

# CS252 – Final Exam Study Guide

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## Lecture #01 – General Introduction

Reasons for Different Programming Languages	Programming Language Design Choices	Features of Good Programming Languages	
<ol style="list-style-type: none"> <li>1. <b>Different domains</b> (e.g. web, security, bioinformatics)</li> <li>2. <b>Legacy code and libraries</b></li> <li>3. <b>Personal preference</b></li> </ol>	<ol style="list-style-type: none"> <li>1. <b>Flexibility</b></li> <li>2. <b>Type safety</b></li> <li>3. <b>Performance</b></li> <li>4. <b>Build Time</b></li> <li>5. <b>Concurrency</b></li> </ol>	<ol style="list-style-type: none"> <li>1. <b>Simplicity</b></li> <li>2. <b>Readability</b></li> <li>3. <b>Learnability</b></li> </ol>	<ol style="list-style-type: none"> <li>4. <b>Safety</b> (e.g. security and can errors be caught at compile time)</li> <li>5. <b>Machine independence</b></li> <li>6. <b>Efficiency</b></li> </ol>
<b>Goals almost always conflict</b>			

<b>Conflict: Type Systems</b> <ul style="list-style-type: none"> <li>• <b>Advantage:</b> Prevents bad programs.</li> <li>• <b>Disadvantage:</b> Reduces programmer flexibility.</li> </ul>	<b>Blub Paradox:</b> Why do I need advanced programming language techniques (e.g. monads, closures, type inference, etc.)? My language does not have it, and it works just fine.	<b>Current Programming Language Issues</b> <ul style="list-style-type: none"> <li>• <b>Multi-core “explosion”</b></li> <li>• <b>Big Data</b></li> <li>• <b>Mobile Devices</b></li> </ul>	<b>Advantages of Web and Scripting Languages</b> <ul style="list-style-type: none"> <li>• <b>Examples:</b> Perl, Python, Ruby, PHP, JavaScript</li> <li>• <b>Highly flexible</b></li> <li>• <b>Dynamic typing</b></li> <li>• <b>Easy to get started</b></li> <li>• <b>Minimal typing</b> (i.e. type systems)</li> </ul>
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<b>Major Programming Language Research Contributions</b> <ul style="list-style-type: none"> <li>• <b>Garbage collection</b></li> <li>• <b>Sound type systems</b></li> <li>• <b>Concurrency tools</b></li> <li>• <b>Closures</b></li> </ul>	<b>Programs that Manipulate Other Programs</b> <ul style="list-style-type: none"> <li>• <b>Compilers &amp; interpreters</b></li> <li>• <b>JavaScript rewriting</b></li> <li>• <b>Instrumentation</b></li> <li>• <b>Program Analyzers</b></li> <li>• <b>IDEs</b></li> </ul>	<b>Formal Semantics</b> <ul style="list-style-type: none"> <li>• Used to <b>share information unambiguously</b></li> <li>• <b>Can formally prove a language supports a given property</b></li> <li>• <b>Crisply define how a language works</b></li> </ul>	<b>Types of Formal Semantics</b> <ul style="list-style-type: none"> <li>• <b>Operational</b> <ul style="list-style-type: none"> <li>◦ Big Step “<b>natural</b>”</li> <li>◦ Small Step “<b>structural</b>”</li> </ul> </li> <li>• <b>Axiomatic</b></li> <li>• <b>Denotational</b></li> </ul>
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### Haskell

<ul style="list-style-type: none"> <li>• <b>Purely functional</b> – Define “<i>what stuff is</i>”</li> <li>• <b>No side effects</b></li> <li>• <b>Referential transparency</b> – A function with the same input parameters will always have the same result.               <ul style="list-style-type: none"> <li>◦ A function call can be replaced with its value and nothing will change.</li> </ul> </li> <li>• <b>Supports type inference.</b></li> </ul>	<b>Duck Typing</b> – Suitability of an object for some function is determined not by its type but by presence of certain methods and properties. <ul style="list-style-type: none"> <li>◦ <b>More flexible</b> but <b>less safe</b>.</li> <li>◦ <b>Supported by Haskell</b></li> <li>◦ <b>Common in scripting languages</b> (e.g. Python, Ruby)</li> </ul>	<b>Side Effects in Haskell</b> <ul style="list-style-type: none"> <li>• Generally not supported.</li> <li>• <b>Example of Support Side Effects:</b> File IO</li> <li>• Functions that do have side effects must be separated from other functions.</li> </ul>
		<b>Lazy Evaluation</b> <ul style="list-style-type: none"> <li>• <b>Results are not calculated until they are needed</b></li> <li>• <b>Allows for the representation of infinite data structures</b></li> </ul>

## Lecture #02 – Introduction to Haskell

<b>Key Traits of Haskell</b> <ol style="list-style-type: none"> <li>1. <b>Purely functional</b></li> <li>2. <b>Lazy evaluation</b></li> <li>3. <b>Statically typed</b></li> <li>4. <b>Type Inference</b></li> <li>5. <b>Fully curried functions</b></li> </ol>	<b>ghci</b> – Interactive Haskell.  <b>let</b> – Keyword required in ghci to set a variable value. <b>Example:</b> <code>&gt; let f x = x + 1</code> <code>&gt; f 3</code> <code>4</code>	<b>Run Haskell from Command Line</b> Use <b>runhaskell</b> keyword.  <b>Example:</b> <code>&gt; runhaskell &lt;FileName&gt;.hs</code>	<b>Hello World in Haskell</b>  <pre>main :: IO () main = do     putStrLn "Hello World"</pre>
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<b>Primitive Classes in Haskell</b> <ol style="list-style-type: none"> <li>1. <b>Int</b> – <b>Bounded</b> Integers</li> <li>2. <b>Integer</b> – <b>Unbounded</b></li> <li>3. <b>Float</b></li> <li>4. <b>Double</b></li> <li>5. <b>Bool</b></li> <li>6. <b>Char</b></li> </ol>	<b>Lists</b> <ul style="list-style-type: none"> <li>• <b>Base 0</b></li> <li>• Comma separated in square brackets</li> <li>• <b>Operators</b> <ul style="list-style-type: none"> <li>◦ <b>:</b> Prepend</li> <li>◦ <b>++</b> Concatenate</li> <li>◦ <b>!!</b> Get element a specific index</li> <li>◦ <b>head</b> First element in list</li> <li>◦ <b>tail</b> All elements after head</li> </ul> </li> </ul>	<b>Ranges</b> <ul style="list-style-type: none"> <li>• Can be infinite or bounded</li> <li>• Use the “<b>..</b>” notation. <b>Examples:</b>  <code>&gt; [1..4]</code>  <code>[1, 2, 3, 4]</code>   <code>&gt; [1,2..6]</code>  <code>[1, 2, 3, 4, 5, 6]</code>   <code>&gt; [1,3..10]</code>  <code>[1, 3, 5, 7, 9]</code>   <code>&gt; [5, 4..1]</code>  <code>[5, 4, 3, 2, 1]</code> </li> </ul>
	<b>List Examples</b>  <code>&gt; putStrLn \$ "Hello " ++ "World"</code> <code>"Hello World"</code>  <code>&gt; let s = bra in s !! 2 : s ++ 'c' : last s : 'd' : s</code> <code>"abracadabra"</code>	<b>Infinite List Example</b> <code>&gt; let even = [2,4..]</code> <code>&gt; take 5 even</code> <code>[2, 4, 6, 8, 10]</code>

<b>List Comprehension</b> <ul style="list-style-type: none"> <li>Based off set notation.</li> <li>Supports filtering as shown in second example</li> <li>If multiple variables (e.g. a, b, c) are specified, iterates through them like nested for loops.</li> <li>Uses the pipe ( ) operator. Examples:</li> </ul> <pre>&gt; [ 2*x   x &lt;- [1..5]] [2, 4, 6, 8, 10]</pre>	<b>A Simple Function</b> <pre>&gt; let inc x = x + 1 &gt; inc 3 4  &gt; inc 4.5 5.5  &gt; inc (-5) -- Negative -4</pre>	<b>Pattern Matching</b> <ul style="list-style-type: none"> <li>Used to handle different input data</li> <li>Guard uses the pipe ( ) operator</li> <li>Example:</li> </ul> <pre>inc :: Int -&gt; Int inc x     x &lt; 0 = error "invalid x" inc x = x + 1</pre>
<pre>&gt; [(a, b, c)   a &lt;- [1..10], b &lt;- [1..10],                c &lt;- [1..10], a^2 + b^2 == c^2]  [(3, 4, 5), (4, 3, 5), (6, 8, 10), (8, 6, 10)]</pre>	<b>Type Signature</b> <ul style="list-style-type: none"> <li>Uses symbols ":" and "&gt;"</li> <li>Example:</li> </ul> <pre>inc :: Int -&gt; Int inc x = x + 1</pre>	

<b>Recursion</b> <ul style="list-style-type: none"> <li>Base Case – Says when recursion should stop.</li> <li>Recursive Step – Calls the function with a smaller version of the problem</li> </ul> <p>Example:</p> <pre>addNum :: [Int] -&gt; Int addNum [] = 0 addNum (x:xs) = x + addNum xs</pre>	<b>Lab #01 – Max Number</b> <pre>&gt; maxNum :: [Int] -&gt; Int &gt; maxNum [] = error "Invalid Input" &gt; maxNum [x] = x &gt; maxNum (x:xs) = if x &gt; max xs then x else max xs &gt; where max xs = maxNum xs</pre>	<b>Reasons for a Large Number of Programming Languages</b> <ul style="list-style-type: none"> <li>Different domains</li> <li>Different design choices</li> </ul>
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<b>Recursion</b> <ul style="list-style-type: none"> <li>:t or :type – Gets the type of a variable or function.</li> </ul> <p>Example:</p> <pre>&gt; :type 'A' 'A' :: Char &gt; :t "Hello" "Hello" :: [Char]</pre>	<b>Haskell's Base Typeclasses</b> <ul style="list-style-type: none"> <li>Ord – Can be ordered</li> <li>Eq – Can perform equality check</li> <li>Show – Can convert to String</li> <li>Read – Can convert from String</li> <li>Enum – Sequentially Ordered</li> <li>Bounded – Has upper and lower bound.</li> </ul>	
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## Lecture #03 – Operational Semantics

<b>Formal Semantics</b> <i>Crisply define how the language features work.</i>	<b>Formal Semantic Styles</b> <ul style="list-style-type: none"> <li>Operational – Specify how expressions should be evaluated.             <ul style="list-style-type: none"> <li>Big-Step ("Natural")</li> <li>Small-Step ("structural")</li> </ul> </li> <li>Axiomatic</li> <li>Denotational</li> </ul>	<b>A Review of Compilers</b>
<b>Abstract Syntax Tree</b> Tree representation of the abstract syntactic structure of a program's source code. Example is Bool* language below.	<b>Big Step Operational Semantics</b> <ul style="list-style-type: none"> <li>Evaluates every expression to a value</li> <li>↓ : "Evaluates to" symbol in Big-Step operational semantics.</li> <li>Example Formatting:</li> </ul> $e \Downarrow v$ <ul style="list-style-type: none"> <li>Read as: "Expression e evaluates to the value v"</li> </ul>	

<b>Small-Step Operational Semantics</b> <ul style="list-style-type: none"> <li>Evaluate an expression until it is in normal form</li> <li>Normal Form – Any form that cannot be evaluated further.</li> <li>→ : "Evaluates to" symbol in small step operational semantics. Example:</li> </ul> $e \rightarrow e' \rightarrow e'' \rightarrow v$ <ul style="list-style-type: none"> <li>→* : Many evaluation steps required. Example:</li> </ul> $e \rightarrow^* v$	<b>Bool* Small-Step Operational Semantics Rules</b> <p><b>E-IfTrue:</b></p> $\frac{}{\text{if true then } e_2 \text{ else } e_3 \rightarrow e_2}$ <p><b>E-IfFalse:</b></p> $\frac{}{\text{if false then } e_2 \text{ else } e_3 \rightarrow e_3}$ <p><b>E-If:</b></p> $\frac{e_1 \rightarrow e'_1}{\text{if } e_1 \text{ then } e_2 \text{ else } e_3 \rightarrow \text{if } e'_1 \text{ then } e_2 \text{ else } e_3}$	<p>Example: Reduce the expression</p> <pre>if (if true then false else true) then true else false</pre> <p>Step #1: Use rule "E-IfTrue" with "E-If"</p> <pre>if false then true else false</pre> <p>Step #2: Use rule "E-IfFalse" (Now in normal form)</p> <pre>false</pre>
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<p><b>Bool* Extension: Numbers</b></p> <ul style="list-style-type: none"> <li>• <b>0</b> : The Number "0"</li> <li>• <b>succ 0</b> : Represents "1"</li> <li>• <b>succ succ 0</b> : Represents "2"</li> <li>• <b>pred n</b> : Gets the predecessor of "n"</li> </ul>	<p><b>Extended Bool * Language</b></p> <pre> e ::=   true   false   if e then e else e   0   succ e   pred e  v ::= true   false       IntV  IntV ::= 0   succ IntV         </pre>	<p><b>Literate Haskell</b></p> <ul style="list-style-type: none"> <li>• File Extension: ".lhs"</li> <li>• <b>Code lines begin with "&gt;"</b></li> <li>• <b>All other lines are comments.</b></li> <li>• "Essentially swaps code with comments."</li> </ul>	<p><b>Case Statement in Haskell</b></p> <ul style="list-style-type: none"> <li>• <b>Keywords: case, of, otherwise</b></li> <li>• <b>Operator: -&gt;</b></li> </ul> <p><b>Example:</b></p> <pre> case x of   val1 -&gt; "Value 1"   val2 -&gt; "Value 2"   otherwise -&gt; "Everything else."         </pre>
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## Lab #02 Review

<p><b>Bool Expression Type</b></p> <pre> &gt; data BoolExp = BTrue     BFalse     Bif BoolExp BoolExp BoolExp     B0     Bsucc BoolExp     Bpred BoolExp   deriving Show         </pre>	<p><b>BoolVal Type</b></p> <pre> &gt; data BoolVal = BVTrue     BVFalse     BVNum BVInt   deriving Show  &gt; data BVInt = BV0     BVSucc BVInt   deriving Show         </pre>	<p><b>Type Constructors:</b> BoolExp, BoolVal, BVInt</p> <p><b>Non-nullary Value Constructors:</b> Blf, Bsucc, Bpred, BVSucc, BVNum</p> <p><b>Note:</b> Even constants like B0, BTrue, BFalse, BVTrue, and BVFalse are nullary value constructors (since they take no arguments)</p>
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## Lecture #04 – Higher Order Functions

<p><b>Lambda</b></p> <ul style="list-style-type: none"> <li>• Analogous to anonymous classes in Java.</li> <li>• <b>Based off Lambda calculus</b></li> <li>• <b>Example:</b></li> </ul> <pre> &gt; (\x -&gt; x + 1) 1 2 &gt; (\x y -&gt; x + y) 2 3 5         </pre>	<p><b>Function Composition</b></p> <ul style="list-style-type: none"> <li>• Uses the <b>period (.)</b></li> <li>• <b>f(g(x))</b> can be rewritten <b>(f . g) x</b></li> </ul>	<p><b>Point-Free Style</b></p> <ul style="list-style-type: none"> <li>• Pass no arguments to a function</li> <li>• <b>Example:</b></li> </ul> <pre> &gt; let inc = (+1) -- No args &gt; inc 3 4         </pre>	<p><b>Example: Lambda with Function Composition</b></p> <pre> &gt; let f = (\x -&gt; x - 5)   . (\y -&gt; y * 2)  &gt; f 7 9  &gt; let f = (\x y -&gt; x - y)   . (\z -&gt; z * (-1))  &gt; f 3 4 -7         </pre>
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<p><b>Iterative vs. Recursive</b></p> <ul style="list-style-type: none"> <li>• <b>Iterative tends to be more efficient than recursive.</b></li> <li>• <b>Compiler can optimize tail recursive function.</b></li> </ul> <p><b>Tail Recursive Function</b> – The recursive call is the last step performed before returning a value.</p>	<p><b>Not Tail Recursive</b></p> <pre> public int factorial(int n) {   if (n==1) return 1;   else {     return n * factorial(n-1);   } }         </pre> <p>Last step is the multiplication so not tail recursive.</p>	<p><b>Tail Recursive Factorial</b></p> <pre> public int factorialAcc(int n, int acc) {   if (n==1) return acc;   else {     return factorialAcc(n-1, n*acc);   } }         </pre> <p><b>Tail recursive code often uses the accumulator pattern like above.</b></p>
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<p><b>Tail Recursion in Haskell</b></p> <pre> fact' :: Int -&gt; Int -&gt; Int fact' 0 acc = acc fact' n acc = fact' (n - 1) (n * acc)         </pre>		
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## Higher Order Functions

<p><b>Functions in Functional Programming</b></p> <ul style="list-style-type: none"> <li>• <b>Functional languages treat programs as mathematical functions.</b></li> <li>• <b>Mathematical Definition of a Function:</b> A function <math>f</math> is a rule that associates to each <math>x</math> from some set <math>X</math> of values a unique <math>y</math> from a set of <math>Y</math> values.</li> </ul> $(x \in X \wedge y \in Y) \rightarrow y = f(x)$ <ul style="list-style-type: none"> <li>• <math>f</math> – Name of the function</li> <li>• <math>x</math> – Independent variable</li> <li>• <math>y</math> – Dependent variable</li> <li>• <math>X</math> – Domain</li> <li>• <math>Y</math> – Range</li> </ul>	<p><b>Qualities of Functional Programming</b></p> <ul style="list-style-type: none"> <li>• <b>Functions clearly distinguish:</b> <ul style="list-style-type: none"> <li>◦ Incoming values (<b>parameters</b>)</li> <li>◦ Outgoing Values (<b>results</b>)</li> </ul> </li> <li>• <b>No (re)assignment</b></li> <li>• <b>No loops</b></li> <li>• <b>Return values depend only on input parameters</b></li> <li>• <b>Functions are first class values;</b> this means they can:           <ul style="list-style-type: none"> <li>◦ <b>Passed as arguments to a function</b></li> <li>◦ <b>Be returned from a function</b></li> <li>◦ <b>Construct new functions dynamically</b></li> </ul> </li> </ul>	<p><b>Higher Order Function</b></p> <p>Any function that <b>takes a function as a parameter or returns a function as a result.</b></p> <p><b>Function Currying</b></p> <p><b>Transform a function with multiple arguments into multiple functions that each take exactly one argument.</b></p> <p>Named after Haskell Brooks Curry.</p> <p><b>Currying Example</b></p> <pre> addNums :: Num a =&gt; a -&gt; a -&gt; a         </pre> <p><b>addNums</b> is a function that takes in a number and returns a function that takes in another number.</p>	
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<p><b>map</b></p> <ul style="list-style-type: none"> <li>Built in Haskell higher order function</li> <li><b>Applies a function to all elements of a list.</b></li> </ul> <pre>map :: (a -&gt; b) -&gt; [a] -&gt; [b]</pre> <pre>&gt; map (+1) [1, 2, 3] [2, 3, 4]</pre>	<p><b>foldl</b></p> <ul style="list-style-type: none"> <li>Built in higher order function</li> <li><b>Does not support infinite lists.</b></li> <li><b>Should only be used for special cases.</b></li> </ul> <pre>foldl :: (b -&gt; a -&gt; b) -&gt; b -&gt; a -&gt; b</pre> <p>Example:</p> <pre>&gt; foldl (\x y -&gt; x - y) 0 [1, 2, 3, 4] -10 -- ((0-1) - 2) - 3) - 4</pre>	
<p><b>filter</b></p> <ul style="list-style-type: none"> <li>Built in Haskell higher order function</li> <li><b>Removes all elements from a list that do not satisfy (i.e. make true) some predicate.</b></li> </ul> <pre>filter :: (a -&gt; Bool) -&gt; [a] -&gt; [a]</pre> <pre>&gt; filter (&gt;2) [1, 2, 3, 4] [3, 4]</pre>	<p><b>foldr</b></p> <ul style="list-style-type: none"> <li>Built in higher order function</li> <li><b>Supports infinite lists.</b></li> <li><b>"Usually the right fold to use"</b></li> </ul> <pre>foldr :: (b -&gt; a -&gt; a) -&gt; a -&gt; b -&gt; a</pre> <p>Example:</p> <pre>&gt; foldr (\x y -&gt; x + y) 0 [1, 2, 3, 4] -2 -- 1 - (2 - (3 - (4 - 0)))</pre>	
<p><b>Thunk</b> – A delayed computation</p> <p>Due to lazy evaluation, <b>foldl</b> and <b>foldr</b> build <b>thunks</b> rather than calculate the results as they go.</p>	<p><b>foldl'</b></p> <ul style="list-style-type: none"> <li><b>Data.List.foldl'</b> evaluates its results eagerly (i.e. does not use <b>thunks</b>)</li> <li><b>Good for large, but finite lists.</b></li> </ul>	<p><b>foldl in terms of foldr</b></p> <pre>myFoldl' f acc x = foldr (flip f) acc (reverse x)</pre>

## Lecture #05 – Small-Step Operational Semantics

<p><b>WHILE Language</b></p> <ul style="list-style-type: none"> <li>Unlike the Bool* language, <b>WHILE supports mutable references.</b></li> </ul>	<p><b>Small Step Semantics with State</b></p> <ul style="list-style-type: none"> <li>Since the WHILE language supports mutable references, the grammar must be updated to support it.</li> </ul> <p><b>While Relation:</b></p> $e, \sigma \rightarrow e', \sigma'$ <ul style="list-style-type: none"> <li><math>\sigma</math> – Store. <b>Maps references to values.</b></li> </ul> <p><b>Example Operations:</b></p> <ul style="list-style-type: none"> <li><math>\sigma(a)</math> – Retrieves the value at address "a"</li> <li><math>\sigma[a := v]</math> – Identical to the original store with the exception that it now stores the value <b>v</b> at address "a"</li> </ul>	<p><b>Evaluation Order Rules</b></p> <ul style="list-style-type: none"> <li><b>Tend to be repetitive and clutter the semantics.</b></li> <li><b>Context based rules tend to represent the same information as evaluation order rules but more concisely.</b></li> </ul> <p><b>Reduction Rule</b></p> <p>Rewrites the expression. Example:</p> <p><b>E-IfFalse:</b></p> <pre>if false then e2 else e3 → e3</pre> <p><b>Context Rule</b></p> <p><b>Specify the order for evaluating expressions.</b> Example:</p> <p><b>E-If:</b></p> $\frac{e_1 \rightarrow e'_1}{\text{if } e_1 \text{ then } e_2 \text{ else } e_3 \rightarrow \text{if } e'_1 \text{ then } e_2 \text{ else } e_3}$
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<p><b>Reducible Expression (Redex)</b> – Any expression that can be transformed (reduced) in one step.</p>	<p><b>Example: Redex</b></p> <pre>if true then (if true then false else false) else true</pre> <p>This reduces to "if true then false else false"</p>	<p><b>Example: Not a Redex</b></p> <pre>if (if true then false else false) then true else true</pre> <p>Not a redex as expression "if true then false else false" must be evaluated first.</p>
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<p><b>Evaluation Contexts</b></p> <ul style="list-style-type: none"> <li><b>Alternative to evaluation order rules.</b></li> <li><b>Marker (•) / hole</b> indicate the <b>next place for evaluation</b> (i.e. where we will do the work).</li> </ul> <p>Example:</p> <pre>C[r]</pre> <pre>= if (if true then false else false) then true else true</pre> <p><b>r</b> = if true then false else false</p> <p><b>C</b> = if • then true else true</p> <p><b>C[r]</b> is the original expression.</p>	<p><b>Rewriting Evaluation Order Rules</b></p> <p><b>Context based rules only apply to reducible expressions (redexs).</b> Example:</p> <p><b>EC-IfFalse:</b></p> <pre>C[if false then e2 else e3] → C[e3]</pre> <p><b>Context Syntax</b></p> <pre>C ::= •         if C then e else e         C op e         v op C         ...</pre>	<p><b>Data.Map</b></p> <ul style="list-style-type: none"> <li><b>Library:</b> import Data.Map as Map</li> <li><b>Immutable</b></li> <li><b>Example Methods:</b> <ul style="list-style-type: none"> <li><b>Map.empty</b> – Creates and returns an empty map</li> <li><b>Map.insert k v m</b> – Inserts a value "v" at key "k" into map "m". <b>Returns a new, updated map.</b></li> <li><b>Map.lookup k m</b> – Returns the value at key "k" in map "m". <b>Wrapped in a Maybe.</b></li> <li><b>Map.member k m</b> – Returns true if k is in map "m" and false otherwise.</li> </ul> </li> </ul>
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<p><b>Precondition</b> – Text above the line in a rule.</p>	<p><b>Context Rule for Binary Op:</b></p> $\frac{v_3 = v_1 \text{ op } v_2}{C[v_1 \text{ op } v_2] \rightarrow C[v_3]}$	<p><b>How to Read a Small Step Semantic Rule:</b> "Given &lt;Precondition&gt;, then &lt;LeftSideArrow&gt; evaluates to &lt;RightSideArrow&gt;."</p>
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## Lecture #06 – LaTeX

<b>TeX</b> <ul style="list-style-type: none"> <li>Created by Donald Knuth</li> <li><b>Domain specific language for typesetting documents.</b></li> <li>Precisely controls the interface of content.</li> <li>Type of <b>Literate Programming</b> – Logic is in natural language and code is interspersed. <i>"Mark code instead of marking comments."</i></li> </ul>	<b>LaTeX</b> <ul style="list-style-type: none"> <li>Developed by Leslie Lamport. Derives from TeX.</li> <li>Type of <b>Domain Specific Language (DSL)</b> – A <b>computer language that is specialized for a particular application domain.</b></li> <li>Enforces <b>separation of concerns</b> – Design principle for <b>separating a computer program into different sections, such that each section addresses a separate concern.</b> <ul style="list-style-type: none"> <li><b>Example:</b> LaTeX separates formatting from content.</li> </ul> </li> <li><b>Literate Programming</b></li> </ul>	<b>Specify Document Type</b> <code>\documentclass{article}</code> <b>Specify Title Block Content</b> <code>\title{Hello World!}</code> <b>Start Document</b> <code>\begin{document}</code> <b>Generate Title from Title Information</b> <code>\title{Hello World!}</code> <b>Close the Document</b> <code>\end{document}</code>	<b>Cross-Reference</b> <code>\ref{&lt;referenceName&gt;}</code> <b>Reference a Bibliography Citation</b> <code>\cite{&lt;citationName&gt;}</code> <b>Create a Reference</b> <code>\label{&lt;referenceName&gt;}</code> <b>Create a Bibliography</b> <code>\bibliography{&lt;bibFileName&gt;}</code> <b>Create a List</b> <code>\begin{itemize}</code> <code>\item Text for #1</code> <code>\item Text for #2</code> <code>\end{itemize}</code>
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<b>Create Section with Label</b> <code>\section{Section #1}</code> <code>\label{sec:one}</code> <b>Create Subsection with Label</b> <code>\subsection{&lt;SubsectionName&gt;}</code> <code>\label{sec:&lt;refName&gt;}</code> <b>Use of Tilde (~)</b> Creates an undividable space so the text "Section~\ref{sec:one}" will appear on one line	<b>BibTeX</b> <ul style="list-style-type: none"> <li>References are tedious to <b>reformat</b> and <b>renumber</b>.</li> <li>Reference details shorted in a <b>"*.bib"</b> file.</li> </ul> <b>Create a Bibliography</b> <code>\bibliography{biblio}</code> BibTeX filename for the example would be <b>"biblio.bib"</b> <b>Define Bibliography Style</b> <code>\bibliographystyle{plainurl}</code>	<b>BibTeX Article Reference Example</b> <pre>@article{citationName,   author = {Donald Knuth},   title = {Literate Programming},   journal = {},   year = {1984},   volume = {27},   number = {2},   pages = {97-111}, }</pre>
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## Lecture #07 – Types and Typeclasses

<b>Maybe Type</b> <ul style="list-style-type: none"> <li><b>Example of an algebraic data type</b></li> <li>Enables behavior similar to <b>null</b> in Java</li> <li>Can be used to provide context.</li> <li><b>Used when:</b> <ul style="list-style-type: none"> <li><b>A function may not return a value</b></li> <li><b>A caller may not pass an argument</b></li> </ul> </li> <li><b>Definition:</b> <pre>data Maybe a = Nothing                 Just a</pre> </li> </ul>	<b>Maybe "Divide" Example</b> <pre>divide :: Int -&gt; Int -&gt; Maybe Int divide _ 0 = Nothing divide x y = Just \$ x `div` y  &gt; divide 5 2 2 &gt; divide 4 0 Nothing</pre> <p><b>DO NOT FORGET THE Just IN CORRECT SOLUTION</b></p>	<b>Maybe Map Example</b> <pre>import Data.Map  m = Map.empty m' = Map.insert "a" 42 m case (Map.lookup "a") of   Nothing -&gt; error "Element not in map"   Just x -&gt; putStrLn \$ show x</pre> <p>Since element may not be in the map, you need to use a maybe</p>
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<b>Algebraic Data Type</b> <ul style="list-style-type: none"> <li>A <b>composite data type</b> (i.e. a type made from other types).</li> <li>Created via the <b>Keyword: data</b></li> <li><b>Examples:</b> <ul style="list-style-type: none"> <li><b>Either</b></li> <li><b>Maybe</b></li> <li><b>Tree</b></li> </ul> </li> </ul>	<b>Example Algebraic Data Type</b> <pre>data Tree k = EmptyTree               Node (Tree k) (Tree k) val             deriving (Show)</pre> <p><b>k – Type parameter. Specifies a type not a value.</b></p> <p><b>Node: Value Constructor that creates values of type "Tree k"</b></p>	<ul style="list-style-type: none"> <li><b>Tree and Tree Int have no types since they themselves form a concrete type.</b></li> <li><b>Node</b> does have a type:           <pre>&gt; :t Node Node :: (Tree k) -&gt; (Tree k) -&gt; k -&gt; (Tree k)</pre> <p><b>Explanation:</b> To make a complete <b>Node</b> object, you pass it two objects of type <b>"Tree k"</b> and another object of type <b>"k"</b> and that returns a <b>"Tree k"</b> object.</p> </li> </ul>
	<b>Partially Applying a Value Constructor</b> <ul style="list-style-type: none"> <li>Value constructors can be partially applied similar to functions. <b>Example:</b> <pre>&gt; let leaf = Node EmptyTree EmptyTree</pre> <pre>&gt; Node (leaf 3) (leaf 7) 5</pre> <p>This creates a three node tree with value 5 at the root and values 3 and 7 at the leaves.</p> </li> </ul>	<b>Type of the "+" Operator</b> <pre>&gt; :t (+) (+) :: (Num a) =&gt; a -&gt; a -&gt; a</pre> <p><b>Explanation:</b> The plus sign takes two numbers of type <b>"a"</b> and returns an object of type <b>"a"</b>.</p>
		<b>Type of a Number</b> <pre>&gt; :t 3 3 :: (Num a) =&gt; a</pre> <p><b>Explanation:</b> Since <b>"3"</b> has no explicit type, it can for now be any type that satisfies the <b>"Num"</b> type class.</p>

Kinds		Typeclasses	
<ul style="list-style-type: none"> <li>• <b>"The type of types".</b></li> <li>• <b>Concrete types have a kind of "*"</b></li> <li>• <b>Keyword</b> :k, :kind</li> <li>• <b>Example:</b></li> </ul> <pre>&gt; :k Tree Tree :: * -&gt; *</pre> <p><b>Explanation:</b> A Tree requires one type parameter (e.g. Int) to be made a concrete type.</p>	<p><b>String Kind</b></p> <pre>&gt; :kind String String :: *</pre> <p><b>Map Kind</b></p> <pre>&gt; :k Map Map :: * -&gt; * -&gt; *</pre> <p><b>Maybe Kind</b></p> <pre>&gt; :k Maybe Map :: * -&gt; *</pre> <p><b>Map String Kind</b></p> <pre>&gt; :kind (Map String) (Map String) :: * -&gt; *</pre> <p><b>Explanation:</b> Map String is has one of the two type parameters filled so it has one less asterisk.</p>	<ul style="list-style-type: none"> <li>• <b>Similar to interfaces in Java.</b> <ul style="list-style-type: none"> <li>○ Like a contract.</li> <li>○ <b>Implementation details can be included in typeclass definition.</b></li> </ul> </li> <li>• No relation to classes in object-oriented programming. <ul style="list-style-type: none"> <li>○ <b>Example:</b> Do not have any data associated with them.</li> </ul> </li> <li>• <b>Simplify polymorphism.</b></li> </ul> <p><b>Example:</b> Eq Typeclass</p> <pre>class Eq a where   (==) :: a -&gt; a -&gt; Bool   (/=) :: a -&gt; a -&gt; Bool   x == y = not (x /= y)   x /= y = not (x == y)</pre> <p>The last two lines in the type class definition allow the developer to program either (==) or (/=) but not necessarily both.</p>	<p><b>Example:</b> Make Maybe an Instance of Eq</p> <pre>instance (Eq a) =&gt; Eq (Maybe a) of   (==) Nothing Nothing = true   (==) (Just x) (Just y) = x == y   (==) _ _ = false</pre> <p>Need to ensure type "a" supports "Eq" so add that as a <b>class constraint</b>.</p> <p><b>Class Constraint</b></p> <ul style="list-style-type: none"> <li>• <b>Operator:</b> =&gt;</li> <li>• Ensures that a type parameter satisfies some typeclass requirement.</li> </ul> <p><b>Kind of Typeclasses</b></p> <pre>&gt; :k Eq Eq :: * -&gt; Constraint</pre> <pre>&gt; :k Num Num :: * -&gt; Constraint</pre> <p><b>Note:</b> Typeclasses are a class constraint (not a type) so their kind is different.</p>

## Lecture #08 – Functors

<p><b>Functor Type Class Definition</b></p> <pre>class Functor f where   fmap :: (a -&gt; b) -&gt; f a -&gt; f b</pre> <p>This is very similar to the definition of the higher order function "map"</p> <pre>map :: (a -&gt; b) -&gt; [a] -&gt; [b]</pre>	<p><b>Functor – Something that can be mapped over.</b></p> <ul style="list-style-type: none"> <li>• Handles things "inside a box"</li> </ul> <p><b>Example:</b> List ([]) as an instance of Functor</p> <pre>instance Functor [] where   fmap = map</pre> <p><b>Explanation:</b> map is a specialized version of fmap for lists.</p>	<p><b>Examples: map and fmap on Lists</b></p> <pre>&gt; map (+1) [1, 2, 3] [2, 3, 4]  &gt; fmap (+1) [1, 2, 3] [2, 3, 4]  &gt; fmap (+1) [] []</pre>	<p><b>Examples: fmap on Maybes</b></p> <pre>&gt; fmap (+1) (Just 3) Just 4  &gt; fmap (+1) Nothing Nothing</pre>
<p><b>Example:</b> Maybe as an Instance of Functor</p> <pre>instance Functor Maybe where   fmap _ Nothing = Nothing   fmap f (Just x) = Just (f x)</pre> <p><b>DO NOT FORGET THE Just IN VALID SOLUTION</b></p>	<p><b>Either Algebraic Data Type</b></p> <pre>data Either a b = Left a                   Right b   deriving (Eq,Ord,Read,Show)</pre> <ul style="list-style-type: none"> <li>• <b>Left – Error type that is not mappable.</b></li> <li>• <b>Right – Expected type</b></li> </ul>	<p><b>Example:</b> Either as an Instance of Functor</p> <pre>instance Functor (Either a) where   fmap _ (Left x) = Left x   fmap f (Right y) = Right (f y)</pre> <pre>&gt; fmap (+1) Leftt 20 20 -- No Change  &gt; fmap (+1) Right 20 21 -- Changed</pre>	

## IO in Haskell

<ul style="list-style-type: none"> <li>• Haskell avoids side effects but they are inevitable in real programs.</li> <li>• <b>Monads</b> <ul style="list-style-type: none"> <li>○ Related to Functors</li> <li>○ Compartmentalize side effects.</li> </ul> </li> <li>• <b>()</b> <ul style="list-style-type: none"> <li>○ Unit type in Haskell</li> </ul> </li> </ul>	<p><b>Type Signature of the main Function in Haskell</b></p> <pre>main :: IO ()</pre> <p><b>Hello World in Haskell</b></p> <pre>main = putStrLn "Hello World"</pre> <p><b>Type Signature of getLine</b></p> <pre>getLine :: IO String</pre>	<ul style="list-style-type: none"> <li>• <b>do</b> – Allows for the chaining of multiple IO/Monad commands together. <b>Syntactic sugar for bind "&gt;&gt;="</b></li> <li>• <b>&lt;-</b> Extracts data out of an IO/Monad "Box"</li> <li>• <b>return</b> – Places data into an IO/Monad "Box"</li> </ul>	
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<p><b>do Example</b></p> <pre>main = do   line &lt;- getLine   if null line -- Checks for empty str   then return ()   else putStrLn \$ reverseWords line  reverseWords :: String -&gt; String reverseWords = unwords .   map reverse . words</pre>	<p><b>return in Haskell</b></p> <ul style="list-style-type: none"> <li>• <b>Unrelated to “return” in other languages</b></li> <li>• <b>Better described as “wrap” or “box”</b></li> </ul> <p><b>Summary:</b>  <b>return</b> – Boxes an IO (since IO is a monad)  <b>&lt;-</b> Unboxes an IO</p>	<p><b>Type of the Unit Type ()</b></p> <ul style="list-style-type: none"> <li>• Base type</li> </ul> <pre>&gt; :t () () :: ()</pre> <hr/> <p><b>Type of return</b></p> <pre>&gt; :t (return ()) (return ()) :: Monad m =&gt; m ()</pre> <p>Monad is a <b>typeclass</b>.</p>
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<p><b>Using IO as a Functor</b></p> <pre>main = do   line &lt;- fmap (++"!!!") getLine   putStrLn line</pre> <p><b>Explanation:</b> This function takes a string input from standard in and appends “!!!” at which point it prints it to the console.</p>	<p><b>Definition of IO as a Functor</b></p> <pre>instance Functor IO where   fmap f action = do     result &lt;- action     return (f result)</pre> <p><b>Explanation:</b> The action object is taken out of the IO box, the function “f” applied to it, and then returned to the IO box.</p>	<p><b>id Function</b></p> <ul style="list-style-type: none"> <li>• <b>Takes one input parameter and returns that input parameter unmodified. Examples:</b></li> </ul> <pre>&gt; id 3 3  &gt; id "Hello World" "Hello World"</pre>
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## Functor Laws

<p><b>Functor Law #1:</b> If we map the id function over a Functor, the Functor that we get back should be the same as the original Functor.</p> <p><b>Examples:</b></p> <pre>&gt; fmap id (Just 3) Just 3 &gt; fmap id Nothing Nothing &gt; fmap id [1, 2, 3] [1, 2, 3]</pre>	<p><b>Functor Law #2:</b> Composing two functions and then mapping the resulting (composed) function over a Functor should be the same as first mapping one function over the Functor and then mapping the other one.</p> <p><b>Law #2 Written Formally</b></p> <pre>fmap (f . g) = fmap f . fmap g</pre>	<p>The Functor laws are NOT enforced. They are good practice that makes the code easier to reason about.</p>
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## Lecture #09 – Applicative Functors

<p><b>Functor – Something that can be mapped over. Allow you to map functions over different data types. Examples:</b></p> <ul style="list-style-type: none"> <li>• Maybe</li> <li>• Either</li> <li>• IO</li> <li>• Lists</li> <li>• &lt;*&gt;</li> </ul> <p><b>Functors return boxed up values.</b></p>	<p><b>Functor Example</b></p> <pre>&gt; fmap (+1) [1, 2, 3] [2, 3, 4]  &gt; let x = fmap (+) [1, 2, 3]</pre> <p><b>Explanation:</b> In this case x is: [(1+), (2+), (3+)]</p>	<p><b>Applicative Functor</b></p> <ul style="list-style-type: none"> <li>• Requires the importing of a special library as shown below:</li> </ul> <pre>import Control.Applicative</pre> <p>Functions in Applicative Typeclass:</p> <ul style="list-style-type: none"> <li>• <b>pure</b> – Wraps/boxes a value</li> <li>• <b>&lt;*&gt;</b> - Infix version of <b>fmap</b>. Is itself a Functor.</li> </ul>	<p><b>Example Uses of pure</b></p> <pre>&gt; pure 7 7  &gt; pure 7 :: Maybe Int Just 7  &gt; pure 7 :: [Int] [7]</pre>
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<p><b>Type Class Definition of Applicative</b></p> <pre>class (Functor f) =&gt; Applicative f where   pure :: a -&gt; f a   &lt;*&gt; :: f (a -&gt; b) -&gt; f a -&gt; f b</pre> <p><b>Only difference between &lt;*&gt; and fmap is that the function in &lt;*&gt; is boxed while it is not in fmap (see the green f).</b></p>	<p><b>Make Maybe an Instance of Applicative</b></p> <pre>instance Applicative Maybe where   pure = Just   Nothing &lt;*&gt; _ = Nothing   (Just f) &lt;*&gt; x = fmap f x</pre> <p><b>Explanation:</b> pure simply wraps the value in Just. No need to explicitly check if “x” is maybe as fmap will do that for you.</p>	<p><b>Examples of Applicative Maybe</b></p> <pre>&gt; Just (+3) &lt;*&gt; Just 4 Just 7 &gt; pure (+3) &lt;*&gt; Just 4 Just 7 &gt; pure (+) &lt;*&gt; Just 3 &lt;*&gt; Just 4 Just 7 &gt; (+) &lt;*&gt; Just 3 &lt;*&gt; Just 4 Just 7</pre> <p><b>Explanation:</b> x &lt;*&gt; is fmap as an infix operator. It is NOT necessarily the same as pure x &lt;*&gt;. It should be based off Applicative Functor Law #1.</p>
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<p><b>Making [] an Instance of Applicative</b></p> <pre>instance Applicative [] where   pure x = [x]   fs &lt;*&gt; xs = [f x   f &lt;- fs, x &lt;- xs]</pre> <p><b>Explanation:</b> The function is actually a list of functions so list comprehension is needed.</p>	<p><b>Example Use of Applicative on Lists</b></p> <pre>&gt; (*) &lt;*&gt; [1, 2, 3] &lt;*&gt; [1,0,0,1] [1,0,0,1,2,0,0,2,3,0,0,3]  &gt; pure 7 7 -- No change &gt; pure 7 :: [Int] [7]</pre>	<p><b>Definition of IO as an Instance of Applicative</b></p> <pre>instance Applicative IO where   pure = return   a &lt;*&gt; b = do     f &lt;- a     x &lt;- b     return (f x)</pre>
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<p><b>Example of Applicative IO</b></p> <pre>import Control.Applicative  main = do   a &lt;- (++) &lt;\$&gt; getLine &lt;*&gt; getLine   putStrLn a</pre>	<p><b>liftA2</b></p> <p>A function that simplifies the application of a normal function to two Functors.</p> <pre>liftA2 :: (Applicative f) =&gt; (a -&gt; b -&gt; c) -&gt; f a -&gt; f b -&gt; fc liftA2 f x y = f &lt;\$&gt; a &lt;*&gt; b</pre>
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<p><b>Example of liftA2</b></p> <pre>&gt; (:) &lt;\$&gt; Just 3 &lt;*&gt; Just [4] Just [3, 4] &gt; liftA2 (:) (Just 3) (Just [4]) Just [3, 4]</pre>	<p><b>Applicative Functor Definition</b></p> <p><b>A functor you can apply to other Functors.</b></p>
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## Applicative Functor Laws

<p><b>Law 1:</b></p> <pre>pure f &lt;*&gt; x = fmap f x</pre>	<p><b>Law 2:</b></p> <pre>pure id &lt;*&gt; v = v</pre>	<p><b>Law 3:</b></p> <pre>pure (.) &lt;*&gt; u &lt;*&gt; v &lt;*&gt; w = u &lt;*&gt; (v &lt;*&gt; w)</pre>
<p><b>Law 4:</b></p> <pre>pure f &lt;*&gt; pure x = pure (f x)</pre>	<p><b>Law 5:</b></p> <pre>u &lt;*&gt; pure y = pure (\$y) &lt;*&gt; u</pre>	<p>Similar to Functor Laws, these are not strictly enforced but are good practice to make it easier to reason about the code.</p>

## Monoids

<p><b>Monoid:</b> An <b>associative</b> binary function and a value that acts as an <b>identity</b> with respect to that function.</p> <p><b>Examples</b></p> <ul style="list-style-type: none"> <li><math>x * 1</math> Identity of <b>Multiplication</b></li> <li><code>lst ++ []</code> Identity of <b>Concatenation</b></li> <li><math>x + 0</math> Identity of <b>Addition</b></li> </ul>	<p><b>Definition of Monoid Typeclass</b></p> <pre>class Monoid m where   mempty :: m   mappend :: m -&gt; m -&gt; m   mconcat :: [m] -&gt; m   mconcat = foldr mappend mempty</pre>	
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## Monoid Rules

<p><b>Rule #1:</b></p> <pre>mempty `mappend` x = x</pre>	<p><b>Rule #2:</b></p> <pre>x `mappend` mempty = x</pre>	<p><b>Rule #3:</b></p> <pre>(x `mappend` y) `mappend` z = x `mappend` (y `mappend` z)</pre>
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## Lecture #10 – Monads

<p><b>Functor</b> – Something that can be mapped over.</p> <p><b>Definition:</b></p> <pre>instance Functor f where   fmap :: (a -&gt; b) -&gt; f a -&gt; f b</pre>	<p><b>Problem with Functors:</b> Do not support chaining of multiple commands. <b>Example:</b></p> <pre>&gt; fmap (+) (Just 3) (Just 4)</pre> <p>Returns an error since it cannot resolve <code>(Just 3+)</code> and <code>(Just 4)</code></p>	<p><b>Applicative Functor:</b> A <b>Functor</b> that can be applied to other <b>Functors</b>.</p> <pre>class (Functor f) =&gt; Applicative f where   (&lt;*&gt;) :: f (a -&gt; b) -&gt; f a -&gt; f b</pre> <p>Requires library <b>Control.Applicative</b></p>
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<p>Even <b>with Applicative Functors</b>, it is not possible to chain together multiple commands. <b>Example:</b></p> <pre>&gt; Just (+3) &lt;*&gt; Just (+4) &lt;*&gt; Just (+5)</pre> <p>Returns error</p>	<p><b>Monads:</b> Can chain through a series of functions.</p> <p><b>Key Operator:</b> <b>&gt;&gt;=</b> (Bind)</p>	<p><b>Example #1:</b> Using <code>Just</code></p> <pre>&gt; (Just 3) &gt;&gt;= (\x -&gt; Just (x + 4)) &gt;&gt;= (\y -&gt; Just (y+5)) 12</pre> <p><b>Example #2:</b> Using <code>return</code></p> <pre>&gt; (return 3) &gt;&gt;= (\x -&gt; return (x + 4)) &gt;&gt;= (\y -&gt; return (y+5)) 12</pre>
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<p><b>Comparing &lt;*&gt; and &gt;&gt;=</b></p> <p><b>Functor:</b>  <code>(&lt;*&gt;) :: Applicative f =&gt; f (a -&gt; b) -&gt; f a -&gt; f b</code></p> <p><b>Monad:</b>  <code>(&gt;&gt;=) :: Monad m =&gt; m a -&gt; (a -&gt; m b) -&gt; m b</code></p> <p><b>Differences:</b></p> <ol style="list-style-type: none"> <li>Order of the arguments changed.</li> <li>The function is boxed in Functor but not Monad</li> <li>Monad function returns a boxed result.</li> </ol>	<p><b>Example of &lt;\$&gt;, &lt;*&gt; and &gt;&gt;=</b></p> <pre>&gt; (\x -&gt; x + 1) &lt;\$&gt; Just 3 Just 4</pre> <pre>&gt; Just (\x -&gt; x + 1) &lt;*&gt; Just 3 Just 4</pre> <pre>&gt; (Just 3) &gt;&gt;= (\x -&gt; Just (x+1)) Just 4</pre>	<p><b>Example:</b> Implement <code>applyMaybe</code> that applies a function to a <code>Maybe</code></p> <pre>applyMaybe :: Maybe a -&gt; (a -&gt; b) -&gt; Maybe b applyMaybe Nothing _ = Nothing applyMaybe (Just x) f = Just (f x)</pre>
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<p><b>Example:</b> Implement <code>applyMaybe</code> that applies a function to a <code>Maybe</code></p> <pre> applyMaybe :: Maybe a -&gt; (a -&gt; Maybe b)               -&gt; (Maybe b)  applyMaybe Nothing _ = Nothing applyMaybe (Just x) f = Just (f x) </pre>	<p><b>Chaining <code>applyMaybe</code></b></p> <pre> &gt; (Just 3) \applyMaybe (\x -&gt; Just (x*2)) \applyMaybe (\y -&gt; Just (y-1)) Just 5  &gt; (Just 3) \applyMaybe (\_ -&gt; Nothing) \applyMaybe (\y -&gt; Just (y-1)) Nothing </pre>	<p><b>Additional Names for Monoids</b></p> <ul style="list-style-type: none"> <li>• “Programmable Semicolons”</li> <li>• “Applicative Functors you can chain.”</li> </ul>
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<p><b>Monad Typeclass Definition</b></p> <pre> class Monad m where   return :: a -&gt; m a   (&gt;=) :: m a -&gt; (a -&gt; m b) -&gt; m b    (&gt;&gt;) :: m a -&gt; m b -&gt; m b   x &gt;&gt; y = x &gt;= (\_ -&gt; y) --Lamda    fail :: String -&gt; m a   fail msg = error msg </pre>	<p><b>Example a Robot Moving Towards a Goal (Not Failure)</b></p> <pre> --Location type Robot = (Int, Int)  -- Functions up (x,y) = (x, y+1) down (x,y) = (x, y-1) left (x,y) = (x-1, y) right (x,y) = (x+1, y)  -- Define Operator and start location x -: f = f x start = (0, 0)  &gt; start -: up -: right (1, 1)  &gt; start -: up -: left -: left -: right -: down (-1, 0) </pre>
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<p><b>Maybe as an Instance of the Monad Typeclass</b></p> <pre> instance Monad Maybe where    return = Just    (&gt;=) Nothing _ = Nothing   (&gt;=) (Just x) f = f x    fail _ = Nothing </pre>	<p><b>Example a Robot Moving Towards a Goal (with Failure)</b></p> <pre> -- Once the goal is reached, -- the robot stops goal := Map.empty       -: (Map.insert (0, 2) True)       -: (Map.insert (-1, 3) True)       -: (Map.insert (-3, -8) True)  moveTo :: Pos -&gt; Maybe Pos moveTo p = if Map.member p goal            then Nothing            else Just p  -- Since these are in bind, no need -- to handle Nothing. Bind handles it. up (x,y) = moveTo (x, y+1) down (x,y) = moveTo (x, y-1) left (x,y) = moveTo (x-1, y) right (x,y) = moveTo (x+1, y) </pre>	<pre> start = (0, 0)  &gt; return start &gt;= up &gt;= left &gt;= left   &gt;= right &gt;= down Just (-1, 0)  &gt; return start &gt;= left &gt;= left &gt;= up   &gt;= up &gt;= right &gt;= up   &gt;= right &gt;= right &gt;= down Nothing  Explanation: Reached one of the goals (-1, 3) at the red up </pre>
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## Integer Division Using Monads

<p><b>Integer Division with Bind and No “do”</b></p> <pre> mydiv :: Maybe Int -&gt; Maybe Int -&gt; Maybe Int mydiv x y = x &gt;= (\number -&gt;   y &gt;= (\denom -&gt;     if denom &gt; 0       then Just (div number denom)       else fail "Div by zero")) </pre>	<p><b>Integer Division with Bind with “do”</b></p> <pre> mydiv :: Maybe Int -&gt; Maybe Int -&gt; Maybe Int mydiv x y = do   number &lt;- x   denom &lt;- y   if denom &gt; 0     then Just (div number denom)     else fail "Div by 0" </pre>	<p><b>Integer Division with Bind with “do” and return</b></p> <pre> mydiv :: Maybe Int -&gt; Maybe Int -&gt; Maybe Int mydiv x y = do   number &lt;- x   denom &lt;- y   if denom &gt; 0     then return \$ div number denom     else fail "Div by 0" </pre>
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## List Monad

<p><b>Making List an Instance of Monad</b></p> <pre> instance Monad [] where   return x = [x]   (&gt;=) xs f = concat(map f xs)   fail _ = [] </pre> <p><b>Explnation:</b> <code>concat</code> is needed here as <code>f</code> returns elements already in a list. As such, <code>concat</code> merges the individual lists (from each call to <code>f</code>) into a single list.</p>	<p><b>Example Use of List as a Monad</b></p> <pre> listOfTuples :: [(Int, Char)] listOfTuples = do   n &lt;- [1, 2]   ch &lt;- ['a', 'b']   return (n, ch)  &gt; listOfTuples [(1, 'a'), (1, 'b'), (2, 'a'), (2, 'b')] </pre>	<p><b>Combining a Maybe and a List Monad</b></p> <pre> &gt; Just [2,3] &gt;= (\x -&gt; Just( fmap (+1) x)) [3, 4] </pre>
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## Lecture #11 – Parsing Combinators

<p><b>Semantics:</b> Enumerate <b>what a program means</b>. Defined by the interpreter or compiler.</p> <p><b>Syntax:</b> Enumerate <b>how a program is structured</b>. Defined by the lexer and parser.</p>	<p><b>Compilation Flow</b></p> <p><b>Step #1:</b> Tokenizer/lexer generates a set of tokens.</p> <p><b>Step #2:</b> Parser turns the tokens into an abstract syntax tree.</p> <p><b>Step #3:</b> Compilers and interpreters convert the AST into machine code or commands respectively.</p>	<p><b>Lexer</b></p> <p>Converts the characters of the program into words of the language.</p> <p><b>Examples:</b></p> <ul style="list-style-type: none"> <li>• Lex/Flex (C/C++)</li> <li>• ANTLR &amp; JavaCC (Java)</li> <li>• Parsec (Haskell)</li> </ul>
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<p><b>Categories of Tokens</b></p> <ul style="list-style-type: none"> <li>• <b>Reserved Words/Keywords.</b> <ul style="list-style-type: none"> <li>◦ <b>Examples:</b> while, if, then, else</li> </ul> </li> <li>• <b>Literals/Constants.</b> <ul style="list-style-type: none"> <li>◦ <b>Examples:</b> 123, "Hello World!"</li> </ul> </li> <li>• <b>Special symbols.</b> <ul style="list-style-type: none"> <li>◦ <b>Examples:</b> ",", "&gt;=", "&amp;&amp;"</li> </ul> </li> <li>• <b>Identifiers.</b> <ul style="list-style-type: none"> <li>◦ <b>Examples:</b> "balance", "myFunction"</li> </ul> </li> </ul>	<p><b>Parsing</b></p> <ul style="list-style-type: none"> <li>• <b>Parser converts tokens to abstract syntax trees.</b></li> <li>• <b>Defined by context free grammars (CFG)</b></li> <li>• <b>Types of Parsers:</b> <ul style="list-style-type: none"> <li>◦ <b>Bottom-up/Shift-Reduce</b> Parsers</li> <li>◦ <b>Top-down</b> parsers</li> </ul> </li> </ul>	<p><b>Context Free Grammars</b></p> <ul style="list-style-type: none"> <li>• Grammars specify the language.</li> <li>• Specified in Backus-Naur form format. <b>Example:</b> <pre>Expr -&gt; Number         Number + Expr</pre> </li> <li>• <b>Terminal</b> – <b>Cannot be broken down</b> further.</li> <li>• <b>Non-terminals</b> – <b>Can be broken down</b> further.</li> </ul> <p><b>Example:</b> "0", "1", "2", ..., "9" are terminals but digit, number, and expression are not.</p>	<p><b>Example Grammar</b></p> <pre>expr -&gt; expr + expr         expr - expr         ( expr )         number  number -&gt; number digit           digit  digit -&gt; 0   1   2   ...   9</pre>
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<p><b>Bottom-Up / Shift-Reduce Parser</b></p> <ul style="list-style-type: none"> <li>• <b>Shift</b> tokens onto a stack</li> <li>• <b>Reduce</b> the stack to a non-terminal.</li> <li>• <b>LR</b> – <b>L</b>eft to right, <b>R</b>ightmost derivation</li> <li>• <b>LALR</b> – <b>L</b>ook-<b>A</b>head <b>LR</b> parsers are the most popular type of LR parsers. <ul style="list-style-type: none"> <li>◦ <b>Examples:</b> YACC/Bison</li> </ul> </li> <li>• <b>Fading from popularity</b></li> </ul>	<p><b>Top-Down Parser</b></p> <ul style="list-style-type: none"> <li>• <b>Non-terminals are expanded to match tokens.</b></li> <li>• <b>LL</b> – <b>L</b>eft to right, <b>L</b>eftmost derivation</li> <li>• <b>LL(k) Parser</b> – Looks ahead up to <i>k</i> elements. <ul style="list-style-type: none"> <li><b>Examples:</b> Java CC, ANTLR</li> <li>◦ The higher the <i>k</i>, the more difficult language is to parse. <i>k</i> <b>can be arbitrary</b>.</li> <li>◦ <b>LL(1)</b> - Easy to parse using either LL or recursive descent parsers. <b>Many computer languages are designed to be LL(1).</b></li> </ul> </li> </ul>	<p><b>Parser Combinator</b></p> <p><b>Combine simpler parsers to make a more complex parser.</b></p> <p><b>Example:</b> Parsec</p>	<p><b>Useful Parsec Functions</b></p> <ul style="list-style-type: none"> <li>• <b>many</b> – Parses <b>zero or more</b> occurrences of the given parser.</li> <li>• <b>many1</b> – Parses <b>1 or more</b> occurrences of the given parser.</li> <li>• <b>noneOf</b> – Anything but the specified value</li> <li>• <b>spaces</b> – Whitespace characters</li> <li>• <b>char</b> – The specific specified character</li> <li>• <b>string</b> – The specific specified string.</li> <li>• <b>sepBy</b> – Separate tokens by some token.</li> </ul>
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Example Parsec Code		
<pre>import Text.ParserCombinators.Parsec  num :: GenParser st String num = many1 digit  main = do     print \$ parse num "Hello" "42"</pre>	<pre>import Text.ParserCombinators.Parsec  num :: GenParser st Integer num = do     str &lt;- many1 digit     return \$ read str  main = do     print \$ parse num "World" "42"</pre>	<ul style="list-style-type: none"> <li>• <b>st</b> – "State." Always required for our purposes.</li> <li>• <b>String/Integer</b> – Parser return type</li> <li>• <b>many1</b> – Select one of more digits.</li> <li>• <b>digit</b> – 0, 1, 2, 3, ..., 9 (<b>terminal</b>)</li> <li>• <b>num</b> – Parser entry function</li> <li>• <b>"Hello"/"World"</b> – Debug string.</li> <li>• <b>"42"</b> – String to parse.</li> </ul>

<p><b>Example with try, &lt; &gt;, and &lt;?&gt;</b></p> <pre>eol = try (string "\n")       &lt; &gt; string "\n\r"       &lt;?&gt; "end of line"</pre> <ul style="list-style-type: none"> <li>• <b>try</b> – If an incomplete match is found, rewind.</li> <li>• <b>&lt; &gt;</b> – "Or" Operator for matching tokens.</li> <li>• <b>&lt;?&gt;</b> – Otherwise with an accompanying error message.</li> </ul>		
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## Practice Midterm and Review Notes

Question #1	Question #2	Question #3	Question #4	Question #5
a. <b>True</b> b. <b>False</b> – Lazy evaluation c. <b>False</b> – Lazy evaluation d. <b>False</b> – Statically type e. <b>True</b>	a. <b>True</b> b. <b>False</b> – Applicative functor c. <b>True</b> d. <b>True</b> e. <b>True</b>	a. <b>False</b> – Big step b. <b>True</b> c. <b>False</b> – Use store d. <b>True</b> e. <b>False</b>	a. <b>False</b> – Imperative b. <b>True</b> c. <b>False</b> d. <b>True</b> e. <b>True</b>	a. <b>True</b> b. <b>False</b> – Typeclass c. <b>True</b> d. <b>False</b> e. <b>False</b> – Algebraic data type

Haskell	Purely Functional	Functional Languages	Operational Semantics
<ul style="list-style-type: none"> <li>• <b>Purely Functional</b></li> <li>• <b>Lazy evaluation</b></li> <li>• <b>Fully Curried Language</b></li> <li>• <b>Statically Typed</b></li> <li>• <b>Type Inference</b> – Via context, Haskell can deduce the type.</li> </ul>	<ul style="list-style-type: none"> <li>• <b>Referential Transparency</b> – A <b>function call</b> can be replaced with its equivalent value without affecting the program</li> <li>• <b>No (re)assignment</b></li> <li>• <b>No loop</b></li> <li>• <b>No side effects</b></li> </ul>	<ul style="list-style-type: none"> <li>• <b>Functions are first class objects</b> meaning they can be passed to a function, returned from it, or created on the fly.</li> <li>• <b>Higher order function support</b></li> </ul>	<ul style="list-style-type: none"> <li>• <b>Small Step</b> – Structural Semantics</li> <li>• <b>Big Step</b> – Natural Semantics</li> <li>• <b>“Get stuck”</b> – When a function is encountered that does not have an associated rule.</li> </ul>

## CSV Parser Example

### Verbose Approach

```
import Text.ParserCombinator.Parsec
import System.Environment

csvFile :: GenParser st [[String]]
csvFile = do
    arr <- many line
    char eof
    return arr

line :: GenParser st [String]
line = do
    result <- many1 cell
    char '\n'
    return result

cells :: GenParser st [String]
cells = do
    firstCell <- cellContents
    nextCells <- remainingCells
    return (firstCell:nextCells)

cellContent :: GenParser st String
cellContent = many $ noneOf "\",\n" -- Two characters

remainingCells :: GenParser st [String]
remainingCells = do
    (char "," >> cells)
    <|> return []

main = do
    args <- getArgs
    p <- parseFromFile csvFile "example 1" (head args)
    case p of
        Left msg -> error msg
        Right csv -> print csv
```

### Concise Approach

```
import Text.ParserCombinator.Parsec
import System.Environment

csvFile = lines `sepBy` eof
line = cells `sepBy` string ","
cells = many (noneOf "\n")
eof = try (string "\n")
    <|> string "\n\r"
    <?> "end of line"

main = do
    args <- getArgs
    p <- parseFromFile csvFile "example 1" (head args)
    case p of
        Left msg -> error msg
        Right csv -> print csv
```

## Miscellaneous

<p><b>Kind of Show and show</b></p> <pre>&gt; :k Show Show :: * -&gt; Constraint</pre> <p><b>Type and Kind of show</b></p> <pre>&gt; :k show Error (A function not a type) &gt; :t show show :: (Show a) =&gt; a -&gt; String</pre>	<p><b>Lambda and ADT Combined</b></p> <pre>&gt; (\x -&gt; Just (x+1)) 1 Just 2</pre> <p><b>Creating Type Alias</b></p> <pre>type String = [Char]</pre> <p>Allows for more readable code as developer can use a type name that makes more sense for a given application.</p>	<p><b>Example:</b> <code>applyMaybe</code> that takes a <code>(Maybe a)</code> and applies to it a function that takes a normal <code>a</code> and returns a <code>(Maybe b)</code></p> <pre>applyMaybe :: (Maybe a) -&gt; (a -&gt; Maybe b) -&gt; (Maybe b) applyMaybe Nothing _ = Nothing applyMaybe (Just x) f = f x</pre> <p><b>Explanation:</b> Since the function “<code>f</code>” already returns a <code>Maybe</code>, you do not need to re-box it. However, since it does not take a <code>Maybe</code>, you need to unbox the first input parameter.</p>
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<p><b>Applying return to Items</b></p> <pre>&gt; return 7 7 &gt; return 7 :: Maybe Int Just 7 &gt; return 7 :: [Int] [7] -- Need Int or get an error</pre> <p><b>Conclusion:</b> Behavior for <code>return</code> is the same as <code>pure</code>. Both put the object in the minimum default context that still yields that value.</p>	<p><b>List comprehension is syntactic sugar for using lists as monads.</b></p>	
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<p><b>Monads and Lambda</b></p> <p>When trying to chain multiple functions together in a <code>Monad</code>, remember the <code>Monad</code> must return a <b>boxed value</b>. Hence, <code>Lambda</code> often work well as they simplifying boxing.</p>	<p><b>Applicative Typeclass</b> – Allows you to use normal functions on values that have a context (i.e. are inside a <code>Functor</code>).</p>	<p><b>return</b> – <code>Monad</code> equivalent of “pure” for <code>Applicative Functors</code>.</p> <p><b>Cannot use <code>fmap</code> in the definition of a <code>Monad</code> since <code>fmap</code> returns a boxed value while the function of the <code>Monad</code> returns a boxed value. Hence, if you used <code>fmap</code> with a <code>Monad</code>, you would return a double boxed value.</b></p>
	<p><b>Monad:</b> Given a value of type, <code>a</code>, in a context, <code>m</code>, apply a function that takes a normal value of type <code>a</code> and returns a value in the context <code>m</code>.</p> <pre>(&gt;&gt;=) :: (Monad m) =&gt; m a -&gt; (a -&gt; m b) -&gt; m b</pre> <p><b>Monads are just applicative functors that support <code>bind (&gt;&gt;=)</code>.</b></p> <p><b>Key Difference:</b> <code>Applicative</code> functors support normal functions that take and return unboxed values while <code>Monads</code> return boxed values.</p>	

## Functor Definitions

<p><b>Lists</b></p> <pre>instance Functor [] where   fmap = map</pre>	<p><b>Maybe</b></p> <pre>instance Functor Maybe where   fmap _ Nothing = Nothing   fmap f (Just x) = Just (f x)</pre>	<p><b>IO</b></p> <pre>instance Functor IO where   fmap f a = do     x &lt;- a     return (f x)</pre>
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## Applicative Functor Definitions

<p><b>Lists</b></p> <pre>instance Applicative [] where   pure x = [x]   (&lt;*&gt;) fs xs = [ f x   f &lt;- fs, x &lt;- xs]</pre>	<p><b>Maybe</b></p> <pre>instance Applicative Maybe where   pure x = Just x   (&lt;*&gt;) Nothing _ = Nothing   (&lt;*&gt;) (Just f) x = fmap f x</pre>	<p><b>IO</b></p> <pre>instance Applicative IO where   a &lt;*&gt; b = do     f &lt;- a     x &lt;- b     return (f x)</pre>
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## Monad Definitions

<p><b>Lists</b></p> <pre>instance Monad [] where   return x = [x]   (&gt;&gt;=) xs f = concat \$ map f x   fail _ = []</pre>	<p><b>Maybe</b></p> <pre>instance Monad Maybe where   return x = Just x   (&gt;&gt;=) Nothing _ = Nothing   (&gt;&gt;=) (Just x) f = f x   fail _ = Nothing</pre>	<p><b>IO</b></p> <pre>instance Monad IO where   (&gt;&gt;=) a f = do     x &lt;- a     f x   fail s = ioerror (userError s)</pre>
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# Lecture #12 – Introduction to JavaScript

<b>JavaScript</b> <ul style="list-style-type: none"> <li>Developed at Netscape by Brendan Eichs in 10 days</li> <li>Originally named “Mocha”</li> <li>Syntax similar to Java</li> </ul>	<b>Multiparadigm JavaScript</b> Supported programming paradigms: <ul style="list-style-type: none"> <li>Imperative</li> <li>Functional</li> <li>Object-Oriented (through <b>prototypes</b>)</li> </ul>	<b>Where JavaScript is Run</b> <ul style="list-style-type: none"> <li><b>Client Side Versions</b> <ul style="list-style-type: none"> <li>Runs on user machine</li> </ul> </li> <li><b>Server-side Versions</b> <ul style="list-style-type: none"> <li>JVM: <b>Rhino</b> &amp; <b>Nashorn</b></li> <li><b>Node.js</b></li> </ul> </li> </ul>	<b>Example: Imperative JavaScript</b> <pre>function addList(list){     var i, sum = 0;     for( i = 0; i &lt; list.length ; i++){         sum += list[i];     }     return sum; }</pre>
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<b>Example: Functional JavaScript</b> <pre>function addList(list){     if(list.length == 0){         return 0;     }      return list[0]         +         addList(list.slice(1)); }</pre> <p><b>slice(begin[, end])</b> – Takes a subset of an array from the “begin” index to the “end” (exclusive). If no “end” is specified, it takes all elements to the end of the list.</p>	<b>Example: Object-Oriented JavaScript</b> <pre>function Adder(amount){     this.amount = amount; } Adder.prototype.add = function(x){     return this.amount + x; } var myAdder = new Adder(1) var y = myAdder.add(7)</pre> <p><b>Adder</b> – Name of a new constructor. <b>Convention is to start constructors with a capital letter.</b></p> <p><b>this</b> – Not optional in JavaScript.</p>	<b>Example: Functional JavaScript</b> <pre>var x = 42; // Create with var y = 7; // No error without var function add(a, b){     return a + b; } function noReturnAdd(a, b){     a + b; }  // c is “undefined” since no return var c = noReturnAdd(x, y)  //Lambda Function var myLambda = function(x){return x * x;}</pre>
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<b>Printing to the Console in JavaScript</b> <ul style="list-style-type: none"> <li><b>Standard Approach:</b> <pre>console.log(“...”)</pre> <ul style="list-style-type: none"> <li>Not supported by all implementations.</li> </ul> </li> <li>JVM based JavaScript Approach:           <pre>print</pre> </li> <li>Solution to Support a Single Interface:           <pre>var print = console.log</pre> </li> </ul>	<b>Closures</b> <ul style="list-style-type: none"> <li>Functions whose inner variables refer to independent (free) variables.</li> </ul> <p><b>Closure Example</b></p> <pre>function getNextInt(){     var nextInt = 0;     return function(){         return nextInt++;     }() // Double paren         // run the function } console.log(getNextInt()); // print “0” console.log(getNextInt()); // print “1” console.log(getNextInt()); // print “2”</pre>	<b>Node.js</b> <ul style="list-style-type: none"> <li>JavaScript runtime environment and library <b>designed to run outside the browser.</b></li> <li>Based off Google’s V8 engine.</li> <li><b>npm</b> – Package manager to get new packages.</li> </ul>
		<b>Callback Function</b> <ul style="list-style-type: none"> <li>Functions in JavaScript are first class objects of type “Object”.</li> <li>Not executed immediately.</li> </ul>
		<b>JavaScript supports both “null” and “undefined”</b>

<b>Reading from a File with Callbacks in Node.js</b> <pre>var fs = require('fs') fs.readFile('myFile.txt',     function(err, data){         if(err)             throw err;         else             console.log(“” + data);     } ) console.log(“All done”)</pre> <p>“All done” prints before the file contents due to callbacks. <b>require</b> – Includes the JavaScript package “fs”</p>	<b>Synchronous File IO in Node</b> <pre>var fs = require('fs') var data =     fs.readFileSync('myFile.txt'); console.log(“All done”)</pre> <p>To eliminate callbacks, most function names can be appended with “Sync”</p>	<b>Creating a JavaScript Object</b> <pre>var myDog = {age : 3,     weight: 100}</pre> <p><b>Every object is a map.</b></p> <p><b>Adding a Field to a JavaScript Object</b></p> <pre>myDog['height'] = 45 // Add a new height field // Note the single quotes</pre> <p><b>Adding a Function to a JavaScript Object’s Prototype</b></p> <pre>myDog.speak = function(){ console.log(“Grr”); }</pre> <p><b>Delete a Function from a JavaScript Object’s Prototype</b></p> <pre>delete myDog.speak</pre>
	<b>Undeclared Object Fields</b> <p><b>Any undeclared object fields or uninstantiated variables are undefined.</b></p> <pre>var y; // Uninstantiated // Both print ‘undefined’ console.log(y) console.log(myDog.name)</pre>	

## Prototypes

<b>Object Prototypes</b> <p><b>JavaScript prototypes are just like any other object.</b></p> <pre>var dogPrototype = {     speak: function(){         console.log(“bark!”);     } }</pre>	<b>Defining an Object’s Prototype</b> <pre>var rex = { name: “Rex”,     __proto__: dogPrototype}</pre>	<b>Prototypical Inheritance:</b> If an object does not have a method or field, JavaScript looks to the object’s <b>__proto__</b> object.
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<p><b>Add a Special "speak" Method to Rex</b></p> <pre> rex.speak = function() {     console.log("Grr"); }; rex.speak(); // Prints "Grr"  delete rex.speak; // Prints "Bark!" from __proto__ rex.speak();  delete rex.speak; // Does nothing rex.speak(); // Prints "Bark!" </pre>	<p><b>Effect of the "new" Keyword</b></p> <pre> function Cat(name, breed) {     var this = {}; // Add when new is used     this.prototype = Cat.prototype; // Also comes from new     this.name = name;     this.breed = breed;     this.speak = function() { console.log("meow"); };     return this; // Also comes from new } </pre>
<p><b>Unspecified Function Arguments:</b> In JavaScript, any unspecified function argument <b>defaults to "undefined"</b>.</p>	<p><b>No "return" in a Function</b></p> <pre> function noReturnAdd(x, y) {     x + y; // without "return" }  // c is "undefined" since no return var c = noReturnAdd(x, y) console.log(c); // Prints "undefined" </pre>

<p><b>Top Prototypes</b></p> <p><b>Object.prototype</b> – Top of all object prototypes</p> <p><b>Function.prototype</b> – Top of all function prototypes.</p>	<p><b>Iterating Using "forEach"</b></p> <pre> var arr = [1, 2, 3]; // Print each element in array arr.forEach(function(val) {     console.log(val); }); </pre>	<p><b>require</b></p> <ul style="list-style-type: none"> <li>Used to <b>import an external module</b> in <b>Node.js</b></li> <li>Can be stored in a variable. <b>Example:</b></li> </ul> <pre>var net = require('net');</pre>	<p><b>Running from the Command Line</b></p> <ul style="list-style-type: none"> <li>Use the keyword <b>"node"</b> for Node.js.</li> </ul> <p><b>Example:</b></p> <pre>\$ node my_program.js</pre>
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## Lecture #13 – Lambda Calculus

Expressions	Function Application	
$e ::= x$ (Variables, immutable) $\mid \lambda x. e$ (Lambda abstraction) $\mid e e$ (Function application)  <b>Note:</b> Lambda ( $\lambda$ ) is simply a function.  $v ::= (\lambda x. e)$ (Lambda abstraction)	Given a function where $E$ is a <b>complex expression</b> :  $\lambda(x. E)v$ Then:  $\lambda(x. E)v \rightarrow E[x \mapsto v]$ Hence, “ $v$ ” replaces “ $x$ ” in “ $E$ ”.	

### Small-Step Evaluation Order Rules for Lambda Calculus

Rule: SS-E1	Rule: SS-E2	Rule: SS-Lambda Context	Optional Rule: Lazy SS-Lambda Context
$\frac{e_1 \rightarrow e'_1}{e_1 e_2 \rightarrow e'_1 e_2}$	$\frac{e_2 \rightarrow e'_2}{(\lambda x. e) e_2 \rightarrow (\lambda x. e) e'_2}$	$(\lambda x. e) v \rightarrow e[x \mapsto v]$	$(\lambda x. e) e_2 \rightarrow e[x \mapsto e_2]$

## Lecture #14 – JavaScript Scoping

<p><b>Example: First Class Function</b></p> <pre>function makeAdder(x) {   return function(y) {     return x + y;   }; } var addOne = makeAdder(1); // Prints "11" console.log(addOne(10));</pre>	<p><b>Example: Function Application</b></p> <pre>function makeAdderList(arr) {   var i;   var output = [];   for(i = 0; i &lt; output.length; i++){     // Need to create a new scope     function() {       // Can add to arr without append       output[i] = function(y) {         return arr[i] + y;       };     }   } }</pre> <p>JavaScript lacks block scope for the closure to be right, must create the function inside another function.</p>	<p><b>Block Scope</b> – The scope (i.e. visibility) of a variable is limited to a specific block (e.g., for loop, if statement, etc.).</p> <ul style="list-style-type: none"> <li>Unlike most languages, JavaScript does not have block scope.</li> <li>To create a new scope, use an anonymous function.</li> </ul> <p><b>Variable Hoisting</b> – All variable declarations (i.e., use of “var”) are treated as if they are at the beginning of the function.</p>	<p><b>“this” in JavaScript</b></p> <p><b>this</b> – Refers to the scope where the function is called.</p> <ul style="list-style-type: none"> <li><b>In Normal Function Calls</b> – <b>this</b> refers to the global “this”</li> <li><b>Object Methods</b> – The object itself.</li> <li><b>Constructor (using “new”)</b> – The newly created object.</li> <li><b>Exceptions: apply, call, and bind.</b> Inline event handles on DOM elements</li> </ul> <p><b>Any time a new function is created, the other “this” is no longer in scope</b></p>
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<p><b>Execution Context</b></p> <p>Consists of three part:</p> <ul style="list-style-type: none"> <li><b>A Variable Object</b> – Container for variables and functions.</li> <li><b>Scope Chain</b> – Variable object plus parent scopes</li> <li><b>Context Object</b> – <b>this</b></li> </ul>	<p><b>Global Context</b></p> <ul style="list-style-type: none"> <li><b>Top Level Context</b></li> <li>Variable object is known as the “global object”</li> <li><b>this</b> – Refers to the global object.</li> </ul> <p><b>Any variable declared without var is added to the global context.</b></p>	<p><b>Function Contexts</b></p> <ul style="list-style-type: none"> <li><b>Activation</b> or <b>Variable Objects</b> which include:           <ul style="list-style-type: none"> <li>Arguments passed to the function</li> <li>A special arguments object</li> <li>Local variables</li> </ul> </li> </ul>
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<p><b>apply, bind, call Example</b></p> <pre>x = 3; function foo(y) {   console.log(this.x + y); } foo(100); // Prints "103"  // Array passed for args foo.apply(null, [100]); // Update the context foo.apply({x:4}, [100]);  // No array needed foo.call({x:4}, 100);  // Create a new function var bf = foo.bind({x:5}); bf(100);</pre>	<ul style="list-style-type: none"> <li><b>apply</b> – Calls a function with the arguments passed as an array.</li> <li><b>call</b> – Calls a function with the arguments passed in comma separated.</li> <li><b>bind</b> – Used to create a new function with a custom context.</li> </ul>	
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## Lecture #14.5 – JSLint and TypeScript

<b>Issues in JavaScript</b> <ul style="list-style-type: none"> <li>• No block scope</li> <li>• Forgetting <b>var</b> can lead to unexpected behavior since variables become global.</li> <li>• Operator <b>"=="</b> is not transitive.</li> <li>• Switch/case statements require <b>"break"</b></li> </ul>	<b>JavaScript Automatically Inserts Semicolons</b> <pre>function makeObject () {   return // Semicolon inserted here   {     madeBy: 'Austin Tech. Sys.'   } } var o = makeObject(); console.log(o.madeBy); // error</pre>	<b>Function <b>"parseInt"</b> can Yield Unexpected Results</b> <pre>// Drops the " tons" console.log("what do you get? "   + parseInt("16 tons"));  // Prints just "1" due to the "Oh" parseInt("101");</pre>
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<b>Behavior of <b>"typeof"</b></b> <p><b>typeof</b> – Returns a string. May yield unexpected results.</p> <pre>typeof 5 // "number" typeof "hi" // "string"  typeof NaN // "number" typeof null // "object"</pre>	<b>Behavior of <b>"typeofChar"</b></b> <p><b>typeChar</b> – Returns a string. Classifies letters as <b>"digits"</b>.</p> <pre>typeofChar "5" // "digit" typeofChar "q" // "digit" // "Other character" typeofChar " "</pre>	<b>JSLint</b> <ul style="list-style-type: none"> <li>• A tool to write cleaner and safer JavaScript.</li> <li>• Requires that <b>"use strict"</b> (with quotes) be added at the beginning of all functions.</li> <li>• Performs static code analysis.</li> <li>• Helps catch common programming errors by requiring:             <ul style="list-style-type: none"> <li>○ Variables declared before they are used.</li> <li>○ Semicolons are always used.</li> <li>○ Double equals never used.</li> </ul> </li> <li>• Inspired by the <b>"lint"</b> tool</li> </ul>
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<b>Benefits of Type Systems</b> <ul style="list-style-type: none"> <li>• Tips for compilers</li> <li>• Hints for IDEs</li> <li>• Enforced documentation</li> <li>• Prevent code with errors from running.</li> </ul>	<b>TypeScript</b> <ul style="list-style-type: none"> <li>• Developed by Microsoft</li> <li>• <b>Static type checker</b> for JavaScript.</li> <li>• A new "superset" language of JavaScript with:             <ul style="list-style-type: none"> <li>○ Type annotations</li> <li>○ Classes</li> </ul> </li> <li>• <b>Compiles to JavaScript</b></li> </ul>	<b>Function Type Annotations in TypeScript</b> <pre>function greet(person: string) {   console.log("Hello " +     person); } var user : string = "Vlad";  // Prints "Hello Vlad" greet(user);</pre>	<b>Types in TypeScript</b> <ul style="list-style-type: none"> <li>• <b>number</b> (<b>var</b> pi : <b>number</b> = 3.14)</li> <li>• <b>boolean</b> (<b>var</b> b : <b>boolean</b> = true)</li> <li>• <b>string</b> (<b>var</b> greet : <b>string</b> = "hi")</li> <li>• <b>array</b> (<b>var</b> lst : <b>number</b>[] = [1, 2])</li> <li>• <b>enum</b></li> <li>• <b>any</b> (<b>var</b> a : <b>any</b> = 3; <b>var</b> b : <b>any</b> = "hi")</li> <li>• <b>void</b></li> </ul>
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<b>TypeScript Class</b> <pre>class Employee{   name : string;   salary : number;    constructor(name : string, salary : number){     this.name = name;     this.salary = salary;   }   display(){ console.log(this.name); } }  var emp = new Employee('Jon', 50000); emp.display();</pre>	
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## Lecture #15 – Event-Based Programming and Cryptocurrencies

<p><b>JavaScript Embedded in HTML</b></p> <p>Create a button on a website that prints "Hello" when clicked. <b>Inline event handlers are considered bad practice.</b></p> <pre>&lt;html&gt; &lt;input   type='button'   onclick='alert("Hello");'   value='Say hi' /&gt; &lt;/html&gt;</pre>	<p><b>Improved JavaScript in HTML</b></p> <p><b>Give buttons an "id" and update its "onclick" method</b></p> <pre>&lt;html&gt; &lt;input id='thebutton'   type='button'   value='Say hi' /&gt;  &lt;script type="text/javascript"&gt;   var btn = document.     getElementById('thebutton');   btn.onclick = function() {     alert('Groovy');   }; &lt;/script&gt; &lt;/html&gt;</pre>	<p><b>Adding an Event Listener</b></p> <ul style="list-style-type: none"> <li>If clicking a button should perform multiple functions, then an event listener should be used.</li> </ul> <pre>function sayGroovy(){   console.log("Groovy"); }  // Add an "onclick" event listener btn.addEventListener('click',   sayGroovy);  // Add another event listener btn.addEventListener('click',   function(){     console.log("Bogus");   });</pre>
<p><b>Removing an Event Listener</b></p> <ul style="list-style-type: none"> <li>Event listeners can be <b>removed by function name</b>.</li> </ul> <p><b>Example:</b></p> <pre>btn.removeEventListener('click',   sayGroovy);</pre>	<p><b>Event Emitter</b></p> <ul style="list-style-type: none"> <li>Import the "events" module using the syntax</li> </ul> <pre>var ee =   require('events').EventEmitter;</pre> <ul style="list-style-type: none"> <li>Used to create event via the keyword "on".</li> </ul> <p><b>Example:</b></p> <pre>ee.on('die', function(){   console.log("Died"); });</pre> <ul style="list-style-type: none"> <li>Invoking (emitting) an event using the keyword "emit" <b>Example:</b></li> </ul> <pre>setTimeout( function() {   ee.emit('die'); }, 100); // in ms</pre>	<p><b>Create a TCP Server in Node.js Using Event Listeners</b></p> <pre>var net = require('net'); var eol = require('os').EOL; var srvr = net.createServer();  // Add an event listener srvr.on('connection', function(client) {   client.write('Hello there!' + eol);   client.end(); });  telnet – Used to connect to a TCP server on the command line.  127.0.0.1 – IP address of localhost</pre>
<p><b>Events in JavaScript</b></p> <ul style="list-style-type: none"> <li><b>JavaScript is single threaded.</b></li> </ul> <p>An event must be run to completion before the next event handler can run.</p>		

## Cryptocurrencies

<p><b>Rep</b></p> <p>Create a button on a website that prints "Hello" when clicked. <b>Inline event handlers are considered bad practice.</b></p> <pre>&lt;html&gt; &lt;input   type='button'   onclick='alert("Hello");'   value='Say hi' /&gt; &lt;/html&gt;</pre>	<p><b>Improved JavaScript in HTML</b></p> <p><b>Give buttons an "id" and update its "onclick" method</b></p> <pre>&lt;html&gt; &lt;input id='thebutton'   type='button'   value='Say hi' /&gt;  &lt;script type="text/javascript"&gt;   var btn = document.     getElementById('thebutton');   btn.onclick = function() {     alert('Groovy');   }; &lt;/script&gt; &lt;/html&gt;</pre>	<p><b>Adding an Event Listener</b></p> <ul style="list-style-type: none"> <li>If clicking a button should perform multiple functions, then an event listener should be used.</li> </ul> <pre>function sayGroovy(){   console.log("Groovy"); }  // Add an "onclick" event listener btn.addEventListener('click',   sayGroovy);  // Add another event listener btn.addEventListener('click',   function(){     console.log("Bogus");   });</pre>
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```
emp.display();
var net = require('net');
var eol = require('os').EOL;
var srvr = net.createServer();
srvr.on('connection', function(client) {
  client.write('Hello there!' + eol);
  client.end();
});
```

```
function makeAdder(x) {
  return function(y) {
    return x + y;
  };
}
```

```

var addOne = makeAdder(1);
// Prints "3"
console.log(addOne(2));

function Cat(name, breed){
  var this = {}; // Done when new keyword is used
  this.prototype = Cat.prototype; // Also comes from new
  this.name = name;
  this.breed = breed;
  this.speak = function(){console.log("meow");};
  return this; // Also comes from new
}

//Lambda Function
var myLambda = function(x){ return x * x; }

```