## -GITHUB-RRc-Gaia

January 18, 2024

# 1 Data for a given star

```
[5]: # ----- example

time_of_brighness_maxima = 2455197.5 # MO
pulsation_period = 0.33 # per
ampG = 0.4 # amplitude in G-band
eampG = 0.01 # error on amplitude in G-band

class_star = "RRc"
```

return -0.5 \* (dy)\*\*2 / std\*\*2 - 0.5\*np.log(2\*np.pi) - np.log(std)

```
time_of_observations = np.array([2455197.62, 2455197.642]) # JD
line_of_sight_velocity = np.array([-30.6, -27.22]) # vlos
uncertainty_line_of_sight_velocity = np.array([1.44, 2.32]) # evlos
```

[]:

#### 1.1 Amplitude scaling relation

```
[6]: # Equations 15 in the paper
scaling_relation_RRc = np.array([62.0])
error_on_scaling_relation_RRc = np.array([2.0])
```

### 1.2 Template and scatter in template

```
[7]: #
                    phase
                           RRab1
                                  RRab2
                                          RRab3
                                                   RR.c.
    err = np.array([[0.000, 0.068, 0.073, 0.053, 0.095],
                   [0.025, 0.068, 0.073, 0.053, 0.095],
                   [0.075, 0.036, 0.071, 0.048, 0.079],
                   [0.125, 0.054, 0.052, 0.047, 0.105],
                   [0.175, 0.051, 0.049, 0.058, 0.062],
                   [0.225, 0.065, 0.033, 0.044, 0.082],
                   [0.275, 0.053, 0.051, 0.043, 0.069],
                   [0.325, 0.069, 0.047, 0.039, 0.064],
                   [0.375, 0.057, 0.051, 0.063, 0.096],
                   [0.425, 0.069, 0.050, 0.058, 0.052],
                   [0.475, 0.053, 0.048, 0.032, 0.086],
                   [0.525, 0.056, 0.051, 0.023, 0.064],
                   [0.575, 0.060, 0.069, 0.031, 0.056],
                   [0.625, 0.057, 0.055, 0.110, 0.061],
                   [0.675, 0.072, 0.049, 0.066, 0.086],
                   [0.725, 0.045, 0.052, 0.071, 0.165],
                   [0.775, 0.058, 0.068, 0.039, 0.121],
                   [0.825, 0.095, 0.073, 0.093, 0.163],
                   [0.875, 0.112, 0.273, 0.215, 0.210],
                   [0.925, 0.218, 0.172, 0.036, 0.091],
                   [0.975, 0.064, 0.094, 0.038, 0.091],
                   [1.000 , 0.064 , 0.094 , 0.038 , 0.091]])
```

```
0.0511, -0.0206])
      template_fourier_rrab3 = np.array([0.0000, -0.2931, -0.2508,
                                         -0.0772, -0.1432, 0.0057,
                                         -0.1009, 0.0577, -0.0403,
                                         0.0386, -0.0041
      template fourier rrc = np.array([0.0000, -0.1997, -0.3880,
                                       0.0328, -0.1382, 0.0455,
                                       -0.02971)
      # Table B5, first column in the paper
      phase_for_scatter_in_template = err[:,0]
      # Table B5, second column in the paper
      scatter_in_template_rrab1 = err[:,1]
      scatter_in_template_rrab2 = err[:,2]
      scatter_in_template_rrab3 = err[:,3]
      scatter_in_template_rrc = err[:,4]
      # Spline function that interpolates the discrete scatter along the pulsation_
       ⇔phase
      f_spline_err_rrab1 = interpolate.interp1d(phase_for_scatter_in_template,_
       scatter_in_template_rrab1, kind='linear')
      f spline err rrab2 = interpolate.interp1d(phase for scatter in template,
      scatter_in_template_rrab2, kind='linear')
      f_spline_err_rrab3 = interpolate.interp1d(phase_for_scatter_in_template,_u
       scatter_in_template_rrab3, kind='linear')
      f_spline_err_rrc = interpolate.interp1d(phase_for_scatter_in_template,__
       ⇔scatter_in_template_rrc, kind='linear')
[11]: vector = ampG
      epsilon_rrc = 4.
      Amp_line_of_sight_vel = scaling_relation_RRc * vector
      uncertainty_Amp_line_of_sight_vel = np.sqrt(vector *_
       ⇔error_on_scaling_relation_RRc * vector
      ⇔(scaling relation RRc[0]**2)*(eampG**2) + epsilon rrc**2)
      print(r"Predicted amplitude of the line of sight velocity and its error is: %.
       →1f ± %.1f kms-1" %(Amp_line_of_sight_vel,
                   uncertainty_Amp_line_of_sight_vel))
```

-0.0931, 0.0419, -0.0642,

Predicted amplitude of the line of sight velocity and its error is:  $24.8 \pm 4.1$  kms-1

```
[]:
 []:
[12]: def systematic_velocity_determ(param, HJD, measured_velocity, u
       →uncertainty_measured_velocity,
                                     P, MO, Alos, eAlos, template_fourier,

¬f_spline_err):
          vsys = param
          # Equation 21 in paper
          phase_star = np.mod(HJD - MO, P) / P
          # Equation 19 in paper
          model_velocity = function_fourier_fit(template_fourier, phase_star)*Alos +__
       ysys
          # Equation 20 in paper
          evel_fin = np.sqrt(uncertainty_measured_velocity**2
                             + (f_spline_err(phase_star)*Alos)**2
       ⇔(function_fourier_fit(template_fourier,phase_star)*eAlos)**2 )
          # Equation 18 in paper
          result = ln_normal(measured_velocity - model_velocity, evel_fin)
          return np.nansum(result[np.isfinite(result)])
      # Possibility for including some priors
      def prior(param):
          # pick a prior
         return 0.0
      def LOG_probability(param, HJD, measured_velocity, __

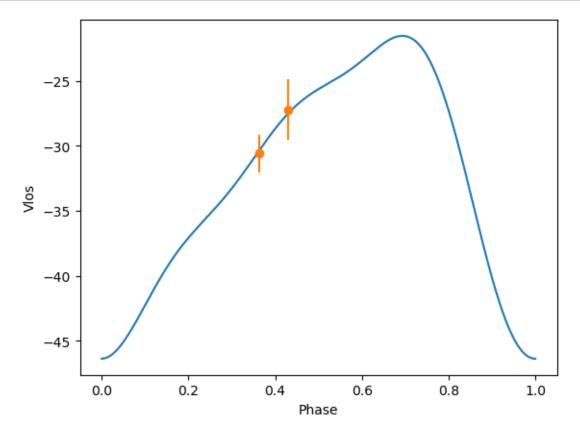
¬uncertainty_measured_velocity, P, MO, Alos, eAlos,
                          template_fourier, f_spline_err):
          lp = prior(param)
```

[]:

#### 1.3 Using Scipy library

Determined systemic velocity and its uncertainty is: -32.6 ± 1.9 kms-1

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