

Exercise 2: Epipolar constraint

According to the stereo vision geometry, we can get the following relationship:

$$\begin{aligned}
 (R \cdot XO_R + O_R O_L) \times XO_L &= 0 \\
 (R \cdot XO_R) \times XO_L + O_R O_L \times XO_L &= 0 \\
 (R \cdot XO_R) \times XO_L + O_R O_L \times (R \cdot XO_R + O_R O_L) &= 0 \\
 (R \cdot XO_R) \times XO_L + O_R O_L \times (R \cdot XO_R) &= 0 \\
 XO_L^T \cdot (R \cdot XO_R) \times XO_L + XO_L^T \cdot (O_R O_L \times (R \cdot XO_R)) &= 0 \\
 XO_L^T \cdot (O_R O_L \times (R \cdot XO_R)) &= 0 \\
 XO_L^T \cdot [O_R O_L]_{\times} R \cdot XO_R &= 0 \\
 XO_L^T \cdot E \cdot XO_R &= 0
 \end{aligned}$$

Thus the essential matrix is in form $E = [O_R O_L]_{\times} R$