

- 29.5 A flange weld is most closely associated with which one of the following joint types: (a) butt, (b) corner, (c) edge, (d) lap, or (e) tee?

Answer. (c).

- 29.6 For metallurgical reasons, it is desirable to melt the weld metal with minimum energy input. Which one of the following heat sources is most consistent with this objective: (a) high power, (b) high power density, (c) low power, or (d) low power density?

Answer. (b).

- 29.7 The amount of heat required to melt a given volume of metal depends strongly on which of the following properties (three best answers): (a) coefficient of thermal expansion, (b) heat of fusion, (c) melting temperature, (d) modulus of elasticity, (e) specific heat, (f) thermal conductivity, and (g) thermal diffusivity?

Answer. (b), (c), and (e).

- 29.8 The heat transfer factor in welding is correctly defined by which one of the following descriptions: (a) the proportion of the heat received at the work surface that is used for melting, (b) the proportion of the total heat generated at the source that is received at the work surface, (c) the proportion of the total heat generated at the source that is used for melting, or (d) the proportion of the total heat generated at the source that is used for welding?

Answer. (b).

- 29.9 The melting factor in welding is correctly defined by which one of the following descriptions: (a) the proportion of the heat received at the work surface that is used for melting, (b) the proportion of the total heat generated at the source that is received at the work surface, (c) the proportion of the total heat generated at the source that is used for melting, or (d) the proportion of the total heat generated at the source that is used for welding?

Answer. (a).

- 29.10 Weld failures always occur in the fusion zone of the weld joint, since this is the part of the joint that has been melted: (a) true, (b) false?

Answer. (b). Failures also occur in the heat-affected zone because metallurgical damage often occurs in this region.

Problems

Power Density

- 29.1 A heat source can transfer 3500 J/sec to a metal part surface. The heated area is circular, and the heat intensity decreases as the radius increases, as follows: 70% of the heat is concentrated in a circular area that is 3.75 mm in diameter. Is the resulting power density enough to melt metal?

Solution: Area $A = \pi(3.75)^2/4 = 11.045 \text{ mm}^2$

Power $P = 0.70(3500) = 2450 \text{ J/s} = 2450 \text{ W}$.

Power density $PD = 2450 \text{ W}/11.0447^2 = \mathbf{222 \text{ W/mm}^2}$. This power density is most probably sufficient for melting the metal.

- 29.2 In a laser beam welding process, what is the quantity of heat per unit time (J/sec) that is transferred to the material if the heat is concentrated in circle with a diameter of 0.2 mm? Assume the power density provided in Table 29.1.

Solution: PD from Table 29.1 is 9000 W/mm^2 for laser beam welding

$P = PD \times A = 9000 \pi(0.2)^2/4 = \mathbf{283 \text{ W} = 283 \text{ J/sec}}$

- 29.3 A welding heat source is capable of transferring 150 Btu/min to the surface of a metal part. The heated area is approximately circular, and the heat intensity decreases with increasing radius as follows: 50% of the power is transferred within a circle of diameter = 0.1 inch and 75% is transferred within a concentric circle of diameter = 0.25 in. What are the power densities in (a) the 0.1-inch diameter inner circle and (b) the 0.25-inch diameter ring that lies around the inner circle? (c) Are these power densities sufficient for melting metal?

Solution: (a) Area $A = \pi(0.1)^2/4 = 0.00785 \text{ in}^2$
150 Btu/min = 2.5 Btu/sec.
Power $P = 0.50(2.5) = 1.25 \text{ Btu/sec}$
Power density $PD = (1.25 \text{ Btu/sec})/0.00785 \text{ in}^2 = \mathbf{159 \text{ Btu/sec-in}^2}$

(b) $A = \pi(0.25^2 - 0.1^2)/4 = 0.0412 \text{ in}^2$
Power $P = (0.75 - 0.50)(2.5) = 0.625 \text{ Btu/sec}$
Power density $PD = (0.625 \text{ Btu/sec})/0.0412 \text{ in}^2 = \mathbf{15.16 \text{ Btu/sec-in}^2}$

(c) Power densities are sufficient certainly in the inner circle and probably in the outer ring for welding.

Unit Melting Energy

- 29.4 Compute the unit energy for melting for the following metals: (a) aluminum and (b) plain low carbon steel.

Solution: (a) From Table 29.2, T_m for aluminum = 930 K (1680 R)
Eq. (29.2) for SI units: $U_m = 3.33(10^{-6})T_m^2$ $U_m = 3.33 \times 10^{-6} (930)^2 = \mathbf{2.88 \text{ J/mm}^3}$
Eq. (29.2) for USCS units: $U_m = 1.467(10^{-5})T_m^2$ $U_m = 1.467 \times 10^{-5} (1680)^2 = \mathbf{41.4 \text{ Btu/in}^3}$

(b) From Table 29.2, T_m for plain low carbon steel = 1760 K (3160 R)
Eq. (29.2) for SI units: $U_m = 3.33(10^{-6})T_m^2$ $U_m = 3.33 \times 10^{-6} (1760)^2 = \mathbf{10.32 \text{ J/mm}^3}$
Eq. (29.2) for USCS units: $U_m = 1.467(10^{-5})T_m^2$ $U_m = 1.467 \times 10^{-5} (3160)^2 = \mathbf{146.5 \text{ Btu/in}^3}$

- 29.5 Compute the unit energy for melting for the following metals: (a) copper and (b) titanium.

Solution: (a) From Table 29.2, T_m for copper = 1350 K (2440 R)
Eq. (29.2) for SI units: $U_m = 3.33(10^{-6})T_m^2$ $U_m = 3.33 \times 10^{-6} (1350)^2 = \mathbf{6.07 \text{ J/mm}^3}$
Eq. (29.2) for USCS units: $U_m = 1.467(10^{-5})T_m^2$ $U_m = 1.467 \times 10^{-5} (2440)^2 = \mathbf{87.3 \text{ Btu/in}^3}$

(b) From Table 29.2, T_m for titanium = 2070 K (3730 R)
Eq. (29.2) for SI units: $U_m = 3.33(10^{-6})T_m^2$ $U_m = 3.33 \times 10^{-6} (2070)^2 = \mathbf{14.27 \text{ J/mm}^3}$
Eq. (29.2) for USCS units: $U_m = 1.467(10^{-5})T_m^2$ $U_m = 1.467 \times 10^{-5} (3730)^2 = \mathbf{204.1 \text{ Btu/in}^3}$

- 29.6 Make the calculations and plot on linearly scaled axes the relationship for unit melting energy as a function of temperature. Use temperatures as follows to construct the plot: 200°C, 400°C, 600°C, 800°C, 1000°C, 1200°C, 1400°C, 1600°C, 1800°C, and 2000°C. On the plot, mark the positions of some of the welding metals in Table 29.2. Use of a spreadsheet program is recommended for the calculations.

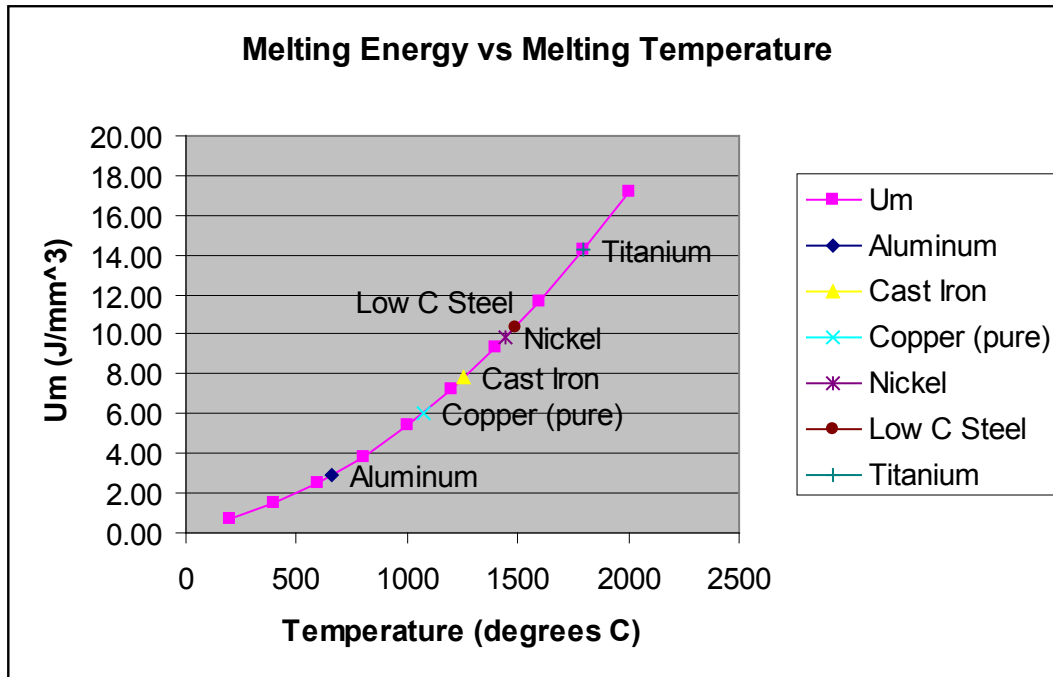
Solution: Eq. (29.2) for SI units: $U_m = 3.33 \times 10^{-6} T_m^2$. The plot is based on the following calculated values.

For $T_m = \mathbf{200^\circ C} = (200 + 273) = 473^\circ K$: $U_m = 3.33 \times 10^{-6} (473)^2 = \mathbf{0.75 \text{ J/mm}^3}$
For $T_m = \mathbf{400^\circ C} = (400 + 273) = 673^\circ K$: $U_m = 3.33 \times 10^{-6} (673)^2 = \mathbf{1.51 \text{ J/mm}^3}$
For $T_m = \mathbf{600^\circ C} = (600 + 273) = 873^\circ K$: $U_m = 3.33 \times 10^{-6} (873)^2 = \mathbf{2.54 \text{ J/mm}^3}$
For $T_m = \mathbf{800^\circ C} = (800 + 273) = 1073^\circ K$: $U_m = 3.33 \times 10^{-6} (1073)^2 = \mathbf{3.83 \text{ J/mm}^3}$
For $T_m = \mathbf{1000^\circ C} = (1000 + 273) = 1273^\circ K$: $U_m = 3.33 \times 10^{-6} (1273)^2 = \mathbf{5.40 \text{ J/mm}^3}$
For $T_m = \mathbf{1200^\circ C} = (1200 + 273) = 1473^\circ K$: $U_m = 3.33 \times 10^{-6} (1473)^2 = \mathbf{7.23 \text{ J/mm}^3}$
For $T_m = \mathbf{1400^\circ C} = (1400 + 273) = 1673^\circ K$: $U_m = 3.33 \times 10^{-6} (1673)^2 = \mathbf{9.32 \text{ J/mm}^3}$

For $T_m = 1600^\circ\text{C} = (1600 + 273) = 1873^\circ\text{K}$: $U_m = 3.33 \times 10^{-6} (1873)^2 = \mathbf{11.68 \text{ J/mm}^3}$

For $T_m = 1800^\circ\text{C} = (1800 + 273) = 2073^\circ\text{K}$: $U_m = 3.33 \times 10^{-6} (2073)^2 = \mathbf{14.31 \text{ J/mm}^3}$

For $T_m = 2000^\circ\text{C} = (2000 + 273) = 2273^\circ\text{K}$: $U_m = 3.33 \times 10^{-6} (2273)^2 = \mathbf{17.20 \text{ J/mm}^3}$



- 29.7 Make the calculations and plot on linearly scaled axes the relationship for unit melting energy as a function of temperature. Use temperatures as follows to construct the plot: 500°F, 1000°F, 1500°F, 2000°F, 2500°F, 3000°F, and 3500°F. On the plot, mark the positions of some of the welding metals in Table 29.2. Use of a spreadsheet program is recommended for the calculations.

Solution: Eq. (29.2) for USCS units: $U_m = 1.467(10^{-5})T_m^2$. The plot is based on the following calculated values. The plot is left as a student exercise.

For $T_m = 500^\circ\text{F} = (500 + 460) = 960^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (960)^2 = \mathbf{13.5 \text{ Btu/in}^3}$

For $T_m = 1000^\circ\text{F} = (1000 + 460) = 1460^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (1460)^2 = \mathbf{31.3 \text{ Btu/in}^3}$

For $T_m = 1500^\circ\text{F} = (1500 + 460) = 1960^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (1960)^2 = \mathbf{56.4 \text{ Btu/in}^3}$

For $T_m = 2000^\circ\text{F} = (2000 + 460) = 2460^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (2460)^2 = \mathbf{88.8 \text{ Btu/in}^3}$

For $T_m = 2500^\circ\text{F} = (2500 + 460) = 2960^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (2960)^2 = \mathbf{128.5 \text{ Btu/in}^3}$

For $T_m = 3000^\circ\text{F} = (3000 + 460) = 3460^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (3460)^2 = \mathbf{175.6 \text{ Btu/in}^3}$

For $T_m = 3500^\circ\text{F} = (3500 + 460) = 3960^\circ\text{R}$: $U_m = 1.467 \times 10^{-5} (3960)^2 = \mathbf{230.0 \text{ Btu/in}^3}$

- 29.8 A fillet weld has a cross-sectional area of 25.0 mm² and is 300 mm long. (a) What quantity of heat (in joules) is required to accomplish the weld, if the metal to be welded is low carbon steel? (b) How much heat must be generated at the welding source, if the heat transfer factor is 0.75 and the melting factor = 0.63?

Solution: (a) Eq. (29.2) for SI units: $U_m = 3.33 \times 10^{-6} T_m^2$

From Table 29.2, T_m for low carbon steel = 1760° K

$U_m = 3.33 \times 10^{-6} (1760)^2 = 10.32 \text{ J/mm}^3$

Volume of metal melted $V = 25(300) = 7500 \text{ mm}^3$

$H_w = 10.32(7500) = \mathbf{77,360 \text{ J at weld}}$

(b) Given $f_1 = 0.75$ and $f_2 = 0.63$, $H = 77,360 / (0.75 \times 0.63) = \mathbf{163,700 \text{ J at source}}$.

- 29.9 A U-groove weld is used to butt weld 2 pieces of 7.0-mm-thick titanium plate. The U-groove is prepared using a milling cutter so the radius of the groove is 3.0 mm. During welding, the penetration of the weld causes an additional 1.5 mm of material to be melted. The final cross-sectional area of the weld can be approximated by a semicircle with a radius of 4.5 mm. The length of the weld is 200 mm. The melting factor of the setup is 0.57 and the heat transfer factor is 0.86. (a) What is the quantity of heat (in Joules) required to melt the volume of metal in this weld (filler metal plus base metal)? Assume the resulting top surface of the weld bead is flush with the top surface of the plates. (b) What is the required heat generated at the welding source?

Solution: (a) From Table 29.2, T_m for titanium is 2070°K

$$U_m = 3.33 \times 10^{-6} (2070)^2 = 14.29 \text{ J/mm}^3$$

$$A_w = \pi r^2 / 2 = \pi (4.5)^2 / 2 = 31.8 \text{ mm}^2$$

$$V = A_w L = 31.8(200) = 6360 \text{ mm}^3$$

$$H_w = U_m V = 14.29(6360) = \mathbf{90,770 \text{ J}}$$

$$(b) H = H_w / (f_1 f_2) = 90,770 / (0.86 \times 0.57) = \mathbf{185,200 \text{ J}}$$

- 29.10 A groove weld has a cross-sectional area = 0.045 in² and is 10 inches long. (a) What quantity of heat (in Btu) is required to accomplish the weld, if the metal to be welded is medium carbon steel? (b) How much heat must be generated at the welding source, if the heat transfer factor = 0.9 and the melting factor = 0.7?

Solution: (a) Eq. (29.2) for USCS units: $U_m = 1.467 \times 10^{-5} T_m^2$

From Table 29.2, T_m for medium carbon steel = 3060 R

$$U_m = 1.467 \times 10^{-5} (3060)^2 = 137.4 \text{ Btu/in}^3$$

$$\text{Volume of metal melted } V = 0.045(10) = 0.45 \text{ in}^3$$

$$H_w = 137.4(0.45) = \mathbf{61.8 \text{ Btu at weld}}$$

$$(b) \text{ Given } f_1 = 0.9 \text{ and } f_2 = 0.7. \quad H = 61.8 / (0.9 \times 0.7) = \mathbf{98.1 \text{ Btu at source.}}$$

- 29.11 Solve the previous problem, except that the metal to be welded is aluminum, and the corresponding melting factor is half the value for steel.

Solution: (a) Eq. (29.2) for USCS units: $U_m = 1.467 \times 10^{-5} T_m^2$

From Table 29.2, T_m for aluminum = 1680 R

$$U_m = 1.467 \times 10^{-5} (1680)^2 = 41.4 \text{ Btu/in}^3$$

$$\text{Volume of metal melted } V = 0.045(10) = 0.45 \text{ in}^3$$

$$H_w = 41.4(0.45) = \mathbf{18.6 \text{ Btu at weld}}$$

$$(b) \text{ Given } f_1 = 0.9 \text{ and } f_2 = 0.35. \quad H = 18.6 / (0.9 \times 0.35) = \mathbf{59.1 \text{ Btu at source.}}$$

- 29.12 In a controlled experiment, it takes 3700 J to melt the amount of metal that is in a weld bead with a cross-sectional area of 6.0 mm² that is 150.0 mm long. (a) Using Table 29.2, what is the most likely metal? (b) If the heat transfer factor is 0.85 and the melting factor is 0.55 for a welding process, how much heat must be generated at the welding source to accomplish the weld?

$$\mathbf{Solution:} \quad V = A_w L = 6.0(150) = 900 \text{ mm}^3$$

$$U_m = H_w / V = 3700 / 900 = 4.111 \text{ J/mm}^3$$

$$T_m = (U_m / k)^{0.5} = (4.111 / 3.33 \times 10^{-6})^{0.5} = 1111^\circ \text{ K}$$

From Table 29.2, the metal with the closest melting point to 1111° is **Bronze (1120° K)**

$$(b) H = H_w / (f_1 f_2) = 3700 / (0.85 \times 0.55) = \mathbf{7,914 \text{ Joules}}$$

- 29.13 Compute the unit melting energy for (a) aluminum and (b) steel as the sum of: (1) the heat required to raise the temperature of the metal from room temperature to its melting point, which is the volumetric specific heat multiplied by the temperature rise; and (2) the heat of fusion, so that this value can be compared to the unit melting energy calculated by Eq. (29.2). Use either the SI units or

U.S. Customary units. Find the values of the properties needed in these calculations either in this text or in other references. Are the values close enough to validate Eq. (29.2)?

Solution: (a) Aluminum properties (from standard sources): heat of fusion $H_f = 395,390 \text{ J/kg} = 170 \text{ Btu/lb}$, melting temperature $T_m = 660^\circ\text{C} = 1220^\circ\text{F}$, density $\rho = 2700 \text{ kg/m}^3 = 0.096 \text{ lb/in}^3$, specific heat $C = 900 \text{ J/kg}\cdot^\circ\text{C} = 0.215 \text{ Btu/lb}\cdot^\circ\text{F}$.

$$U_m = \rho C(T_m - T_{\text{ambient}}) + \rho H_f$$

$$U_m = (2.7 \times 10^{-6} \text{ kg/mm}^3)(900 \text{ J/kg}\cdot^\circ\text{C})(660 - 21) + (2.7 \times 10^{-6} \text{ kg/mm}^3)(395390 \text{ J/kg}) = \mathbf{2.62 \text{ J/mm}^3}$$

This compares with Eq. (29.2): $U_m = 3.33 \times 10^{-6} (660 + 273)^2 = \mathbf{2.90 \text{ J/mm}^3}$, which is about a 10% difference. These values for aluminum show good agreement.

$$\text{In USCS, } U_m = \rho C(T_m - 70) + \rho H_f = 0.096(0.215)(1220 - 70) + 0.096(170) = \mathbf{40.1 \text{ Btu/in}^3}$$

This compares with Eq. (29.2): $U_m = 1.467 \times 10^{-5} (1220 + 460)^2 = \mathbf{41.4 \text{ Btu/in}^3}$, which is about a 3% difference.

(b) Steel properties (from standard sources): heat of fusion $H_f = 272,123 \text{ J/kg} = 117 \text{ Btu/lb}$, melting temperature $T_m = 1480^\circ\text{C} = 2700^\circ\text{F}$, density $\rho = 7900 \text{ kg/m}^3 = 0.284 \text{ lb/in}^3$, specific heat $C = 460 \text{ J/kg}\cdot^\circ\text{C} = 0.11 \text{ Btu/lb}\cdot^\circ\text{F}$.

$$U_m = \rho C(T_m - T_{\text{ambient}}) + \rho H_f$$

$$U_m = (7.9 \times 10^{-6} \text{ kg/mm}^3)(460 \text{ J/kg}\cdot^\circ\text{C})(1480 - 21) + (7.9 \times 10^{-6} \text{ kg/mm}^3)(272123 \text{ J/kg}) = \mathbf{7.45 \text{ J/mm}^3}$$

This compares with Eq. (29.2): $U_m = 3.33 \times 10^{-6} (1480 + 273)^2 = \mathbf{10.23 \text{ J/mm}^3}$, which is about a 37% difference.

$$\text{In USCS, } U_m = \rho C(T_m - 70) + \rho H_f = 0.284(0.11)(2700 - 70) + 0.284(117) = \mathbf{115.4 \text{ Btu/in}^3}$$

This compares with Eq. (29.2): $U_m = 1.467 \times 10^{-5} (2700 + 460)^2 = \mathbf{146.5 \text{ Btu/in}^3}$, which is about a 27% difference.

Comment: These values show a greater difference than for aluminum. This is at least partially accounted for by the fact that the specific heat of steel increases significantly with temperature, which would increase the calculated values based on $U_m = \rho C(T_m - T_{\text{ambient}}) + \rho H_f$.

Energy Balance in Welding

- 29.14 The welding power generated in a particular arc-welding operation = 3000 W. This is transferred to the work surface with a heat transfer factor = 0.9. The metal to be welded is copper whose melting point is given in Table 29.2. Assume that the melting factor = 0.25. A continuous fillet weld is to be made with a cross-sectional area = 15.0 mm^2 . Determine the travel speed at which the welding operation can be accomplished.

Solution: From Table 29.2, $T_m = 1350^\circ\text{K}$ for copper.

$$U_m = 3.33 \times 10^{-6} (1350)^2 = 6.07 \text{ J/mm}^3$$

$$v = f_1 f_2 R_H / U_m A_w = 0.9(0.25)(3000) / (6.07 \times 15) = \mathbf{7.4 \text{ mm/s.}}$$

- 29.15 Solve the previous problem except that the metal to be welded is high carbon steel, the cross-sectional area of the weld = 25.0 mm^2 , and the melting factor = 0.6.

Solution: From Table 29.2, $T_m = 1650^\circ\text{K}$ for high carbon steel.

$$U_m = 3.33 \times 10^{-6} (1650)^2 = 9.07 \text{ J/mm}^3$$

$$v = f_1 f_2 R_H / U_m A_w = 0.9(0.6)(3000) / (9.07 \times 25) = \mathbf{7.15 \text{ mm/s.}}$$

- 29.16 A welding operation on an aluminum alloy makes a groove weld. The cross-sectional area of the weld is 30.0 mm^2 . The welding velocity is 4.0 mm/sec . The heat transfer factor is 0.92 and the melting factor is 0.48. The melting temperature of the aluminum alloy is 650°C . Determine the rate of heat generation required at the welding source to accomplish this weld.

$$\text{Solution: } U_m = 3.33 \times 10^{-6} (650 + 273)^2 = 2.84 \text{ J/mm}^3$$

$$f_1 f_2 R_H = U_m A_w v$$

$$R_H = U_m A_w v / f_1 f_2 = 2.84(30)(4) / (0.92 \times 0.48) = \mathbf{771 \text{ J/s} = 771 \text{ W.}}$$

- 29.17 The power source in a particular welding operation generates 125 Btu/min, which is transferred to the work surface with heat transfer factor = 0.8. The melting point for the metal to be welded = 1800°F and its melting factor = 0.5. A continuous fillet weld is to be made with a cross-sectional area = 0.04 in². Determine the travel speed at which the welding operation can be accomplished.

Solution: $U_m = 1.467 \times 10^{-5} (1800 + 460)^2 = 74.9 \text{ Btu/in}^3$
 $v = f_1 f_2 R_H / U_m A_w = 0.8(0.5)(125) / (74.9 \times 0.04) = \mathbf{16.7 \text{ in/min}}$

- 29.18 In a certain welding operation to make a fillet weld, the cross-sectional area = 0.025 in² and the travel speed = 15 in/min. If the heat transfer factor = 0.95 and melting factor = 0.5, and the melting point = 2000°F for the metal to be welded, determine the rate of heat generation required at the heat source to accomplish this weld.

Solution: $U_m = 1.467 \times 10^{-5} (2000 + 460)^2 = 88.8 \text{ Btu/in}^3$
 $v = 15 = f_1 f_2 R_H / U_m A_w = 0.95(0.5)R_H / (88.8 \times 0.025) = 0.214 R_H$
 $R_H = 15 / 0.214 = \mathbf{70.1 \text{ Btu/min}}$

- 29.19 A fillet weld is used to join 2 medium carbon steel plates each having a thickness of 5.0 mm. The plates are joined at a 90° angle using an inside fillet corner joint. The velocity of the welding head is 6 mm/sec. Assume the cross section of the weld bead approximates a right isosceles triangle with a leg length of 4.5 mm, the heat transfer factor is 0.80, and the melting factor is 0.58. Determine the rate of heat generation required at the welding source to accomplish the weld.

Solution: $A_w = bh/2 = 4.5(4.5)/2 = 10.125 \text{ mm}^2$
 From Table 29.2, $T_m = 1700^\circ\text{K}$
 $U_m = 3.33 \times 10^{-6} (1700)^2 = 9.62 \text{ J/mm}^3$
 $R_H = U_m A_w v / (f_1 f_2) = 9.62(10.125)(5.0) / (0.8 \times 0.58) = \mathbf{1260 \text{ J/sec} = 1260 \text{ W.}}$

- 29.20 A spot weld was made using an arc-welding process. In a spot-welding operation, two 1/16-in-thick aluminum plates were joined. The melted metal formed a nugget that had a diameter of 1/4 in. The operation required the power to be on for 4 sec. Assume the final nugget had the same thickness as the two aluminum plates (1/8 in thick), the heat transfer factor was 0.80 and the melting factor was 0.50. Determine the rate of heat generation that was required at the source to accomplish this weld.

Solution: From Table 29.2, $T_m = 1680^\circ\text{R}$ for aluminum.
 $U_m = 1.467 \times 10^{-5} (1680)^2 = 41.4 \text{ Btu/in}^3$
 $V = \pi D^2/4 (2t) = \pi (0.25^2/4)(2)(1/16) = 0.0061 \text{ in}^3$
 $H_w = U_m V = 41.4(0.0061) = 0.254 \text{ Btu}$
 $H = H_w / (f_1 f_2) = 0.254 / (0.80 \times 0.5) = 0.635 \text{ Btu}$
 $R_H = H/T = 0.635/4 = \mathbf{0.159 \text{ Btu/sec} = 9.53 \text{ Btu/min}}$

- 29.21 A surfacing weld is to be applied to a rectangular low carbon steel plate that is 200 mm by 350 mm. The filler metal to be added is a harder (alloy) grade of steel, whose melting point is assumed to be the same. A thickness of 2.0 mm will be added to the plate, but with penetration into the base metal, the total thickness melted during welding = 6.0 mm, on average. The surface will be applied by making a series of parallel, overlapped welding beads running lengthwise on the plate. The operation will be carried out automatically with the beads laid down in one long continuous operation at a travel speed = 7.0 mm/s, using welding passes separated by 5 mm. Assume the welding bead is rectangular in cross section: 5 mm by 6 mm. Ignore the minor complications of the turnarounds at the ends of the plate. Assuming the heat transfer factor = 0.8 and the melting factor = 0.6, determine (a) the rate of heat that must be generated at the welding source, and (b) how long will it take to complete the surfacing operation.

Solution: (a) From Table 29.2, $T_m = 1760^\circ\text{K}$ for low carbon steel.
 $U_m = 3.33 \times 10^{-6} (1760)^2 = 10.32 \text{ J/mm}^3$
 $R_H = U_m A_w v / f_1 f_2 = 10.32(6 \times 5)(7) / (0.8 \times 0.6) = \mathbf{4515 \text{ J/s}}$

(b) Total length of cut = $350(200/5) = 14,000$ mm
 Time to travel at $v = 7$ mm/s = $14,000/7 = 2000$ s = **33.33 min**

- 29.22 An axle-bearing surface made of high carbon steel has worn beyond its useful life. When it was new, the diameter was 4.00 in. In order to restore it, the diameter was turned to 3.90 in to provide a uniform surface. Next the axle was built up so that it was oversized by the deposition of a surface weld bead, which was deposited in a spiral pattern using a single pass on a lathe. After the weld buildup, the axle was turned again to achieve the original diameter of 4.00 in. The weld metal deposited was a similar composition to the steel in the axle. The length of the bearing surface was 7.0 in. During the welding operation, the welding apparatus was attached to the tool holder, which was fed toward the head of the lathe as the axle rotated. The axle rotated at a speed of 4.0 rev/min. The weld bead height was 3/32 in above the original surface. In addition, the weld bead penetrated 1/16 in into the surface of the axle. The width of the weld bead was 0.25 in, thus the feed on the lathe was set to 0.25 in/rev. Assuming the heat transfer factor was 0.80 and the melting factor was 0.65, determine (a) the relative velocity between the workpiece and the welding head, (b) the rate of heat generated at the welding source, and (c) how long it took to complete the welding portion of this operation.

Solution: (a) $v = N\pi D = 4.0\pi(3.90) = 49.01$ in/min = **0.8168 in/sec**

(b) From Table 29.2, $T_m = 2960^\circ\text{R}$ for high carbon steel.

$$U_m = 1.467 \times 10^{-5} (2960)^2 = 128.5 \text{ Btu/in}^3$$

$$R_H = U_m A_w v / f_1 f_2 = 128.5 (0.25(3/32 + 1/16)) 49.01 / (0.8 \times 0.65) \\ = 128.5(0.0391)(49.01)/0.52 = \mathbf{473 \text{ Btu/min}}$$

(c) $T_{\text{weld}} = L/(fN) = 7.0/(0.25 \times 4) = \mathbf{7.0 \text{ min}}$