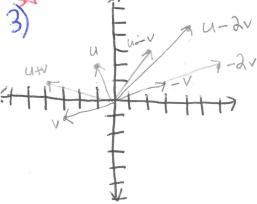
$$U = \begin{bmatrix} -1 \\ 2 \end{bmatrix} \quad V = \begin{bmatrix} -3 \\ -1 \end{bmatrix}$$

$$\vec{u} + \vec{v} = \begin{bmatrix} -4 \\ 1 \end{bmatrix}$$

b) 
$$\vec{u} - d\vec{v} = \begin{bmatrix} -1 - (2 \cdot -3) \\ 3 - (2 \cdot -1) \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$$



$$\vec{U} - \vec{V} = \begin{bmatrix} -1 - (-3) \\ 2 - (-1) \end{bmatrix} = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$\vec{u} - 2\vec{v} = \begin{bmatrix} -1 - 2(-3) \\ 2 - 2(-1) \end{bmatrix} = \begin{bmatrix} 5 \\ 4 \end{bmatrix}$$

$$5) \times_{1} \begin{bmatrix} 6 \\ -1 \\ 5 \end{bmatrix} + \times_{2} \begin{bmatrix} -3 \\ 4 \\ 0 \end{bmatrix} = \begin{bmatrix} 1 \\ -7 \\ -5 \end{bmatrix}$$

## System of equations

$$6x_1 - 3x_2 = 1$$

7)

- a) Itis a combination of USV
- b) It is a combination of ull v 2u-27
- c) Itis a combination of ullv 22 -3.52
- d) It is a combination of ulv 3u-4v

9) 
$$x_2 + 5x_3 = 0$$
  
 $4x_1 + 6x_2 - x_3 = 0$ 

$$\begin{array}{c} x_1 \begin{bmatrix} 0 \\ 4 \\ -1 \end{bmatrix} + x_2 \begin{bmatrix} 1 \\ 6 \\ 3 \end{bmatrix} + x_3 \begin{bmatrix} 5 \\ -1 \\ -8 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \end{array}$$

$$Q_{1} = \begin{bmatrix} 1 \\ -2 \\ 0 \end{bmatrix} \qquad Q_{2} = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix} \qquad Q_{3} = \begin{bmatrix} 5 \\ -6 \\ 8 \end{bmatrix} \qquad b = \begin{bmatrix} 2 \\ -6 \\ 6 \end{bmatrix}$$

Is balinear combination of a, an andon?

$$R_a = R_a + 2R_i$$

$$\begin{bmatrix}
1 & 0 & 5 & 2 \\
0 & 1 & 4 & 3 \\
0 & 2 & 8 & 6
\end{bmatrix}$$

Systemis consistat so bisa linear combination Homework #1-3

$$A = \begin{bmatrix} 1 & -4 & 8 \\ 0 & 3 & 5 \\ -2 & 8 & -4 \end{bmatrix} \quad b = \begin{bmatrix} 3 \\ -7 \\ -3 \end{bmatrix}$$

Is b a linear combination of A?

$$\begin{bmatrix} 1 & -4 & 2 & 3 \\ 0 & 3 & 5 & -7 \\ -2 & 8 - 4 & -3 \end{bmatrix}$$

$$R_{3}^{1} = R_{3} + 2R,$$

$$\begin{bmatrix} 1 & -4 & 2 & 3 \\ 0 & 3 & 5 & -7 \\ 0 & 0 & 0 & 3 \end{bmatrix} \leftarrow Contradiction$$

$$\vec{V}_1 = \begin{bmatrix} 7 \\ 1 \\ -6 \end{bmatrix}$$
  $\vec{V}_2 = \begin{bmatrix} -5 \\ 3 \\ 0 \end{bmatrix}$ 

List five vectors in Span Evi, va and give the Vector weights

$$\begin{array}{c}
0 \\
0 \\
0
\end{array} = 0\vec{v}_1 + 0\vec{v}_2$$

a) 
$$\begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} = 0\vec{v}_1 + 0\vec{v}_2$$
 e)  $\begin{bmatrix} 5 \\ -3 \\ 0 \end{bmatrix} = 0\vec{v}_1 - |\vec{v}_2|$ 

b) 
$$\begin{bmatrix} 7 \\ 1 \\ -6 \end{bmatrix} = |\vec{v_1} + 0\vec{v_2}|$$

$$\begin{vmatrix} -5 \\ 3 \\ 0 \end{vmatrix} = 0 \vec{v}_1 + 1 \vec{v}_2$$

$$\frac{d}{d} \begin{bmatrix} -7 \\ -1 \\ 6 \end{bmatrix} = -1 v_1 + c v_2$$

17) 
$$\alpha_1 = \begin{bmatrix} 1 \\ 4 \\ -2 \end{bmatrix} \quad \alpha_2 = \begin{bmatrix} -2 \\ -3 \\ 7 \end{bmatrix} \quad b = \begin{bmatrix} 4 \\ 1 \\ h \end{bmatrix}$$

Forwhat values of his bin the plane spanned by a, 892?

$$R_a = R_a - 4R_i$$

$$R_0 = \frac{1}{5}R_2$$

If b is in the plane Spanned by a, and az

then

19) \$

$$V_{1} = \begin{bmatrix} 8 \\ 3 \\ -6 \end{bmatrix}, V_{2} = \begin{bmatrix} 12 \\ 3 \\ -9 \end{bmatrix}$$

Give a geometric description of span {v, v2}

Hence, span Eviva3 is the set of all points along the line between the origin and v.

Had và not been a scalar multiple of v, then the Span would have been the plane between the origin, v, and v2.

a) 
$$\vec{u} = \begin{bmatrix} 2 \\ -1 \end{bmatrix}, \vec{v} = \begin{bmatrix} 2 \\ -1 \end{bmatrix}$$
  $\vec{b} = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$ 

$$\begin{bmatrix} 3 & h \\ -1 & -1 \\ R & -1 \end{bmatrix}$$

Novalue of hork can make the augmented matrix inconsistat so all Combinations of hand Kare covered by the Span.

a) False - [-4] is a vector in TR2 while [-4 x3] isa 1x2 matrix, notavectorin R2

- b) False Since the two vectors are not scalar multiples of feach Other the points corresponding to [3] and [3] forma plane, not aline, modale
- C) True A linear combination of V. andus can be written in the form:

C, V, + C2 V2.

Inthis case, c= a and ca=0

- d) True [a, a, a, a, b] is a complimentary representation of the linear system: X, a, + Y2 \( \frac{1}{2} + \text{Y}\_3 \( \arg{a}\_3 = \frac{7}{5} \)
- e) False-The spancantake many shopes including a plane, line, or hyperplane.

 $A = \begin{bmatrix} 1 & 0 & -4 \\ 0 & 3 & -2 \\ 2 & 6 & 3 \end{bmatrix} = \begin{bmatrix} \vec{a}_1 & \vec{a}_2 & \vec{a}_3 \\ \vec{a}_3 & \vec{a}_3 & \vec{b}_3 \end{bmatrix}, \vec{b} = \begin{bmatrix} 47 \\ -47 \end{bmatrix}$ W= Span {a, an as}

- a) Is bin in the set Ea, an, 933? How many vectors are in Ea, az, az3 No. Ea, az, azz only contains threevectors namely [ 02], [3] and [ ] none of which are b.
- DIS bin W? How many vectors are

$$\begin{bmatrix} 1 & 0 - 4 & 4 \\ 0 & 3 & - 2 & 1 \\ -2 & 6 & 3 & - 4 \end{bmatrix}$$

$$R_3 = R_3 + 2R.$$

$$\begin{bmatrix} 1 & 0 & -4 & 4 \\ 0 & 3 & - 2 & 1 \\ 0 & 6 & 5 & 4 \end{bmatrix}$$

This matrix is consistent so b is in W.

c) Show a, is in Wi

W=CV1 + C2V2+ C3V3 C1=1, C2 = 0, C3=0

= V, meaning V, is in the Span.