

# Package ‘timeFA’

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**Type** Package

**Title** Factor Models and Autoregressive Models for Time Series

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**Description** More about what it does (maybe more than one line)

Use four spaces when indenting paragraphs within the Description.

**License** GPL (>= 2)

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igraph

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dynamic_A	<i>dynamic_A</i>
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**Description**

Get the adjacency matrix for plotting

**Usage**

dynamic\_A(x, factor\_count, simple.flag, threshold)

**Arguments**

- x                   input the original estimated loading matrix
- factor\_count       The number of factors to use
- simple.flag         if True, only eliminate the entries below threshold and make all row sums to be 1; if False, the approach further eliminates the entries of the rows that are very close to threshold value and only leaves the maximum entry of each row
- threshold          A parameter to eliminate very small entries of the loading matrix

**Value**

The new loading matrix with all rows sum to be 1

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grouping.loading	<i>grouping.loading</i>
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**Description**

Get the group of loadings

**Usage**

grouping.loading/loading, ncluster, rowname, plot = T)

**Arguments**

- loading            The estimated loading matrix
- ncluster           The number of clusters to use, usually the dimension of the factor matrix
- rowname            The name of the rows
- plot                plot the clustering graph, defacult True

**Value**

Loading matrix after grouping

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MAR.SE	<i>Asymptotic Covariance Matrix of MAR1.otimes</i>
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**Description**

Asymptotic covariance Matrix of MAR1.otimes for given A, B and matrix-valued time series xx, see Theory 3 in paper.

**Usage**

```
MAR.SE(xx, B, A, Sigma)
```

**Arguments**

xx	T * p * q matrix-valued time series
B	q by q matrix in MAR(1) model
A	p by p matrix in MAR(1) model
Sig	covariance matrix cov(vec(E_t)) in MAR(1) model

**Value**

asmptotic covariance matrix

**Examples**

```
# given T * p * q time series xx
out2=MAR1.LS(xx)
FnormLL=sqrt(sum(out2$LL))
xdim=p;ydim=q
out2Xi=MAR.SE(xx.nm,out2$RR*FnormLL,out2$LL/FnormLL,out2$Sig)
out2SE=sqrt(diag(out2Xi))
SE.A=matrix(out2SE[1:xdim^2],nrow=xdim)
SE.B=t(matrix(out2SE[-(1:xdim^2)],nrow=ydim))
```

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MAR1.LS	<i>Least Squares Iterative Estimation</i>
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**Description**

Iterated least squares estimation in the model  $X_t = LL * X_{t-1} * RR + E_t$ .

**Usage**

```
MAR1.LS(xx, niter = 50, tol = 1e-06, print.true = FALSE)
```

**Arguments**

xx	T * p * q matrix-valued time series
niter	maximum number of iterations if error stays above tol
tol	relative Frobenius norm error tolerance
print.true	printe LL and RR

**Value**

a list containing the following:

LL estimator of LL, a p by p matrix  
 RR estimator of RR, a q by q matrix  
 res residual of the MAR(1)  
 Sig covariance matrix  $\text{cov}(\text{vec}(E_t))$   
 dis Frobenius norm difference of last update  
 niter number of iterations

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MAR1.otimes

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*MLE under a structured covariance tensor*


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**Description**

MAR(1) iterative estimation with Kronecker covariance structure:  $X_t = LL * X_{t-1} * RR + E_t$   
 such that  $\Sigma = \text{cov}(\text{vec}(E_t)) = \Sigma_r \otimes \Sigma_l$ .

**Usage**

```
MAR1.otimes(
  xx,
  LL.init = NULL,
  Sigl.init = NULL,
  Sigr.init = NULL,
  niter = 50,
  tol = 1e-06,
  print.true = FALSE
)
```

**Arguments**

xx	T * p * q matrix-valued time series
LL.init	initial value of LL
Sigl.init	initial value of Sigl
Sigr.init	initial value of Sigr
niter	maximum number of iterations if error stays above tol
tol	relative Frobenius norm error tolerance
print.true	print LL and RR

**Value**

a list containing the following:

LL estimator of LL, a p by p matrix  
 RR estimator of RR, a q by q matrix  
 res residual of the MAR(1)

Sigl one part of structured covariance matrix  $\Sigma = \Sigma_r \otimes \Sigma_l$

Sigr one part of structured covariance matrix  $\Sigma = \Sigma_r \otimes \Sigma_l$

dis Frobenius norm difference of the final update step

niter number of iterations

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MAR1.projection	<i>Projection Method</i>
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### Description

MAR(1) one step projection estimation in the model  $X_t = LL * X_{t-1} * RR + E_t$ .

### Usage

MAR1.projection(xx)

### Arguments

xx T \* p \* q matrix-valued time series

### Value

a list containing the following:

LL estimator of LL, a p by p matrix

RR estimator of RR, a q by q matrix

res residual of the MAR(1)

Sig covariance matrix cov(vec(E\_t))

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matrix_factor	<i>matrix_factor</i>
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### Description

The main estimation function

### Usage

matrix\_factor(Yt, inputk1, inputk2, iscentering = 1, hzero = 1)

### Arguments

Yt Time Series data for a matrix

inputk1 The pre-determined row dimension of the factor matrix

inputk2 The pre-determined column dimension of the factor matrix

iscentering The data is subtracted by its mean value

hzero Pre-determined parameter

**Value**

a list containing the following:

eigval1 estimated row dimension of the factor matrix

eigval2 estimated column dimension of the factor matrix

loading1 estimated left loading matrix

loading2 estimated right loading matrix

Ft Estimated factor matrix with pre-determined number of dimensions

Ft.all Sum of Ft

Et The estimated residual, by subtracting estimated signal term from the data

**Examples**

```
A <- 1:180
dim(A) <- c(3,3,20)
out = matrix_factor(A,3,3)
eig1 = out$eigval1
loading1 = out$loading1
Ft = out$Ft.all
```

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mfmda	<i>mfmda</i>
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**Description**

This is a wrapper for all approaches

**Usage**

```
mfmda(Yt, approach = "3", hzero = 1, iscentering = 1)
```

**Arguments**

approach	Select estimation approaches, 1 for noniterative approach with no NaNs, 2 for iterative approach with NaNs, 3 for iterative approach allowing NaNs.
hzero	Pre-determined parameter
iscentering	The data is subtracted by its mean value
Yc	Time Series data for a matrix

**Value**

The sample version of M matrix

**Examples**

```
A <- 1:180
dim(A) <- c(3,3,20)
M <- mfmda(A,"3",1,0)
```

mfmda.estqk

*mfmda.estqk***Description**

Compute the estimated number of factors and the corresponding eigen-space

**Usage**

```
mfmda.estqk(Mhat, inputk = 1)
```

**Arguments**

Mhat	The estimated value for matrix M
inputk	The pre-determined number of dimension of factor matrix

**Value**

The estimated number of factors to use, the corresponding estimated Q matrix, the eigenvalue, the estimated Q matrix with requested number of factors

**Examples**

```
A <- 1:180
dim(A) <- c(3,3,20)
M <- mfmda(A,"3",1,0)
inputk <- 3
eig.ans <- mfmda.estqk(M,inputk)
khat <- eig.ans$estk
Qhat <- eig.ans$Qhatestk
eigval <- eig.ans$eigval
Qhatinputk <- eig.ans$Qhatinputk
```

mfmda.na.iter

*mfmda.na.iter***Description**

The input data could have NaNs. The estimation approach is iterative.

**Usage**

```
mfmda.na.iter(Yc, hzero)
```

**Arguments**

Yc	Time Series data for a matrix allowing NaNs
hzero	Pre-determined parameter

**Value**

The sample version of M matrix

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mfmda.na.vec

*mfmda.na.vec*


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### Description

This approach is for the vector-valued estimation with NaNs.

### Usage

```
mfmda.na.vec(Yc, hzero)
```

### Arguments

Yc	Time Series data for a matrix(dimensions $n \times p \times q$ ), allowing NA input
hzero	Pre-scribed parameter h

### Value

The sample version of M matrix

---

mfmda.nona.iter

*mfmda.nona.iter*


---

### Description

The input data do not have zeros. The estimation approach is iterative.

### Usage

```
mfmda.nona.iter(Yc, hzero)
```

### Arguments

Yc	Time Series data for a matrix(dimensions $n \times p \times q$ ), no NA input allowed
hzero	Pre-scribed parameter

### Value

The sample version of M matrix



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mfmda.nona.noniter	<i>mfmda.nona.noiter</i>
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**Description**

The input data do not have zeros. The estimation approach is noniterative.

**Usage**

```
mfmda.nona.noniter(Yc, hzero)
```

**Arguments**

Yc	Time Series data for a matrix(dimensions n*p*q), no NA input allowed
hzero	Pre-scribed parameter

**Value**

The sample version of M matrix

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mfmda.nona.vec	<i>mfmda.nona.vec</i>
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**Description**

This approach is for the vector-valued estimation WITHOUT NaNs.

**Usage**

```
mfmda.nona.vec(Yc, hzero)
```

**Arguments**

Yc	Time Series data for a matrix(dimensions n*p*q), no NA input allowed
hzero	Pre-scribed parameter

**Value**

The sample version of M matrix

**Examples**

```
A <- 1:180
dim(A) <- c(3,3,20)
M <- mfmda.nona.vec(A,2)
```

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PlotNetwork_AB	<i>PlotNetwork_AB</i>
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**Description**

Plot the network graph

**Usage**

PlotNetwork\_AB(Ft, iterated\_A, iterated\_B = iterated\_A, labels = use2)

**Arguments**

- |            |                             |
|------------|-----------------------------|
| Ft         | The estimated factor matrix |
| iterated_A | The left loading matrix     |
| iterated_B | The right loading matrix    |
| labels     | The row labels              |

**Value**

Plot the network graph

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projection	<i>Kronecker Product Approximation</i>
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**Description**

Kronecker product approximation used in Projection Method of matrix-value time series.

**Usage**

projection(A, m1, m2, n1, n2)

**Arguments**

- |    |   |
|----|---|
| A  | m by n matrix such that $m = m1 * n1$ and $n = m2 * n2$ |
| m1 | ncol of A   |
| m2 | ncol of B   |
| n1 | nrow of A   |
| n2 | nrow of B   |

**Value**

a list containing two estimator (matrix)

**See Also**

[MAR1.projection](#)

**Examples**

```
A <- matrix(runif(6),ncol=2),
projection(A,3,3,2,2)
```

rearrange

*Rearrangement Operator***Description**

Rearrangement Operator used for projection method.

**Usage**

```
rearrange(A, m1, m2, n1, n2)
```

**Arguments**

A	m by n matrix such that $m = m1 * n1$ and $n = m2 * n2$
m1	ncol of A
m2	ncol of B
n1	nrow of A
n2	nrow of B

**Value**

rearengement matrix #'@seealso [MAR1.projection](#)

**Examples**

```
A <- matrix(runif(6),ncol=2),
B <- matrix(runif(6),ncol=2),
M <- kronecker(B,A)
rearrange(M,3,3,2,2) == t(as.vector(A)) %*% as.vector(B)
' TRUE '
```

var1

*Stacked vector AR(1) Model***Description**

vector AR(1) Model.

**Usage**

```
var1(xx)
```

**Arguments**

xx	$T * p * q$ matrix-valued time series
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**Value**

a list containing the following:

coef coefficient of the fitted VAR(1) model

res residual of the VAR(1) model

**Examples**

```
out.var1=var1(xx)
sum(out.var1$res**2)
```

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vector_factor	<i>vector_factor</i>
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**Description**

The main estimation function, vector version

**Usage**

```
vector_factor(Yt, inputk.vec, iscentering = 1, hzero = 1)
```

**Arguments**

Yt	Time Series data for a matrix
inputk.vec	The pre-determined dimensions of the factor matrix in vector
iscentering	The data is subtracted by its mean value
hzero	Pre-determined parameter

**Value**

a list containing the following:

eigval1 estimated dimensions of the factor matrix

loading estimated loading matrices

Ft Estimated factor matrix with pre-determined number of dimensions

Ft.all Sum of Ft

Et The estimated random term, by subtracting estimated signal term from the data

**Examples**

```
A <- 1:180
dim(A) <- c(3,3,20)
M <- mfmda(A,"3",1,0)
eig.ans <- vector_factor(M,3,0,1)
khat <- eig.ans$estk
Qhat <- eig.ans$Qhatestk
eigval <- eig.ans$eigval
Q1hatinputk <- eig.ans$Qhatinputk
```

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