Human Visual Perception

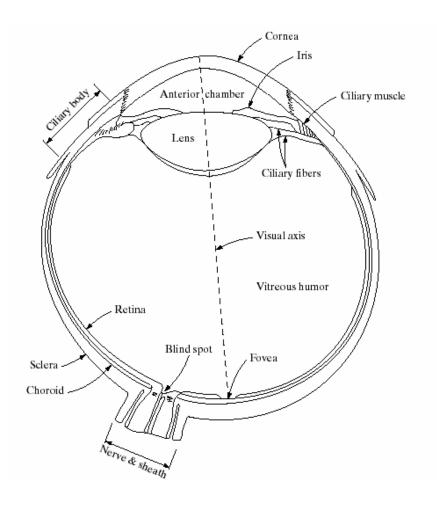


FIGURE 2.1 Simplified diagram of a cross section of the human eye.

The Human Eye

- Diameter: 20 mm
- 3 membranes enclose the eye
 - Cornea & sclera
 - Choroid
 - Retina

The Choroid

- The choroid contains blood vessels for eye nutrition and is heavily pigmented to reduce extraneous light entrance and backscatter.
- It is divided into the ciliary body and the iris diaphragm, which controls the amount of light that enters the pupil (2 mm ~ 8 mm).

The Lens

 The lens is made up of fibrous cells and is suspended by fibers that attach it to the ciliary body.

• It is slightly yellow and absorbs approx. 8% of the visible light spectrum.

The Retina

- The retina lines the entire posterior portion.
- Discrete light receptors are distributed over the surface of the retina:
 - cones (6-7 million per eye) and
 - rods (75-150 million per eye)

Cones

- Cones are located in the fovea and are sensitive to color.
- Each one is connected to its own nerve end.
- Cone vision is called *photopic* (or bright-light vision).

Rods

- Rods are giving a general, overall picture of the field of view and are not involved in color vision.
- Several rods are connected to a single nerve and are sensitive to low levels of illumination (*scotopic* or dim-light vision).

Receptor Distribution

- The distribution of receptors is radially symmetric about the fovea.
- Cones are most dense in the center of the fovea while rods increase in density from the center out to approximately 20% off axis and then decrease.

Cones & Rods

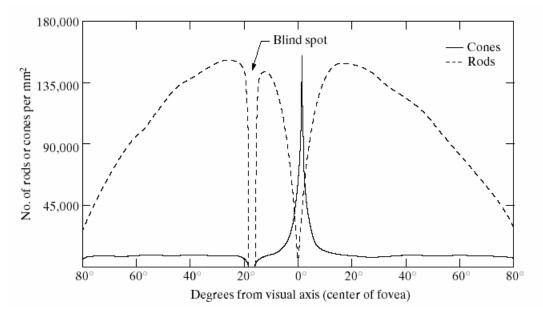


FIGURE 2.2 Distribution of rods and cones in the retina.

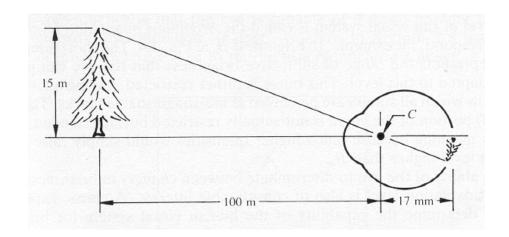
The Fovea

- The fovea is circular (1.5 mm in diameter) but can be assumed to be a square sensor array (1.5 mm x 1.5 mm).
- The density of cones: 150,000 elements/mm²
 337,000 for the fovea.
- A CCD imaging chip of medium resolution needs 5 mm x 5 mm for this number of elements

- The eye lens (if compared to an optical lens) is flexible.
- It gets controlled by the fibers of the ciliary body and to focus on distant objects it gets flatter (and vice versa).

- Distance between the center of the lens and the retina (*focal length*):
 - varies from 17 mm to 14 mm (refractive power of lens goes from minimum to maximum).
- Objects farther than 3 m use minimum refractive lens powers (and vice versa).

- Example:
 - Calculation of retinal image of an object



$$\frac{15}{100} = \frac{x}{17}$$

$$x = 2.55mm$$

- Perception takes place by the relative excitation of light receptors.
- These receptors transform radiant energy into electrical impulses that are ultimately decoded by the brain.

- Range of light intensity levels to which HVS (human visual system) can adapt: on the order of 10¹⁰.
- Subjective brightness (i.e. intensity as perceived by the HVS) is a logarithmic function of the light intensity incident on the eye.

- The HVS cannot operate over such a range simultaneously.
- For any given set of conditions, the current sensitivity level of HVS is called the brightness adaptation level.

 The eye also discriminates between changes in brightness at any specific adaptation level.

 $\frac{\Delta I_c}{I}$ \rightarrow Weber ratio

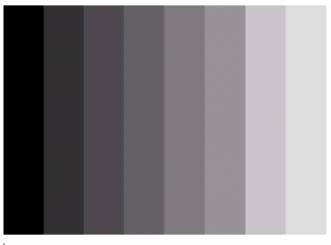
Where: △I_c: the increment of illumination discriminable 50% of the time and I: background illumination

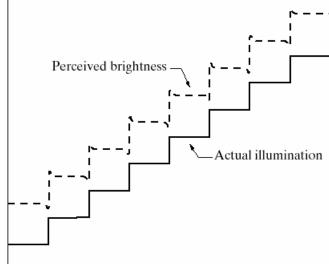
- Small values of Weber ratio mean good brightness discrimination (and vice versa).
- At low levels of illumination brightness discrimination is poor (rods) and it improves significantly as background illumination increases (cones).

- The typical observer can discern one to two dozen different intensity changes
 - i.e. the number of different intensities a person can see at any one point in a monochrome image

- Overall intensity discrimination is broad due to different set of incremental changes to be detected at each new adaptation level.
- Perceived brightness is not a simple function of intensity
 - Scalloped effect, Mach band pattern
 - Simultaneous contrast

Perceived Brightness



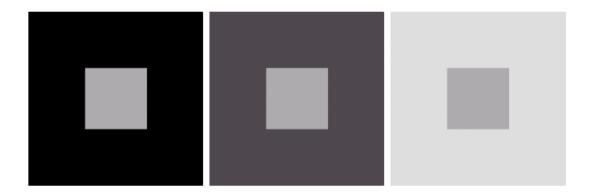


1

FIGURE 2.7

(a) An example showing that perceived brightness is not a simple function of intensity. The relative vertical positions between the two profiles in (b) have no special significance; they were chosen for clarity.

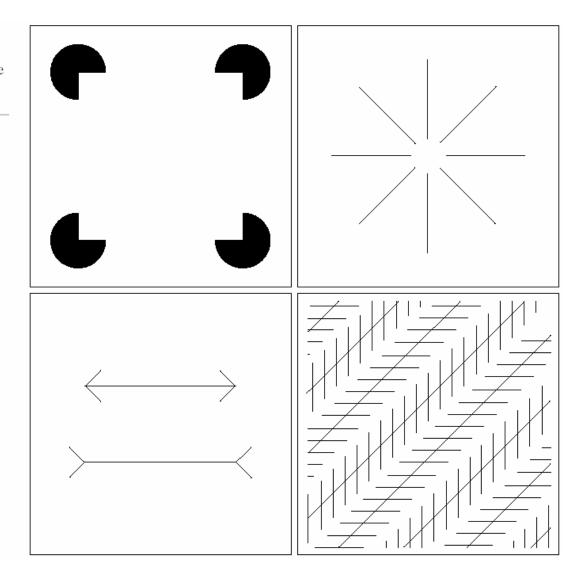
Simultaneous Contrast



Illusions

a b c d

FIGURE 2.9 Some well-known optical illusions.



- Image: a 2-D light-intensity function f(x,y)
- The value of f at $(x,y) \rightarrow$ the intensity (brightness) of the image at that point
- $0 < f(x,y) < \infty$

Digital Image Acquisition

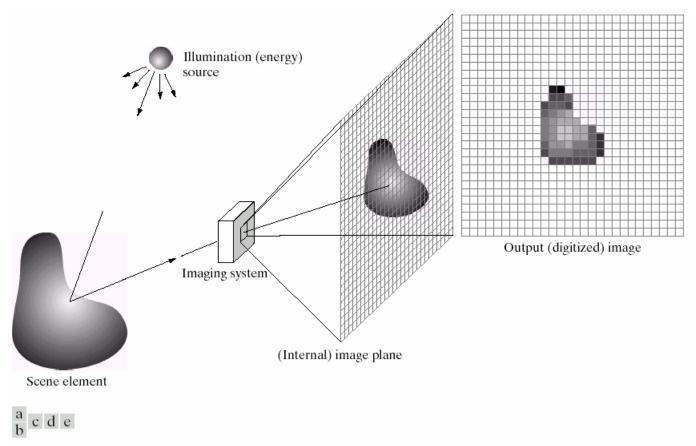


FIGURE 2.15 An example of the digital image acquisition process. (a) Energy ("illumination") source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

- Nature of f(x,y):
 - The amount of source light incident on the scene being viewed
 - The amount of light reflected by the objects in the scene

• Illumination & reflectance components:

- Sample values of r(x,y):
 - 0.01: black velvet
 - 0.93: snow
- Sample values of i(x,y):
 - 9000 foot-candles: sunny day
 - 1000 foot-candles: cloudy day
 - 0.01 foot-candles: full moon

 Intensity of a monochrome image f at (x₀, y₀): gray level I of the image at that point I=f(x₀, y₀)

- $L_{min} \le I \le L_{max}$
 - Where L_{min}: positive

L_{max}: finite

- In practice:
 - $L_{min} = i_{min} r_{min}$ and
 - $L_{max} = i_{max} r_{max}$
- E.g. for indoor image processing:
 - $-L_{\min} \approx 10 \qquad L_{\max} \approx 1000$
- [L_{min}, L_{max}] : gray scale
 - Often shifted to $[0,L-1] \rightarrow I=0$: black

I=L-1: white

Sampling & Quantization

- The spatial and amplitude digitization of f(x,y) is called:
 - image sampling when it refers to spatial coordinates (x,y) and
 - gray-level quantization when it refers to the amplitude.

Digital Image

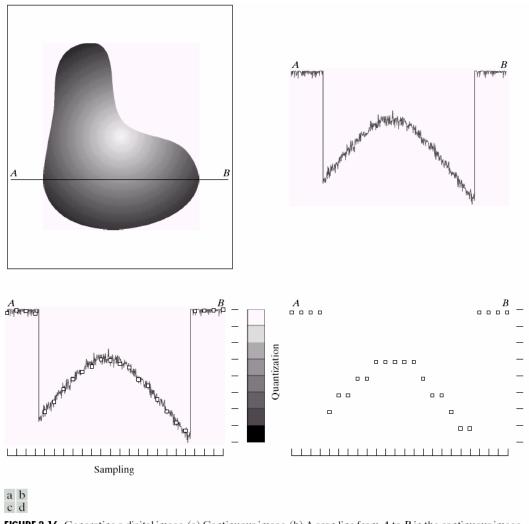
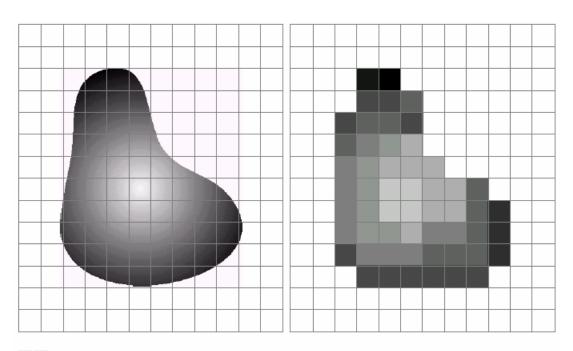


FIGURE 2.16 Generating a digital image. (a) Continuous image. (b) A scan line from A to B in the continuous image, used to illustrate the concepts of sampling and quantization. (c) Sampling and quantization. (d) Digital scan line.

Sampling and Quantization



a b

FIGURE 2.17 (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.

A Digital Image

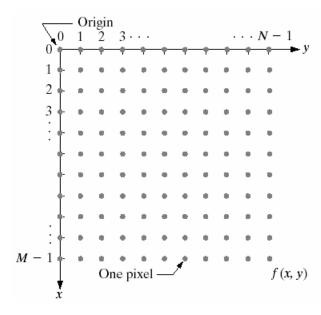


FIGURE 2.18

Coordinate convention used in this book to represent digital images.

Sampling & Quantization

$$f(x,y) = \begin{bmatrix} f(0,0) & f(0,1) & \dots & f(0,M-1) \\ f(1,0) & \dots & \dots & f(1,M-1) \\ \dots & \dots & \dots & \dots \\ f(N-1,0) & f(N-1,1) & \dots & f(N-1,M-1) \end{bmatrix}$$
Digital Image
Image Elements
(Pixels)

Sampling & Quantization

- Important terms for future discussion:
 - Z: set of real integers
 - R: set of real numbers

- Sampling: partitioning xy plane into a grid
 - the coordinate of the center of each grid is a pair of elements from the Cartesian product Z x Z (Z²)
- Z² is the set of all ordered pairs of elements (a,b) with a and b being integers from Z.

- f(x,y) is a digital image if:
 - (x,y) are integers from Z^2 and
 - f is a function that assigns a gray-level value (from R) to each distinct pair of coordinates (x,y) [quantization]
- Gray levels are usually integers
 - then Z replaces R

- The digitization process requires decisions about:
 - values for N,M (where N x M: the image array)
 and
 - the number of discrete gray levels allowed for each pixel.

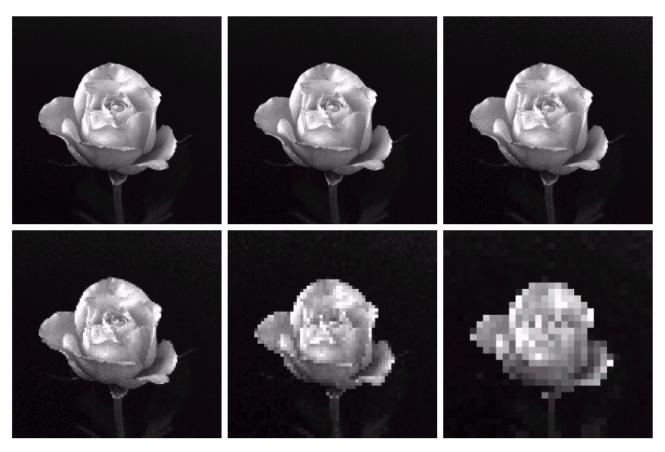
 Usually, in DIP these quantities are integer powers of two:

$$N=2^n$$
 and $G=2^k$ \downarrow number of gray levels

 Another assumption is that the discrete levels are equally spaced between 0 and L-1 in the gray scale.

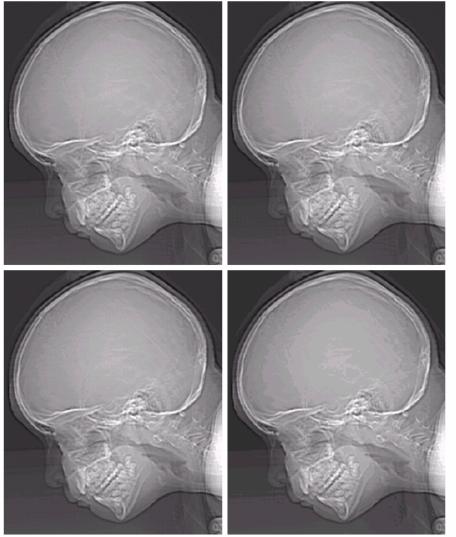


FIGURE 2.19 A 1024 \times 1024, 8-bit image subsampled down to size 32 \times 32 pixels. The number of allowable gray levels was kept at 256.



a b c d e f

FIGURE 2.20 (a) 1024×1024 , 8-bit image. (b) 512×512 image resampled into 1024×1024 pixels by row and column duplication. (c) through (f) 256×256 , 128×128 , 64×64 , and 32×32 images resampled into 1024×1024 pixels.

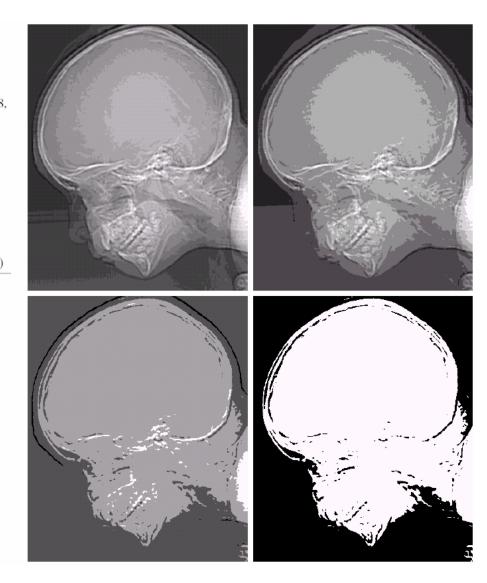


a b c d

FIGURE 2.21
(a) 452 × 374,
256-level image.
(b)–(d) Image
displayed in 128,
64, and 32 gray
levels, while
keeping the
spatial resolution
constant.

e f g h

FIGURE 2.21
(Continued)
(e)-(h) Image
displayed in 16, 8,
4, and 2 gray
levels. (Original
courtesy of
Dr. David
R. Pickens,
Department of
Radiology &
Radiological
Sciences,
Vanderbilt
University
Medical Center.)



 If b is the number of bits required to store a digitized image then:

```
- b = N \times M \times k (if M=N, then b=N^2k)
```

Storage

TABLE 2.1 Number of storage bits for various values of N and k.

N/k	1(L=2)	2(L=4)	3(L = 8)	4(L=16)	5(L = 32)	6(L = 64)	7(L = 128)	8(L=256)
32	1,024	2,048	3,072	4,096	5,120	6,144	7,168	8,192
64	4,096	8,192	12,288	16,384	20,480	24,576	28,672	32,768
128	16,384	32,768	49,152	65,536	81,920	98,304	114,688	131,072
256	65,536	131,072	196,608	262,144	327,680	393,216	458,752	524,288
512	262,144	524,288	786,432	1,048,576	1,310,720	1,572,864	1,835,008	2,097,152
1024	1,048,576	2,097,152	3,145,728	4,194,304	5,242,880	6,291,456	7,340,032	8,388,608
2048	4,194,304	8,388,608	12,582,912	16,777,216	20,971,520	25,165,824	29,369,128	33,554,432
4096	16,777,216	33,554,432	50,331,648	67,108,864	83,886,080	100,663,296	117,440,512	134,217,728
8192	67,108,864	134,217,728	201,326,592	268,435,456	335,544,320	402,653,184	469,762,048	536,870,912

- How many samples and gray levels are required for a good approximation?
 - Resolution (the degree of discernible detail) of an image depends on sample number and gray level number.
 - i.e. the more these parameters are increased, the closer the digitized array approximates the original image.

- How many samples and gray levels are required for a good approximation? (cont.)
 - But: storage & processing requirements increase rapidly as a function of N, M, and k

- Different versions (images) of the same object can be generated through:
 - Varying N, M numbers
 - Varying k (number of bits)
 - Varying both

- Isopreference curves (in the Nm plane)
 - Each point: image having values of N and k equal to the coordinates of this point
 - Points lying on an isopreference curve correspond to images of equal subjective quality.







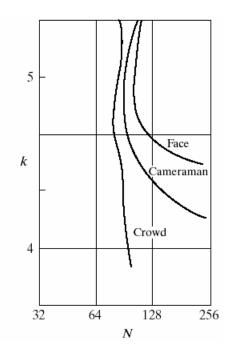
a b c

FIGURE 2.22 (a) Image with a low level of detail. (b) Image with a medium level of detail. (c) Image with a relatively large amount of detail. (Image (b) courtesy of the Massachusetts Institute of Technology.)

Isopreference Curves

FIGURE 2.23

Representative isopreference curves for the three types of images in Fig. 2.22.



• Conclusions:

- Quality of images increases as N & k increase
- Sometimes, for fixed N, the quality improved by decreasing k (increased contrast)
- For images with large amounts of detail, few gray levels are needed

Nonuniform Sampling & Quantization

- An adaptive sampling scheme can improve the appearance of an image, where the sampling would consider the characteristics of the image.
 - i.e. fine sampling in the neighborhood of sharp gray-level transitions (e.g. boundaries)
 - Coarse sampling in relatively smooth regions
- Considerations: boundary detection, detail content

Nonuniform Sampling & Quantization

- Similarly: nonuniform quantization process
- In this case:
 - few gray levels in the neighborhood of boundaries
 - more in regions of smooth gray-level variations (reducing thus false contours)

Some Basic Relationships Between Pixels

• Definitions:

- f(x,y): digital image
- Pixels: q, p
- Subset of pixels of f(x,y): S

Neighbors of a Pixel

 A pixel p at (x,y) has 2 horizontal and 2 vertical neighbors:

$$-(x+1,y), (x-1,y), (x,y+1), (x,y-1)$$

 This set of pixels is called the 4-neighbors of p: N₄(p)

Neighbors of a Pixel

The 4 diagonal neighbors of p are: (N_D(p))

$$-(x+1,y+1), (x+1,y-1), (x-1,y+1), (x-1,y-1)$$

• $N_4(p) + N_D(p) \rightarrow N_8(p)$: the 8-neighbors of p

Connectivity

- Connectivity between pixels is important:
 - Because it is used in establishing boundaries of objects and components of regions in an image

Connectivity

- Two pixels are connected if:
 - They are neighbors (i.e. adjacent in some sense e.g. N₄(p), N₈(p), ...)
 - Their gray levels satisfy a specified criterion of similarity (e.g. equality, ...)
- V is the set of gray-level values used to define adjacency (e.g. V={1} for adjacency of pixels of value 1)

- We consider three types of adjacency:
 - 4-adjacency: two pixels p and q with values from
 V are 4-adjacent if q is in the set N₄(p)
 - 8-adjacency: p & q are 8- adjacent if q is in the set N₈(p)

- The third type of adjacency:
 - m-adjacency: p & q with values from V are madjacent if
 - q is in $N_4(p)$ or
 - q is in $N_D(p)$ and the set $N_4(p) \cap N_4(q)$ has no pixels with values from V

 Mixed adjacency is a modification of 8adjacency and is used to eliminate the multiple path connections that often arise when 8-adjacency is used.

• Two image subsets \$1 and \$2 are adjacent if some pixel in \$1 is adjacent to some pixel in \$2.

Path

- A path (curve) from pixel p with coordinates (x,y) to pixel q with coordinates (s,t) is a sequence of distinct pixels:
 - $(x_0, y_0), (x_1, y_1), ..., (x_n, y_n)$
 - where $(x_0, y_0) = (x, y)$, $(x_n, y_n) = (s, t)$, and (x_i, y_i) is adjacent to (x_{i-1}, y_{i-1}) , for $1 \le i \le n$; n is the length of the path.
- If $(x_0, y_0) = (x_n, y_n)$: a closed path

Paths

- 4-, 8-, m-paths can be defined depending on the type of adjacency specified.
- If p,q ∈ S, then q is connected to p in S if there is a path from p to q consisting entirely of pixels in S.

Connectivity

 For any pixel p in S, the set of pixels in S that are connected to p is a connected component of S.

 If S has only one connected component then S is called a connected set.

Boundary

- R a subset of pixels: R is a region if R is a connected set.
- Its boundary (border, contour) is the set of pixels in R that have at least one neighbor not in R
- Edge can be the region boundary (in binary images)

 For pixels p,q,z with coordinates (x,y), (s,t), (u,v), D is a distance function or metric if:

```
- D(p,q) \ge 0  (D(p,q)=0 \text{ iff } p=q)
```

- D(p,q) = D(q,p) and
- $D(p,z) \le D(p,q) + D(q,z)$

• Euclidean distance:

-
$$D_e(p,q) = [(x-s)^2 + (y-t)^2]^{1/2}$$

- Points (pixels) having a distance less than or equal to r from (x,y) are contained in a disk of radius r centered at (x,y).

• D₄ distance (city-block distance):

$$- D_4(p,q) = |x-s| + |y-t|$$

- forms a diamond centered at (x,y)
- e.g. pixels with D₄≤2 from p

• D₈ distance (chessboard distance):

```
- D_8(p,q) = max(|x-s|,|y-t|)
```

- Forms a square centered at p
- e.g. pixels with D₈≤2 from p

D₄ and D₈ distances between p and q are independent of any paths that exist between the points because these distances involve only the coordinates of the points (regardless of whether a connected path exists between them).

 However, for m-connectivity the value of the distance (length of path) between two pixels depends on the values of the pixels along the path and those of their neighbors.

• e.g. assume $p_1, p_2, p_4 = 1$

$$p_1, p_2, p_4 = 1$$

 p_1 , p_3 = can have either 0 or 1

If only connectivity of pixels valued 1 is allowed, and p₁ and p₃ are 0, the mdistance between p and p₄ is 2.

If either p_1 or p_3 is 1, the distance is 3.

If both p₁ and p₃ are 1, the distance is 4 $(pp_1p_2p_3p_4)$