Homework #1.2

3)
$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 4 & 5 & 6 & 7 \\ 6 & 7 & 8 & 9 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & -1 & -2 & -3 \\ 0 & -1 & -2 & -3 \end{bmatrix} R_3^1 = \frac{1}{5}R_2$$

$$\begin{bmatrix} 1234 \\ 0123 \\ 0000 \end{bmatrix} R_2 = -1.R_2$$

$$\begin{array}{ccc} & & & \\ &$$

Pivot Positions Original

Pivot Positions RREF:

Describe the echolon

forms for a 2x2

matix.

Homework 1,2

7)
$$\begin{bmatrix} 1 & 3 & 4 & 7 \\ 3 & 9 & 7 & 6 \end{bmatrix}$$

$$R_{3}^{1} = R_{2} - 3R_{1}$$

$$V$$

$$\begin{bmatrix} 0 & 3 & 4 & 7 \\ 0 & 0 & -5 - 15 \end{bmatrix}$$

$$V$$

$$R_{2}^{1} = -\frac{1}{5} \cdot R_{2}$$

$$\begin{bmatrix} 13 & 47 \\ 00 & 13 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 13 \\ 0 & 1 & 3 \end{bmatrix}$$

$$\begin{bmatrix} 13 & 0 & -5 \\ 0 & 0 & 1 & 3 \end{bmatrix}$$

$$\begin{array}{c} x_3 = 3 \\ x_1 = -5 - 3x_2 \\ x_2 \text{ is free} \end{array}$$

a)
$$\begin{bmatrix} 0 & 1 & -65 \\ 1 & -2 & 7 & -6 \end{bmatrix}$$

R. \Leftrightarrow Ra (interchange)

$$\begin{bmatrix} 1 & -2 & 7 & -6 \\ 0 & 1 & -6 & 5 \end{bmatrix}$$

R. $= R_1 + 2R_2$

$$\begin{bmatrix} 1 & 0 & -5 & 4 \\ 0 & 1 & -6 & 5 \end{bmatrix}$$
 $X_1 = \frac{1}{1} + 5x_3$
 $X_2 = 5 + 6x_3$

$$\begin{bmatrix}
3 & -4 & 20 & 0 \\
-9 & 8 & -4 & 3R \\
-6 & 8 & -4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 \\
-6 & 8 & -4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 8 & -8 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 3R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
3 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6 & 1 & 3 & 4 & 4R
\end{bmatrix}$$

$$\begin{bmatrix}
4 & 0 & 0 & 0 & 0 & 0 & 0 \\
-6$$

$$\begin{bmatrix} 1 & 0 & 0 & -1 & -1a & 1 \\ 0 & 1 & 0 & 0 & -4 & 1 \\ 0 & 0 & 0 & 1 & 9 & 4 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$R' = R, + R_3$$

Homework 1-2

Consistent and unique since each variable has a pivot

Inconsistent since last now has a Contradiction as 0 + 0

$$R_{a}'=R_{2}-2R_{1}$$

a) No Solution 8-4h=0

8-4K=0

if Kx 8, then no solution if h=2

6) Unique Solution

This is the Set of all cases not infinite and not inconsident.

h = 2

1 Infinite Solution

K=8, h=2 since last row becomes allzeon

Homework 1.2

- al) Mark each Selection as & true or false
- a) False The reduced echelon matrix is unique
- A False The row reduction algorithm applies to all matrices not just augmented Ones.
- orresponds to pivot corresponds to pivot columns in the coefficient andaugmental matrix
 - d) True Solvina a system amounts to finding a parametric description of the solution set
 - e) False-This is not enough information to determine if the system is consistent as the row [00050] is not a contradiction.

23)

Yes it is consistent, since with three rows and three pivot columns, there connot be a row in the form:

[0000h]

where h \$0 in the augmented matrix

25)

Ifalinear System has a pivot position in every row, it means there are no rows in the augmented matric that can have a contradiction in the toin

[0 0 0:.0 h]

where h \$0

Column

Hence, there is no room for a pivot in the augmented column.

可以 If a linear system is consistent, then the solution is unique if and only if each column the coefficient matrix is a pivot

aa) An undetermined system always has more variable, than equation. There cannot be more basic variable, than there are quations. As such, there must be at least one free variable. Such a variable may be assigned infinitely many values. It a System is consistent, each different value of a freevariable will produce a different Solution.