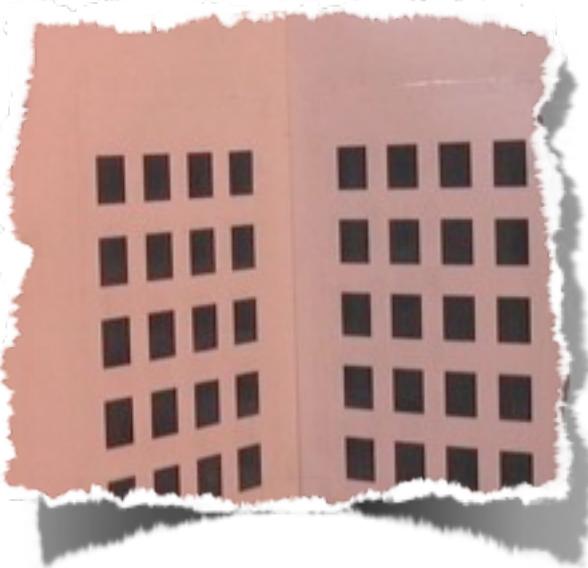
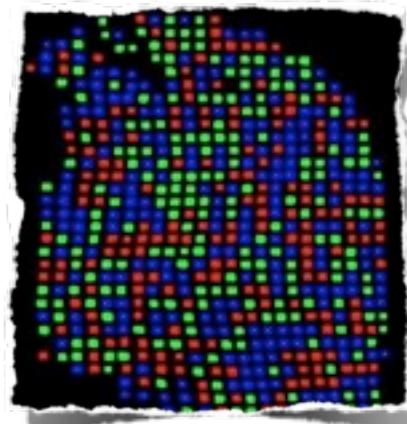
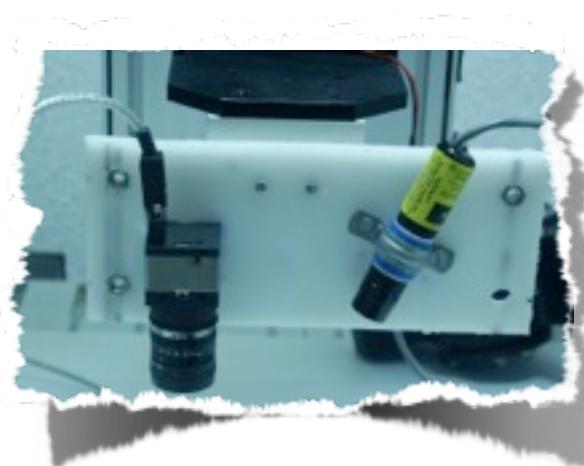


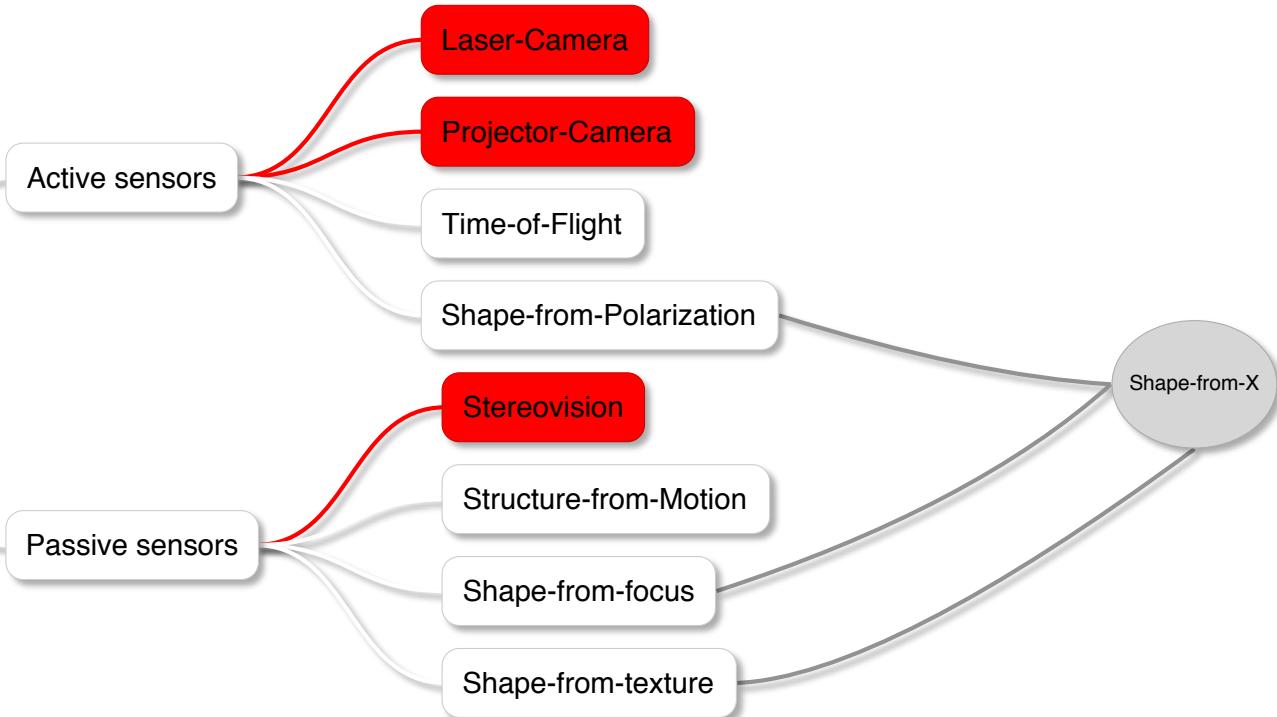
An Introduction to 3D Vision

David Fofi





3D Sensing

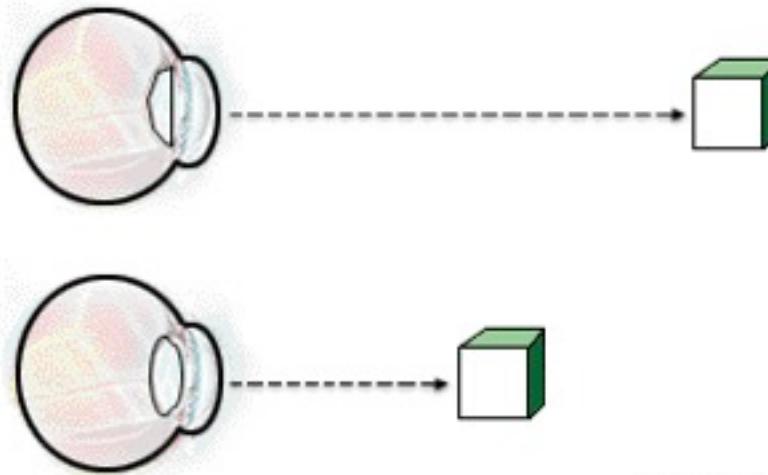


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Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.

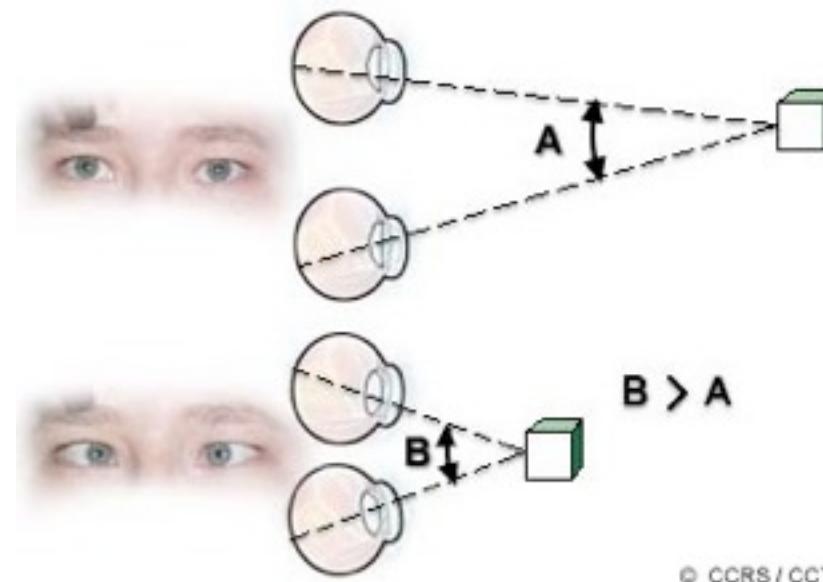


© CCRS / CCT

Accommodation : adapting the focal length of the crystalline lens
minor clue

Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.



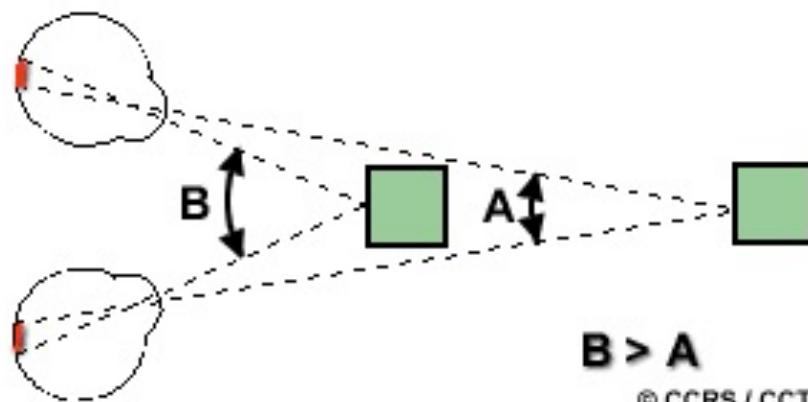
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Convergence : angle between the line of sight of each eye
minor clue

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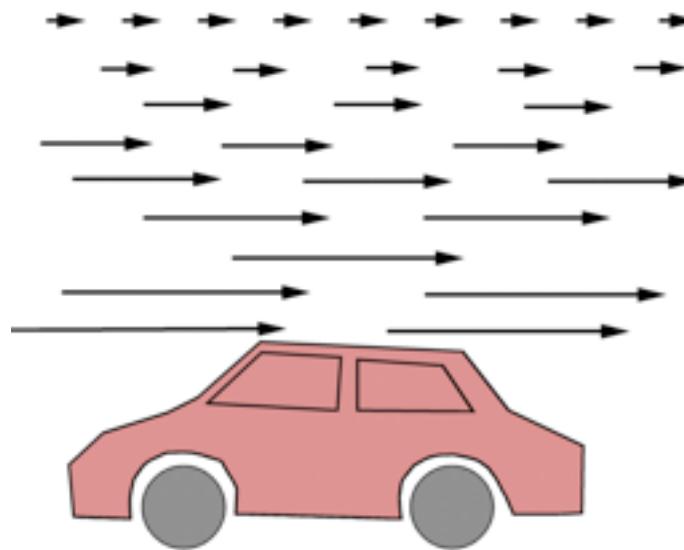


Disparity : differences between two images of the same object
major clue

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Depth perception relies on 10 different clues:

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Motion parallax: distant objects appear to move slowly compared to near objects

Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.

Size of the retinal image: the bigger
the closer



Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.



Linear perspective: gradually reducing the image size as the distance of the object increases

Depth perception relies on 10 different clues:

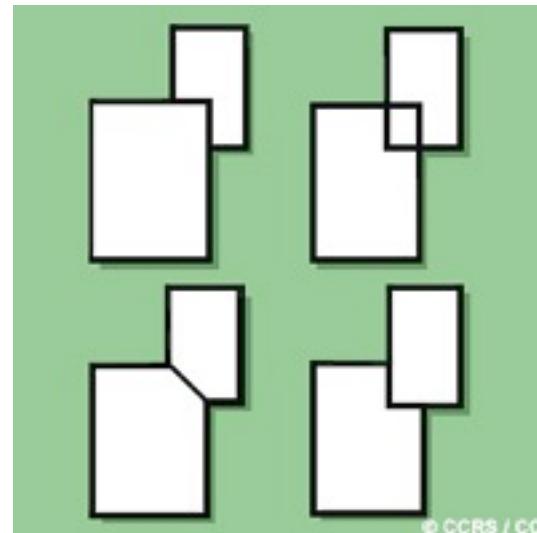
- 4 are physiological clues;
- 6 are psychological clues.



Aerial perspective : blur appearing with the distance

Depth perception relies on 10 different clues:

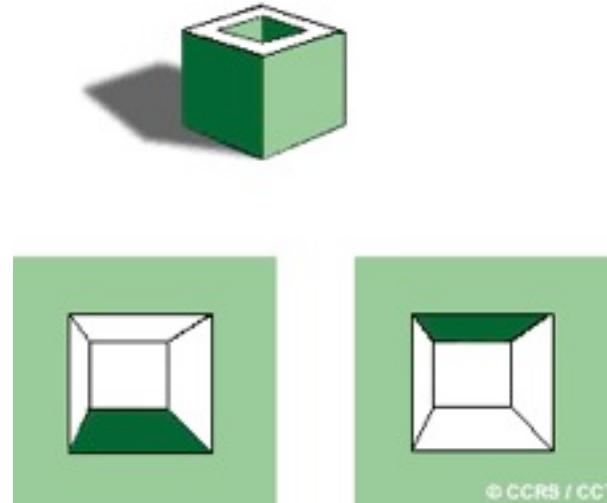
- 4 are physiological clues;
- 6 are psychological clues.



Occlusion: continuous outline appears closer to the observer

Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.

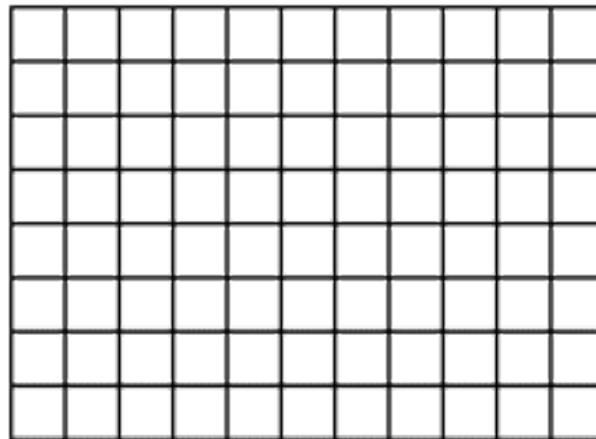


Lightning and shading: impression of concavity/convexity caused by...

Depth perception relies on 10 different clues:

- 4 are physiological clues;
- 6 are psychological clues.

Texture gradient: fine details on nearby objects can be seen clearly, whereas such details are not visible on faraway objects





What about computer vision?

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What about computer vision?



Focus/defocus

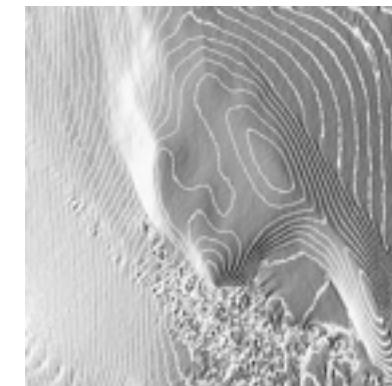
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What about computer vision?



Focus/defocus

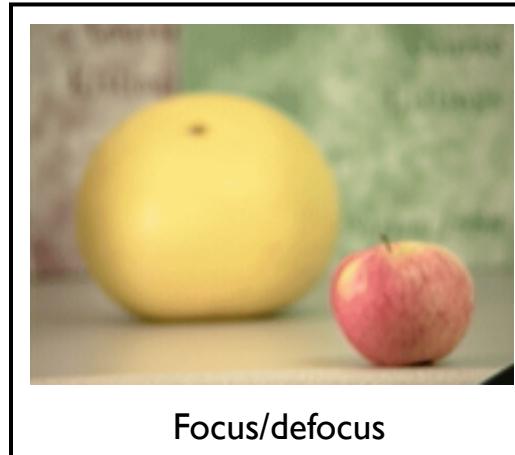


Shadow

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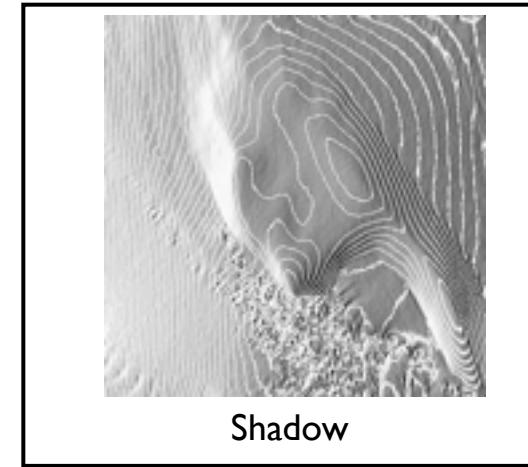
What about computer vision?



Focus/defocus



Stereovision/multiple-view



Shadow

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What about computer vision?



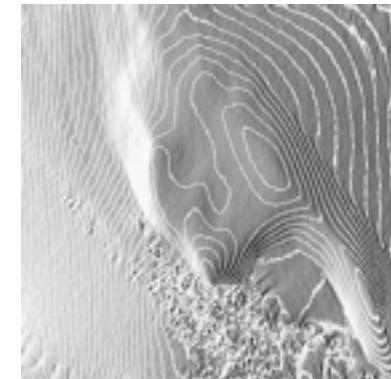
Focus/defocus



Stereovision/multiple-view



Structured light

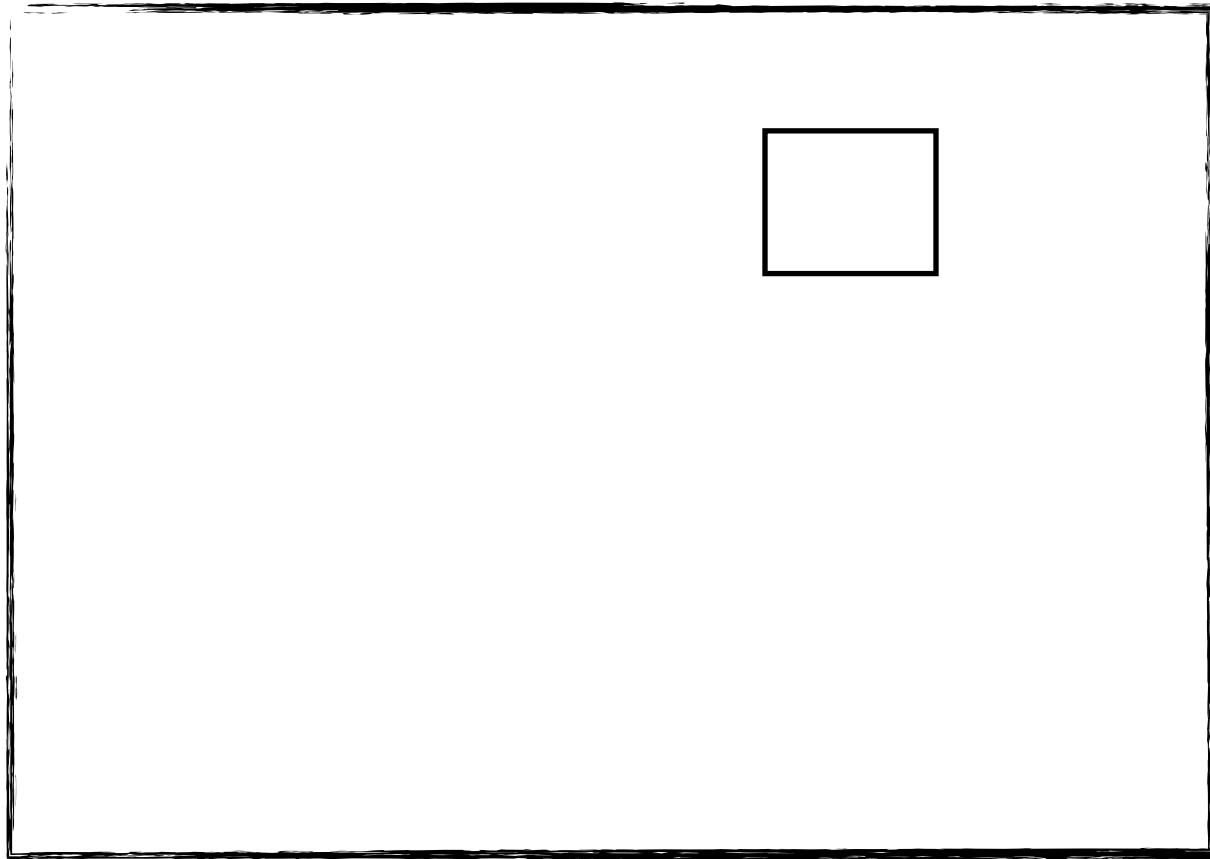


Shadow

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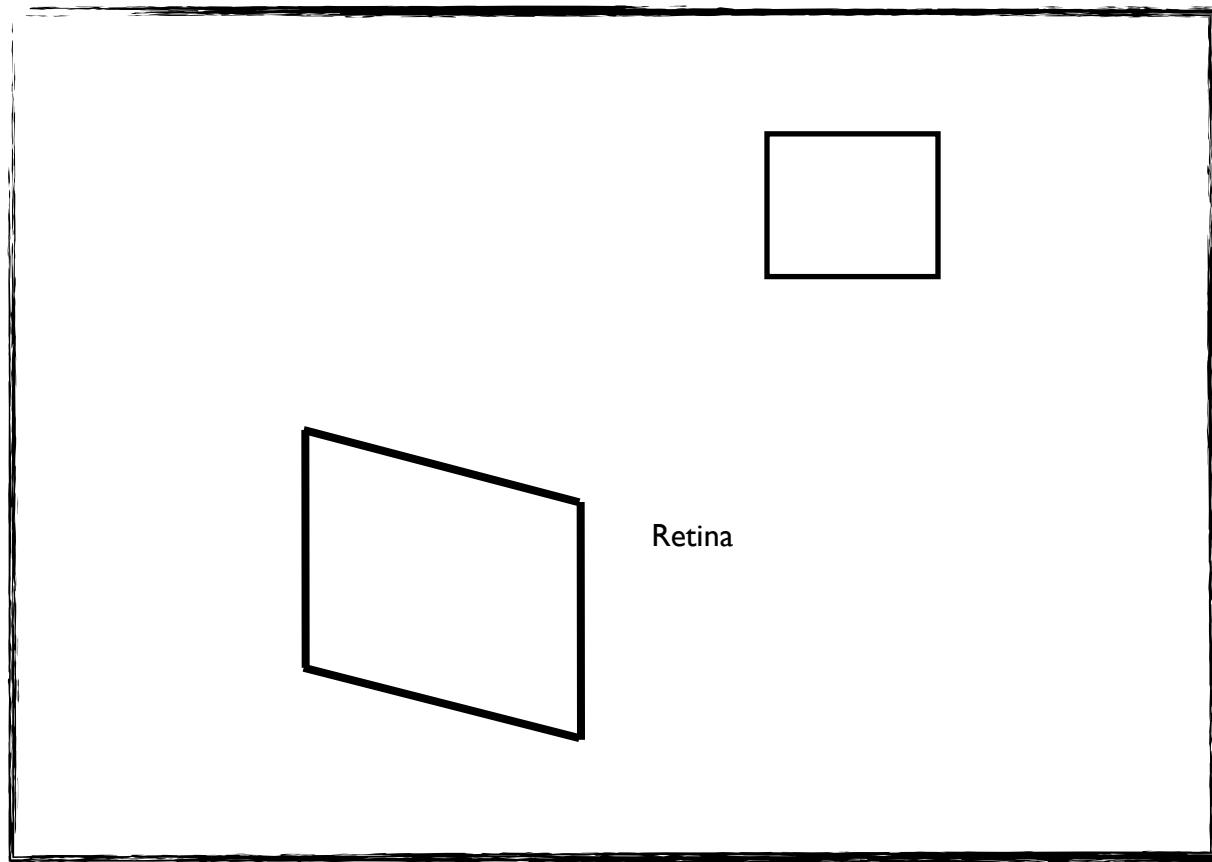
Pinhole model



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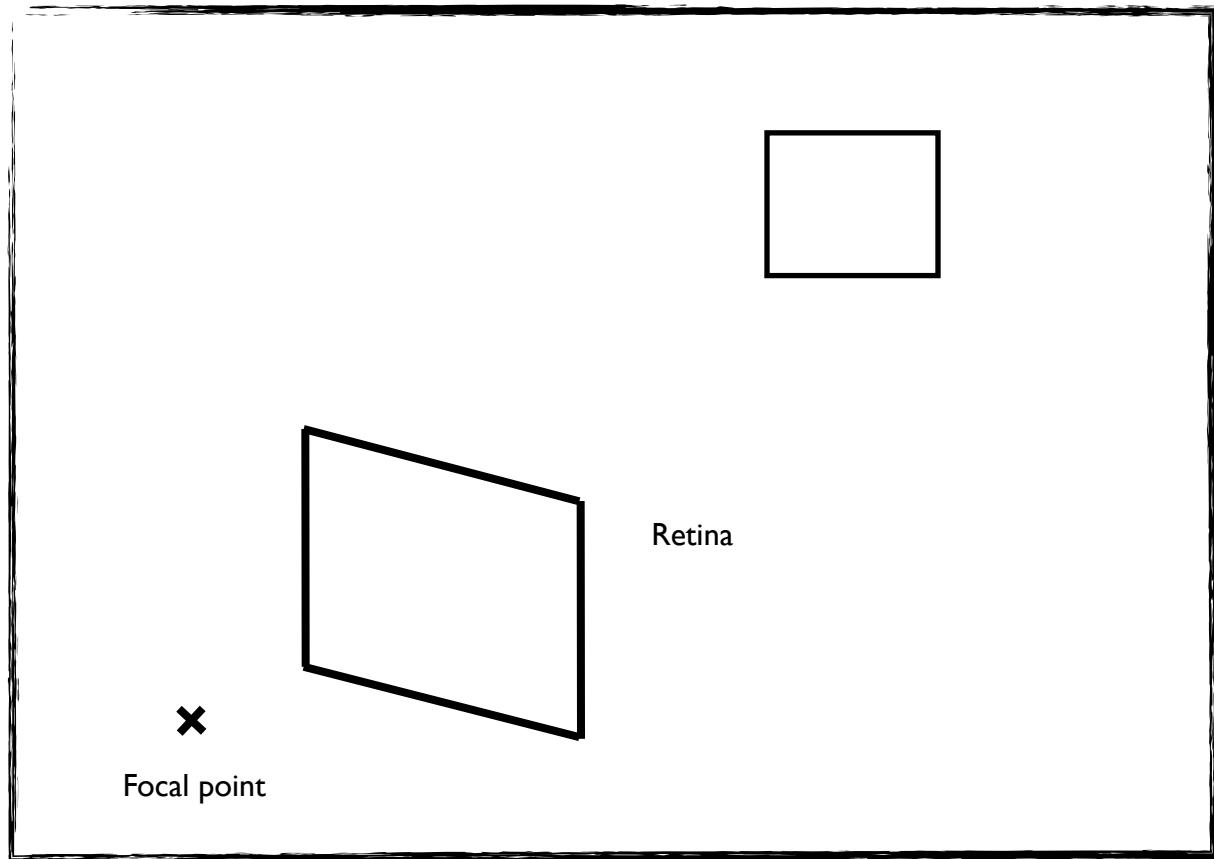
Pinhole model



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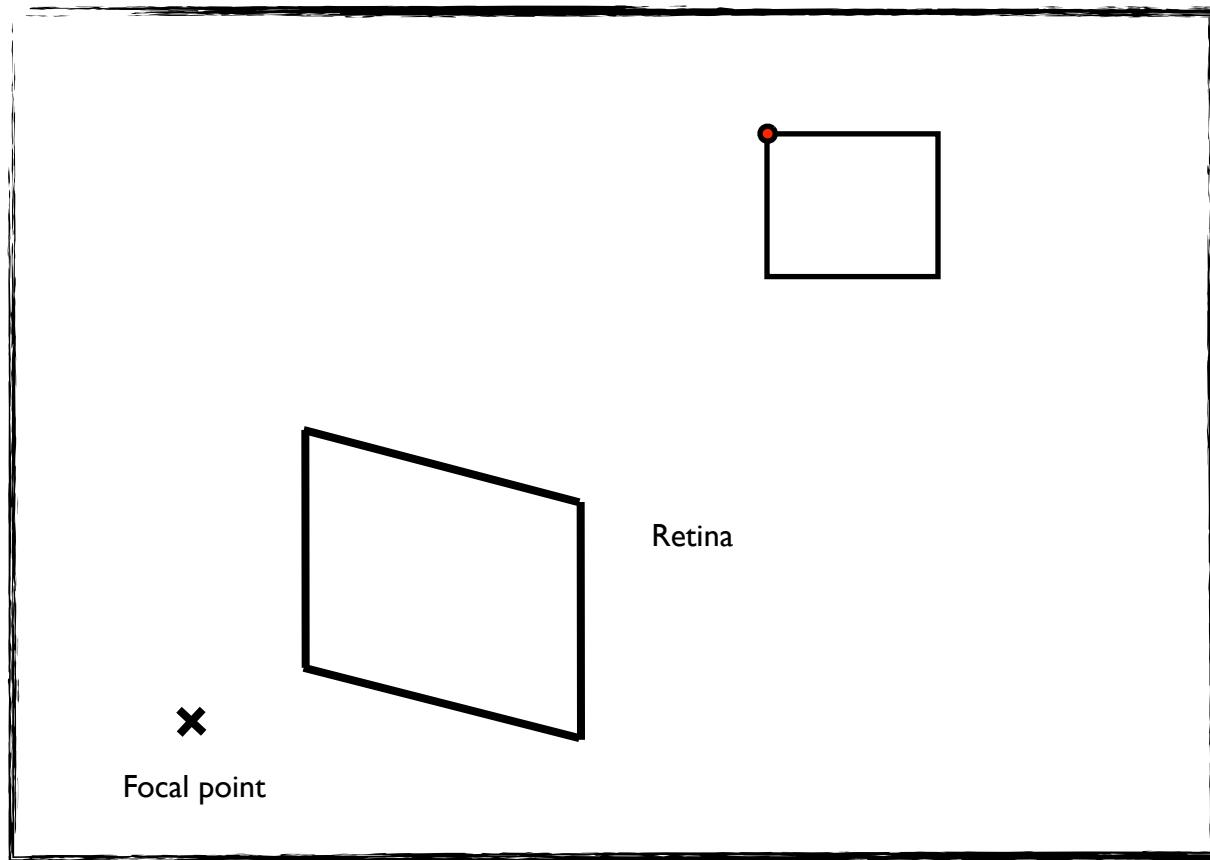
Pinhole model



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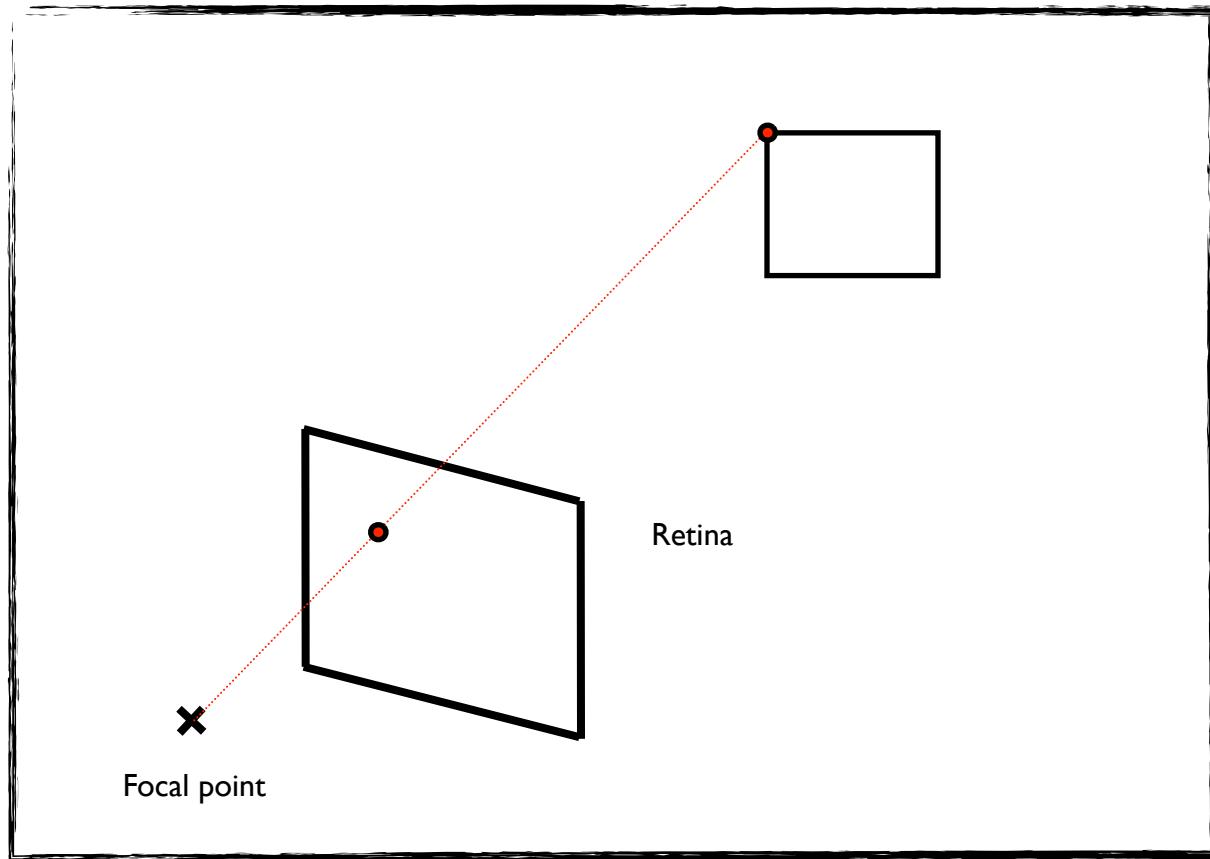


Pinhole model





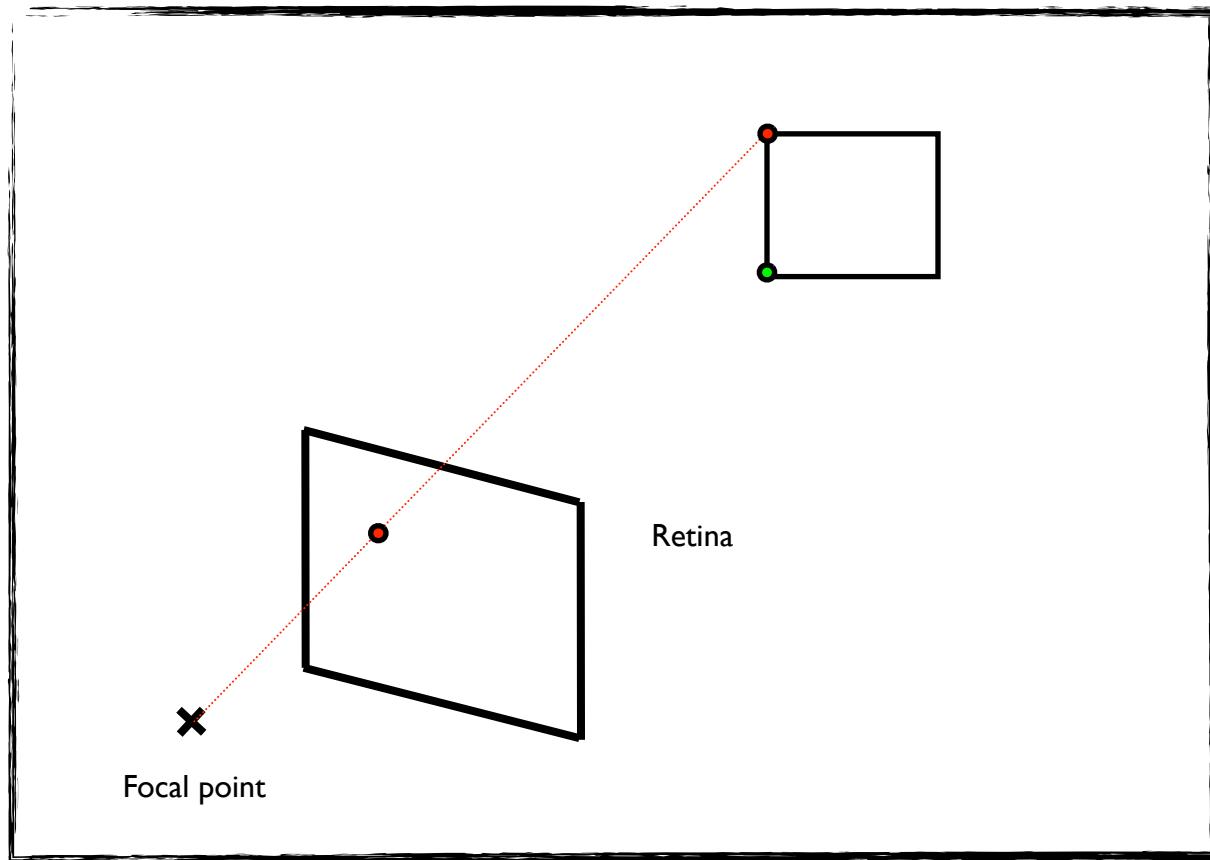
Pinhole model



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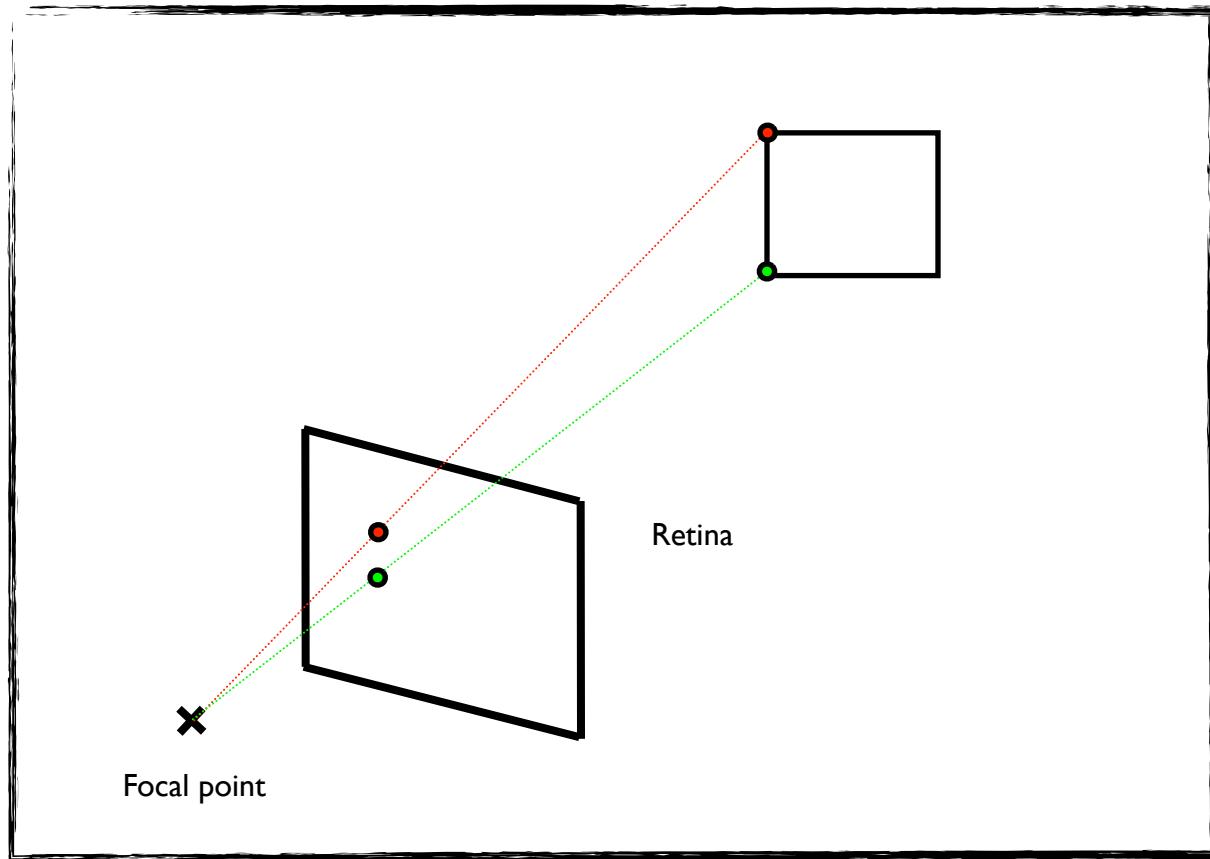
Pinhole model



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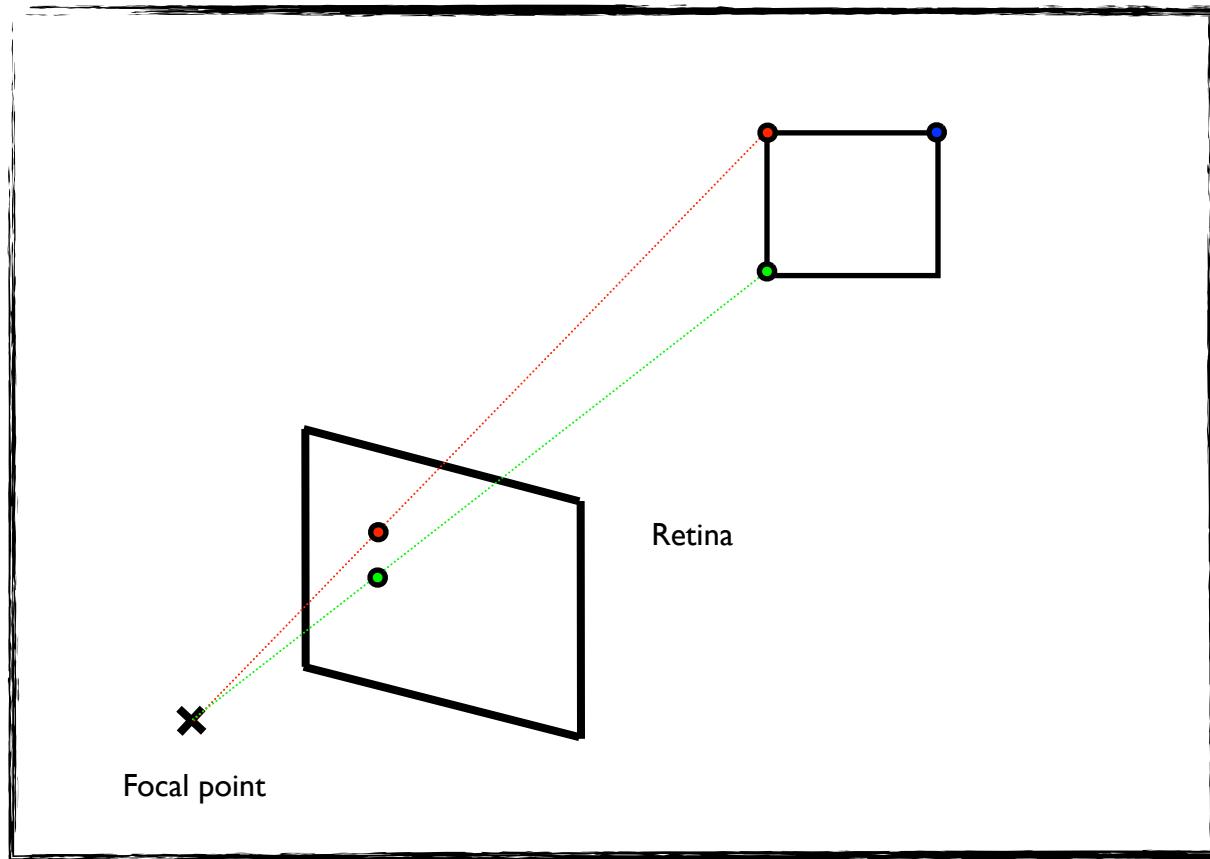
Pinhole model



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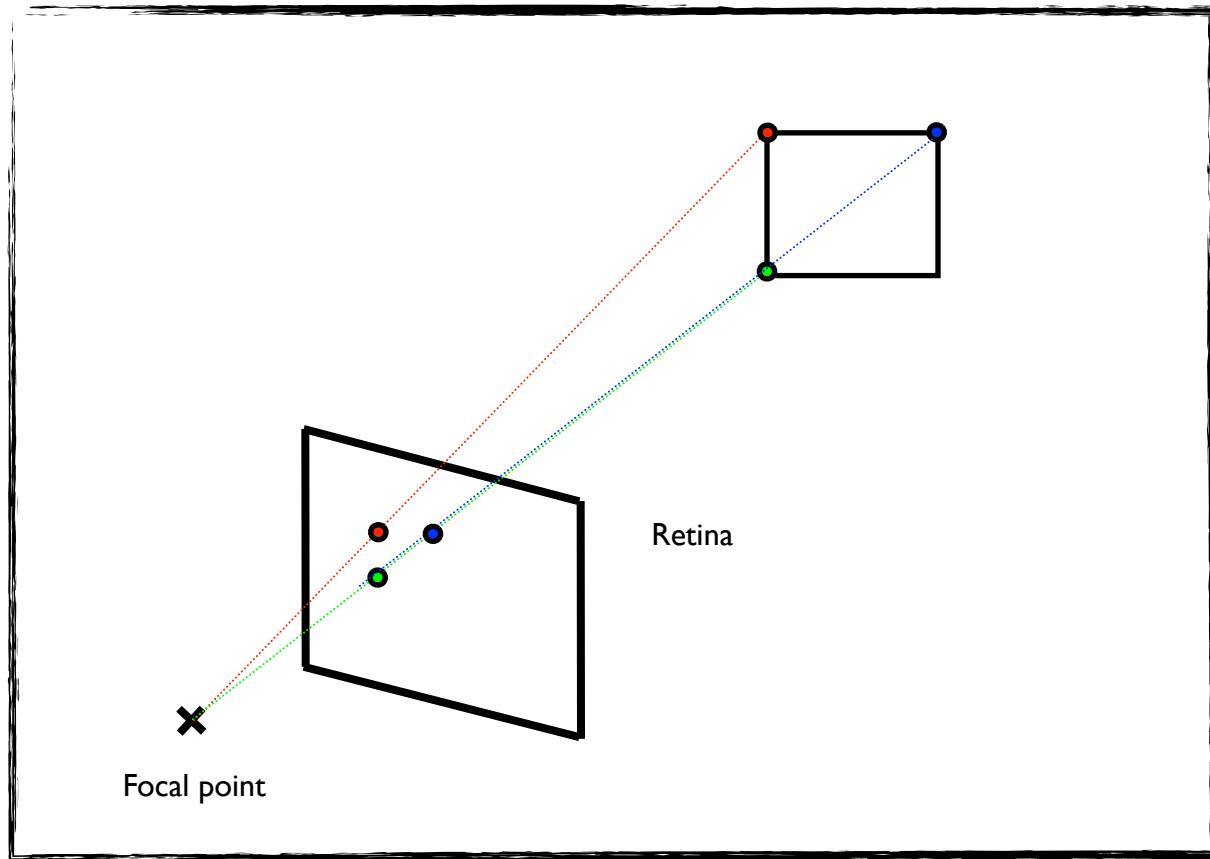
Pinhole model



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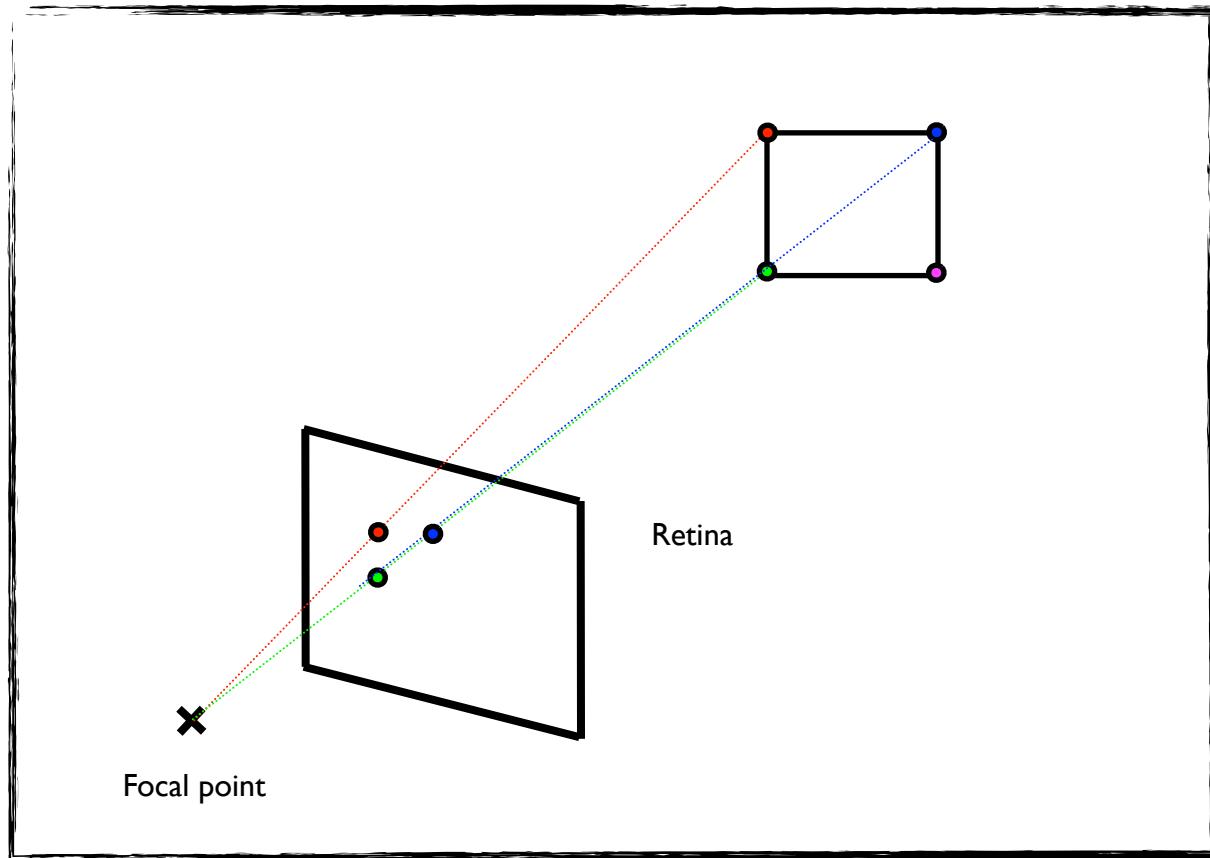
Pinhole model



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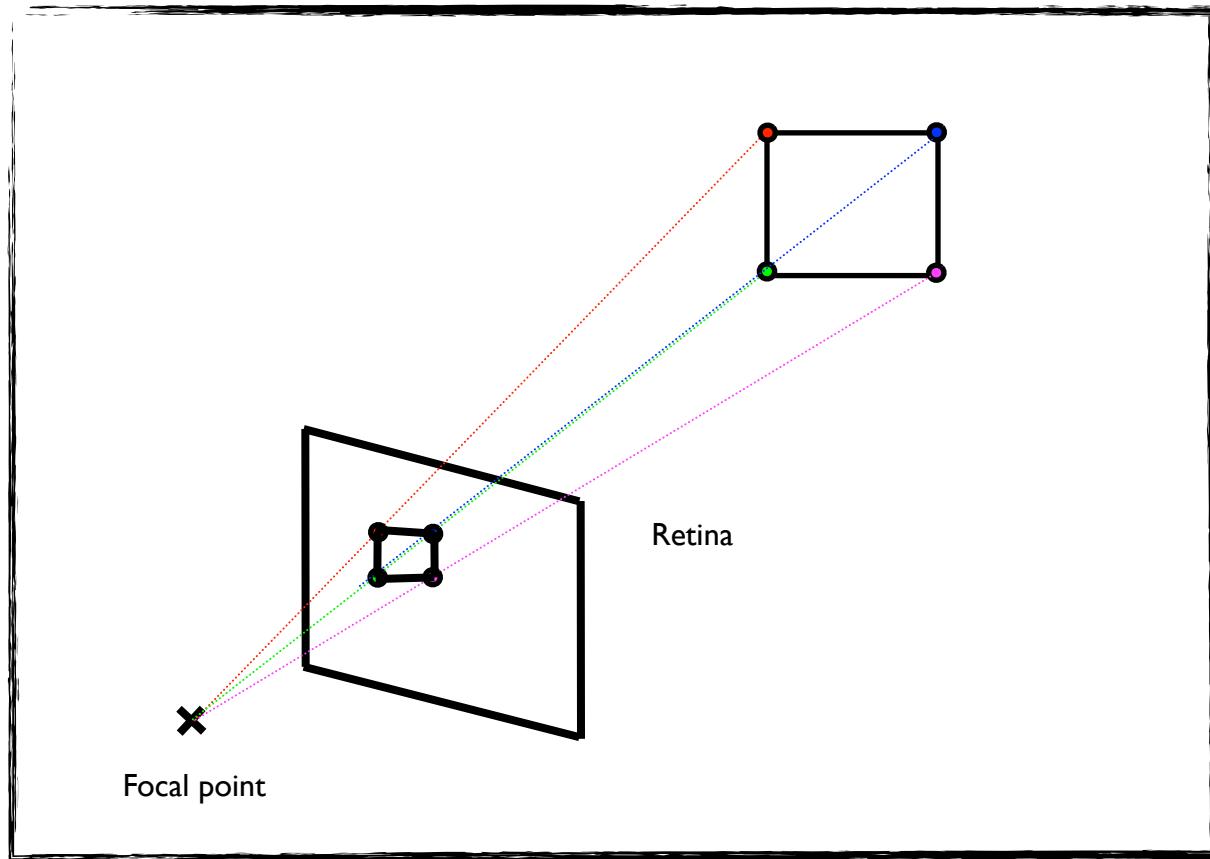
Pinhole model



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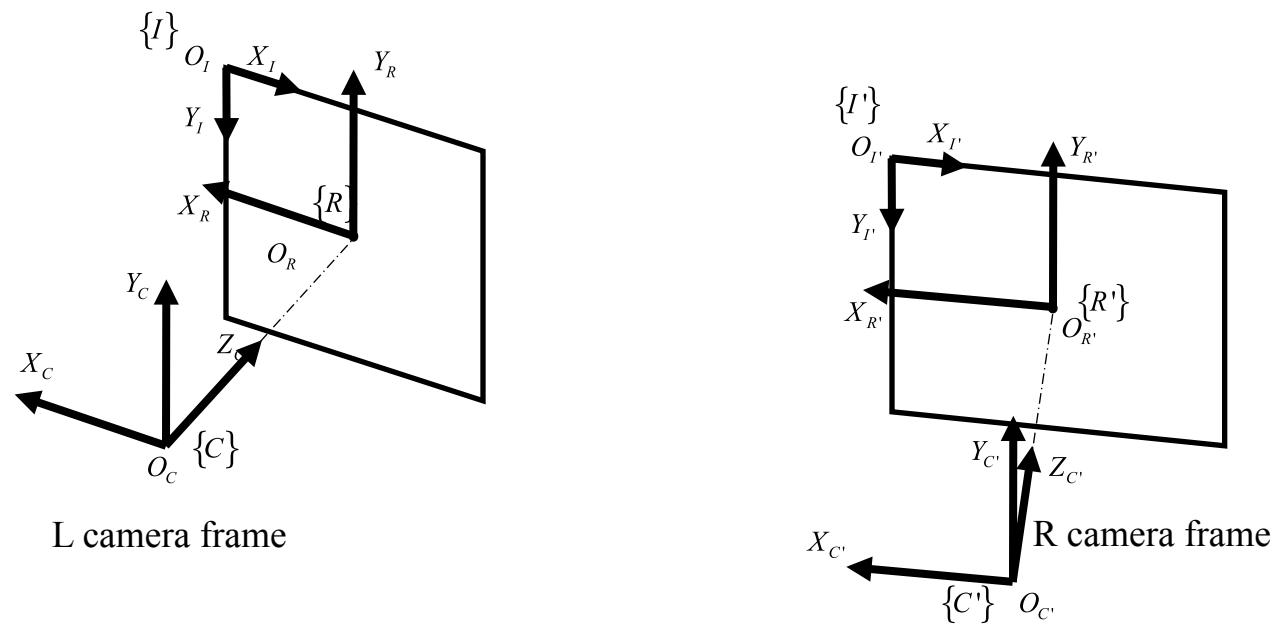


Pinhole model



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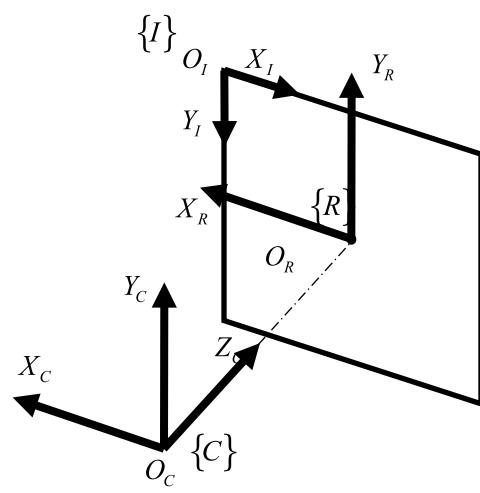
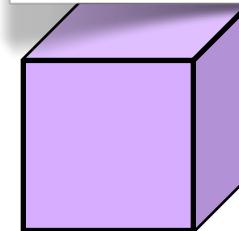
Stereovision principle



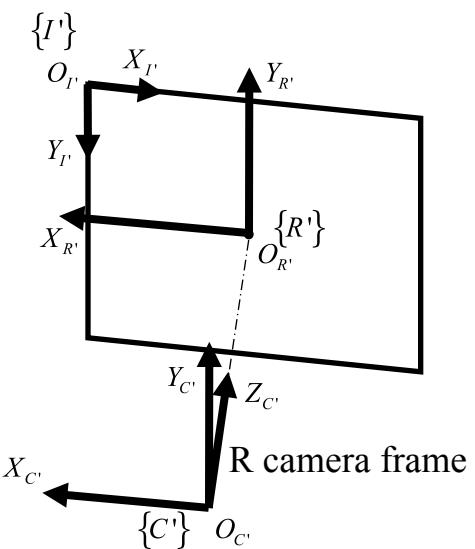
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Stereovision principle



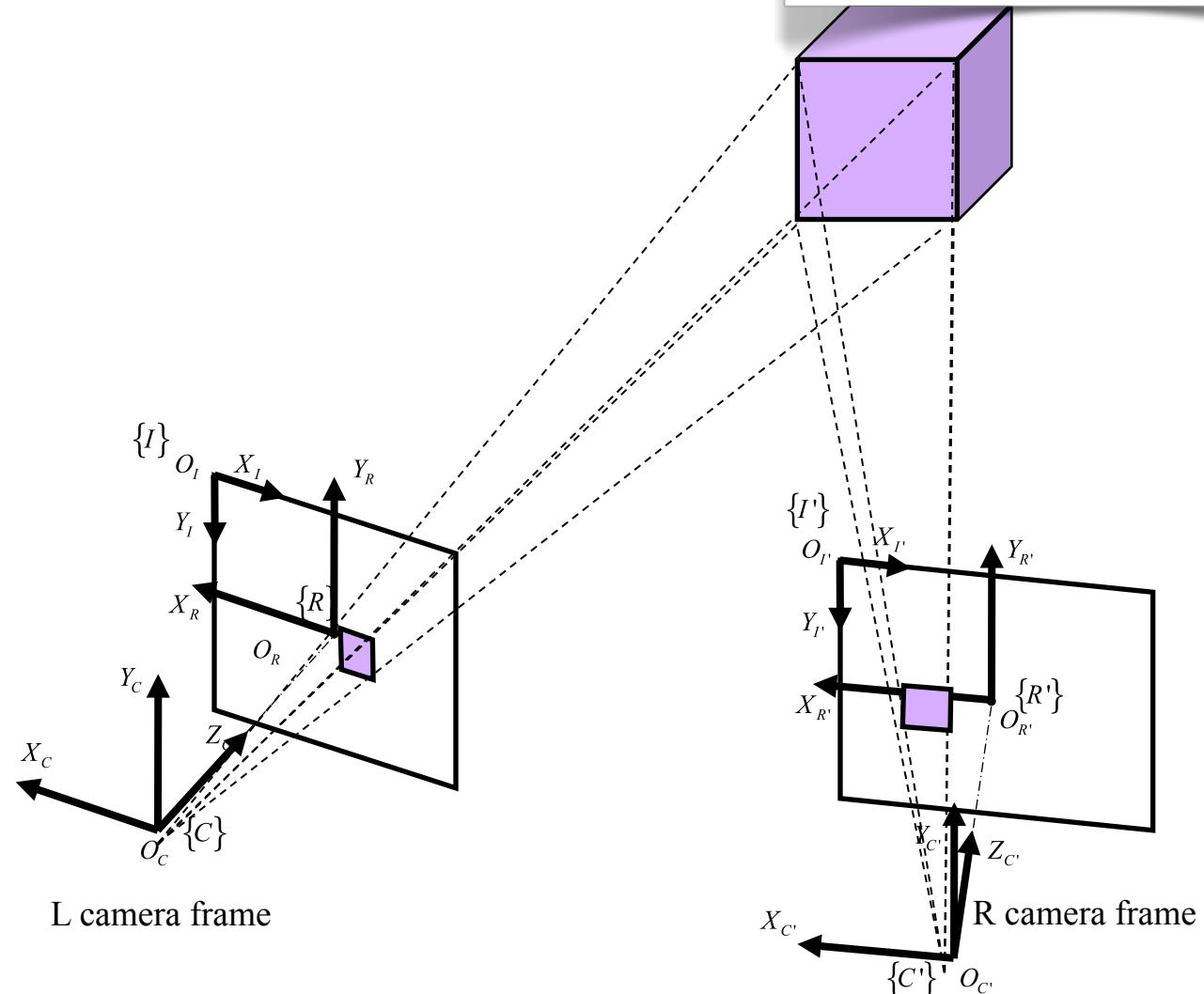
L camera frame



R camera frame

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Stereovision principle

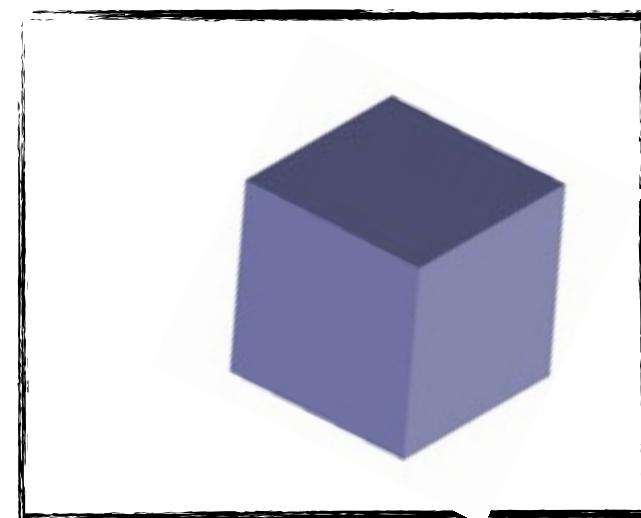
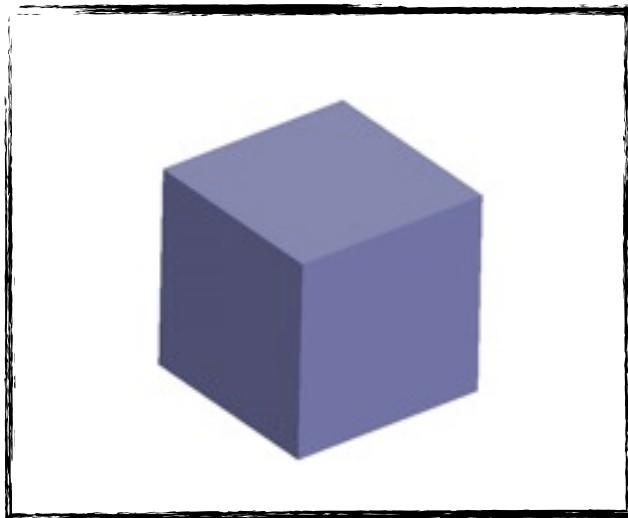


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Feature matching

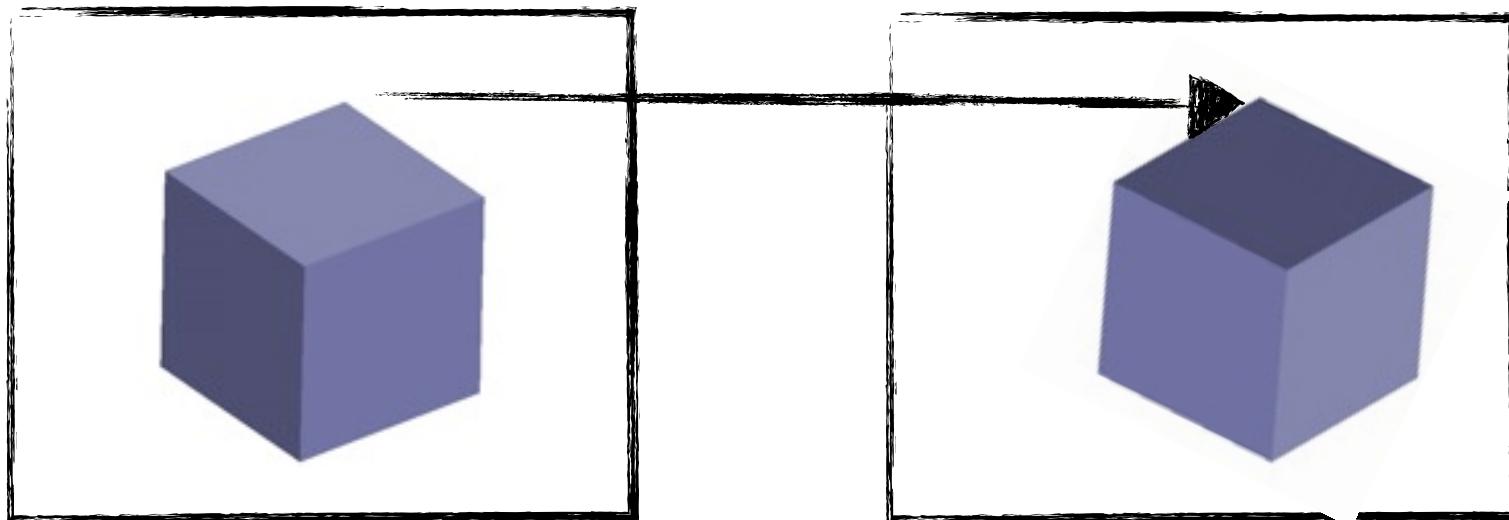
Objective: associating two points from two images corresponding to the same physical (3D) point.





Feature matching

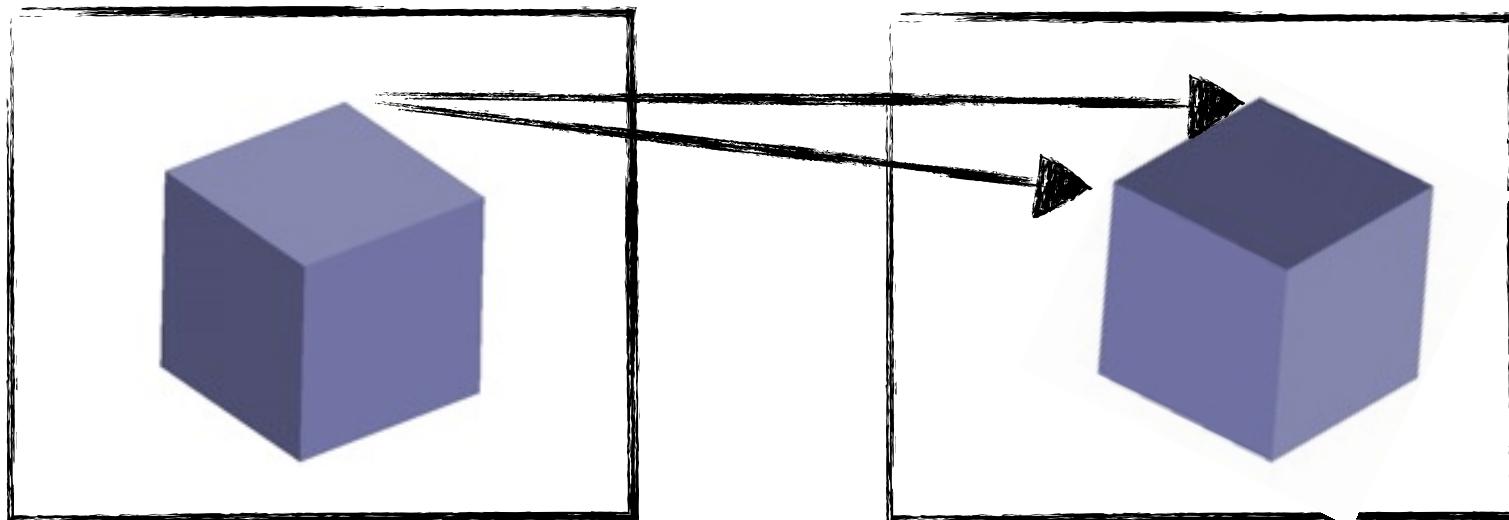
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Feature matching

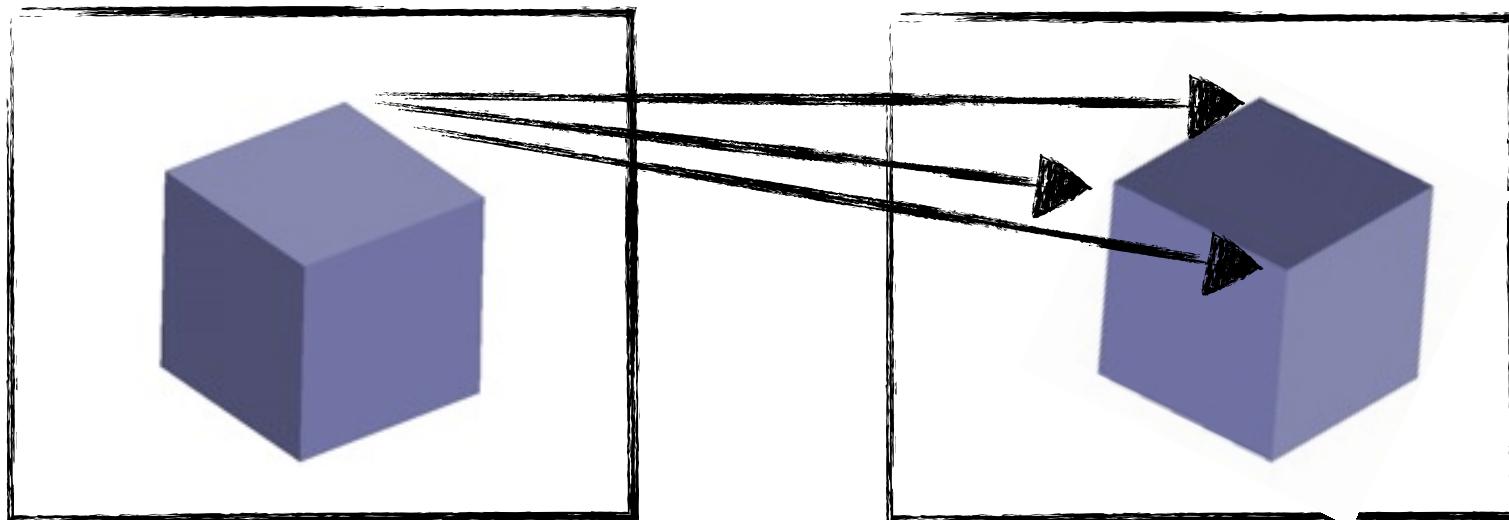
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Feature matching

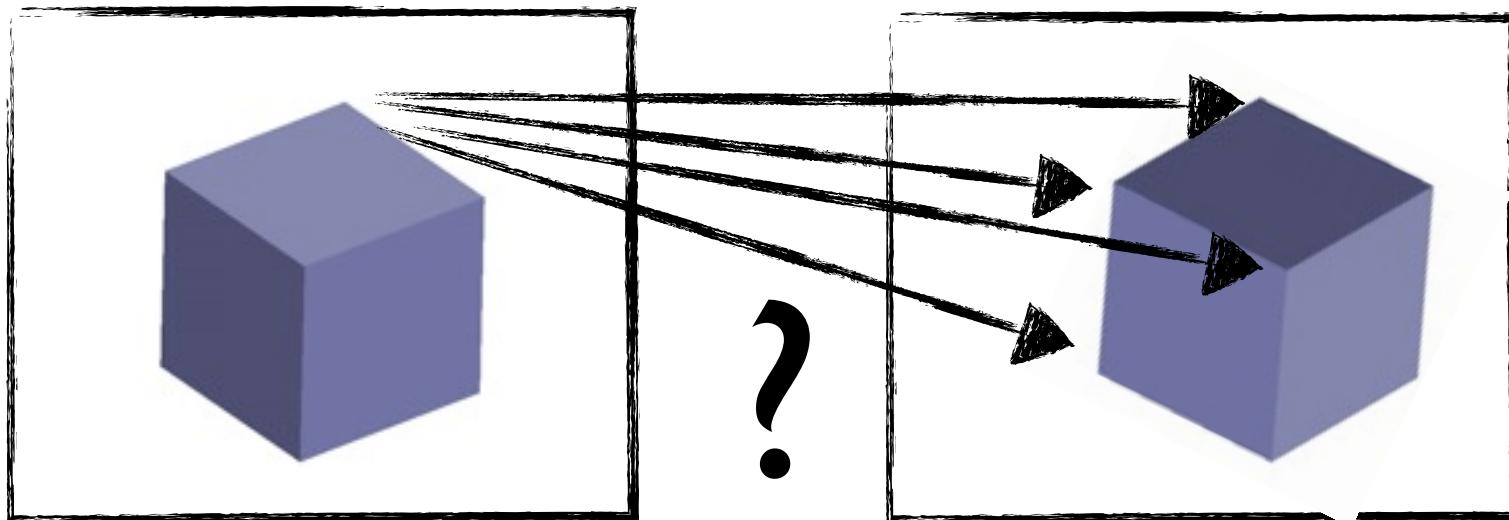
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Feature matching

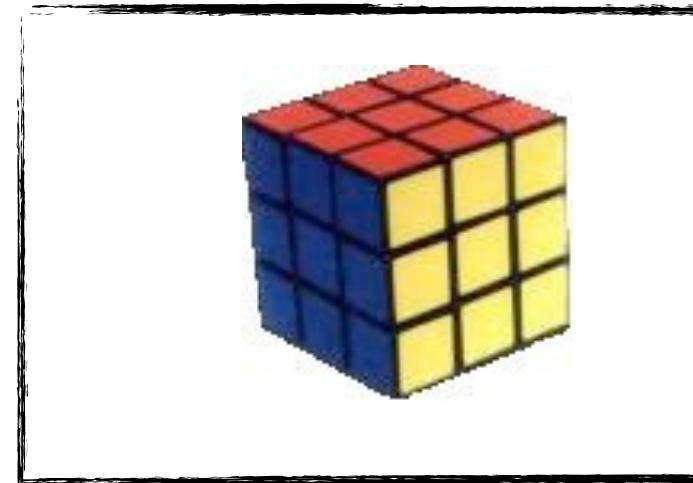
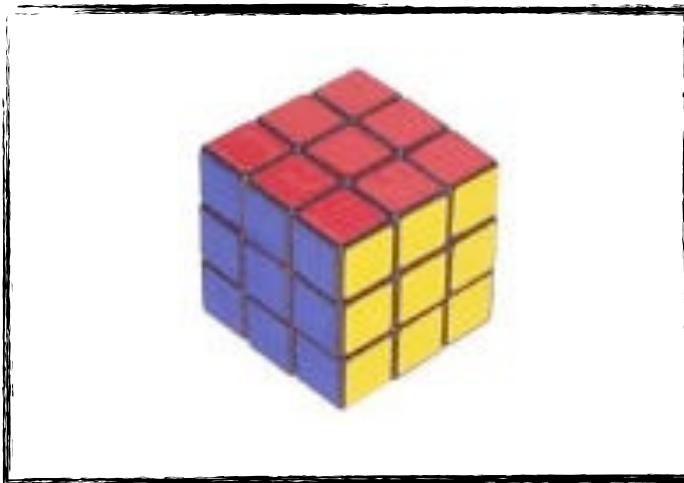
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Feature matching

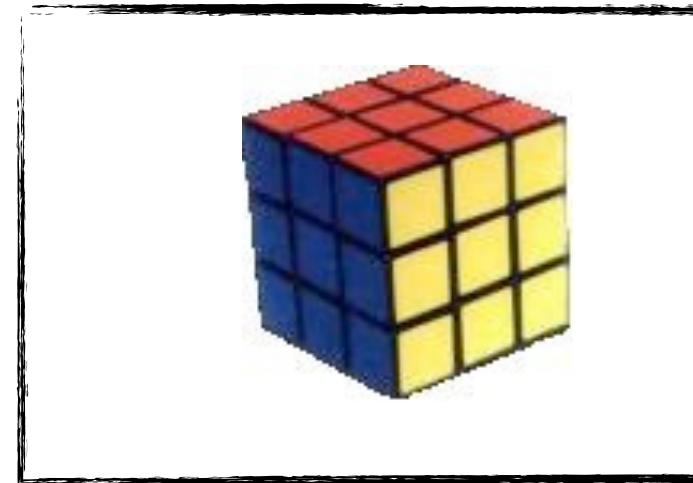
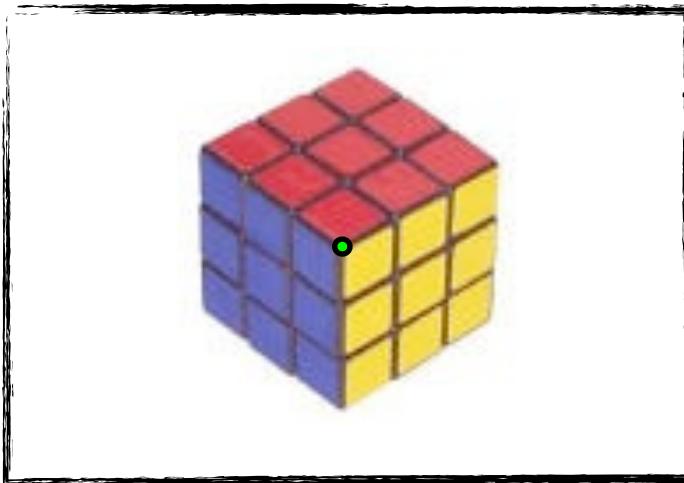
Matching is facilitated by the use of visual clues, such as the colour....





Feature matching

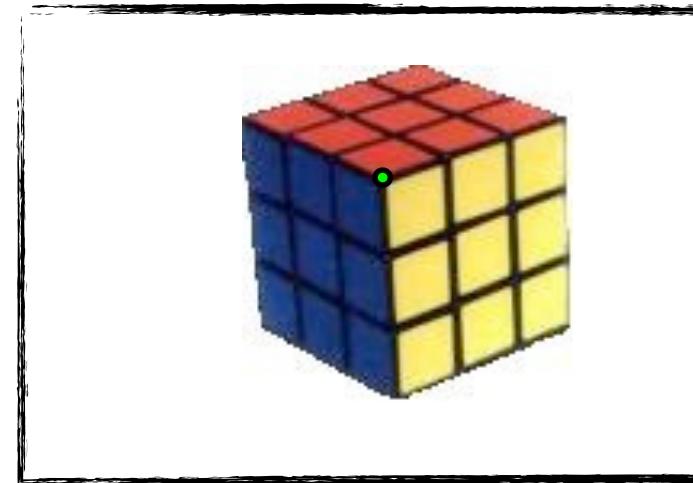
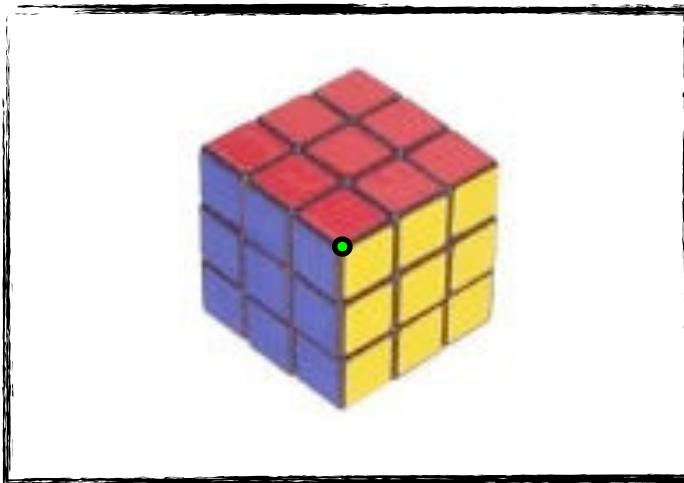
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Feature matching

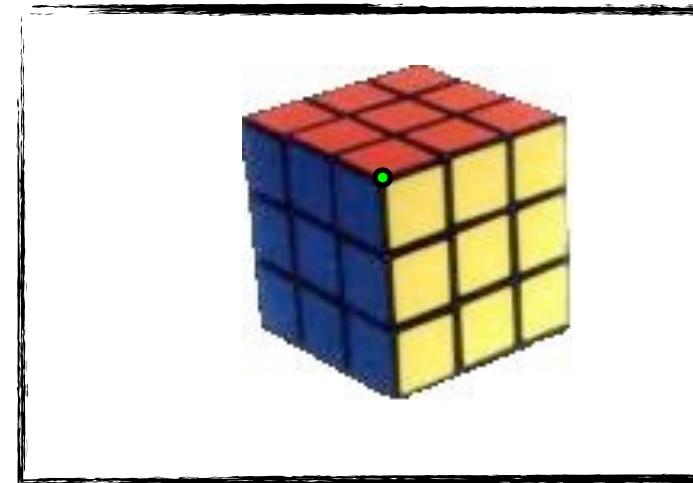
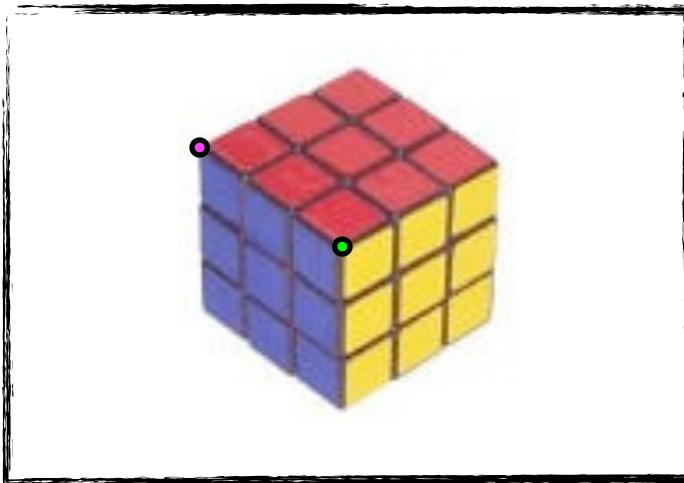
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Feature matching

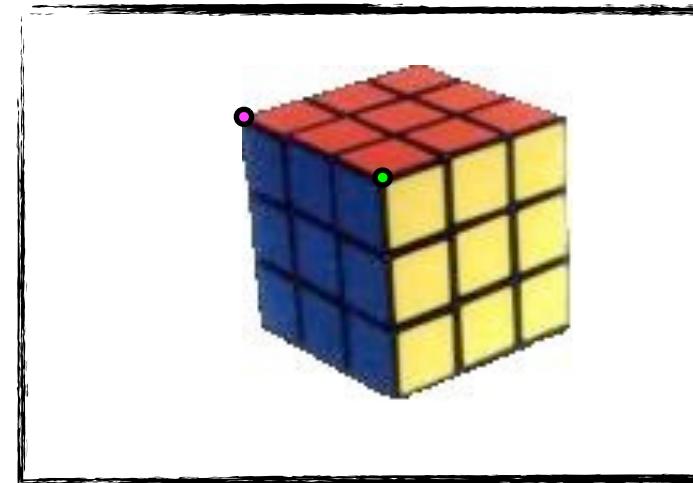
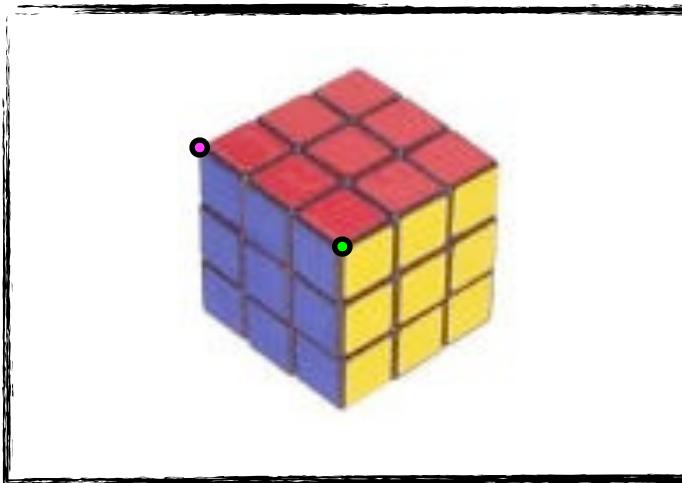
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Feature matching

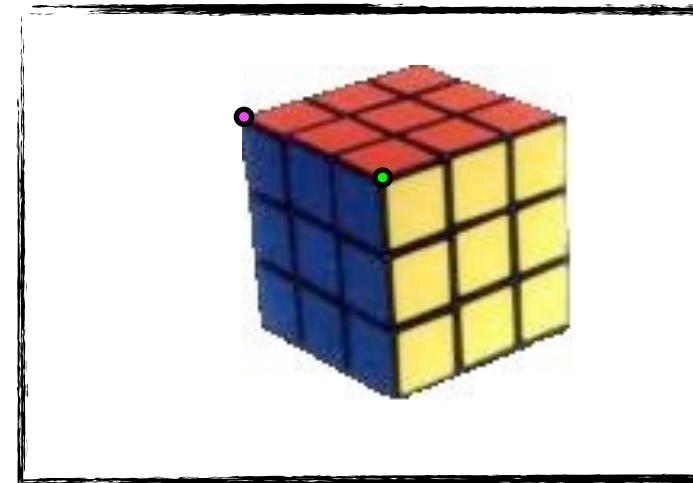
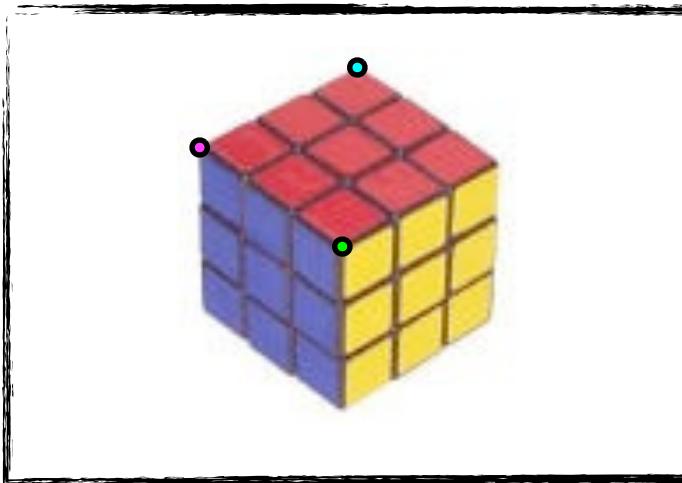
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Feature matching

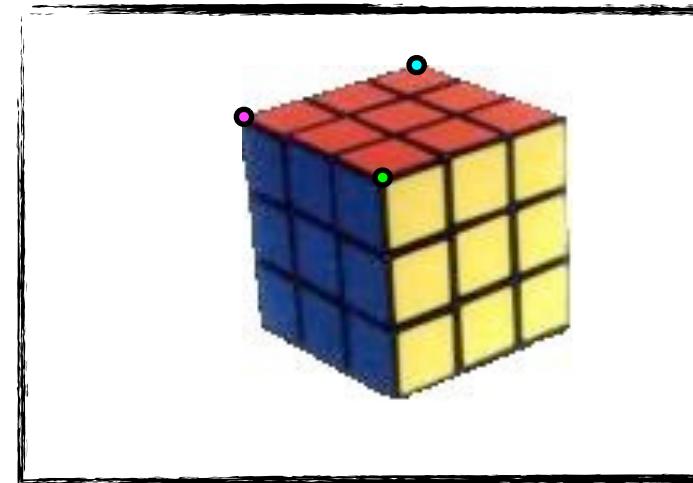
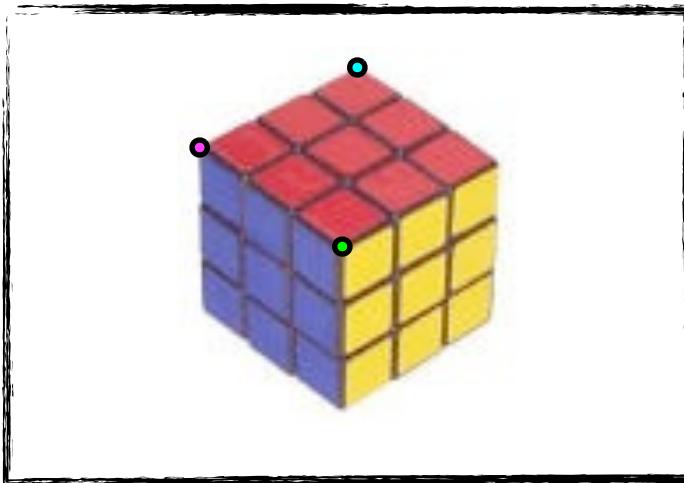
Matching is facilitated by the use of visual clues, such as the colour....





Feature matching

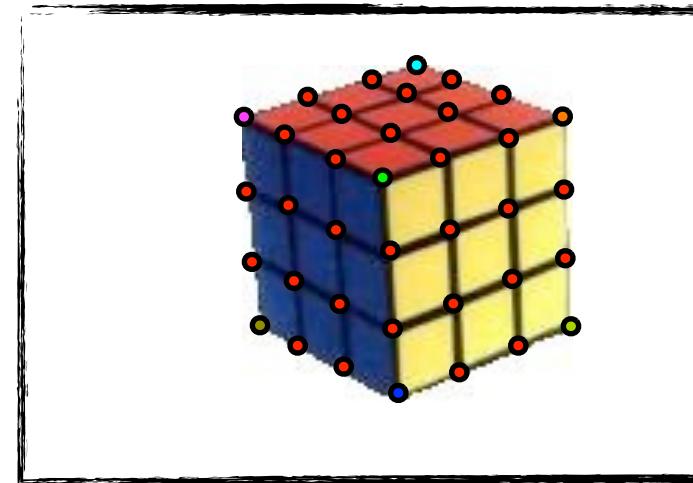
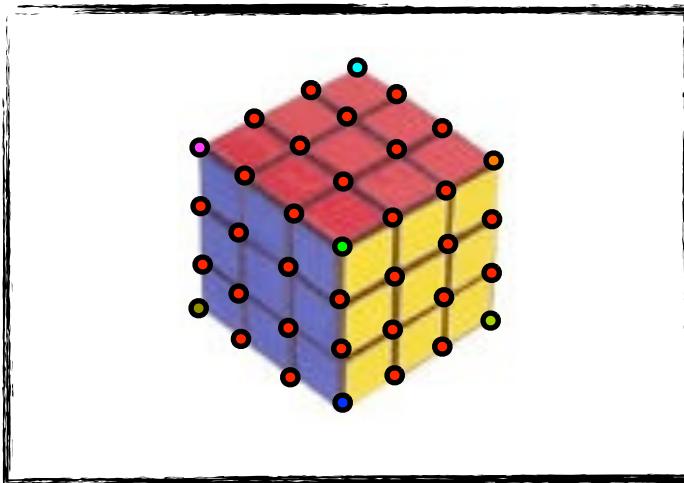
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Feature matching

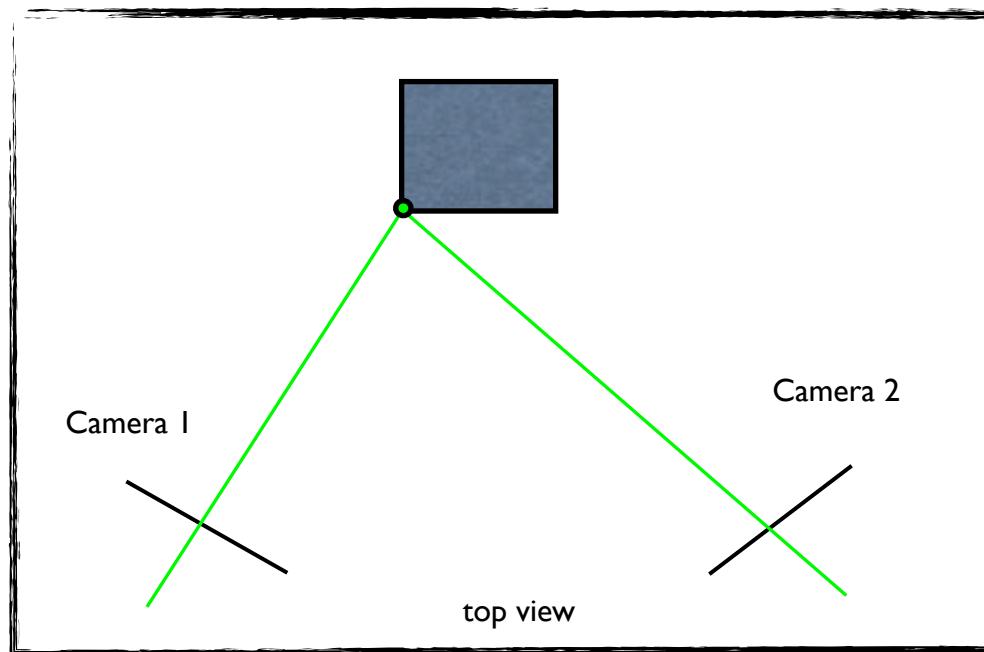
Matching is facilitated by the use of visual clues, such as the colour....





Feature matching

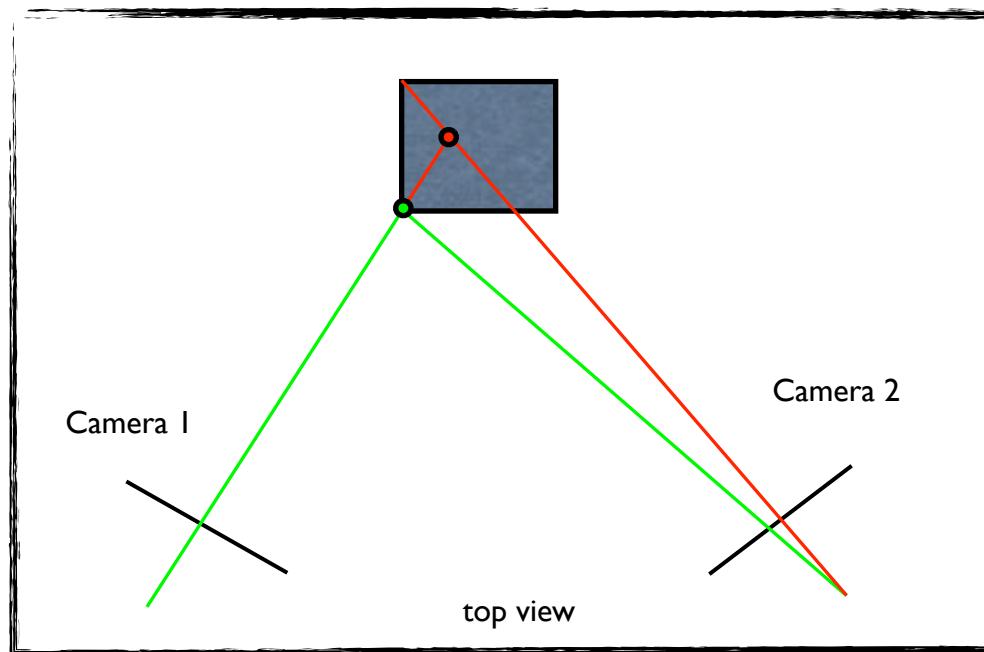
Bad matching leads to bad reconstruction...





Feature matching

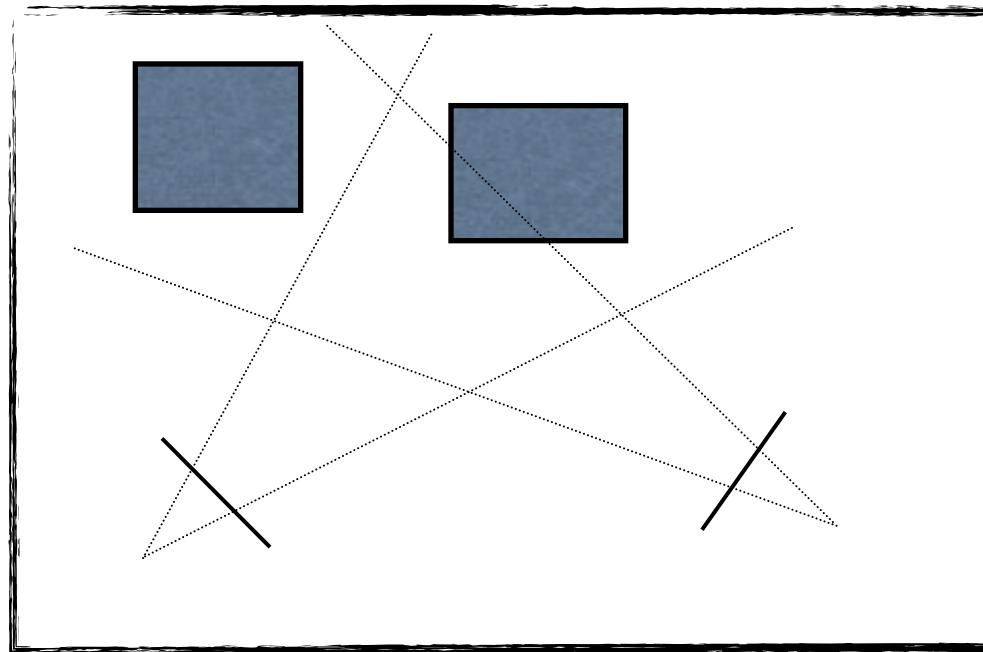
Bad matching leads to bad reconstruction...





Feature matching

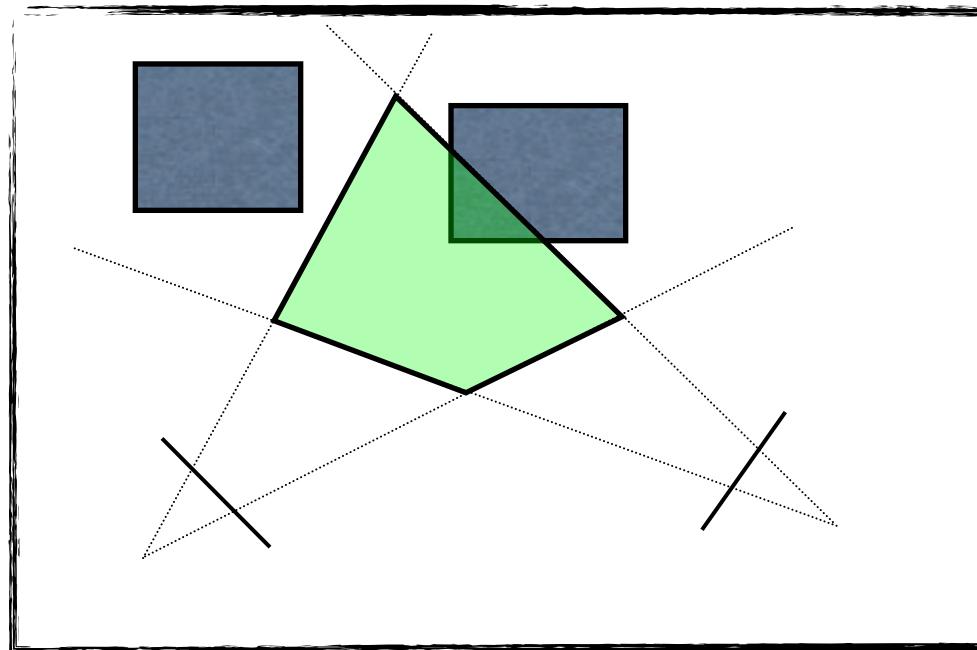
A tricky problem because of **occlusions**, contraction,
homogeneous area...





Feature matching

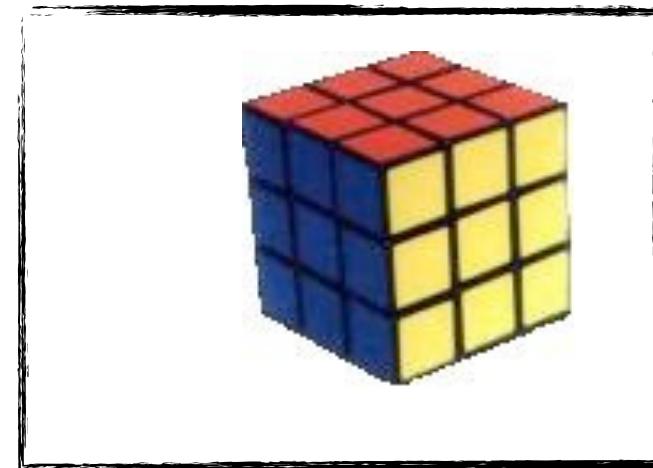
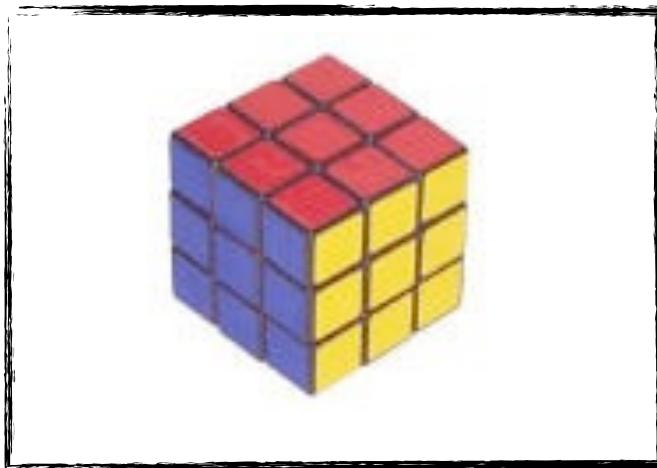
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Feature matching

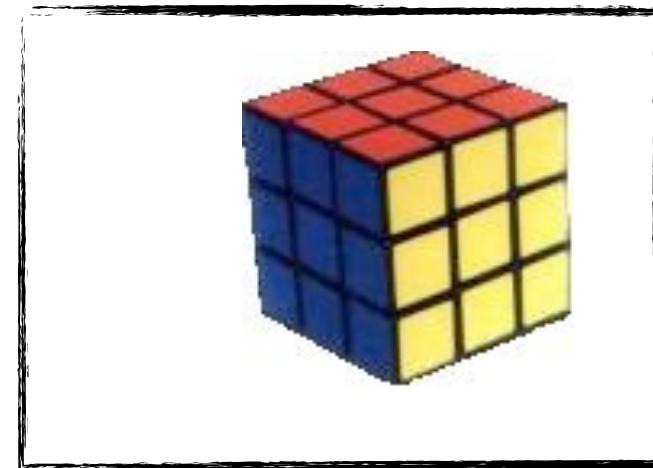
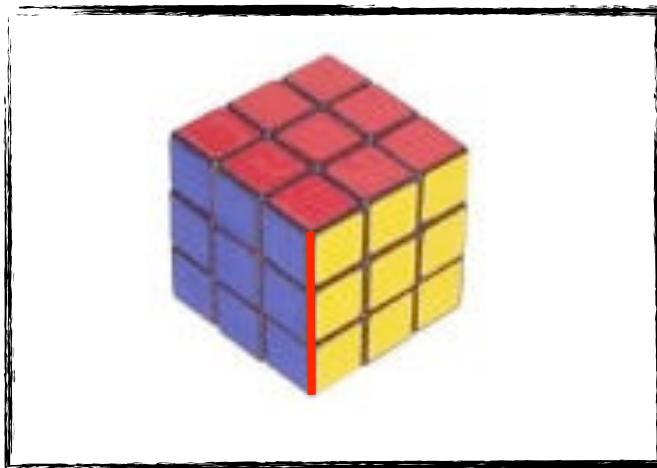
A tricky problem because of occlusions, **contraction**,
homogeneous area...





Feature matching

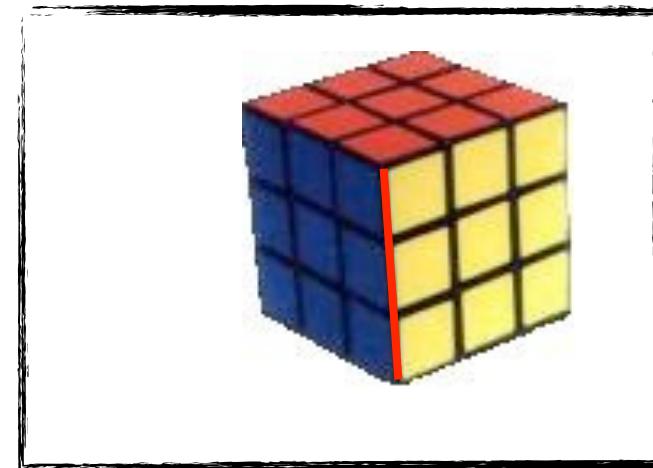
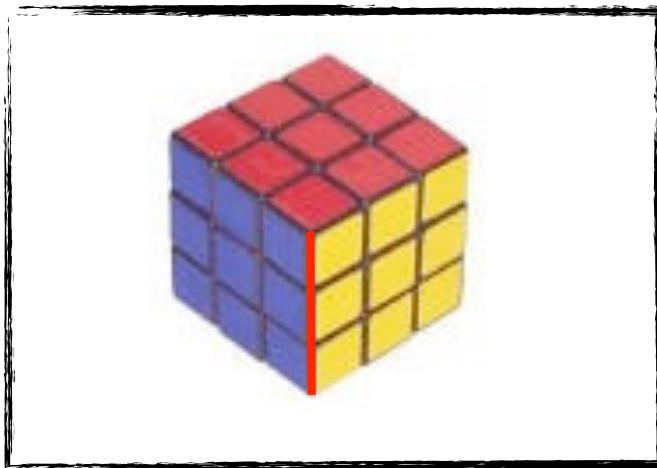
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Feature matching

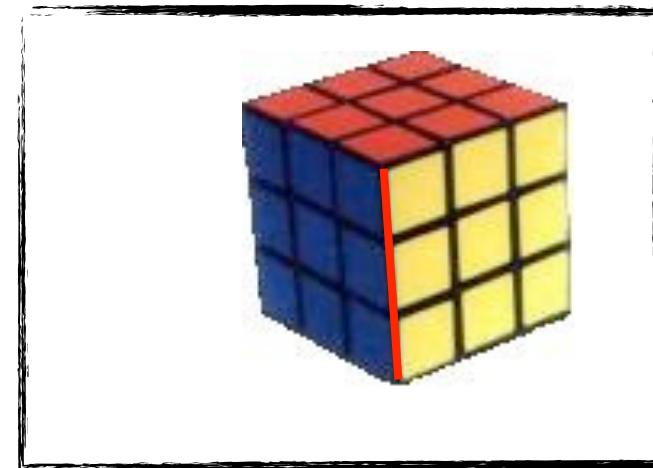
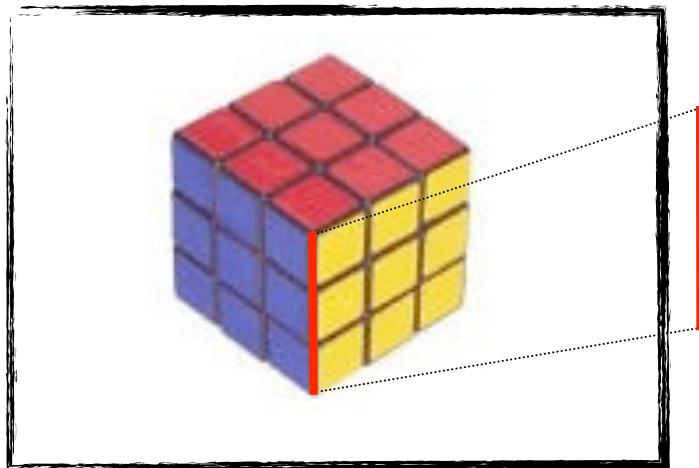
A tricky problem because of occlusions, **contraction**,
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Feature matching

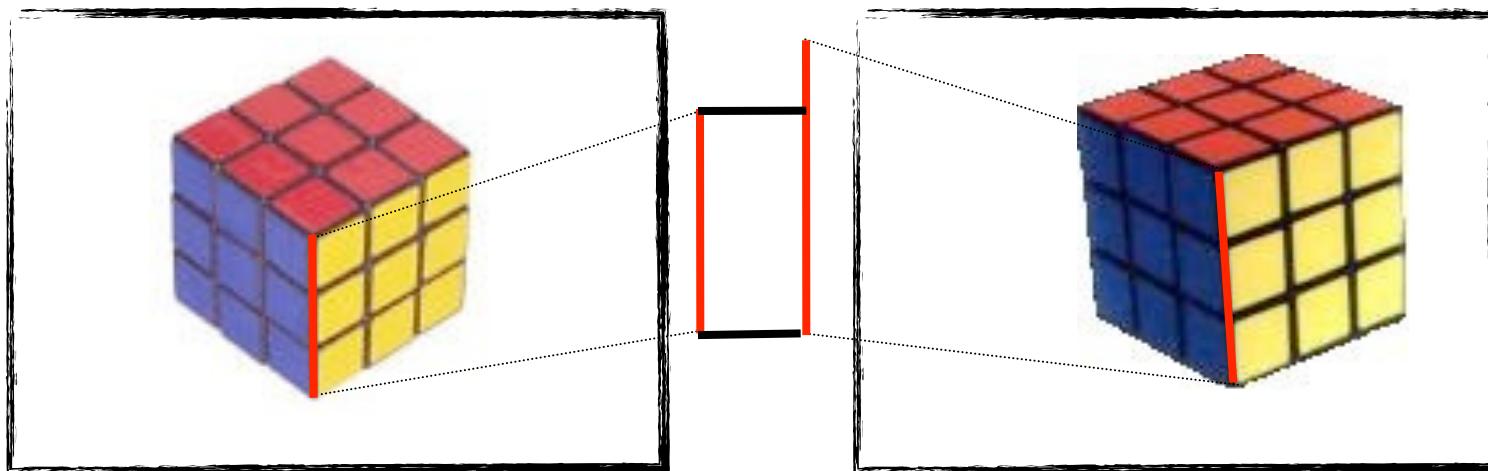
A tricky problem because of occlusions, **contraction**,
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Feature matching

A tricky problem because of occlusions, **contraction**,
homogeneous area...





Feature matching

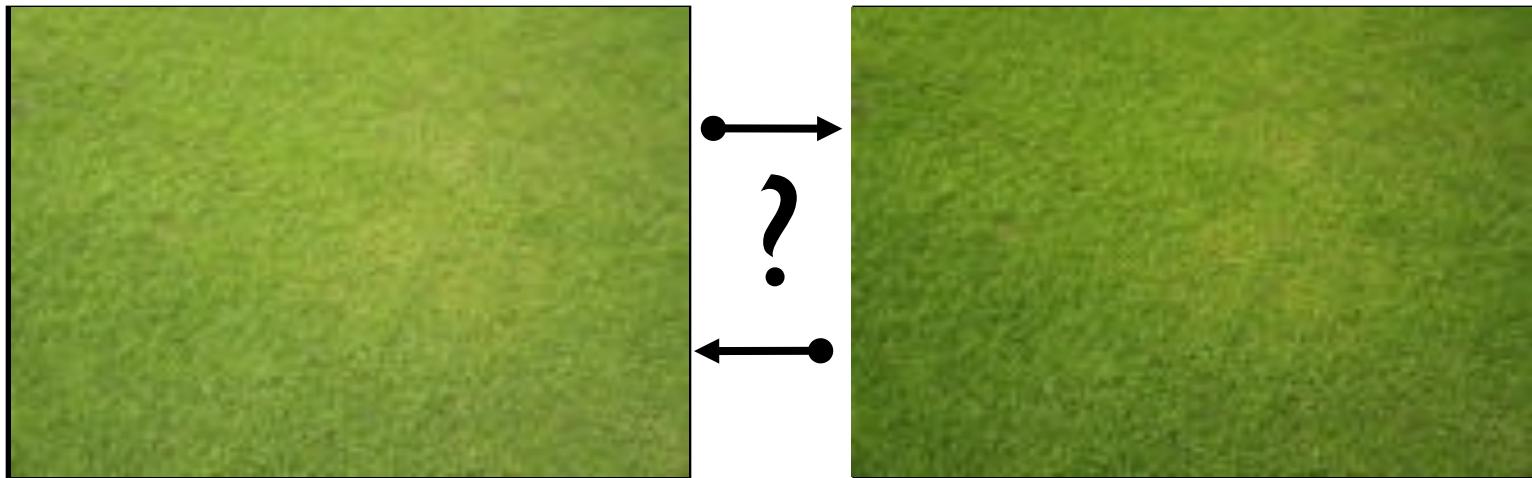
A tricky problem because of occlusions, contraction,
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Feature matching

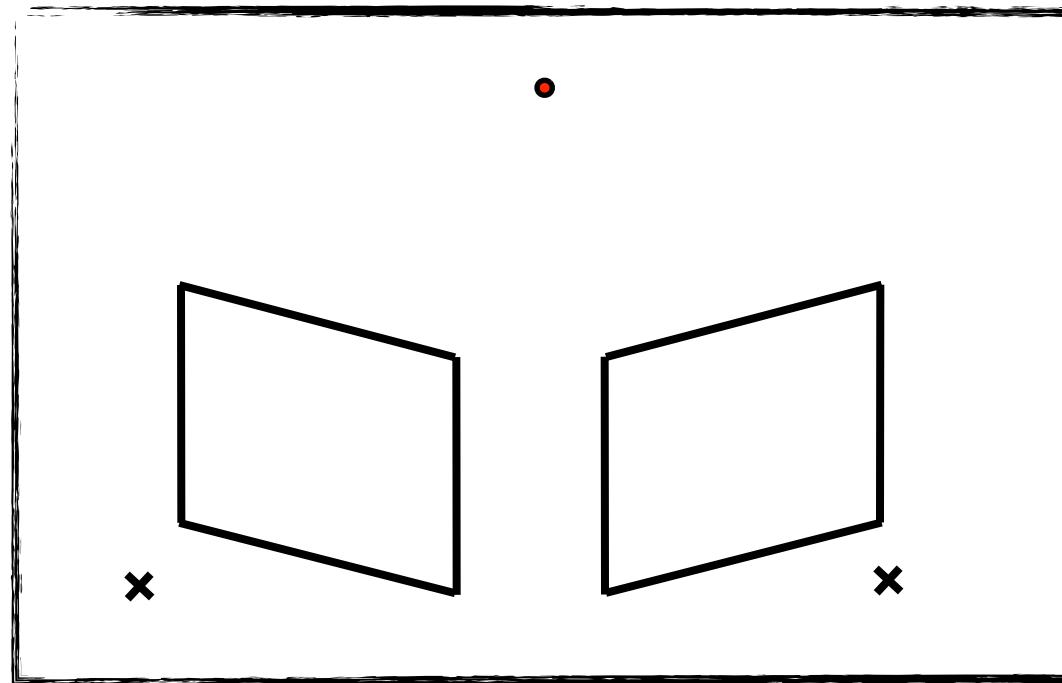
A tricky problem because of occlusions, contraction,
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Feature matching

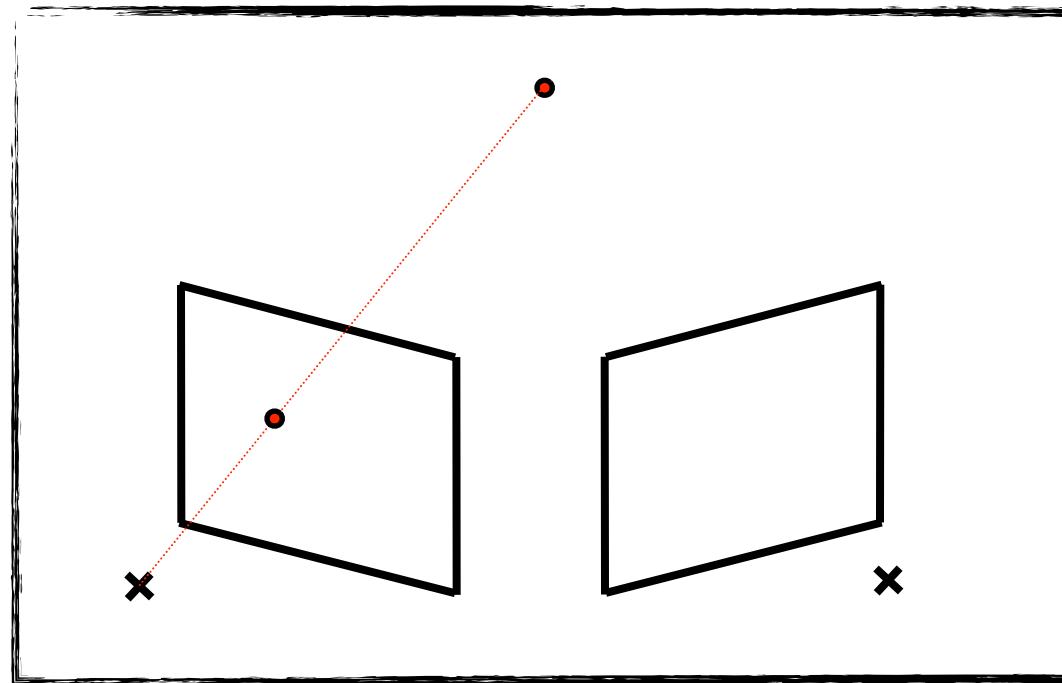
A physical constraint that eases the correspondence problem:
the **epipolar geometry!**





Feature matching

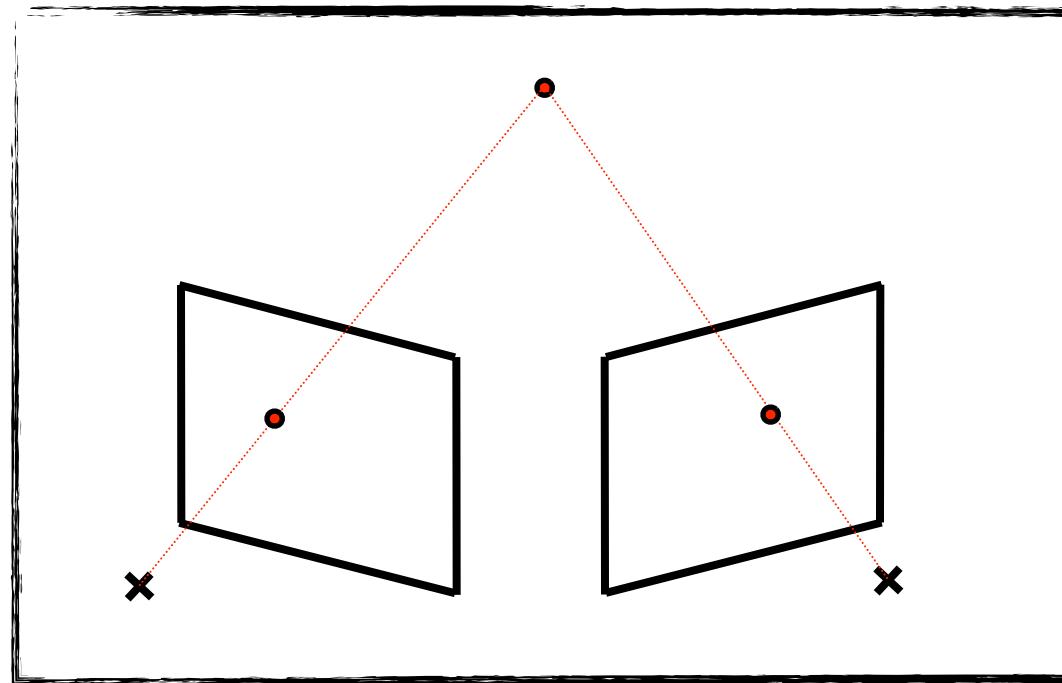
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Feature matching

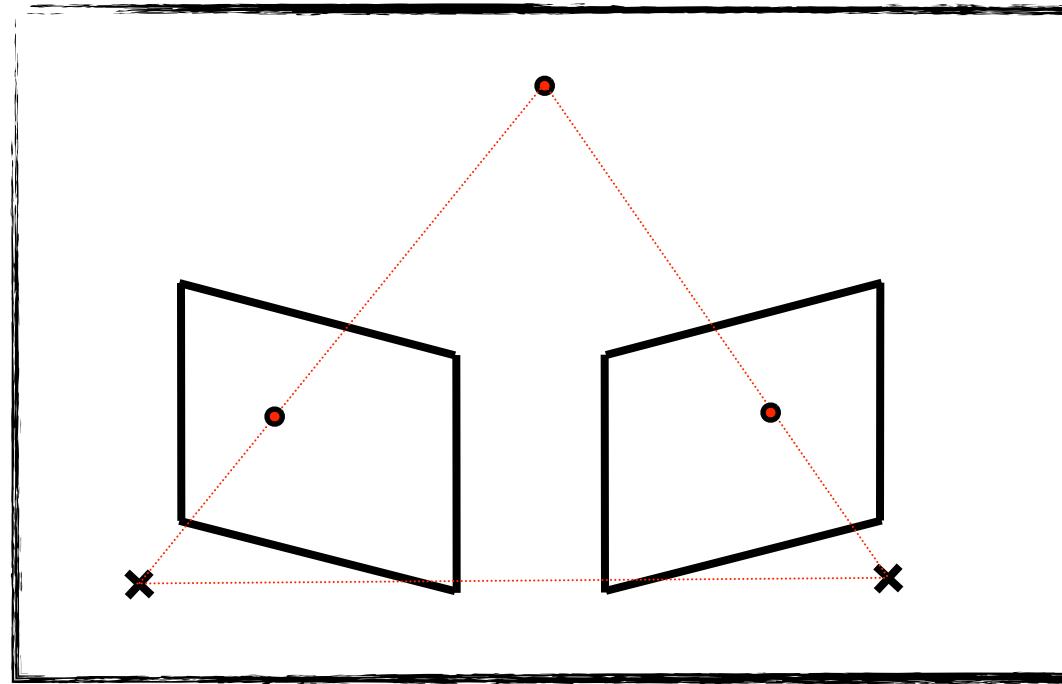
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Feature matching

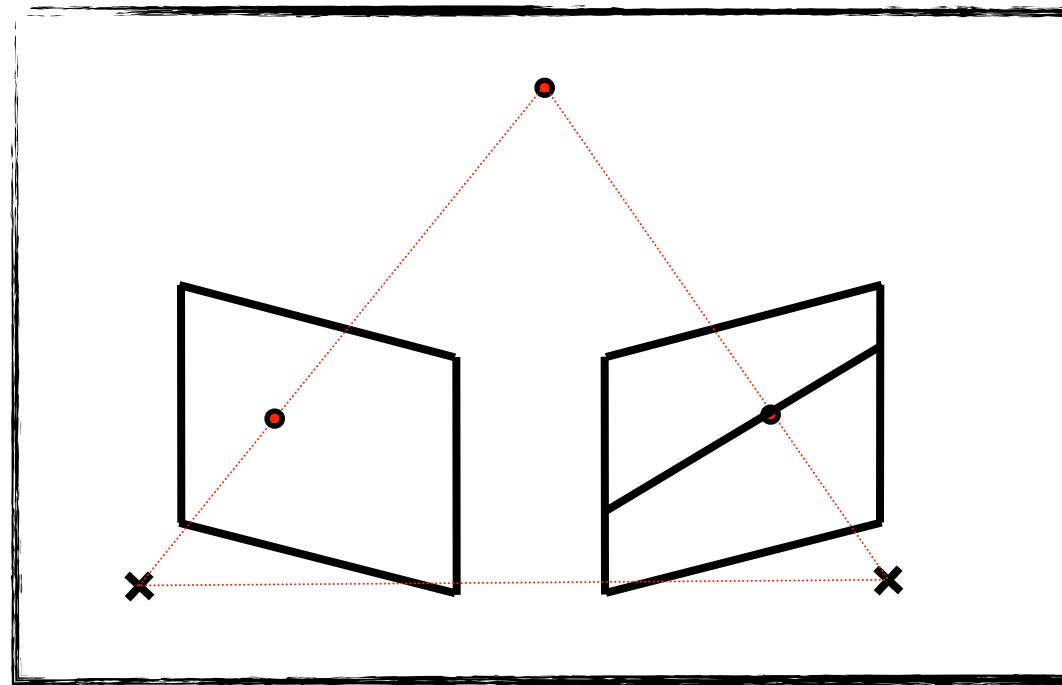
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Feature matching

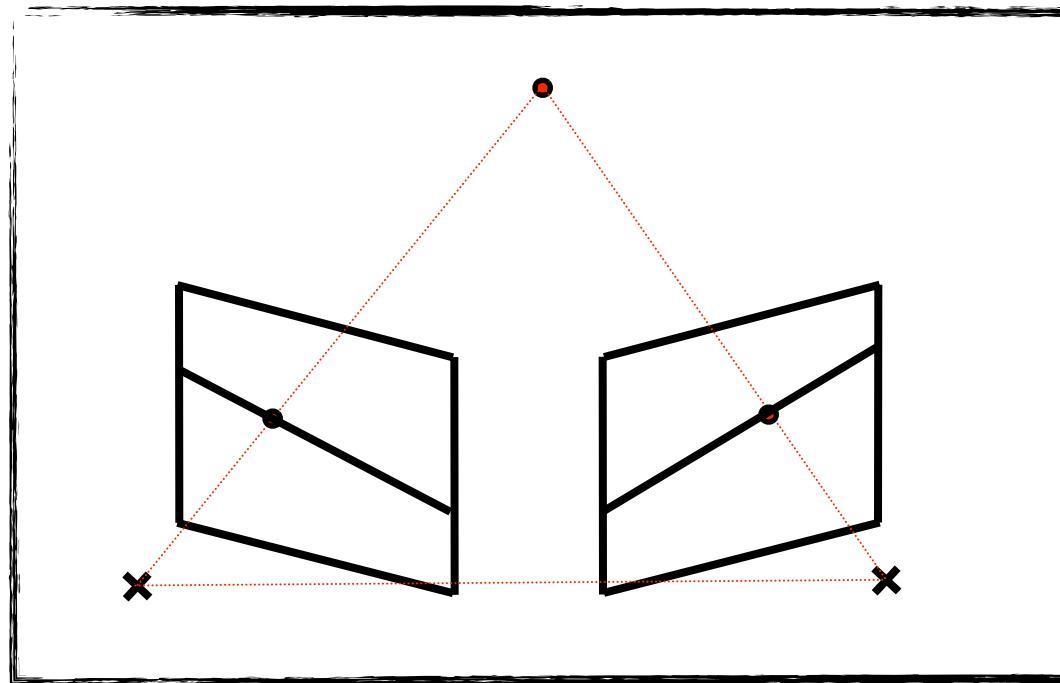
A physical constraint that eases the correspondence problem:
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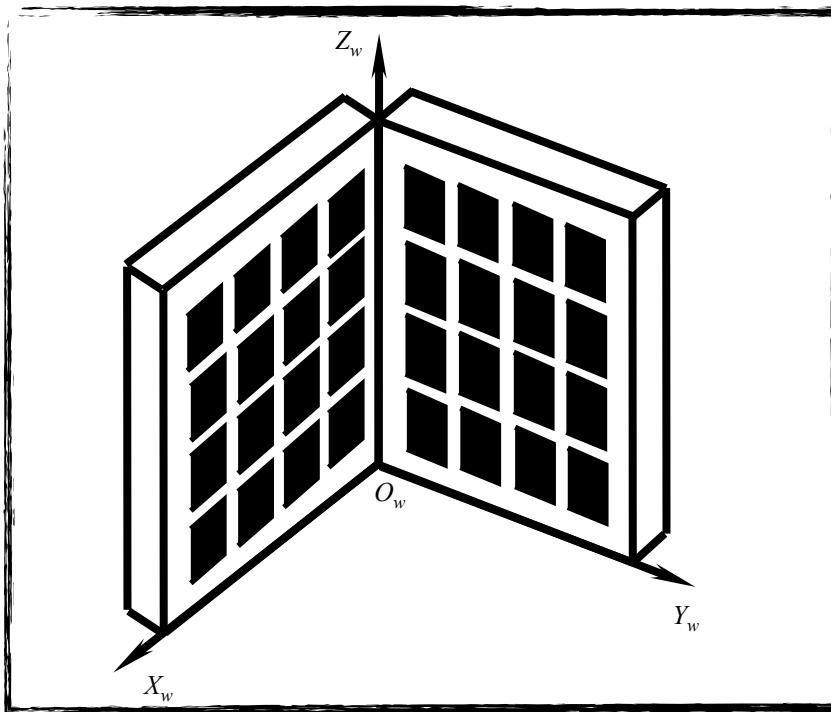


Feature matching

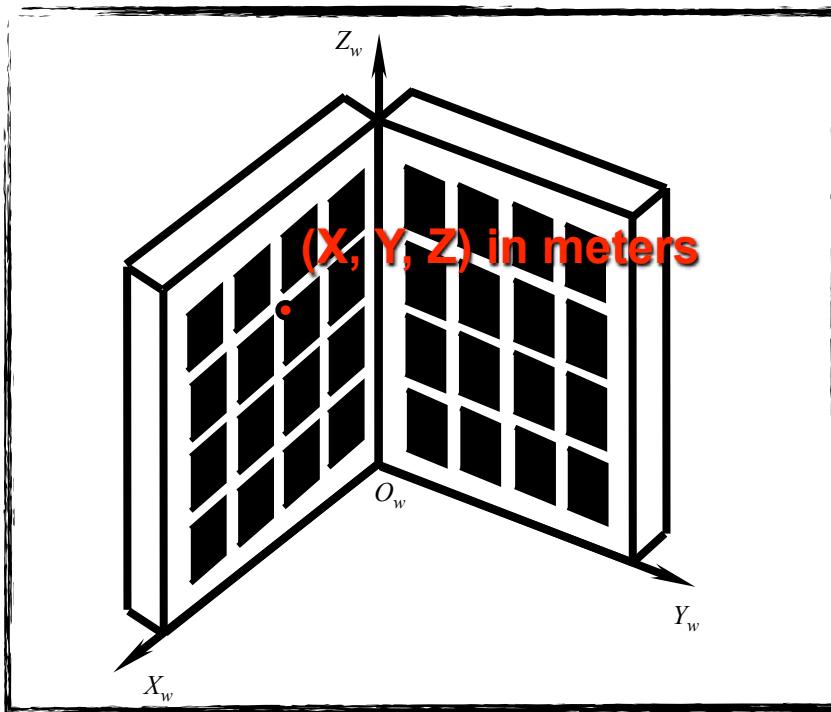
A physical constraint that eases the correspondence problem:
the **epipolar geometry!**



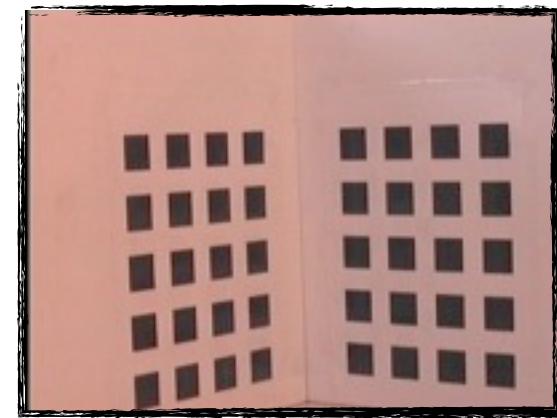
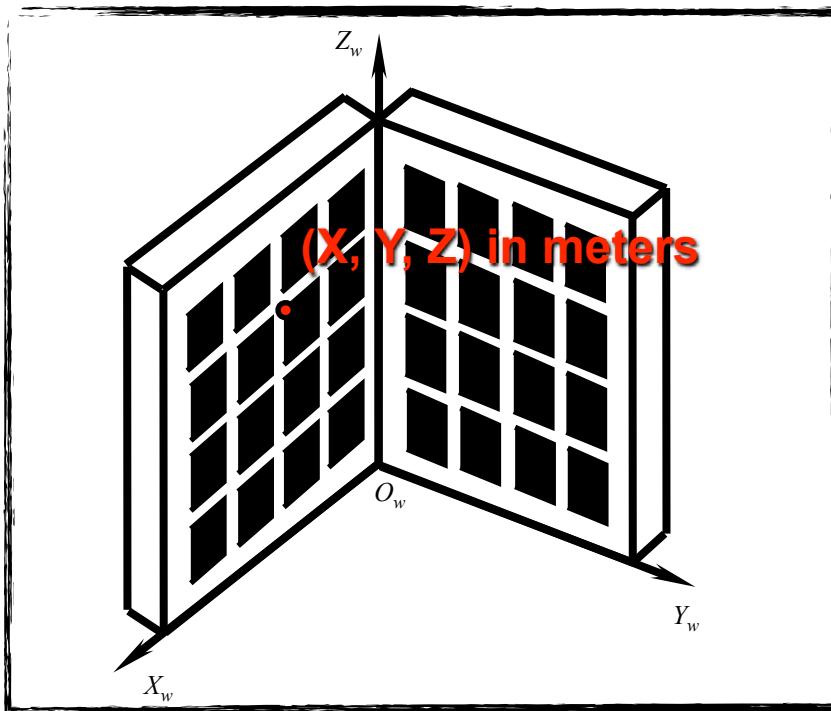
Calibrating is estimating the transformation to pass from 3D (m) to 2D (px)



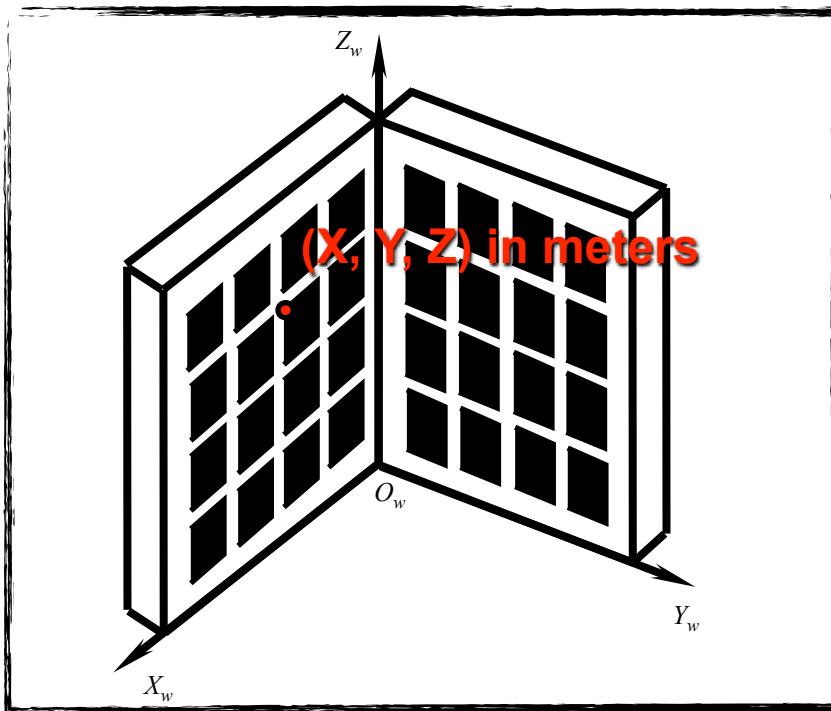
Calibrating is estimating the transformation to pass from 3D (m) to 2D (px)



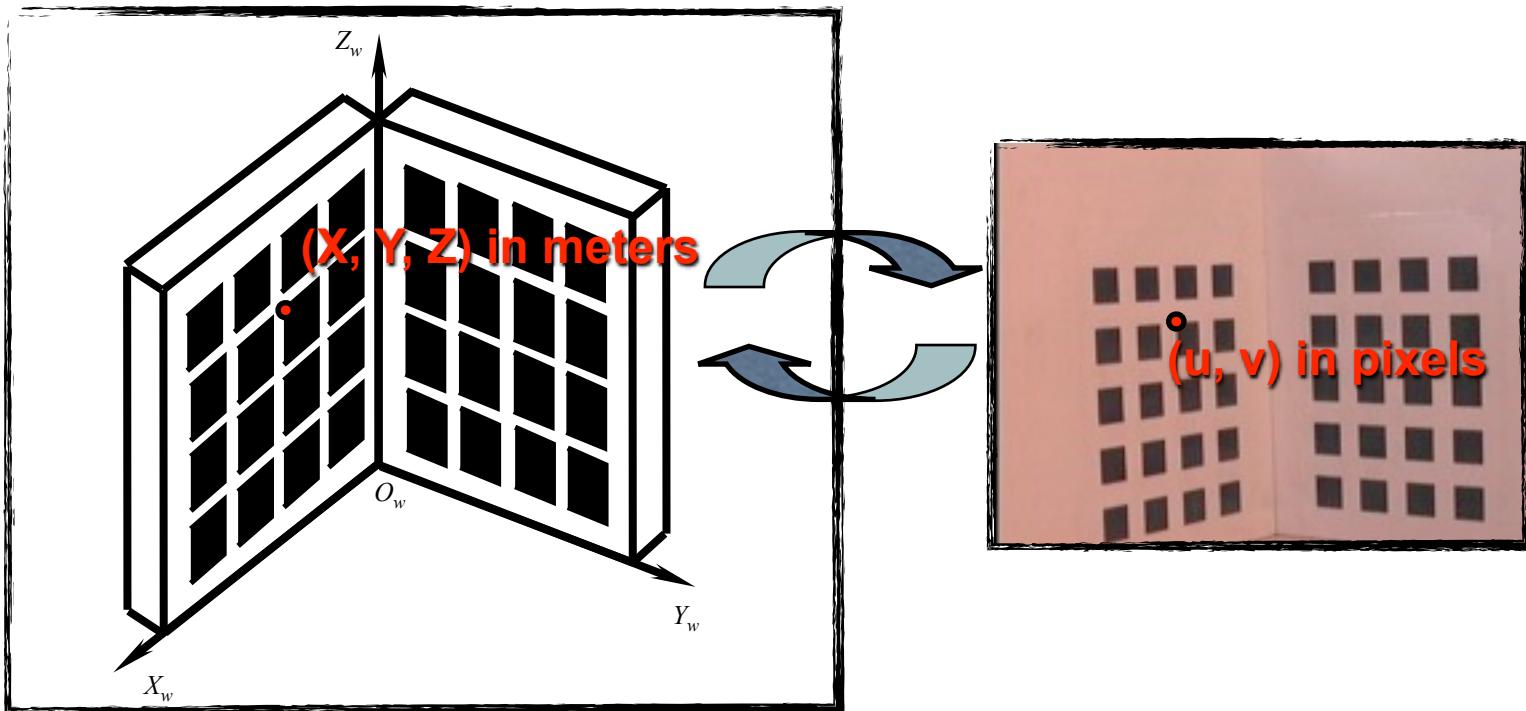
Calibrating is estimating the transformation to pass from 3D (m) to 2D (px)



Calibrating is estimating the transformation to pass from 3D (m) to 2D (px)



Calibrating is estimating the transformation to pass from 3D (m) to 2D (px)



$$\begin{bmatrix} u \\ v \\ s \end{bmatrix} = \begin{bmatrix} \alpha_u & 0 & u_0 & 0 \\ 0 & \alpha_v & v_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$



$$\begin{bmatrix} u \\ v \\ s \end{bmatrix} = \begin{bmatrix} \alpha_u & 0 & u_0 & 0 \\ 0 & \alpha_v & v_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & 1 \\ 1 & 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

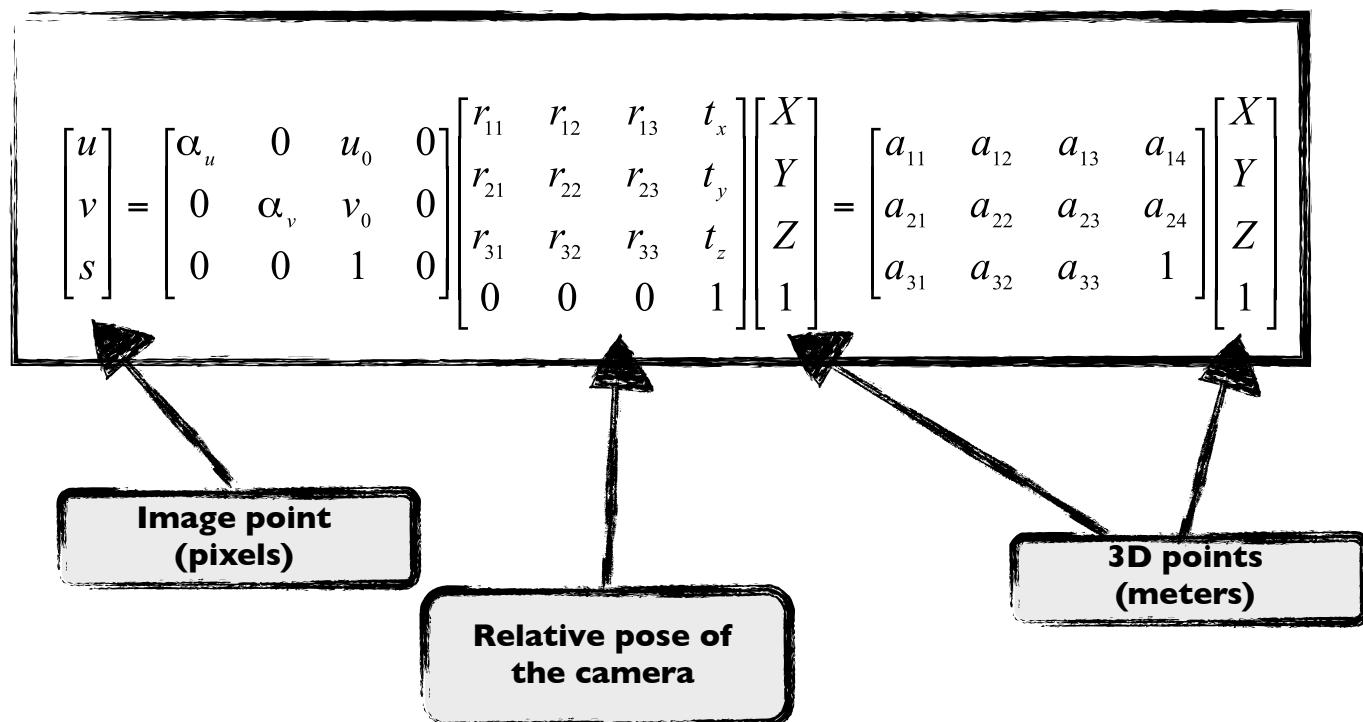
Image point
(pixels)



$$\begin{bmatrix} u \\ v \\ s \end{bmatrix} = \begin{bmatrix} \alpha_u & 0 & u_0 & 0 \\ 0 & \alpha_v & v_0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & 1 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

Diagram illustrating the camera calibration process:

- Image point (pixels)** is mapped to the left side of the equation.
- 3D points (meters)** are mapped to the right side of the equation.
- The middle part of the equation represents the internal and external camera parameters.



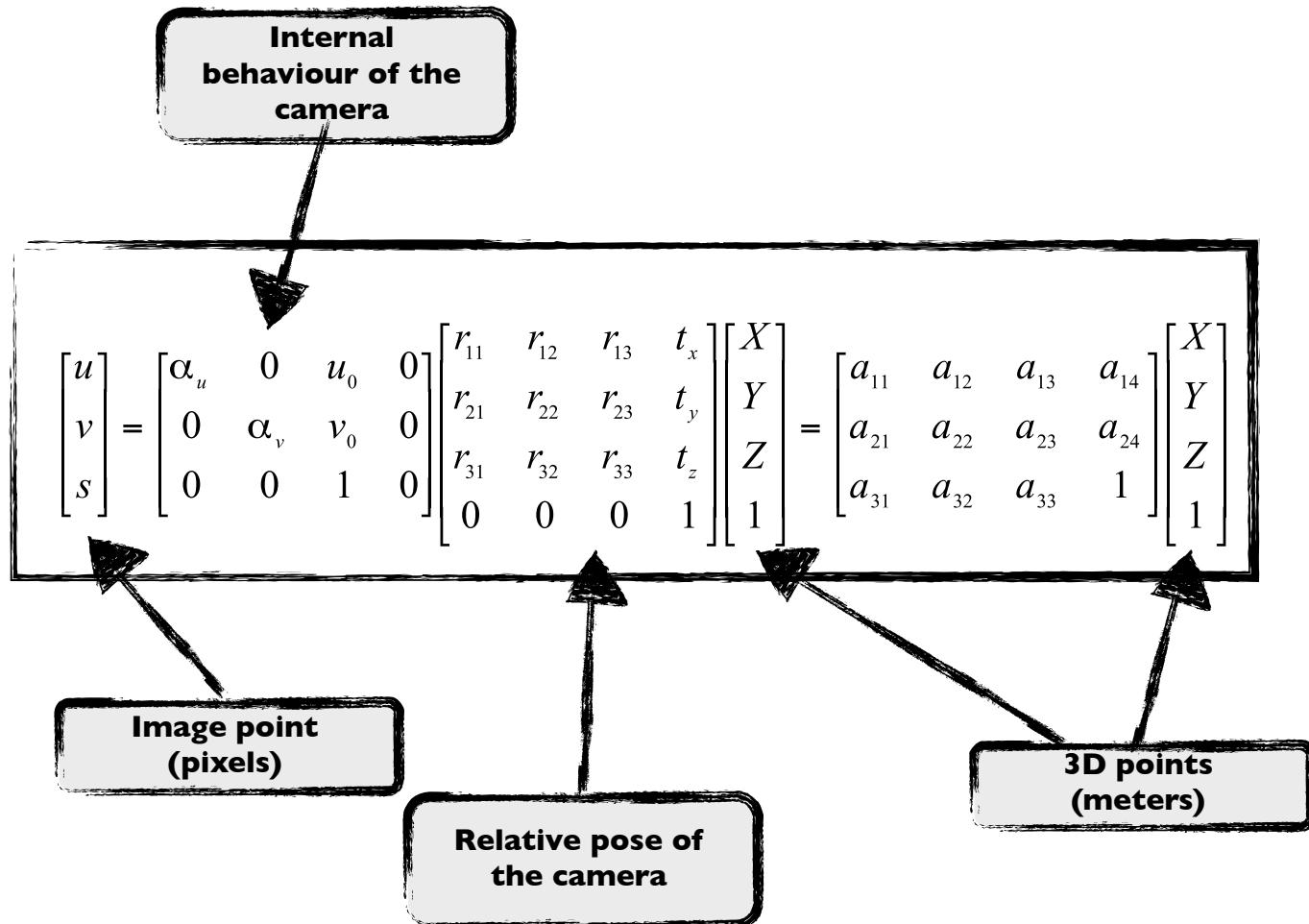
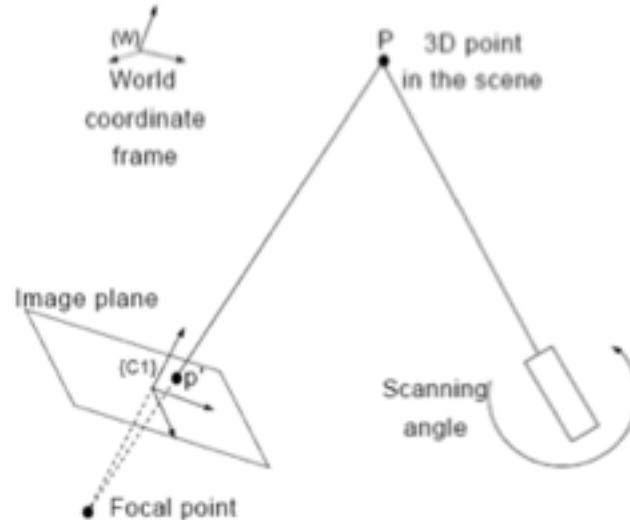




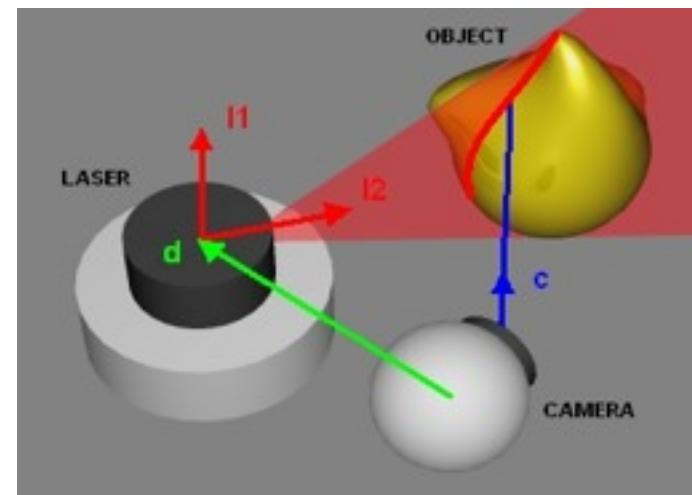
Table 2
Accuracy of 2D coordinate measurement

	2D distorted image (pix.)			2D undistorted image (pix.)		
	Mean	σ	Max	Mean	σ	Max
Hall	0.2676	0.1979	1.2701	0.2676	0.1979	1.2701
Faugeras	0.2689	0.1997	1.2377	0.2689	0.1997	1.2377
Faugeras NR without distortion	0.2770	0.2046	1.3692	0.2770	0.2046	1.3692
Faugeras NR with distortion	0.0840	0.0458	0.2603	0.0834	0.0454	0.2561
Tsai	0.1836	0.1022	0.6082	0.1824	0.1011	0.6011
Tsai optimized	0.0838	0.0457	0.2426	0.0832	0.0453	0.2386
Tsai with principal point of Tsai optimized	0.0879	0.0466	0.2277	0.0872	0.0463	0.2268
Tsai optimized with principal point of Tsai optimized	0.0836	0.0457	0.2500	0.0830	0.0454	0.2459
Weng	0.0845	0.0455	0.2680	0.0843	0.0443	0.2584

Référence : J. Salvi, X. Armangué, J. Batlle, "A comparative review of camera calibrating methods with accuracy evaluation", *Pattern Recognition*, 35, pp. 1617-1635, 2002.

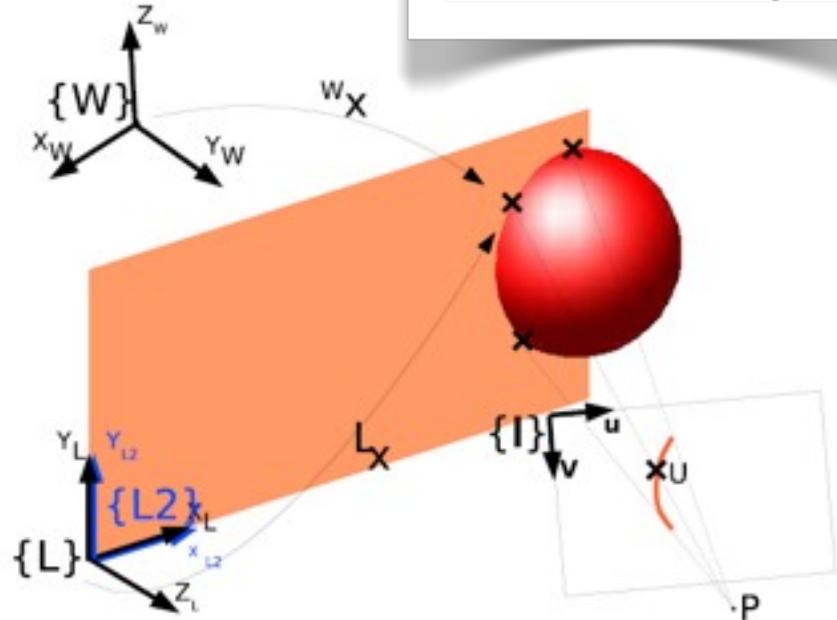


One of the cameras is replaced by a laser source that projects either a dot, a line or a bi-dimensional pattern onto the object...





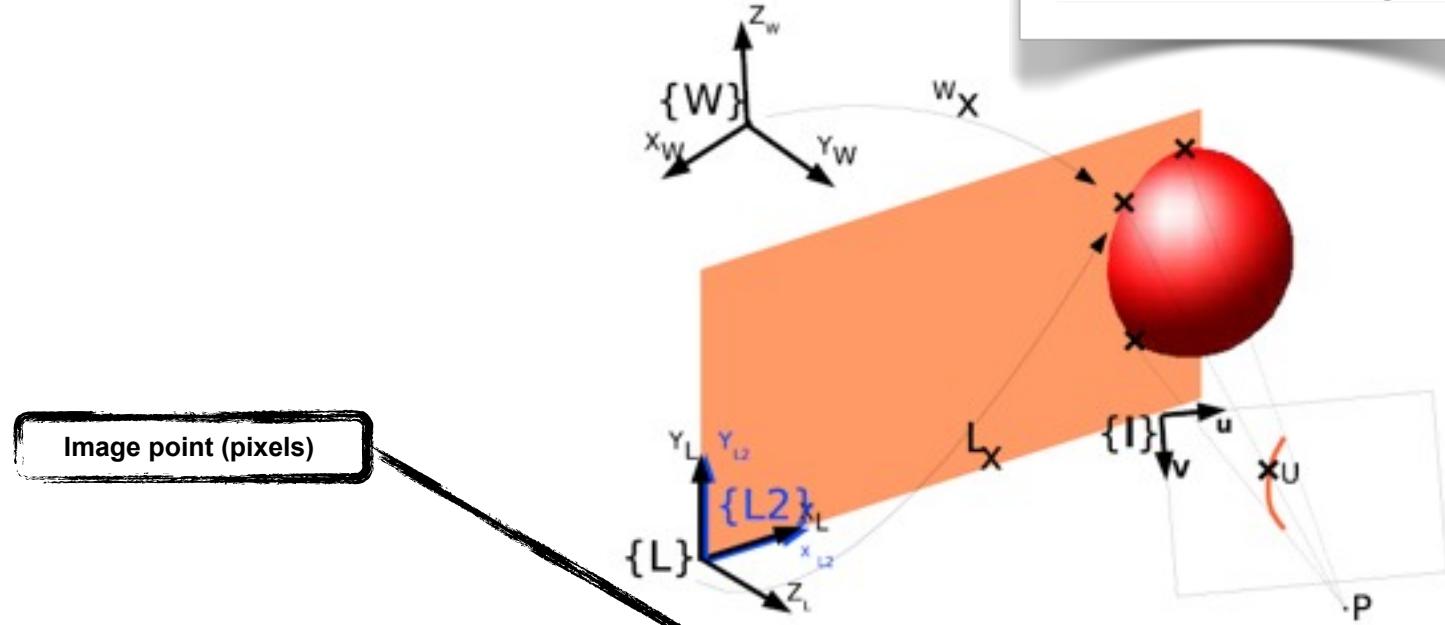
Structured light



$$\begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = {}^W T_L \cdot {}^L T_{L2} \cdot {}^{L2} H_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_L \cdot \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} e_{11} & e_{12} & e_{13} \\ e_{21} & e_{22} & e_{23} \\ e_{31} & e_{32} & e_{33} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ t_{31} & t_{32} & t_{33} \\ t_{41} & t_{42} & t_{43} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix}$$



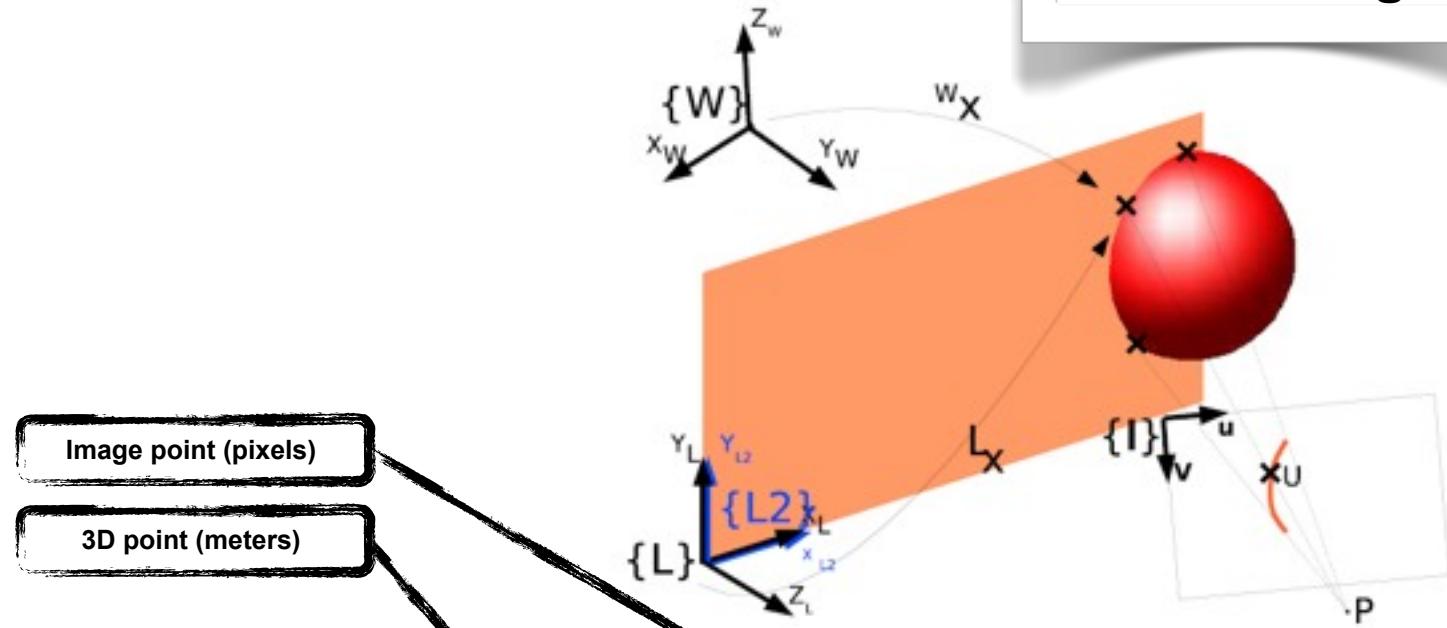
Structured light



$$\begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = {}^W T_L \cdot {}^L T_{L2} \cdot {}^{L2} H_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_L \cdot \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} e_{11} & e_{12} & e_{13} \\ e_{21} & e_{22} & e_{23} \\ e_{31} & e_{32} & e_{33} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ t_{31} & t_{32} & t_{33} \\ t_{41} & t_{42} & t_{43} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix}$$



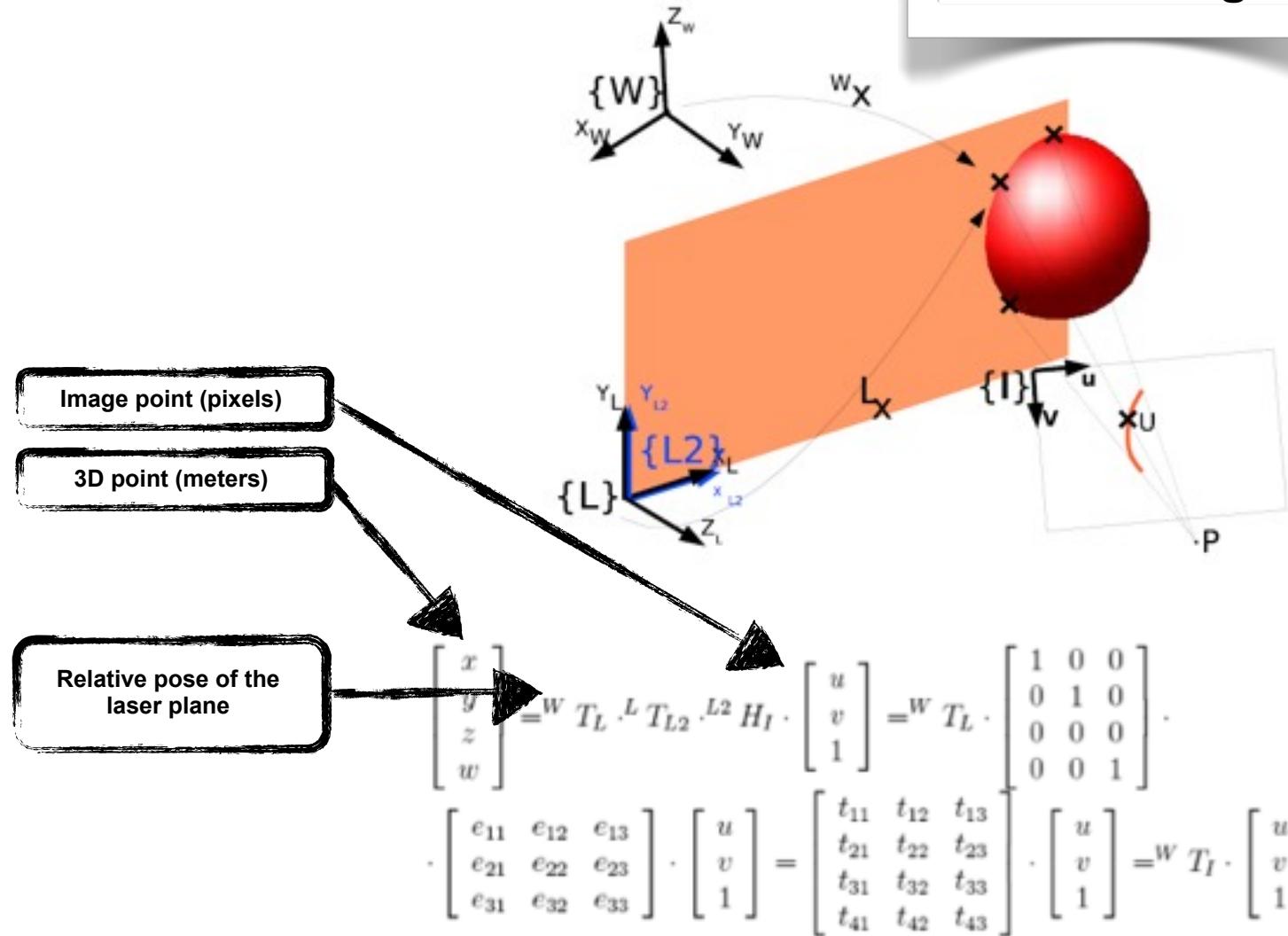
Structured light



$$\begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix} = {}^W T_L \cdot {}^L T_{L2} \cdot {}^{L2} H_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_L \cdot \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} e_{11} & e_{12} & e_{13} \\ e_{21} & e_{22} & e_{23} \\ e_{31} & e_{32} & e_{33} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} t_{11} & t_{12} & t_{13} \\ t_{21} & t_{22} & t_{23} \\ t_{31} & t_{32} & t_{33} \\ t_{41} & t_{42} & t_{43} \end{bmatrix} \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = {}^W T_I \cdot \begin{bmatrix} u \\ v \\ 1 \end{bmatrix}$$

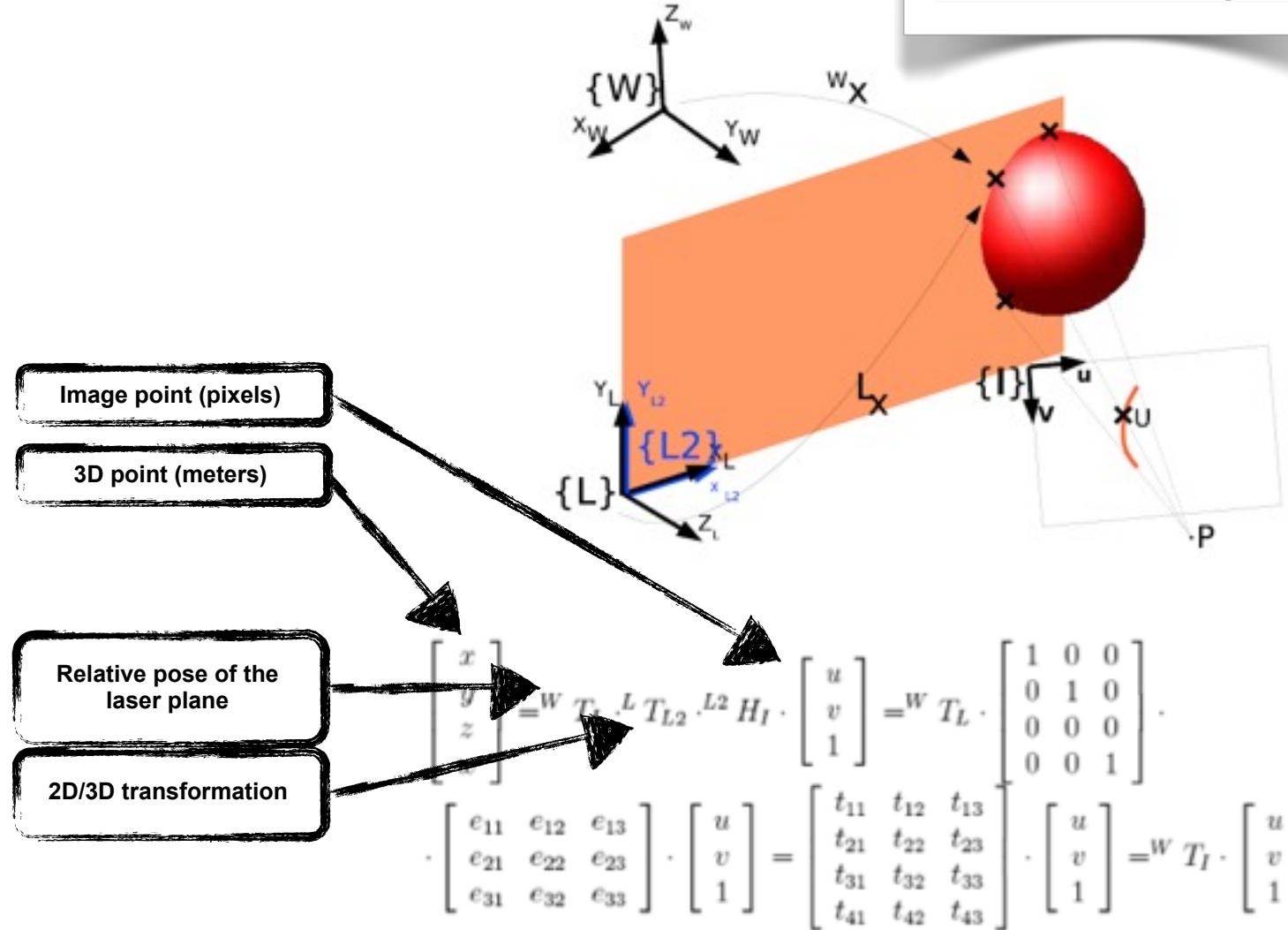


Structured light



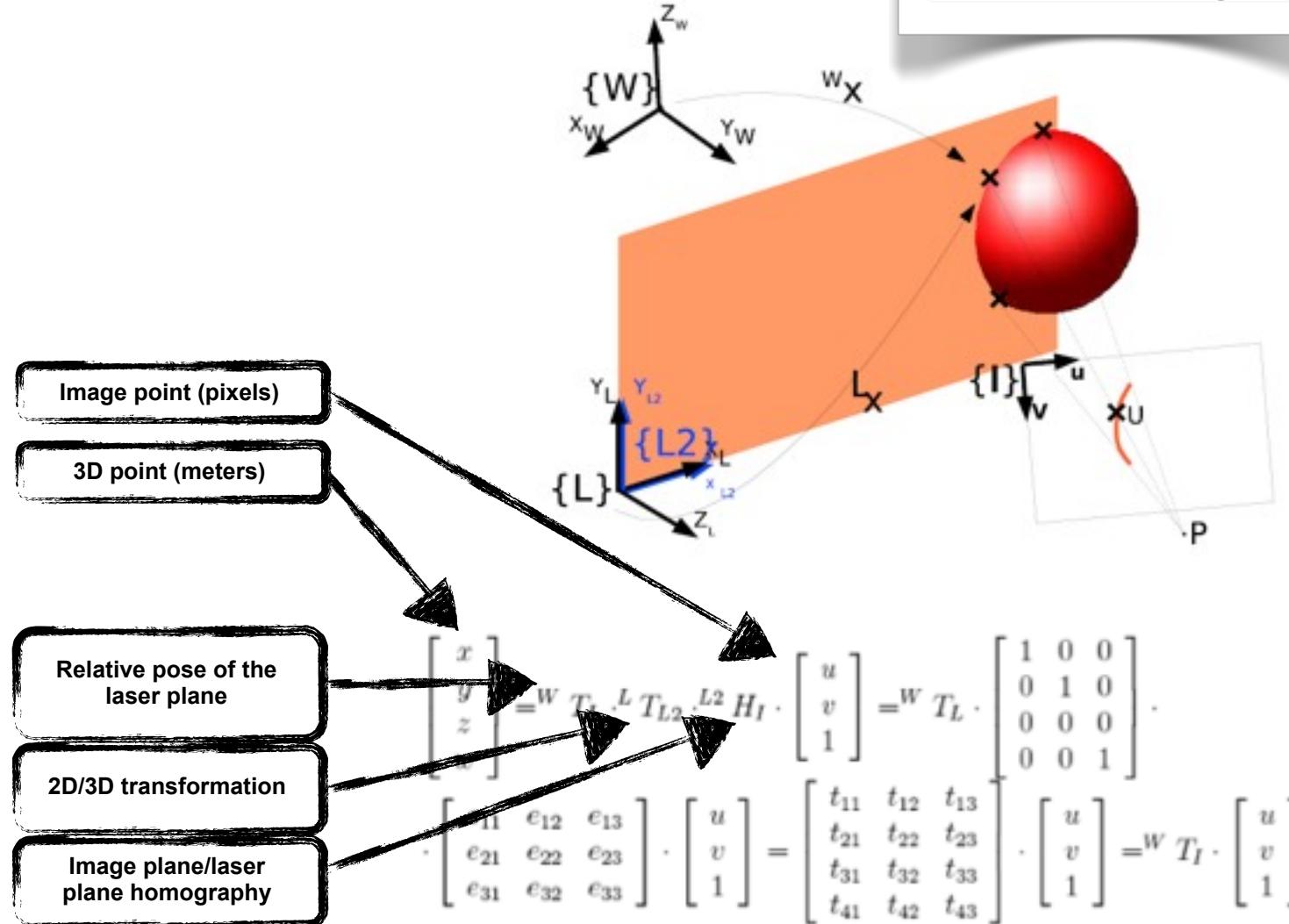


Structured light



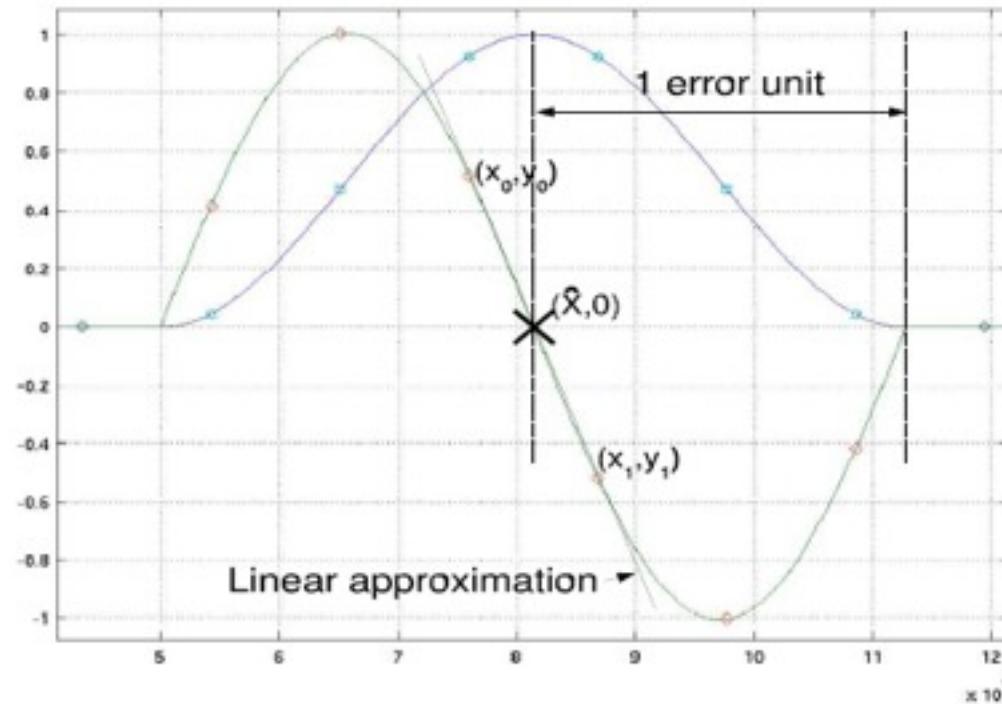


Structured light





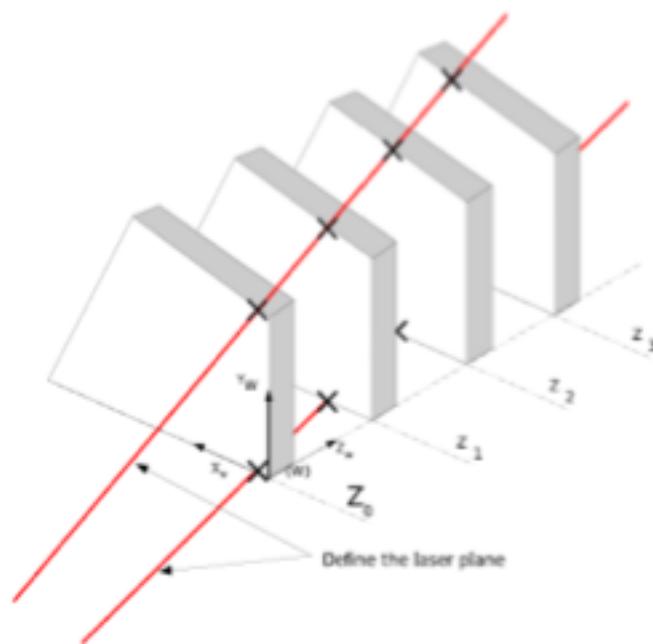
Peak detection



Introduction • Stereovision • **Laser-Camera** • Projector-Camera • Applications • Conclusion

How to retrieve the coordinate of 3D points lighted by the laser (to establish the 3D/2D correspondence)?

One method: the complete quadrangle!



Référence : J. Forest, "New methods for triangulation-based shape acquisition using laser scanners",
Thèse de doctorat, Université de Gérone, Espagne, mai 2004.

Performances

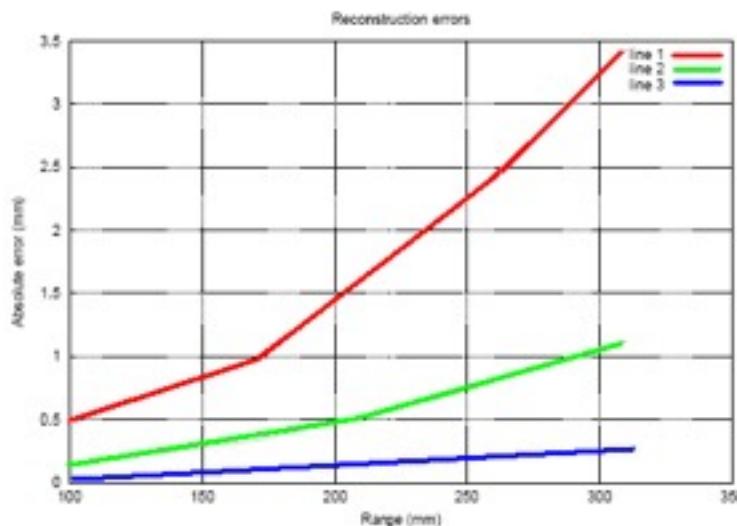
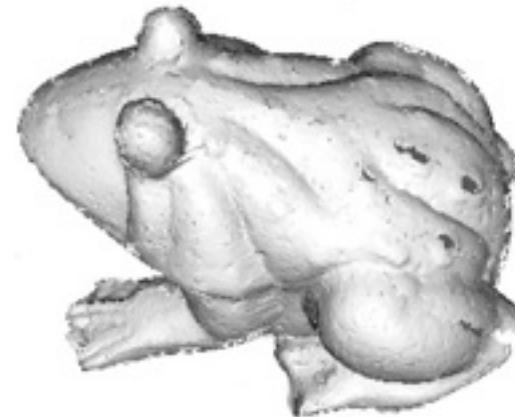


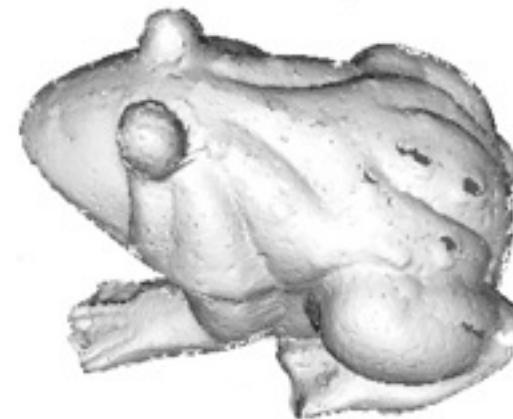
Table A.1: Performance of the Chen and Kak scanner.

Range (mm)	100	170	240	310
Image error (pix.)	6,8916	7,0088	7,0505	7,0395
X error (mm)	0,144	0,3342	0,6703	1,1239
Y error (mm)	0,0573	0,0963	0,1594	0,2651
Z error (mm)	0,4535	0,9967	2,0569	3,4345



Examples

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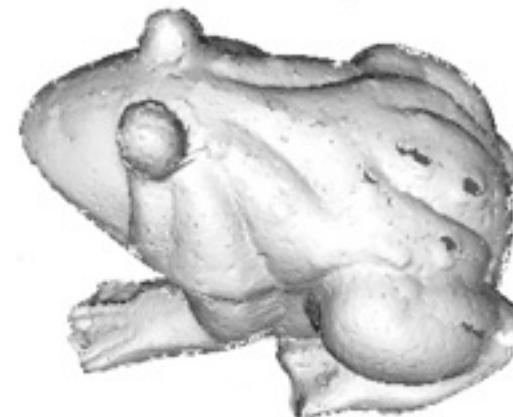


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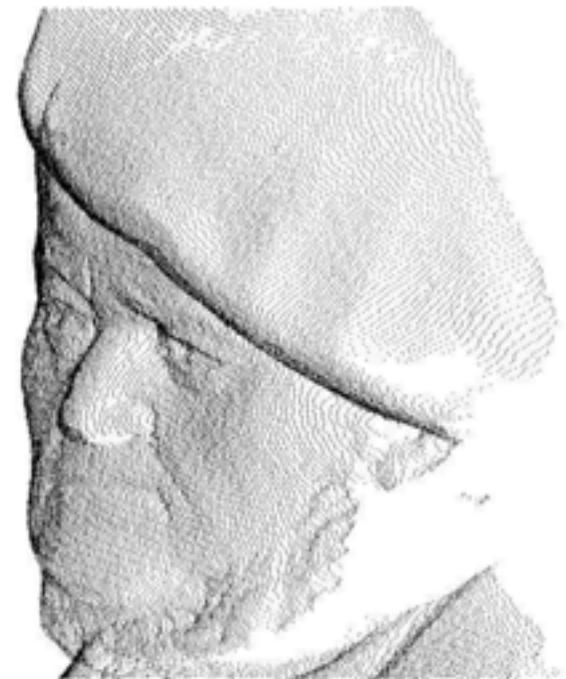
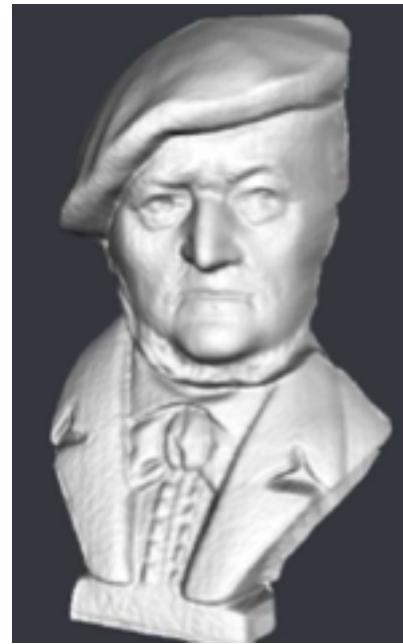


Examples



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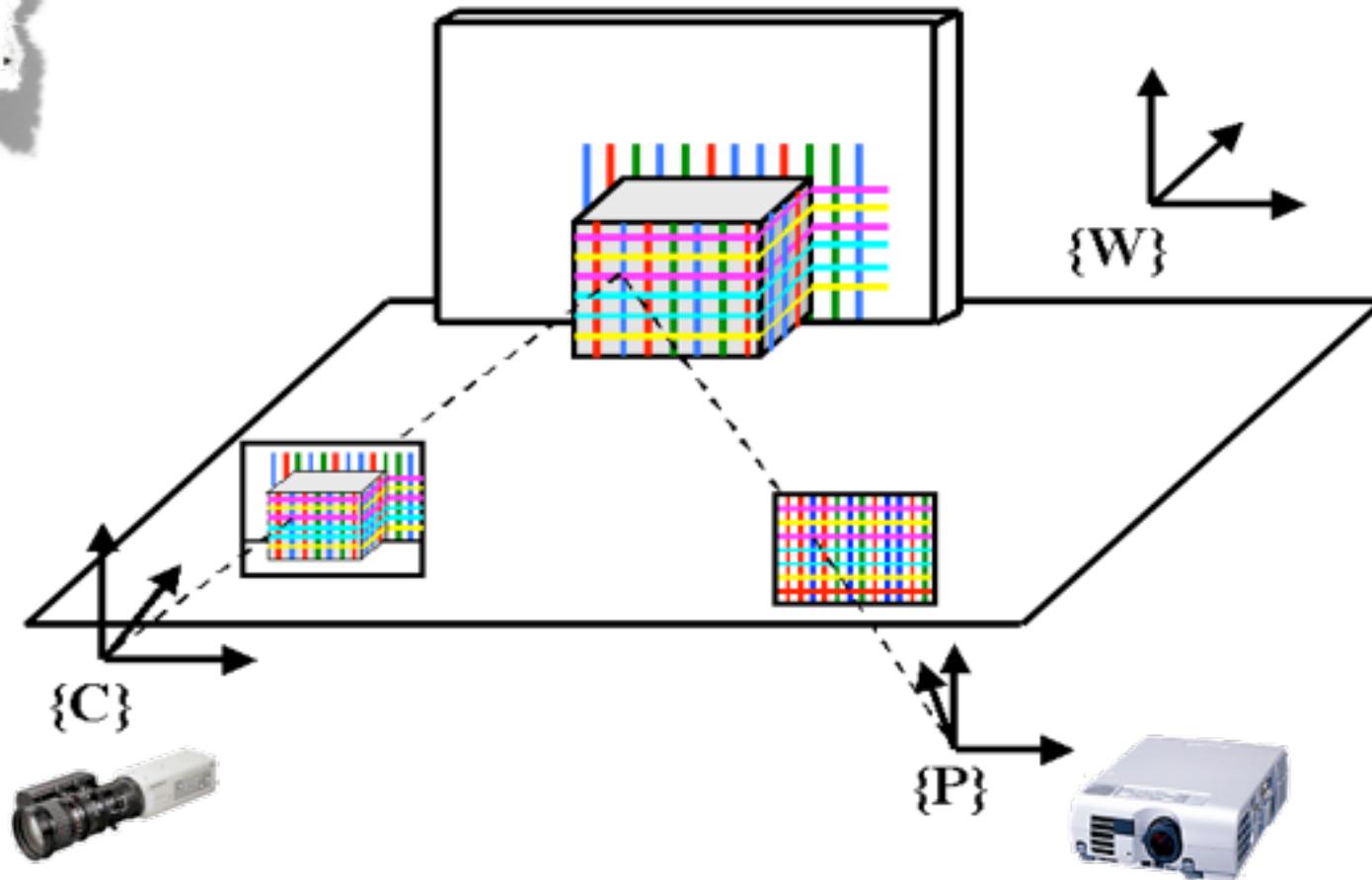
Examples



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Projector-Camera

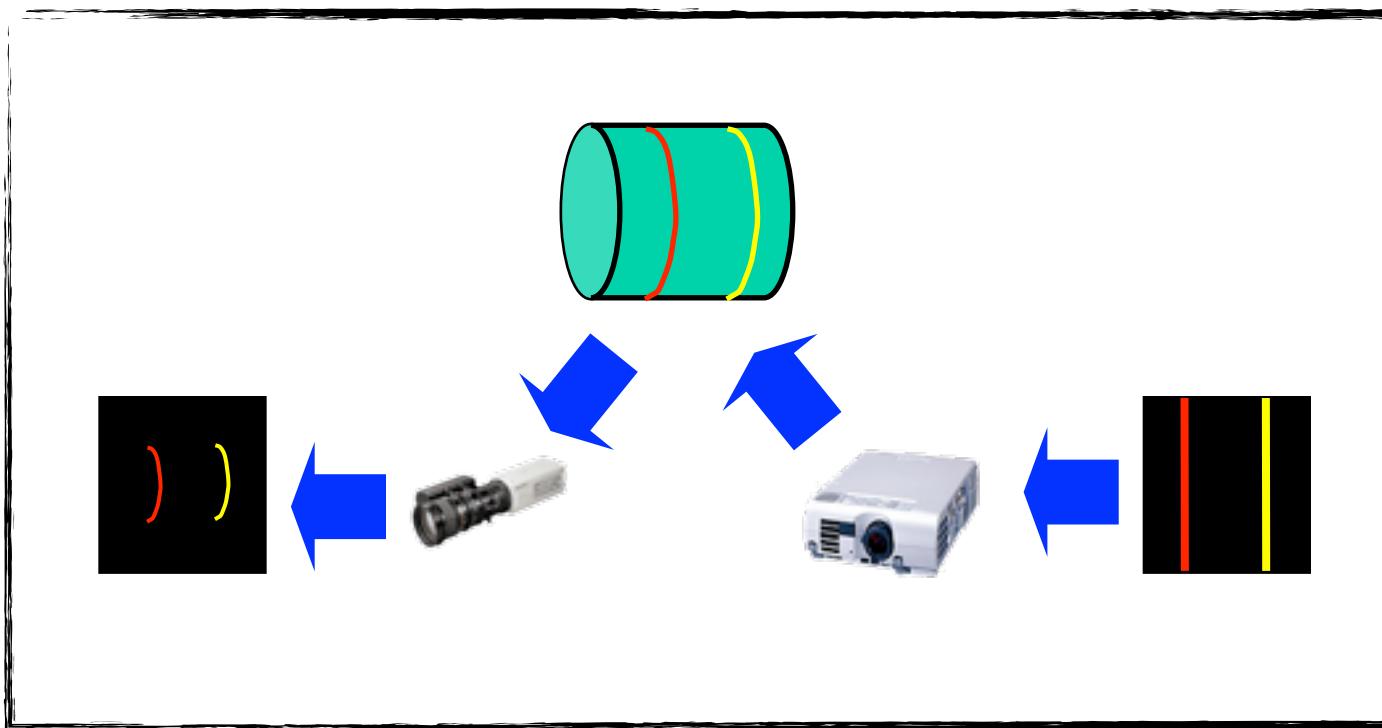


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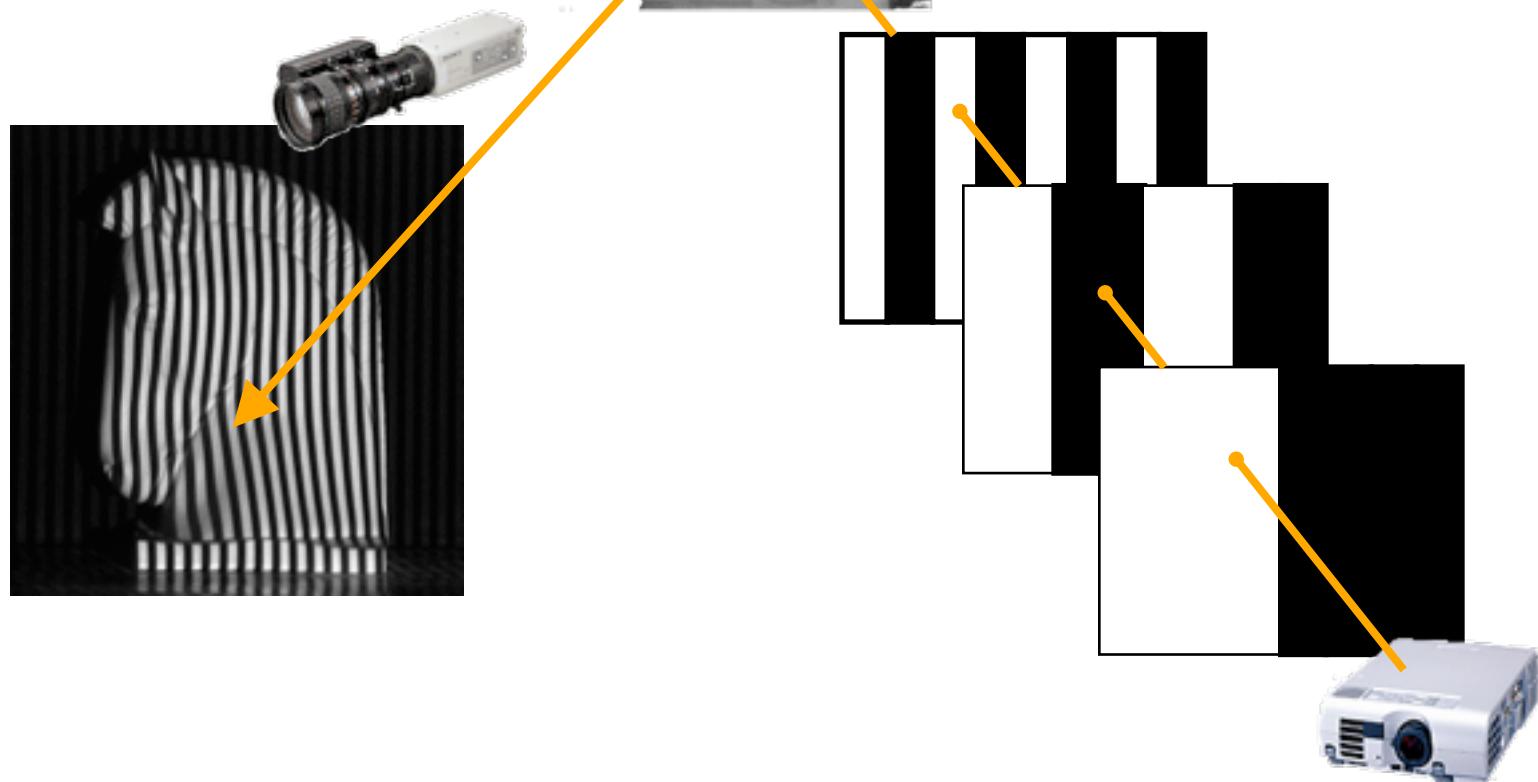
Projector-Camera

In order to ease the correspondence problem, the projected light can be coded...





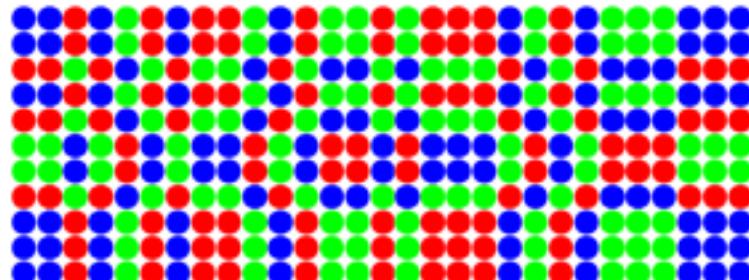
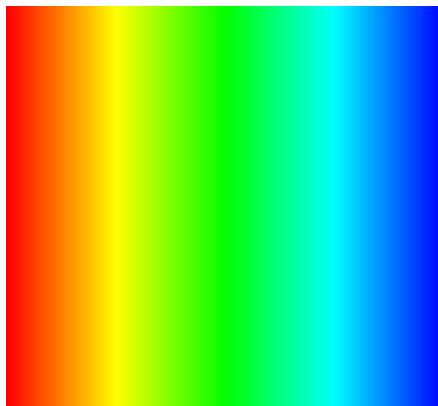
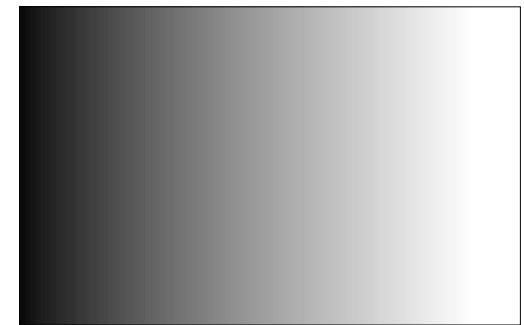
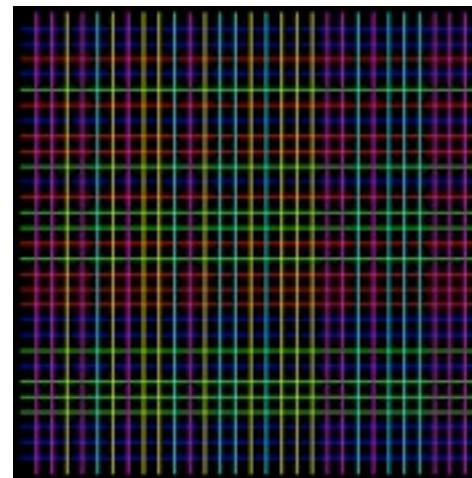
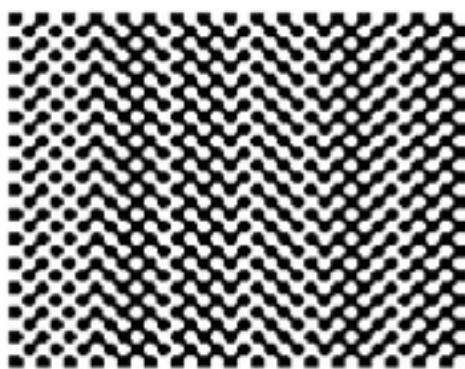
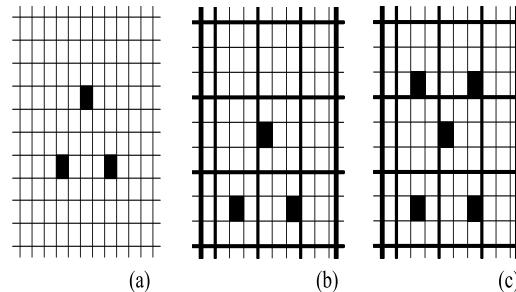
Example



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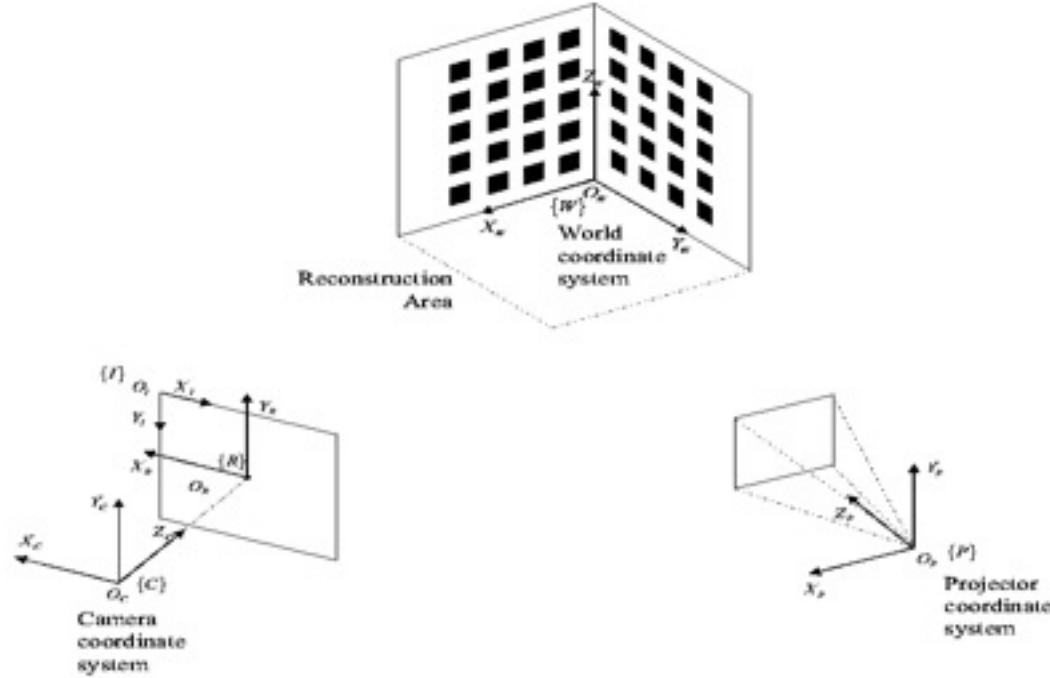


Pattern codification

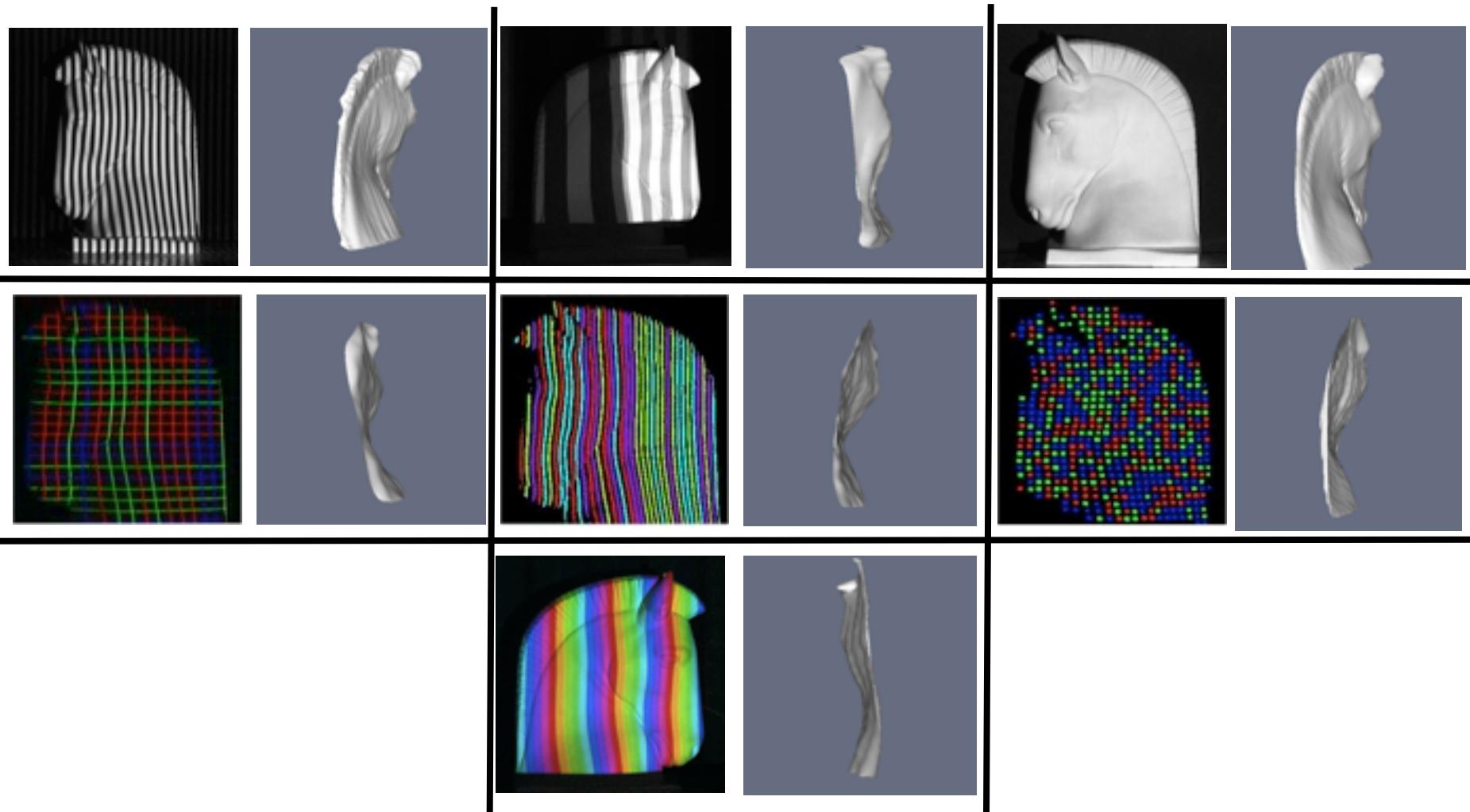


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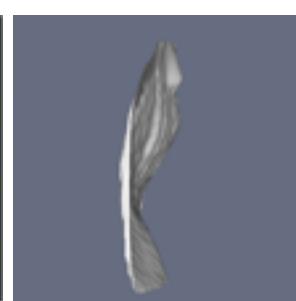
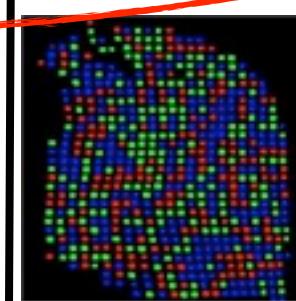
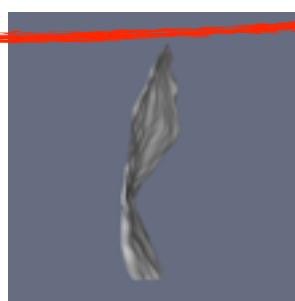
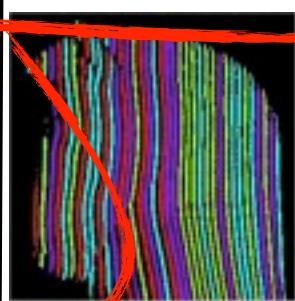
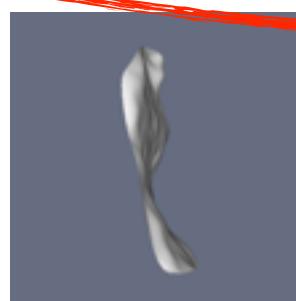
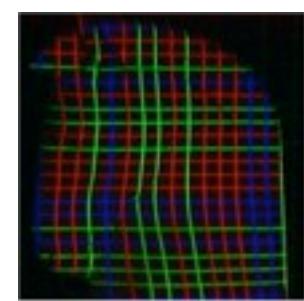
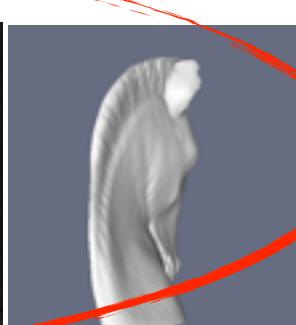
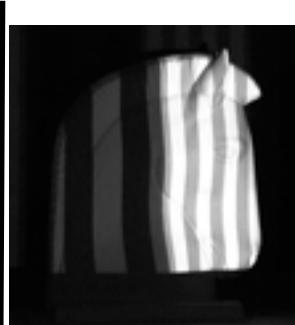
A projector can be seen as a camera acting in reverse!



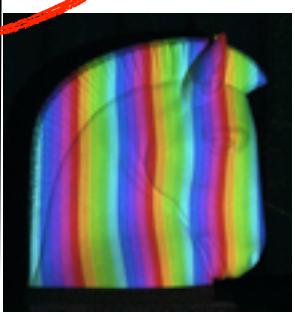
Examples



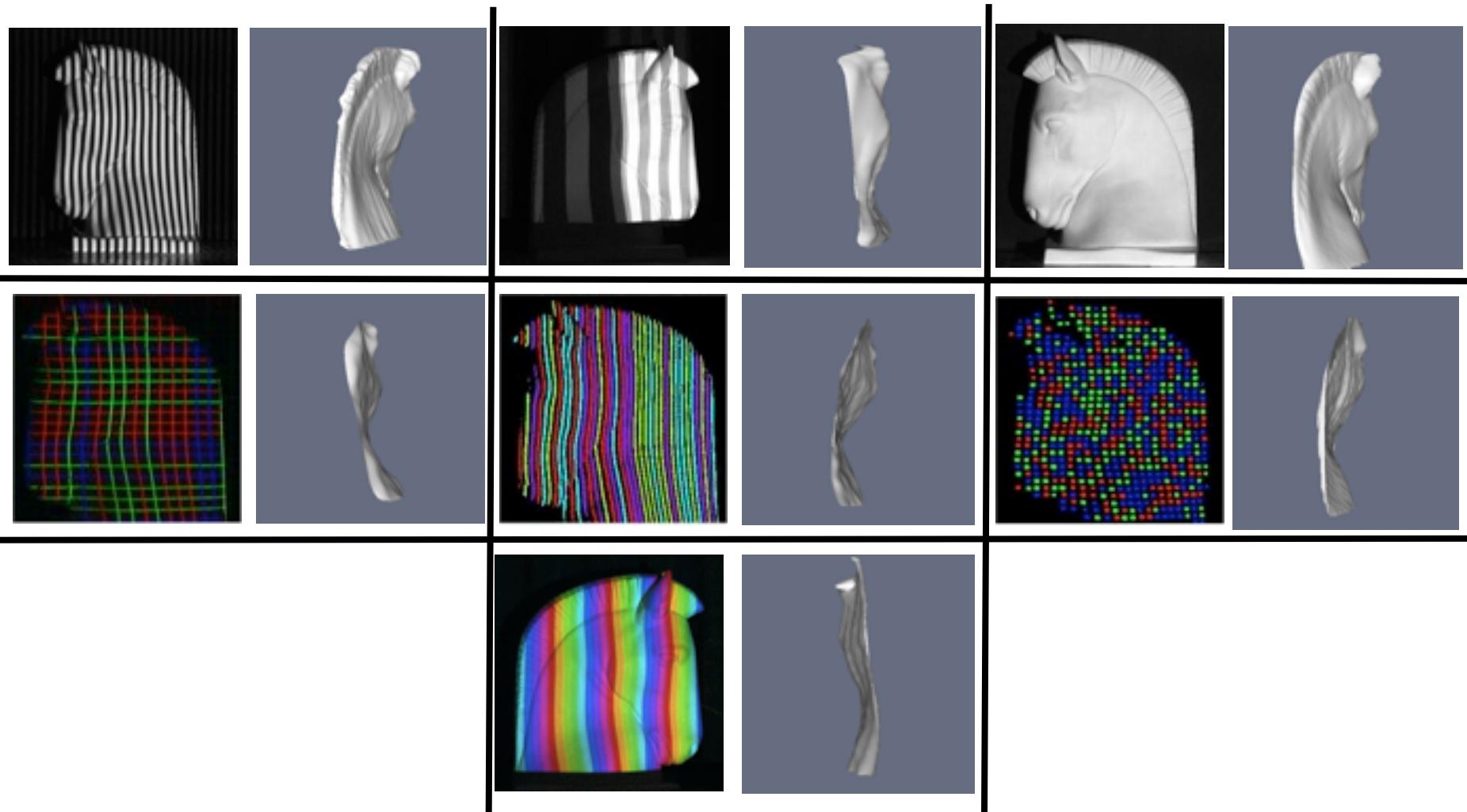
Examples



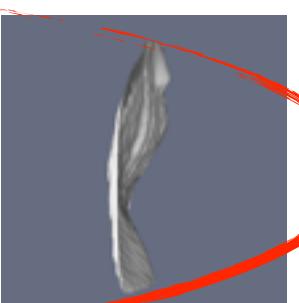
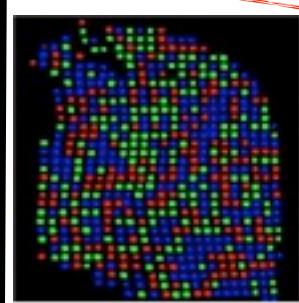
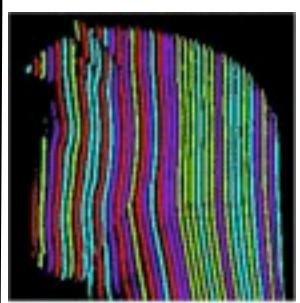
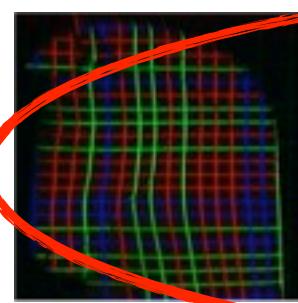
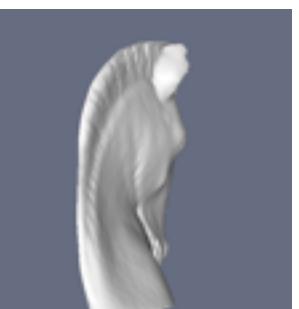
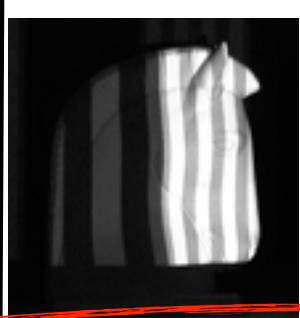
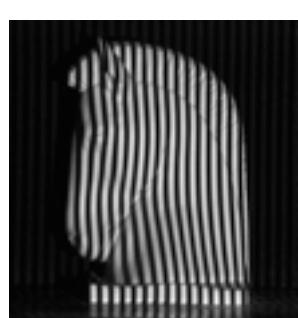
Temp. codification



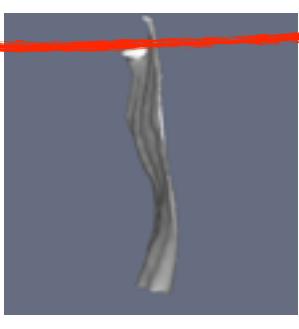
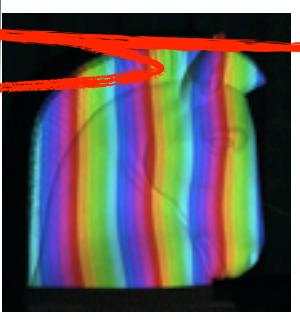
Examples



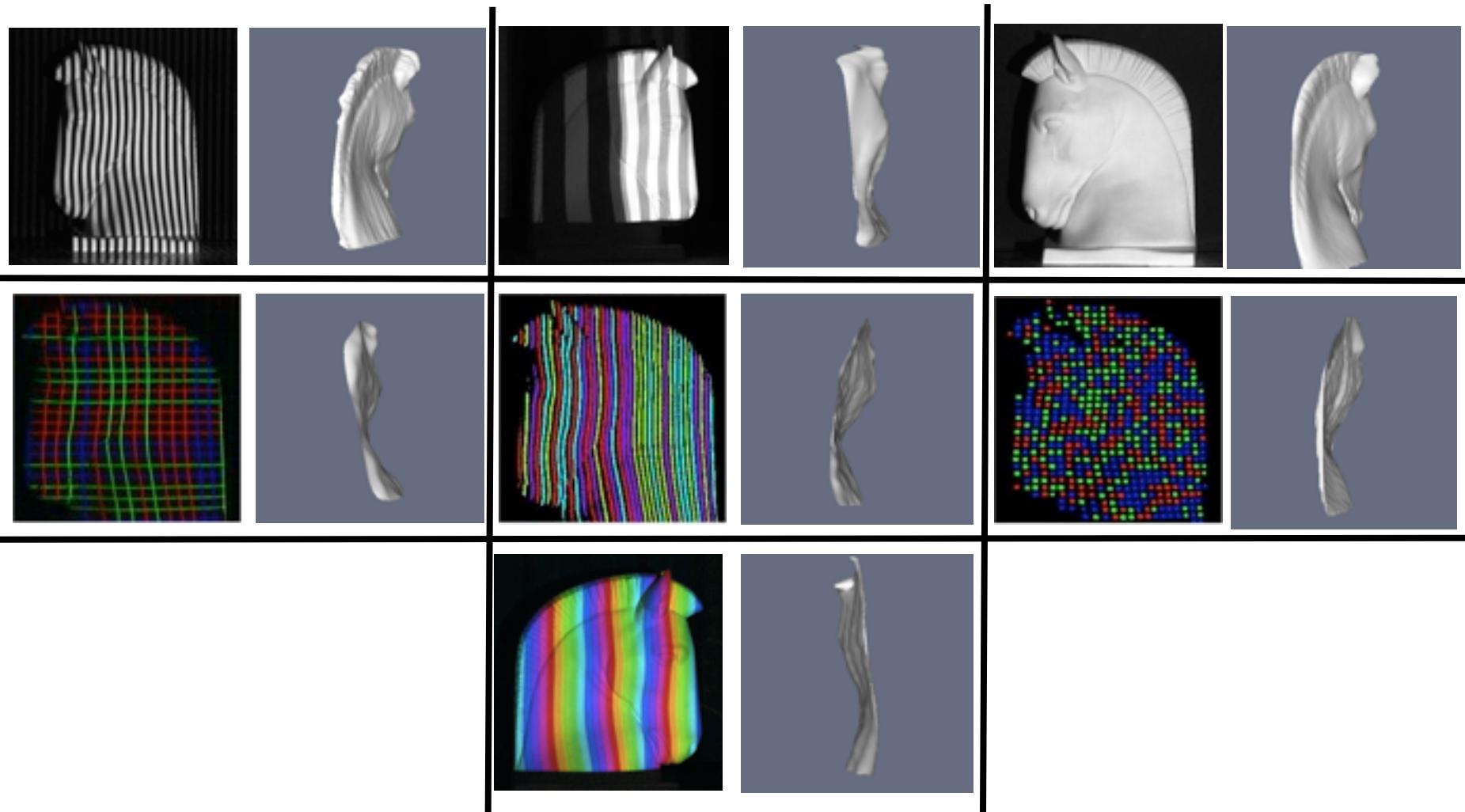
Examples



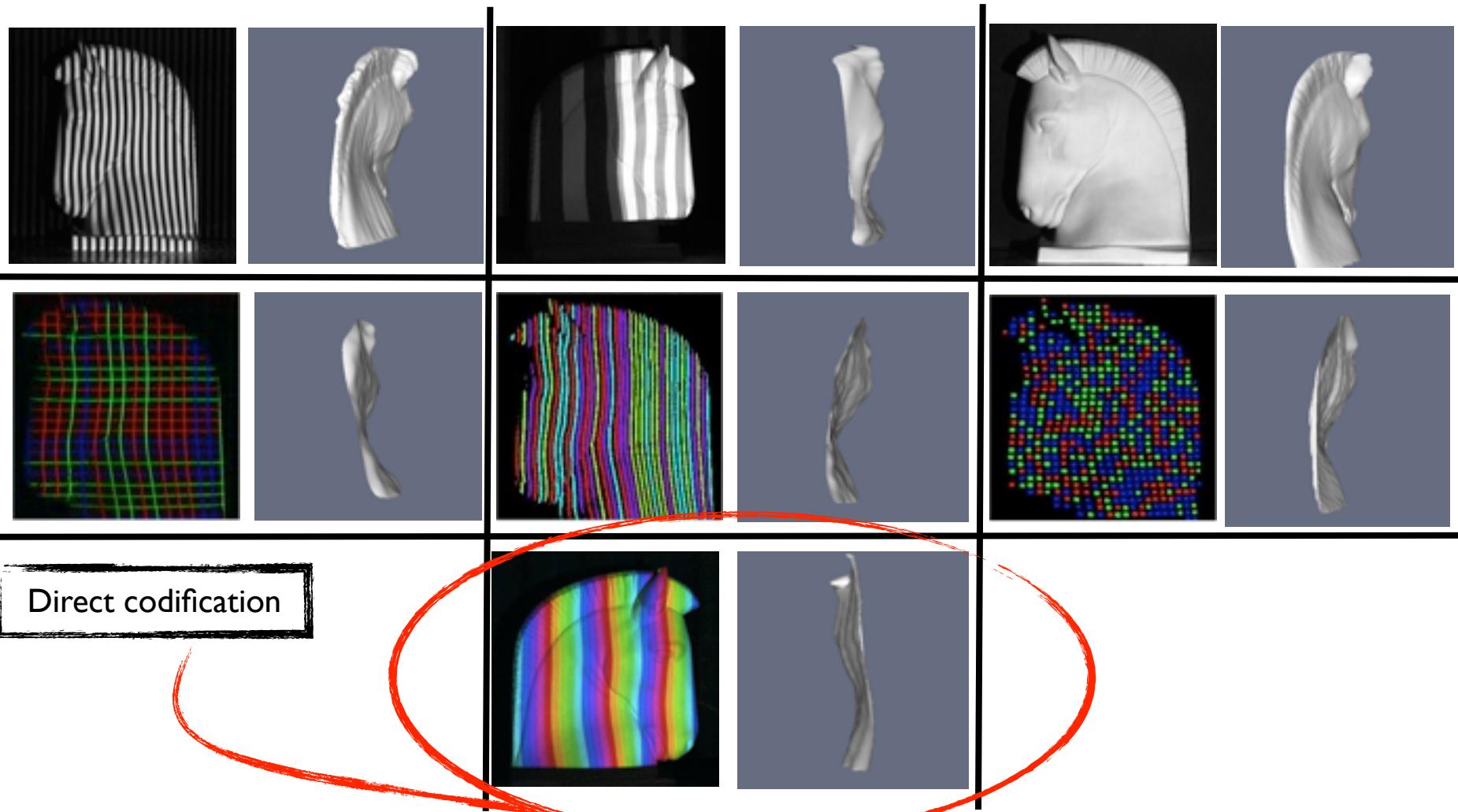
Spatial codification



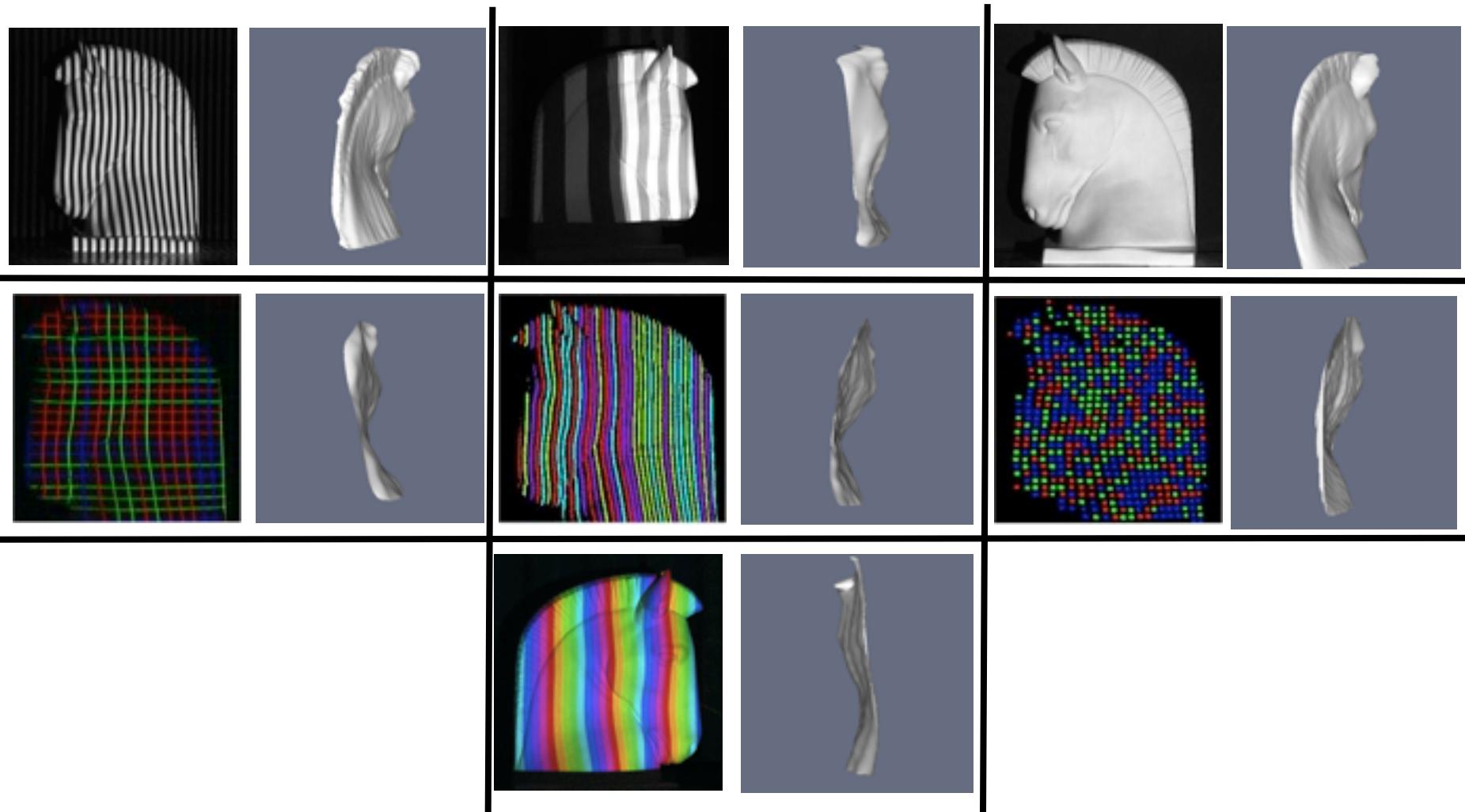
Examples



Examples

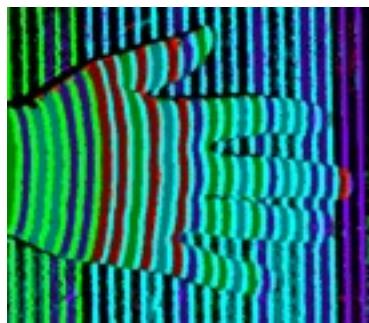
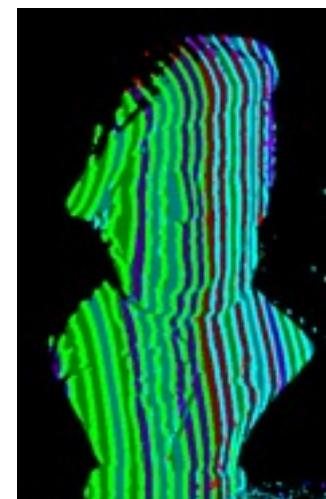


Examples





Examples



Introduction • Stereovision • Laser-Camera • **Projector-Camera** • Applications • Conclusion



Stereo and robotics

Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion



Stereo and robotics



Pioneer 2

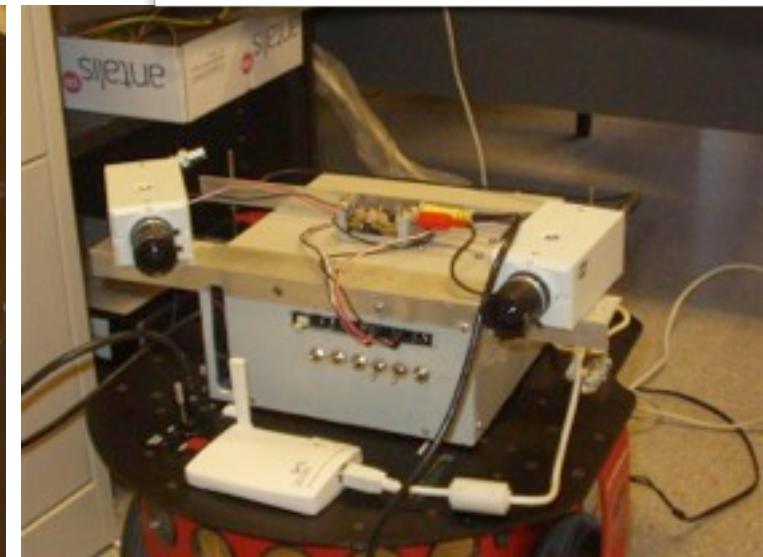
Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion



Stereo and robotics



vue interne



vue externe



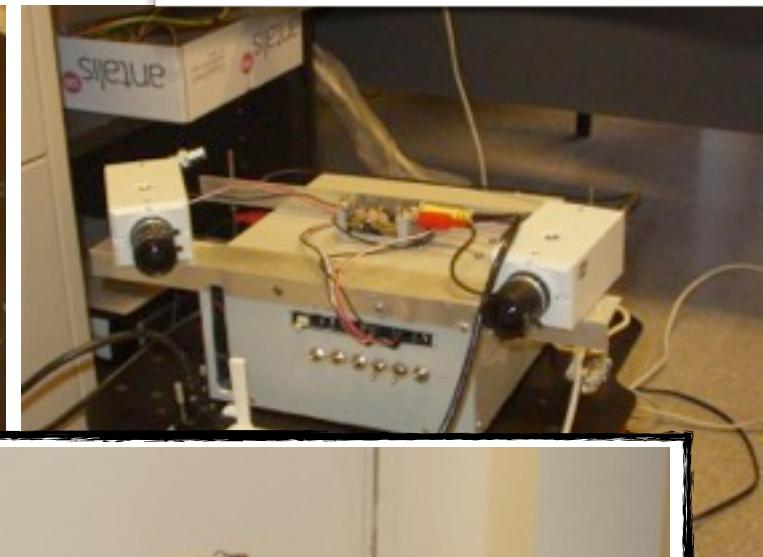
Pioneer 2

Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion

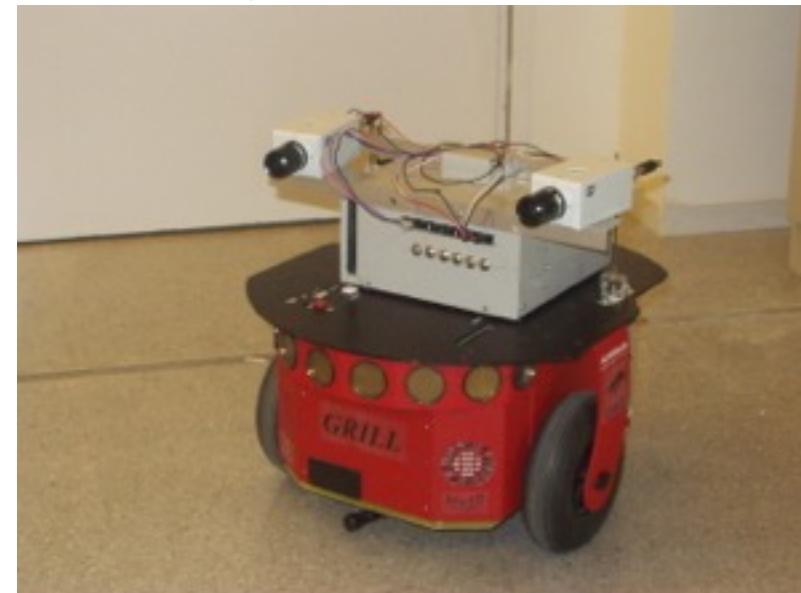
Stereo and robotics



vue interne



Pioneer 2



GRILL, le robot mobile

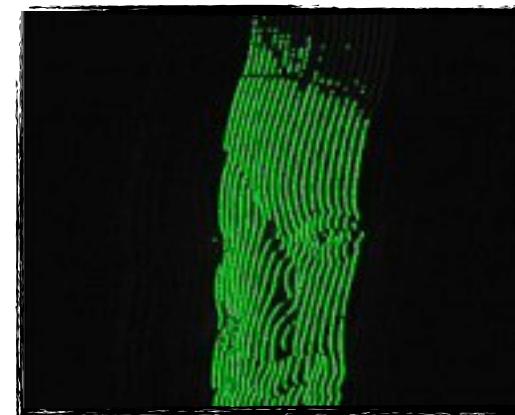
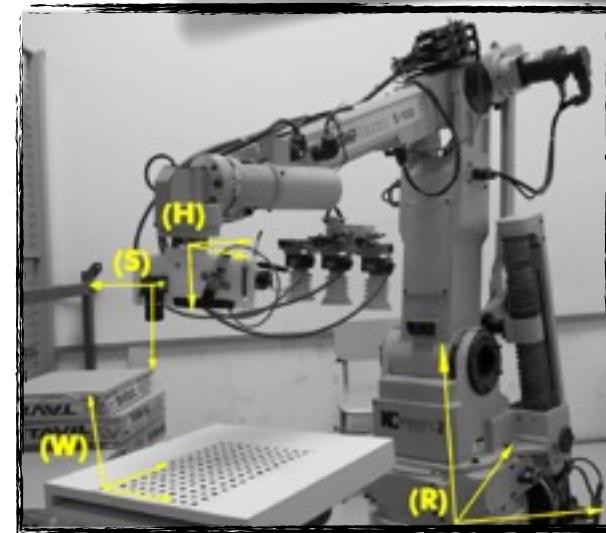
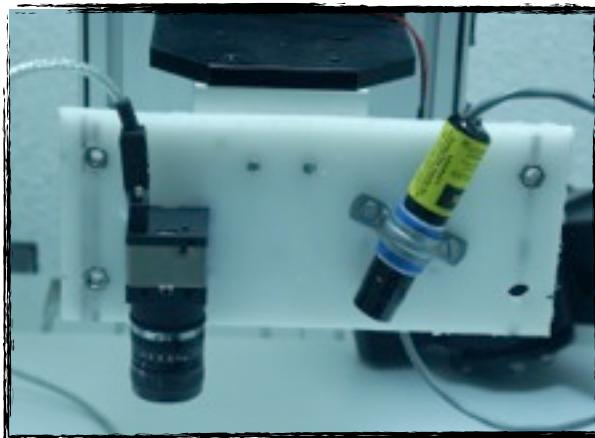
Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion

Input Stereo Image



Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion

Structured light



Introduction • Stereovision • Laser-Camera • Projector-Camera • **Applications** • Conclusion



Structured light



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Stereovision

- Sparse reconstruction (in general)
- Correspondence problem
- Applications to SfM/SLAM for mobile robotics

Laser-Camera

- High density, high resolution, high accuracy
- Mechanical scanning
- Intrusive sensor
- Applications to 3D modeling and measurements

Projector-Camera

- In between...
- Kinect...