

4.5.2

$$|\uparrow\rangle = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

$$|\downarrow\rangle = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$|\psi_1\rangle = c_{10}|\uparrow\rangle + c_{11}|\downarrow\rangle = \begin{bmatrix} c_{10} \\ c_{11} \end{bmatrix} \rightarrow \in \mathbb{C}^2$$

$$|\psi_2\rangle = c_{20}|\uparrow\rangle + c_{21}|\downarrow\rangle = \begin{bmatrix} c_{20} \\ c_{21} \end{bmatrix} \rightarrow \in \mathbb{C}^2$$

$$|\psi_1\rangle \otimes |\psi_2\rangle = \begin{bmatrix} c_{10}c_{20} \\ c_{10}c_{21} \\ c_{11}c_{20} \\ c_{11}c_{21} \end{bmatrix} \in \mathbb{C}^4$$

$$= c_{10}c_{20}|\uparrow\rangle \otimes |\uparrow\rangle + c_{10}c_{21}|\uparrow\rangle \otimes |\downarrow\rangle + c_{11}c_{20}|\downarrow\rangle \otimes |\uparrow\rangle + c_{11}c_{21}|\downarrow\rangle \otimes |\downarrow\rangle$$

Es un vector de estado genérico el cual pertenece a \mathbb{C}^{2^n}

4.5.3

$$|\phi\rangle = |x_0\rangle \otimes |y_0\rangle + |x_1\rangle \otimes |y_1\rangle$$

$$|\psi\rangle = c_0|x_0\rangle + c_1|x_1\rangle = \begin{bmatrix} c_0 \\ c_1 \end{bmatrix}$$

$$|\psi_1\rangle = c'_0|y_0\rangle + c'_1|y_1\rangle = \begin{bmatrix} c'_0 \\ c'_1 \end{bmatrix}$$

$$|\phi\rangle = c_0c'_0|x_0\rangle \otimes |y_0\rangle + c_0c'_1|x_0\rangle \otimes |y_1\rangle + c_1c'_0|x_1\rangle \otimes |y_0\rangle + c_1c'_1|x_1\rangle \otimes |y_1\rangle$$

$$\left. \begin{array}{l} c_0c'_0 = 0 \\ c_0c'_1 = 1 \\ c_1c'_0 = 0 \\ c_1c'_1 = 1 \end{array} \right\} \begin{array}{l} c_0 = 0 \\ c_0 = 1 \\ c_1 = 1 \\ c_1 = 1 \end{array}$$

el sistema si es separable

$$|\psi_1\rangle = |x_0\rangle + |x_1\rangle = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad |\psi_2\rangle = |y_1\rangle = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$