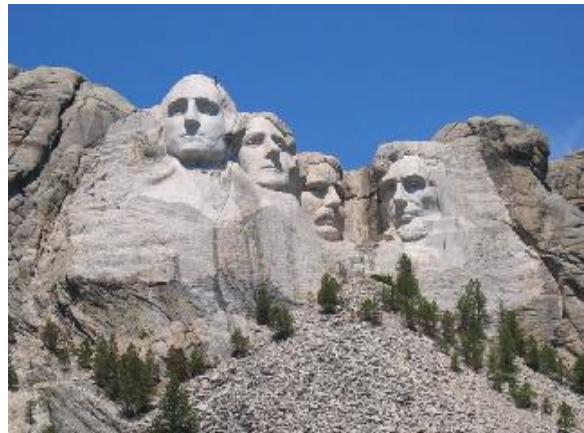
- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines



Local view selection

- Automatically select neighboring views for each **point** in the image
- Desiderata: good matches AND good baselines

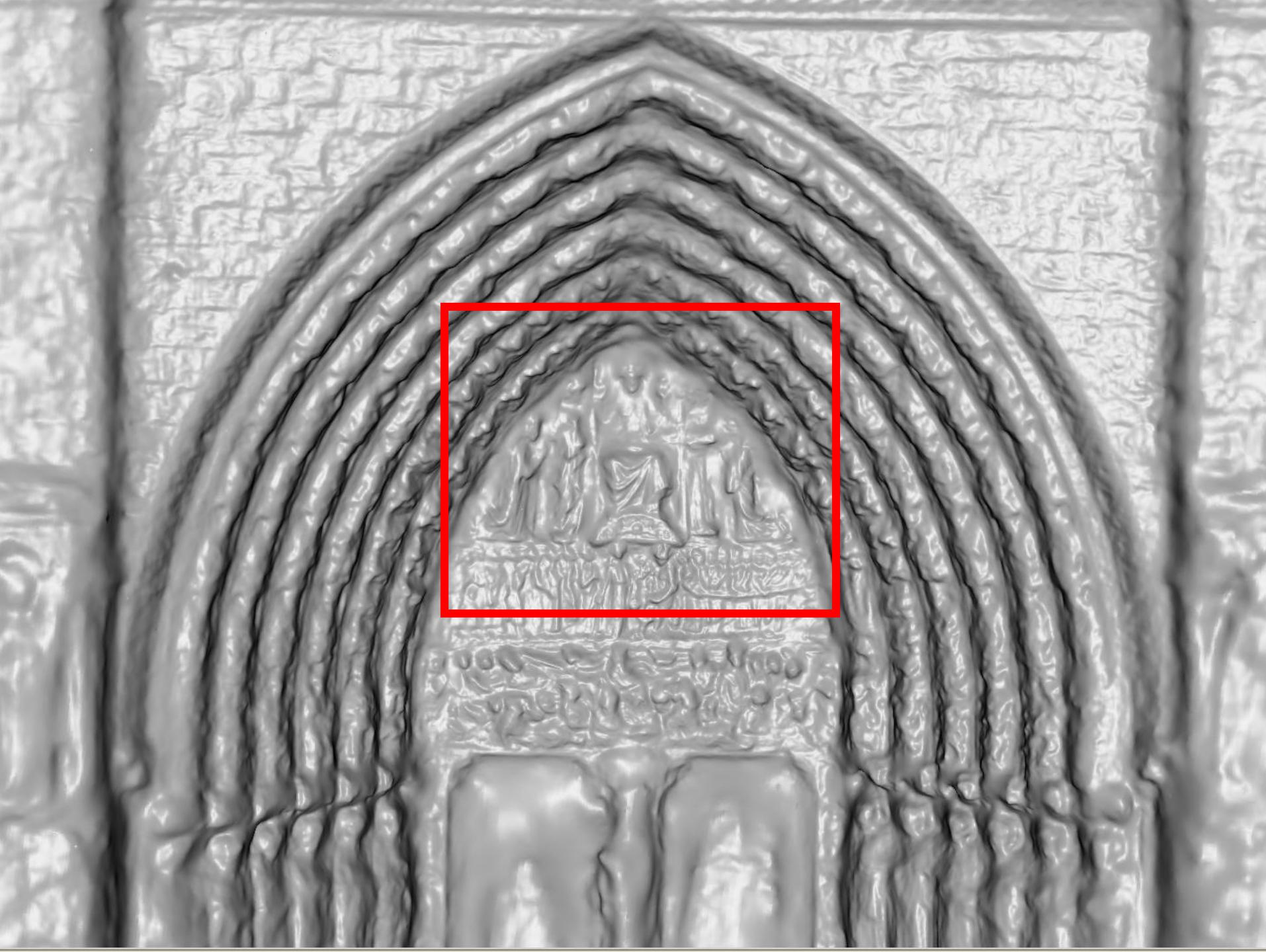
Results

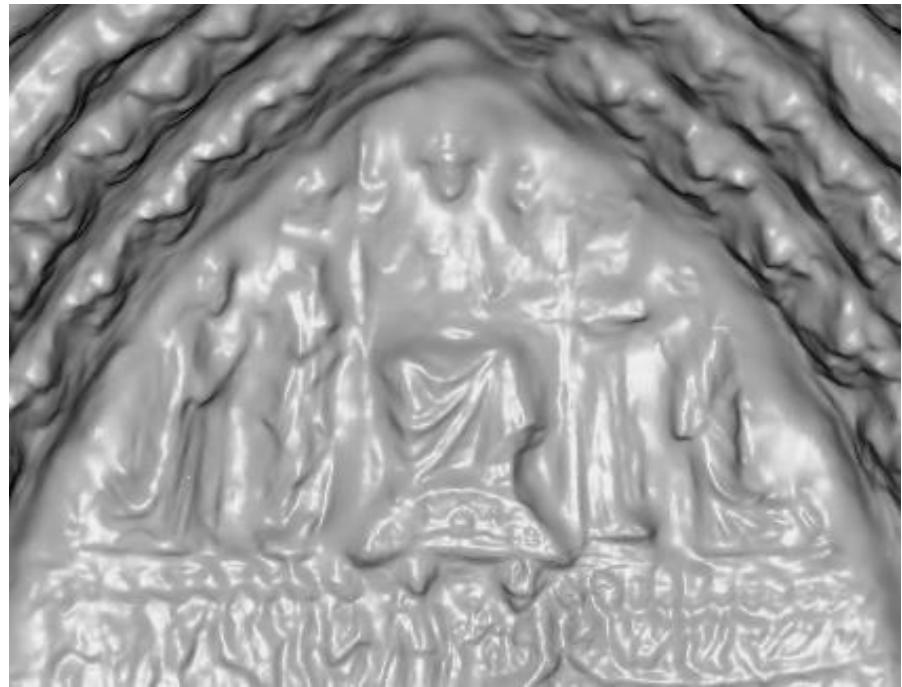
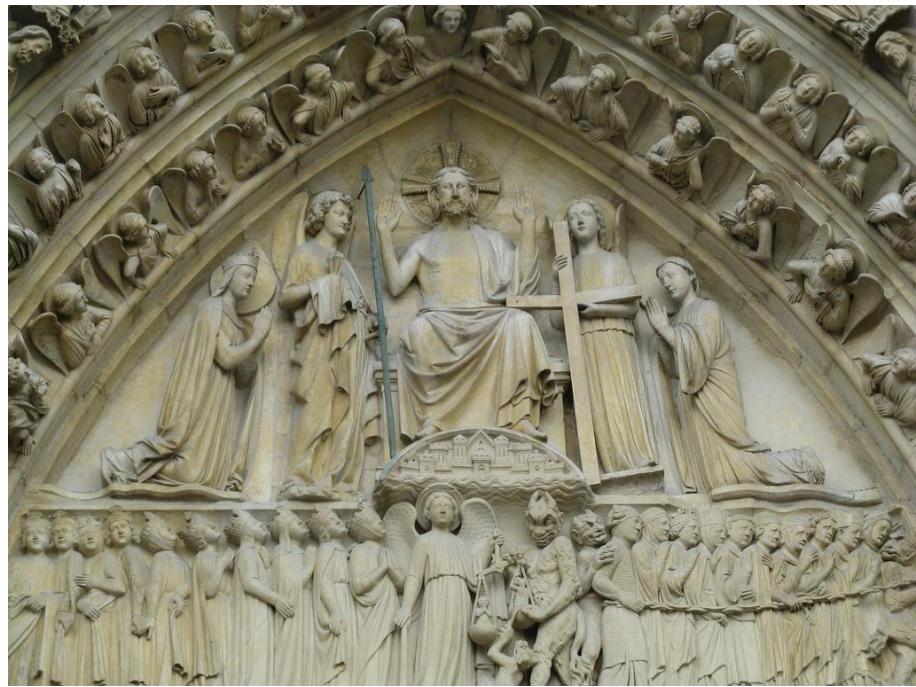


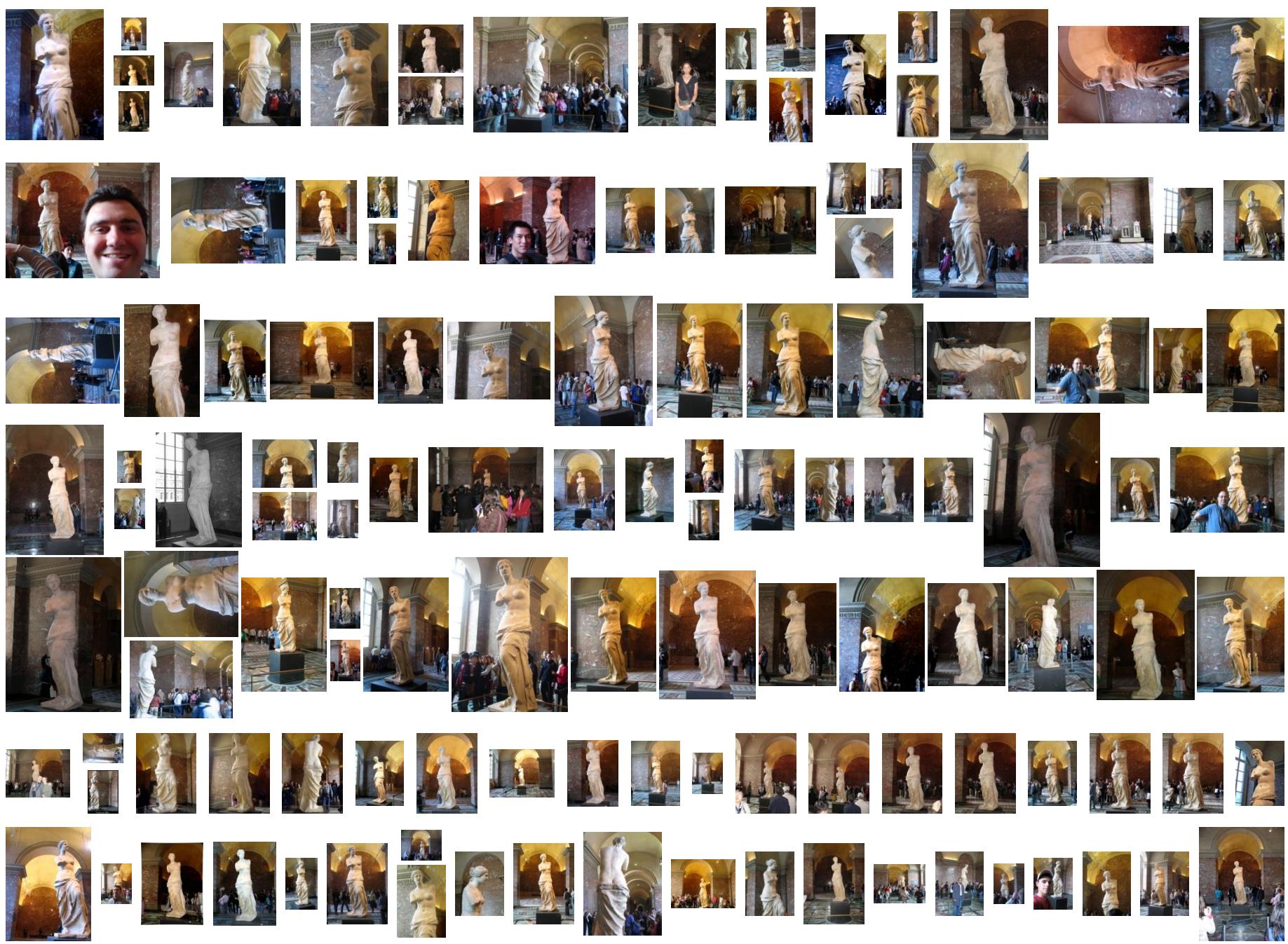
Notre Dame de Paris

653 images
313 photographers



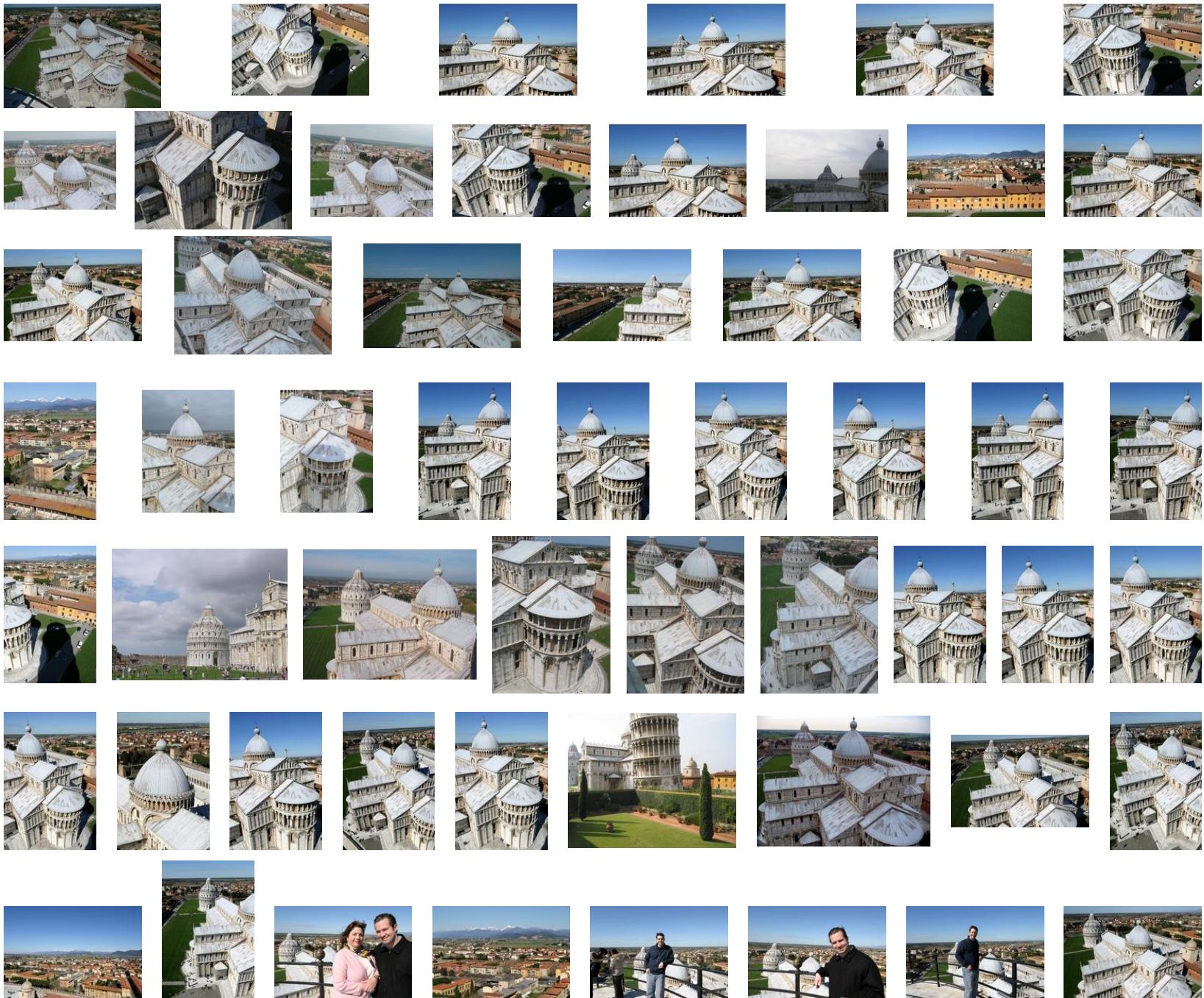


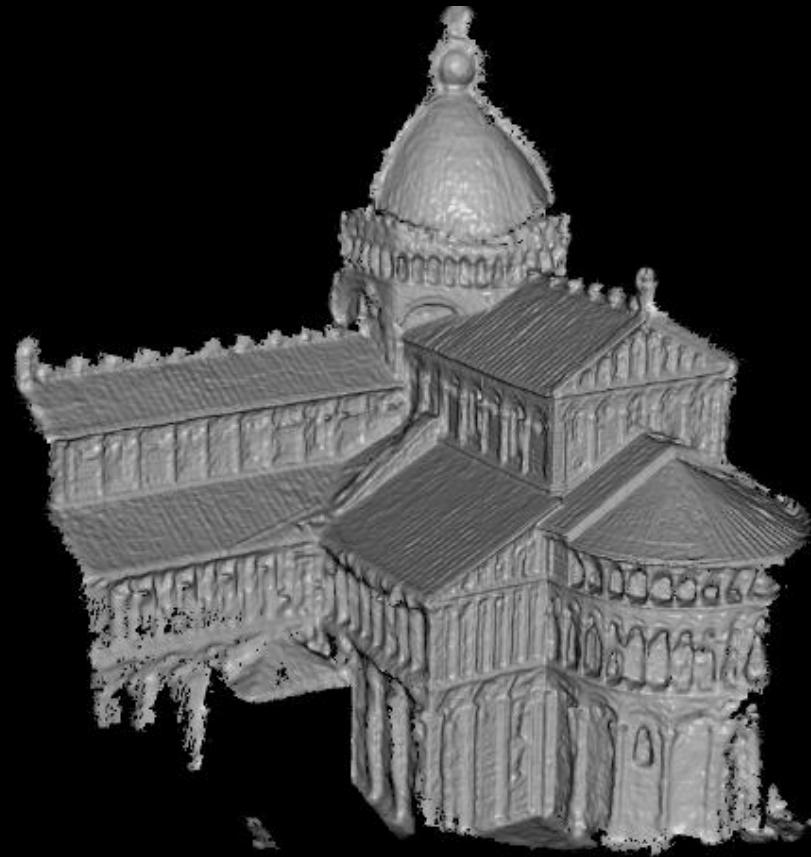




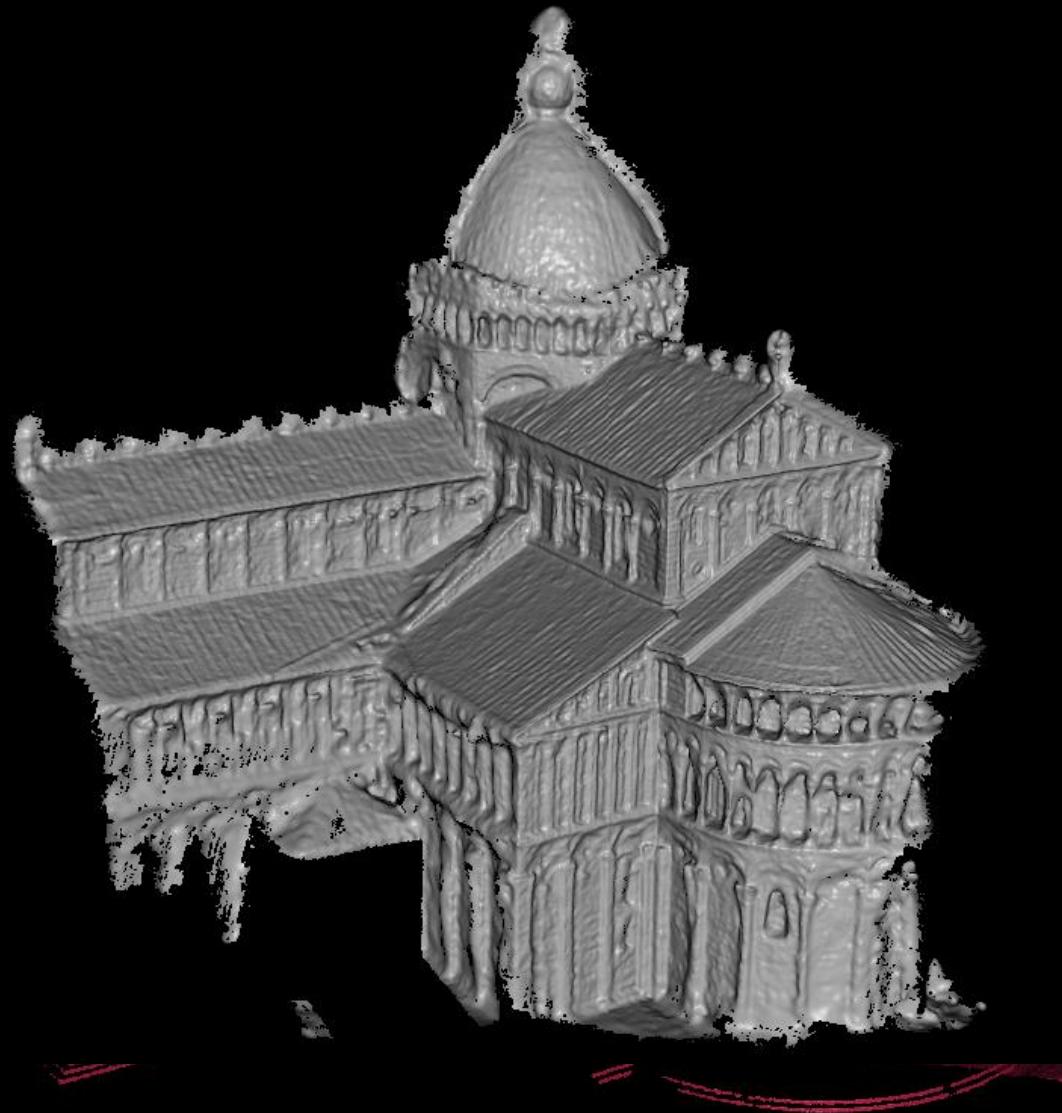


merged model of Venus de Milo





merged model of Pisa Cathedral



Accuracy compared to laser scanned model:
90% of points within 0.25% of ground truth