

CS256 – Midterm Exam Study Guide

By: Zayd Hammoudeh

Chapter #04 – Classification: Basic Concepts, Decision Trees, and Model Evaluation

Classification Task of assigning objects to one of several predefined categories.	Training Set A collection of records. Each record contains a set of attributes one of which is the class .	Model A function from the value of record attributes to the class attribute.	Test Set A collection of records used to determine the accuracy of the classification model.	Example Classification Techniques <ol style="list-style-type: none"> 1. Neural Networks 2. Decision Tree 3. Rule Based Classifier 4. Memory Based Reasoning 5. Support Vector Machines 6. Naïve Bayes and Bayesian Belief Networks
---	--	--	--	---

Induction Using a training set to generate a model. Deduction Process of applying a model to a training set. Decision Tree Induction <ul style="list-style-type: none"> • Greedy Strategy • Key Decision #1: Attribute to expand next • Key Decision #2: When to stop expanding 	Hunt's Decision Tree Induction Algorithm: <ul style="list-style-type: none"> • Let D_t be the set of training records that reach a node t. <ol style="list-style-type: none"> 1. If D_t contains records that all belong to the same class y_t, then t is a leaf node with class value y_t. 2. If D_t is an empty set, then t is a leaf node with default value y_d. 3. If D_t contains records that belong to more than one class and there are no attributes left, then t is a leaf node with default value y_d. 4. If D_t contains records that belong to more than one class, then use an attribute test to split the data into smaller subsets. Recursively apply the same procedure above. 	Attribute Types <ul style="list-style-type: none"> • Binary – Attribute with exactly two possible values. • Nominal – Two or more class values with no intrinsic Order • Ordinal – Two or more class values that can be ordered or ranked • Continuous – Quantitative attribute that can be measured along a continuum.
--	--	--

Splitting Nominal and Ordinal Attributes <ul style="list-style-type: none"> • Binary – Divides attribute values into two subsets. This requires the additional step of finding optimal partitioning. • Multi-way – Use as many partitions as distinct values. 	Splitting Based on Continuous Attributes <ul style="list-style-type: none"> • Discretization – Form an ordinal categorical attribute. <ul style="list-style-type: none"> ◦ Static – Discretize once at the beginning ◦ Dynamic – Ranges can be found by equal interval bucketing, equal frequency bucketing, or clustering. • Binary Decision ($A < v$ or $A > v$) – Consider all possible splits and find the best cut. <ul style="list-style-type: none"> ◦ Binary Decision Procedure: Go between each training set record value and calculate the GINI index if the splitting point was at that value. Select the splitting point with the lowest $GINI_{SPLIT}$ value. <ul style="list-style-type: none"> ▪ Computationally inefficient $O(n)$ – where n is the number of records. 	Homogeneity/Low Impurity – Extent to which nodes in the decision tree have the same class value/distribution. Nodes with high levels of homogeneity (i.e. low levels of impurity) are preferred.
---	--	---

Impurity Measures

For all of these metrics, a lower score is generally preferable.

GINI Index $GINI(t) = 1 - \sum_{j=1}^{n_c} (p(j t))^2$ <ul style="list-style-type: none"> • t – Node in the decision tree • j – Class value • n_c – Number of class values • $p(j t)$ – Probability (i.e. relative frequency) of class value j in node t Minimum Value: 0 when: $\exists j(p(j t) = 1)$ Maximum Value: $1 - \frac{1}{n_c}$ when: $\forall j \left(p(j t) = \frac{1}{n_c} \right)$	$GINI_{SPLIT}$ $GINI_{SPLIT} = \sum_{i=1}^k \frac{n_i}{n} \cdot GINI(i)$ <ul style="list-style-type: none"> • i – Child node • n – Number of records in parent node. Note: $n = \sum_{i=1}^k n_i$ • n_i – Number of child nodes (i.e. attribute partitions) • $GINI(i)$ – GINI index value of node i. Minimum Value: 0 when: $\forall i(GINI(i) = 0)$ Maximum Value: $1 - \frac{1}{n_c}$ when: $\forall i \left(GINI(i) = 1 - \frac{1}{n_c} \right)$	Entropy $Entropy(t) = - \sum_{j=1}^{n_c} p(j t) \cdot \log_2(p(j t))$ <ul style="list-style-type: none"> • t – Node in the decision tree • j – Class value • n_c – Number of class values • $p(j t)$ – Probability (i.e. relative frequency) of class value j in node t Minimum Value: 0 when: $\exists j(p(j t) = 1)$ Maximum Value: $\log_2(n_c)$ when: $\forall j \left(p(j t) = \frac{1}{n_c} \right)$
--	---	---

Information Gain		Classification Error
$GAIN_{SPLIT}(t) = Entropy(p) - \left(\sum_{i=1}^k \frac{n_i}{n} \cdot Entropy(i) \right)$ <ul style="list-style-type: none"> p – Parent node in the decision tree i – Child node in the decision tree k – Number of child nodes n_i – Number of records in child node i n – Number of records in parent node p $n = \sum_{i=1}^k n_i$ <p>Key Note: A higher $GAIN_{SPLIT}$ is preferable unlike with the other metrics where a lower value was better.</p> <p>Disadvantage of Information Gain: Tends to prefer splits that result in a large number of partitions, each being small but pure (i.e. overfitting)</p>	<p>Normalizing for Split Size</p> $GainRATIO_{Split} = \frac{Gain_{SPLIT}(t)}{SplitINFO}$ $SplitINFO = - \sum_{i=1}^k \frac{n_i}{n} \cdot \log_2 \left(\frac{n_i}{n} \right)$ <p>SplitINFO penalizes a large split by reducing the gain.</p>	$Error(t) = 1 - \max_j(p(j t))$ <ul style="list-style-type: none"> t – Node in the decision tree j – Class value $p(j t)$ – Probability (i.e. relative frequency) of class value j in node t <p>Minimum Value: 0 when: $\exists j(p(j t) = 1)$</p> <p>Maximum Value: $1 - \frac{1}{n_c}$ when: $\forall j \left(p(j t) = \frac{1}{n_c} \right)$</p>

Stopping Criteria for Decision Tree Induction

<p>Three Stopping Criteria for Decision Tree Induction</p> <ul style="list-style-type: none"> When all records in a node have the same class value When all records in a node have similar attribute values. Early Termination 	<p>Underfitting – When a model is too simple, both training and test errors are large.</p>	<p>Overfitting – When a model becomes too complex (e.g. too large a tree), the test error begins to increase even though the training error decreases.</p> <ul style="list-style-type: none"> Result: Training error is NOT representative for generalization error. 	<p>Causes of Overfitting</p> <ul style="list-style-type: none"> Noise Insufficient training records (i.e. lack of representative samples)
--	---	--	--

Generalization Error Estimation		
<p>Resubstitution Error Error on the training set.</p> <p>Single Leaf Node Error: $e(t)$ Total Resubstitution Error: $e(T)$</p> $e(T) = \sum e(t)$	<p>Generalization Error Error on the testing data.</p> <p>Single Leaf Node Error: $e'(t)$ Total Generalization Error: $e'(T)$</p> $e'(T) = \sum e'(t)$	<p>Optimistic Estimation Training error is equal to the testing error. $\sum e(t) = \sum e'(t)$</p> <p>Pessimistic Estimation Assign a penalty term to ea. $e'(t) = e(t) + 0.5$</p> <p>Total Pessimistic Error $e'(T) = \sum(e(t)) + N \cdot 0.5$</p> <p>$N$ – Number of leaf nodes.</p> <p>Reduced Error Pruning Use a validation set to estimate the generalization error.</p>

<p>Occam's Razor</p> <p>Given two models with similar generalization errors, one should prefer the simpler model over the more complex model.</p> <p>This is because more complex model has a greater chance of fitting accidentally by errors in the data.</p>	<p>Pre-pruning (Early Stopping Rule)</p> <ul style="list-style-type: none"> Stop the induction algorithm before it becomes a full tree. Typical Stopping Rules: <ul style="list-style-type: none"> All remaining records have the same class value All attribute values are the same. More restrictive conditions: <ul style="list-style-type: none"> Number of instances is below a user-specified threshold. Expanding the current node does not improve impurity measures (e.g. GINI Index, Information Gain) Class distribution of instances are independent of available features. 	<p>Post-pruning (Early Stopping Rule)</p> <ul style="list-style-type: none"> Grow the decision tree to its entirety. Trim nodes in the tree in a bottom-up fashion. Only trim nodes if by trimming the estimate of the generalization error improves. New leaf node's class label is determined from the majority class of instances in the merged node.
---	--	--

Example of Post-Pruning	Examples of Post-pruning
<p>Training Error (Before splitting) = 10/30 Pessimistic error = $(10 + 0.5)/30 = 10.5/30$ Training Error (After splitting) = 9/30 Pessimistic error (After splitting) = $(9 + 4 \times 0.5)/30 = 11/30$ PRUNE!</p> <p>Class = Yes 20 Class = No 10 Error = 10/30</p> <p>A?</p> <p>A1 A2 A3 A4</p> <p>Class = Yes 8 Class = Yes 3 Class = Yes 4 Class = Yes 5 Class = No 4 Class = No 4 Class = No 1 Class = No 1</p>	<p>– Optimistic error? Don't prune for both cases</p> <p>– Pessimistic error? Don't prune case 1, prune case 2</p> <p>– Reduced error pruning? Depends on validation set</p> <p>Case 1:</p> <p>C0: 11 C0: 2 C1: 3 C1: 4</p> <p>Case 2:</p> <p>C0: 14 C0: 2 C1: 3 C1: 2</p>

Handling Missing Attribute Values

Issues Associated with Missing Attribute Values

- Affects how impurity measures are computed
- Affects how to distribute instances with missing value to child nodes.
- Affects how to test instance with missing value is classified.

Computing Impurity Measure

- Calculate entropies (i.e. information gain) with element with missing value **EXCLUDED**.
- Multiply by scalar of elements included over total number of elements (in below example 9 elements included over 10 total elements hence 0.9):

Computing Impurity Measure

Tid	Refund	Marital Status	Taxable Income	Class
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	?	Single	90K	Yes

Missing value

Before Splitting:
Entropy(Parent)
= $-0.3 \log(0.3) - (0.7) \log(0.7) = 0.8813$

	Class = Yes	Class = No
Refund=Yes	0	3
Refund=No	2	4
Refund=?	1	0

Split on Refund:

Entropy(Refund=Yes) = 0

Entropy(Refund=No)
= $-(2/6) \log(2/6) - (4/6) \log(4/6) = 0.9183$

Entropy(Children)
= $0.3(0) + 0.6(0.9183) = 0.551$

Gain = $0.9 \times (0.8813 - 0.551) = 0.3303$

Distribute Instances

- Split the missing record between the two child nodes
- Percentage of child node that goes to each child is portion to the relative frequency of that attribute value.

Distribute Instances

Tid	Refund	Marital Status	Taxable Income	Class
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No

Refund	
Yes	No
Class=Yes 0	Cheat=Yes 2
Class=No 3	Cheat=No 4

Tid	Refund	Marital Status	Taxable Income	Class
10	?	Single	90K	Yes

Refund	
Yes	No
Class=Yes 0 + 3/9	Class=Yes 2 + 6/9
Class=No 3	Class=No 4

Probability that Refund=Yes is 3/9

Probability that Refund=No is 6/9

Assign record to the left child with weight = 3/9 and to the right child with weight = 6/9

Classifying New/Unseen Records with Missing Data

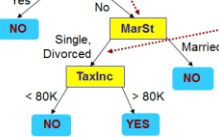
- Pick the most likely of child nodes and use continue down that portion of the tree.

Classify Instances

New record:

Tid	Refund	Marital Status	Taxable Income	Class
11	No	?	85K	?

	Married	Single	Divorced	Total
Class=No	3	1	0	4
Class=Yes	6/9	1	1	2.67
Total	3.67	2	1	6.67



Probability that Marital Status = Married is 3.67/6.67

Probability that Marital Status = (Single, Divorced) is 3/6.67

Data Fragmentation – At each level of the tree, the number of instances gets smaller. At leaf nodes, the number of instances could be too small to be statistically significant.

Tree Induction: NP Hard

Alternate Strategies

- Bottom Up Tree Generation
- Bidirectional Tree Generation
 - Inside-out Bidirectional
 - Outside-in Bidirectional

Decision Boundary – Borderline between two neighboring regions of different classes. In non-oblique decision trees, this is parallel to access since it involves a single attribute at a time.

Oblique Decision Tree – Test condition in a node may involve multiple attributes.

- Advantage** – Most expressive decision tree
- Disadvantage** – Finding optimal test condition is computationally expensive.

Expressiveness – Decision trees do not generalize well to certain types of functions including a parity function which would require a complete tree.

Tree Replication – In a decision tree, a subtree may appear in multiple branches. This leads to unnecessary memory usage.

Performance Evaluation

- Focus on the predictive capability of a model.

Confusion Matrix

	Predicted Class		
Actual Class		Class = Yes	Class=No
	Class = Yes	a	b
	Class=No	c	d

- a – True Positive (TP)
- b – False Negative (FN)
- c – False Positive (FP)
- d – True Negative (TN)

Accuracy

$$Accuracy = \frac{A + D}{A + B + C + D}$$

$$Accuracy = \frac{TP + TN}{TP + FN + FP + TN}$$

- Accuracy only tells part of the story.
 - Example: Two Class Problem
 - Number of Class 0 Examples: 9990
 - Number of Class 1 Examples: 10
 - If the model predicts everything as class 0, its accuracy is 99.9% but it cannot detect any class 1.

Cost Matrix

	Predicted Class		
Actual Class		Class = Yes	Class=No
	Class = Yes	$C(Y Y)$	$C(N Y)$
	Class=No	$C(Y N)$	$C(N N)$

- $C(j|k)$ – Cost of predicting class “j” given the actual class is “k”.

$$TotalCost = a \cdot C(Y|Y) + b \cdot C(N|Y) + c \cdot C(Y|N) + d \cdot C(N|N)$$

- Cost matrix can be a better performance evaluation as it accounts for different costs of depending on the type of error.

$$Precision(p) = \frac{a}{a + c}$$

- Precision** – Accuracy of positive predictions. Biased towards $C(Y|Y)$ & $C(Y|N)$.
 - a – True positive.
 - c – False positive.

$$Recall(r) = \frac{a}{a + b}$$

- Precision** – Accuracy of records with positive class value. Biased towards $C(Y|Y)$ & $C(N|Y)$.
 - a – True positive.
 - b – False negative.

$$F_Measure(F) = \frac{2 \cdot r \cdot p}{r + p} = \frac{a + c}{2 \cdot a + b + c}$$

- F-Measure** – Biased two all except $C(N|N)$ (i.e. true negative)
 - r – Recall
 - p – Precision
 - c – False Positive

$WA = \frac{w_1 \cdot a + w_4 \cdot d}{w_1 \cdot a + w_2 \cdot b + w_3 \cdot c + w_4 \cdot d}$ <p> n – Number of instances covered by rule n_c – Number of positive instances covered by rule. </p>	<p>Proportionality of Cost and Accuracy</p> <ul style="list-style-type: none"> Cost and accuracy are proportional if: $\mathcal{C}(Y Y) = \mathcal{C}(N N) \text{ and } \mathcal{C}(Y N) = \mathcal{C}(N Y)$	<p>Sample Size and Model Performance</p> <ul style="list-style-type: none"> Learning Curve – Shows how model accuracy changes (and varies) with sample size. Effects of Small Sample Size: <ul style="list-style-type: none"> Bias in the estimate Variance in the estimate.
--	--	--

Methods for Model Comparison

<p>Holdout – Reserve 2/3 of labelled examples for training and 1/3 for testing.</p> <p>Disadvantages</p> <ul style="list-style-type: none"> Uses on a subset of the labelled examples when training the model. Model dependent on the composition of the training and test sets. Training and test sets are not independent since come from same original set. If one class value is over- or under-represented in either set, it will skew the results. 	<p>Random Subsampling – Repeats the whole out method multiple times with replacement.</p> <p>Disadvantages:</p> <ul style="list-style-type: none"> Still uses only a subset of the labelled examples to build the model. No control of how many times each record appears in the training and test sets. If a particular record is always in the training set, it may skew the model. <p>Accuracy of k Random Subsamplings</p> $acc_{sub} = \frac{1}{k} \cdot \sum_{i=1}^k acc_i$ <ul style="list-style-type: none"> k – Number of iterations acc_i – Accuracy of the i^{th} iteration. 	<p>Cross Validation – Partition the labelled dataset into k disjoint subsets.</p> <ul style="list-style-type: none"> k-Fold – Train on $k-1$ partitions and test on the remaining one. Leave-One-Out – The number of partitions equals the number of training samples. <p>Accuracy of k-Fold Cross Validation</p> $acc_{sub} = \frac{1}{k} \cdot \sum_{i=1}^k acc_i$ <ul style="list-style-type: none"> k – Number of iterations acc_i – Accuracy of the i^{th} iteration. <p>Disadvantages:</p> <ul style="list-style-type: none"> Computationally expensive as process is repeated k times. Depending on size of partition (e.g. 1 for Leave-One-Out), accuracy from iteration to iteration can vary significantly.
<p>Bootstrap –</p>		

Minimum Description Length	
----------------------------	--

Chapter #05 – Additional Classification Techniques

Rule-Based Classifiers

<p>Classifies records using a collection of “if...then...” rules.</p> <p>Form of Rule:</p> <p>$(Condition) \rightarrow y$</p> <ul style="list-style-type: none"> Condition (Antecedent, LHS) – Conjunction of attributes. y (Consequent, RHS) – Class value. 	<p>Cover – A rule r covers an instance x if the attributes of x satisfy the condition (LHS) of the rule.</p> <p>Coverage of a Rule – Fraction of records that satisfy the antecedent of a rule.</p> <p>Accuracy of a Rule – For records covered by a rule, it is the fraction of records that have the matching class value.</p>	<p>Mutually Exclusive Rule Set – Rules in the set are independent of each other such that each record is covered by at most one rule.</p> <p>Exhaustive Rule Set – A set of rules that covers every possible combination of attribute values. Hence, each record is covered by at least one rule.</p>	<p>Decision Tree – Can be used to form a mutually exclusive, exhaustive rule set.</p> <p>Rules in a decision tree can be simplified.</p> <p>Effects of rule simplification:</p> <ul style="list-style-type: none"> Problem #1: Rules become non-mutually exclusive. Solution: <ul style="list-style-type: none"> Ordered Rule Set – Rules ordered from highest to lowest priority. Records classified according to highest priority rule they satisfy. Unordered Rule Set – Voting scheme Problem #2: Rules become non-exhaustive. Solution: Use a default class.
---	--	---	--

<p>Rule Ordering Schemes</p> <p>Rules Based Ordering – Individual rules are ranked based off their quality.</p> <ul style="list-style-type: none"> Advantage: Ensures each record is classified by the “best rule” covering it. Disadvantage: Interpreting lower priority rules becomes more difficult as they are negations of higher priority rules. <p>Class-Based Ordering – Rules that belong to the same class appear together.</p> <ul style="list-style-type: none"> Advantage: Simplifies rule ordering. Disadvantage: May allow a lower quality rule to have higher priority than a higher quality one. 	<p>Direct Method for Rule Building – Extract rules directly from the data.</p> <ul style="list-style-type: none"> Examples: RIPPER, CN2, Holte’s IR <p>Indirect Method for Rule Building – Extract rules from other classification models (e.g. decision tree, neural network, etc.)</p> <ul style="list-style-type: none"> Examples: C4.5rules 	<p>Sequential Covering Algorithm</p> <ol style="list-style-type: none"> Start with an empty rule set. Grow a rule using the “Learn-One-Rule” function. Remove training records covered by the rule. Repeat steps #2 and #3 until stopping criterion is met. <p>Aspects of Sequential Covering</p> <ol style="list-style-type: none"> Rule Growing Instance Elimination Rule Evaluation Stopping Criterion Rule Pruning 	<p>Rule Growing Strategies</p> <ol style="list-style-type: none"> General to Specific <ol style="list-style-type: none"> Example: Ripper Specific to General <p>CN2 Algorithm</p> <ol style="list-style-type: none"> Start from an empty rule Add conjuncts that minimize the entropy measure. Determine the rule consequent by taking majority class of covered instances.
--	---	---	--

<p>Instance Elimination</p> <ul style="list-style-type: none"> Reason for Eliminating Instances – Otherwise next rule is identical to previous rule. Reason for Removing Positive Instances – To ensure future rules are different. Reason for Removing Negative Instances – Prevent underestimating accuracy of the rule. 	<p>Stopping Criterion</p> <p>Compute the information gain with the rule. If the gain is insignificant, discard the rule.</p>	<p>Rule Pruning</p> <ul style="list-style-type: none"> Similar to post-pruning of decision trees. Uses reduced error pruning. <ul style="list-style-type: none"> Remove one of the conjuncts of the rule. Compare error rate on validation set before and after pruning. If error improves, remove the conjunct. 	<p>Rule Simplification – Used to reduce the likelihood of overfitting.</p>
---	---	--	---

Rule Evaluation Metrics

<p>Accuracy = $\frac{n_c}{n}$</p> <p>n – Number of instances covered by rule n_c – Number of positive instances covered by rule.</p>	<p>Laplace = $\frac{n_c + 1}{n + k}$</p> <p>n – Number of instances covered by rule n_c – Number of positive instances covered by rule. k – Number of classes Used to ensure greater coverage for a rule.</p>	<p>m_estimate = $\frac{n_c + p \cdot k}{n + k}$</p> <p>$n$ – Number of instances covered by rule n_c – Number of positive instances covered by rule. k – Number of classes p – Prior probability of positive class.</p>
---	--	--

<p>FOIL Information Gain</p> <p>$Gain(R0, R1) = p_1 \cdot \left(\log_2 \left(\frac{p_1}{p_1 + n_1} \right) + \log_2 \left(\frac{p_0}{p_0 + n_0} \right) \right)$</p> <p>$R0$ – Initial Rule $R1$ – Modified version of $R0$ with added conjunct t – Number of positive instances covered by both $R0$ and $R1$ p_0 – Positive instances covered by $R0$ n_0 – Negative instances covered by $R0$ p_1 – Positive instances covered by $R1$ n_1 – Negative instances covered by $R1$</p>	<p>RIPPER Algorithm</p> <ol style="list-style-type: none"> For two classes, define one class as positive class and other as negative class. <ol style="list-style-type: none"> In two class problem, negative class is the default class. In multi-class problem, create list of classes ordered by increasing prevalence. <ol style="list-style-type: none"> Select smallest as first as positive class and rest are negative class. Learn rules for the smallest class first. Repeat with next smallest class. 	<p>RIPPER Algorithm – Growing a Rule</p> <ol style="list-style-type: none"> Start from an empty rule set. Add conjuncts as long as they improve FOIL Information Gain (i.e. General-to-Specific). Stop adding conjuncts when the rule starts covering negative examples. Begin pruning the rule immediately (i.e. before generating new rules) using Reduced Error Pruning. Delete conjuncts to maximize v as defined by: $v = \frac{p - n}{p + n}$ <p>p – Number of positive instances covered by the rule. n – Number of negative instances covered by the rule.</p>
---	---	--

RIPPER Algorithm – Building the Rule Set	C4.5rules – Indirect Method	
<ol style="list-style-type: none"> 1. Use Sequential Covering <ol style="list-style-type: none"> a. Find the rule that best covers the current set of positive examples. b. Eliminate both positive and negative examples covered by the rule. c. Uses ordered rule set with class based ordering. 2. Each time a rule is added to the rule set, compute the new description length. Example Stopping Conditions: <ol style="list-style-type: none"> a. Stopping growing the rule set if the new rule increases the description length of the rule set by more than d (e.g. 64) bits. b. Stop if the error rate of the rule on the validation set is more than 50%. 	<ol style="list-style-type: none"> 1. Start from an unpruned decision tree. 2. For each rule $r: A \rightarrow y$, <ol style="list-style-type: none"> a. Consider an alternative rule $r': A' \rightarrow y$ where A' is obtained by removing one of the conjuncts of A b. Keep the rule with the lowest pessimistic error rate (assuming it is less than the original). c. Repeat until it is no longer possible to improve the generalization error. 	<ol style="list-style-type: none"> 3. Use class-based ordering for the rule set (i.e. group by the rule consequent). 4. Compute the description length of each class and order the rules by increasing description length. <p>DescriptionLength = $L(\text{error}) + g \cdot L(\text{model})$</p> <ul style="list-style-type: none"> • $L(\text{error})$ – Number of bits required to encode misclassified examples. • $L(\text{model})$ – Number of bits required to encode the model. • g – Tuning parameter whose default is 0.5 and takes into account the presence of redundant attributes in the rule set.

Nearest Neighbor Classifiers

<p>Instance-Based Classifier – Stores all training records and uses the training records directly to predict the class label of unseen records.</p> <p>Rote-Learner – Memorizes the entire training set and performs classification only if attributes of a record match one the training examples exactly.</p> <p>Nearest Neighbor – Uses k “closest” training records (i.e. nearest neighbors) for performing classification.</p>	<p>Nearest Neighbor Classifier Requirements</p> <ol style="list-style-type: none"> 1. Set of stored labelled records. 2. Distance metric to compute distance between records. 3. Value of k, the number of nearest neighbors to retrieve. 	<p>Classifying an Unseen Record</p> <ol style="list-style-type: none"> 1. Compute the distance to all other training records. 2. Identify the k nearest neighbors. 3. Use class labels of nearest neighbors to determine the class label of unknown records
---	---	--

<p>Voronoi Diagram – Used to depict the decision boundaries for a Nearest Neighbor classifier.</p> <p>Euclidean Distance</p> $d(p, q) = \sqrt{\sum_i (p_i - q_i)^2}$ <p>Manhattan Distance</p> $d(p, q) = \sum_i p_i - q_i $	<p>Determining the Class from the Nearest Neighbor List</p> <p>Option #1 – Take the majority vote among the k-Nearest Neighbors.</p> <p>Option #2 – Weight the vote according to the distance using the weight factor:</p> $\text{WeightFactor} = \frac{1}{d^2}$	<p>Effect of the Value of k</p> <ul style="list-style-type: none"> • k is too Small – Underfitting and the classifier becomes sensitive to noise points. • k is too Large – Overfitting and the neighborhood make include points from other classes. 	<p>Attribute Value Scaling Issues</p> <ul style="list-style-type: none"> • Attributes may have to be scaled to normalize for different attribute ranges and values. • This is done to prevent one of the attributes dominating the distance measure.
--	--	--	---

PEBLs

<p>PEBLs</p> <ul style="list-style-type: none"> • Nearest neighbor algorithm that works with both continuous and nominal features. • Each record is assigned a weight factor. • Number of nearest neighbors, $k = 1$ <p>Weighted Euclidean Distance</p> $d(p, q) = \sqrt{\sum_i w_i \cdot (p_i - q_i)^2}$ <p>w_i – Weight of parameter i</p>	<p>Distance Between Nominal Attributes Value Difference Metric</p> $d(v_1, v_2) = \sum_i \left \frac{n_{1,i}}{n_1} - \frac{n_{2,i}}{n_2} \right $ <p> v_1 – Attribute value 1 v_2 – Attribute value 2 i – The i^{th} class value. $n_{1,i}$ – Number of records with attribute value 1 and class value i $n_{2,i}$ – Number of records with attribute value 2 and class value i n_1 – Total number of records with attribute value 1 n_2 – Total number of records with attribute value 2 </p>	<p>Similarity Function Used in PEBLS</p> $d(X, Y) = w_X \cdot w_Y \sum_{i=1}^k d(X_i, Y_i)^2$ <p> X & Y – Two records w_X – Distance weighting factor for record X w_Y – Distance weighting factor for record Y. If Y is an unseen record, then $w_Y = 1$ $d(X_i, Y_i)$ – Distance between records X and Y in the i^{th} dimension. </p> <p>$w_X = \frac{\text{Number of Times } X \text{ is Used in Prediction}}{\text{Number of Times } X \text{ Predicts Correctly}}$</p> <p>If $w_X \cong 1$, then X makes an accurate prediction most of the time. If $w_X > 1$, then X does not make reliable predictions.</p>
--	--	---

Bayesian Classifiers

<p>Condition Probability Review</p> <p>$P(C A)$ – Probability of C given A.</p> $P(C A) = \frac{P(C \cap A)}{P(A)}$ $P(A C) = \frac{P(C \cap A)}{P(C)}$	<p>Bayes Theorem</p> $P(A C) = \frac{P(C A) \cdot P(A)}{P(C)}$ <p>Bayes Classifier – A probabilistic framework for solving classification problems.</p>	<p>Bayes Theorem Example</p> $P(SN M) = 0.5$ $P(M) = \frac{1}{50000}$ $P(SN) = \frac{1}{20}$ <p>Hence:</p> $P(M SN) = \frac{P(SN M) \cdot P(M)}{P(SN)} = \frac{0.5 \cdot \frac{1}{50000}}{\frac{1}{20}}$ $P(M SN) = 0.0002$	<p>Requirement of Naïve Bayesian Classifiers</p> <ul style="list-style-type: none">Consider each attribute (A_1, A_2, \dots, A_n) as independent random variables.Consider the class (C) label as a random variable. <p>Goal is to find:</p> $P(C A_1, A_2, \dots, A_n)$
<p>Multi-Attribute Bayes Theorem</p> $P(C A_1, A_2, \dots, A_n) = \frac{P(C A_1, A_2, \dots, A_n) \cdot P(C)}{P(A_1, A_2, \dots, A_n)}$ <p>Classification Approach: Select the value of C that maximizes the above equation.</p>	<p>Naïve Bayesian Simplification</p> $P(C A_1, A_2, \dots, A_n) = P(C A_1) \cdot P(C A_2) \cdot \dots \cdot P(C A_n)$ <p>This equations assumes independence among each A_i attribute when the class is given.</p>	<p>Estimating Class Probability</p> $P(C) = \frac{N_C}{N}$ <p>C – Class value N_C – Number of training records with class value C N – Total number of training records.</p>	

	ROC Curve	
	<ul style="list-style-type: none"> Used to illustrate the performance of a binary classifier. Two Dimensional <ul style="list-style-type: none"> X-Axis – False Positive Rate Y-Axis – True Positive Rate 	

Miscellaneous

Decision Tree Algorithm

Advantages

- Inexpensive to construct
- Extremely fast at classifying unknown records.
- Easy to interpret for small sized trees.
- Accuracy is comparable to other classification techniques for many simple datasets. (Since everything comes right from the data)

Disadvantages

- May not generalize well for certain types of functions (e.g. Parity function requires a complete tree)
- May be insufficient for modelling continuous variables that do not allow oblique nodes.

Rule Based Classifiers

Advantages

- As highly expressive as decision trees
 - A decision tree can be expressed via rules based classifier).
 - Allows for more complex models than a decision tree by allowing multiple rules to trigger on a single rule.
- Easy to interpret.
- Easy to generate.
- Can classify new records quickly.
- Performance comparable to decision trees
- Well suited for handling data sets with imbalanced class distributions.

Rule Based Classifiers

Advantages

- **Lazy Learner** – Does not require the building of a complex model.
- Can create complex decision boundaries unlike rule-based and decision trees which generally create rectilinear boundaries.

Disadvantages

- Each unseen records are computationally expensive (since must be compared to all training records).
- Susceptible to wrong prediction without appropriate proximity measure and preprocessing is done.
- Uses local data to make classification decisions so potentially susceptible to noise.