## **CS256 – Midterm Exam Study Guide**

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# Chapter #04 - Classification: Basic Concepts, Decision Trees, and Model Evaluation

#### Classification

Task of assigning objects to one of several predefined categories.

### **Training Set**

A collection of records. Each **record** contains a set of attributes one of which is the **class**.

#### Model

A function from the value of record attributes to the class attribute.

#### **Test Set**

A collection of records used to determine the accuracy of the classification model.

#### **Example Classification Techniques**

- 1. Neural Networks
- 2. Decision Tree
- 3. Rule Based Classifier
- 4. Memory Based Reasoning
- 5. Support Vector Machines
- 6. Naïve Bayes and Bayesian Belief Networks

#### Induction

Using a training set to generate a model.

### Deduction

Process of applying a model to a training set.

#### **Decision Tree Induction**

- Greedy Strategy
- Key Decision #1: Attribute to expand next
- Key Decision #2: When to stop expanding

#### **Hunt's Decision Tree Induction Algorithm:**

- Let  $D_t$  be the set of training records that reach a node t.
- If D<sub>t</sub> contains records that all belong to the same class y<sub>t</sub>, then t is a leaf node with class value y<sub>t</sub>.
- 2. If  $D_t$  is an **empty set**, then t is a leaf node with default value  $V_{dt}$ .
- If D<sub>t</sub> contains records that belong to more than one class and there are no attributes left, then t is a leaf node with default value is a leaf node with default value y<sub>d</sub>.
- 4. If  $D_t$  contains records that belong to more than one class, then use an attribute test to split the data into smaller subsets. Recursively apply the same procedure above.

### **Attribute Types**

- Binary Attribute with exactly two possible values.
- Nominal Two or more class values with no intrinsic Order
- Ordinal Two or more class values that can be ordered or ranked
- Continuous Quantitative attribute that can be measured along a continuum.

### Splitting Nominal and Ordinal Attributes

- Binary Divides attribute values into two subsets. This requires the additional step of finding optimal partitioning.
- Multi-way Use as many partitions as distinct values.

### **Splitting Based on Continuous Attributes**

- Discretization Form an ordinal categorical attribute.
  - Static Discretize once at the beginning
  - Dynamic Ranges can be found by equal interval bucketing, equal frequency bucketing, or clustering.
- Binary Decision (A < v or A > v) Consider all possible splits and find the best cut.
  - Binary Decision Procedure: Go between each training set record value and
    calculate the GINI index if the splitting point was at that value. Select the splitting
    point with the lowest GINI<sub>SPUT</sub> value.
    - **Computationally inefficient** O(n) where n is the number of records.

Homogeneity/Low Impurity – Extent to which nodes in the decision tree have the same class value/distribution.

Nodes with high levels of homogeneity (i.e. low levels of impurity) are preferred.

### **Impurity Measures**

For all of these metrics, a lower score is generally preferable.

### **GINI Index**

$$GINI(t) = 1 - \sum_{i=1}^{n_c} (p(j|t))^2$$

- t Node in the decision tree
- *i* Class value
- $n_c$  Number of class values
- p(j|t) Probability (i.e. relative frequency) of class value j in node t

Minimum Value: 0 when:

$$\exists i(p(i|t) = 1)$$

**Maximum Value:**  $1 - \frac{1}{n_c}$  when:

$$\forall j \left( p(j|t) = \frac{1}{n_s} \right)$$

### **GINI<sub>SPLIT</sub>**

$$GINI_{SPLIT} = \sum_{i=1}^{k} \frac{n_i}{n} \cdot GINI(i)$$

- *i* Child node
- *n* Number of records in parent node. Note:

$$n = \sum_{i=1}^k n_i$$

- n<sub>i</sub> Number of child nodes (i.e. attribute partitions)
- **GINI**(i) GINI index value of node i.

Minimum Value: 0 when:

$$\forall i(GINI(i) = 0)$$

**Maximum Value:**  $1 - \frac{1}{n}$  when:

$$\forall i \left( GINI(i) = 1 - \frac{1}{n_c} \right)$$

### **Entropy**

$$Entropy(t) = -\sum_{i=1}^{n_c} p(j|t) \cdot log_2(p(j|t))$$

- *t* Node in the decision tree
- j Class value
- $n_c$  Number of class values
- p(j|t) Probability (i.e. relative frequency) of class value j in node t

Minimum Value: 0 when:

$$\exists j(p(j|t) = 1)$$

Maximum Value:  $log_2(n_c)$  when:

$$\forall j \left( p(j|t) = \frac{1}{n_c} \right)$$

### **Information Gain**

$$GAIN_{SPLIT}(t) = Entropy(p) - \left(\sum_{i=1}^{k} \frac{n_i}{n} \cdot Entropy(i)\right)$$

- p Parent node in the decision tree
- *i* Child node in the decision tree
- **k** Number of child nodes
- $n_i$  Number of records in child node i
- n Number of records in parent node p

$$n = \sum_{i=1}^{k} n_i$$

**Key Note:** A higher *GAIN<sub>SPLIT</sub>* is preferable unlike with the other metrics where a lower value was better.

**Disadvantage of Information Gain:** Tends to prefer splits that result in a large number of partitions, each being small but pure (i.e. overfitting)

### **Normalizing for Split Size**

$$GainRATIO_{Split} = \frac{Gain_{SPLIT}(t)}{SplitINFO}$$

$$SplitINFO = -\sum_{i=1}^{k} \frac{n_i}{n} \cdot log_2\left(\frac{n_i}{n}\right)$$

 $Split_{INFO}$  penalizes a large split by reducing the gain.

### **Classification Error**

$$Error(t) = 1 - max_i(p(j|t))$$

- *t* Node in the decision tree
- j Class value
- p(j|t) Probability (i.e. relative frequency) of class value j in node t

Minimum Value: 0 when:

$$\exists j(p(j|t) = 1)$$

Maximum Value:  $1 - \frac{1}{n_c}$  when:

$$\forall j \left( p(j|t) = \frac{1}{n_c} \right)$$

### **Stopping Criteria for Decision Tree Induction**

**Optimistic Estimation** 

 $\sum e(t) = \sum e'(t)$ 

Training error is equal

to the testing error.

# Three Stopping Criteria for Decision Tree Induction

- When all records in a node have the same class value
- When all records in a node have similar attribute values.
- Early Termination

Underfitting – When a model is too simple, both training and test errors are large.

**Overfitting** – When a model becomes too complex (e.g. too large a tree), the test error begins to increase even though the training error decreases.

 Result: Training error is NOT representative for generalization error.

### **Causes of Overfitting**

- Noise
- Insufficient training records (including non-representative training set)

### **Resubstitution Error**

Error on the training set.

Single Leaf Node Error: e(t)Total Resubstitution Error: e(T)

$$e(T) = \sum e(t)$$

## Generalization Error

Error on the **testing** data.

Single Leaf Node Error: e'(t)Total Generalization Error: e'(T)

$$e'(T) = \sum e'(t)$$

### **Generalization Error Estimation**

# **Pessimistic Estimation**Assign a penalty term to ea.

e'(t) = e(t) + 0.5

Total Pessimistic Error  $e'^{(T)} = \sum (e(t)) + N \cdot 0.5$ 

N – Number of leaf nodes.

### **Reduced Error Pruning**

Use a validation set to estimate the generalization error.

#### Occam's Razor

Given two models with similar generalization errors, one should prefer the simpler model over the more complex model.

This is because more complex model has a greater chance of fitting accidentally by errors in the data.

### Pre-pruning (Early Stopping Rule)

- Stop the induction algorithm before it becomes a full tree.
- Typical Stopping Rules:
  - o All remaining records have the same class value
  - o All attribute values are the same.
- More restrictive conditions:
  - o Number of instances is below a user-specified threshold.
  - Expanding the current node does not improve impurity measures (e.g. GINI Index, Information Gain)
  - Class distribution of instances are independent of available features

#### Post-pruning (Early Stopping Rule)

- Grow the decision tree to its entirety.
- Trim nodes in the tree in a bottom-up fashion.
- Only trim nodes if by trimming the estimate of the generalization error improves.
- New leaf node's class label is determined from the majority class of instances in the merged node.

**Minimum Description Length** 

# Miscellaneous

<b>Decision Tree Algorithm</b>	
Advantages	
Inexpensive to construct	
<ul> <li>Extremely fast at classifying unknown records.</li> </ul>	
Easy to interpret for small sized trees.	
Accuracy is comparable to other classification	
techniques for many simple datasets. (Since	
everything comes right from the data)	