

GADTs Practice

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Exercise 5

- Parse a series of tokens.
- Stack push and pop.
- Evaluate a sequence of tokens.
- Calculate a string.

Recall: GADTs

Generalised Algebraic Datatypes (*GADTs*) is an extension to Haskell that, among other things, allows data types to be specified by writing the types of their constructors:

```
{-# LANGUAGE GADTs, KindSignatures #-}
-- Unary natural numbers, e.g. 3 is S (S (S Z))
data Nat = Z | S Nat
-- is the same as
data Nat :: * where
    Z :: Nat
    S :: Nat -> Nat
```

Consider the well known C function printf:

```
printf("Hello %s You are %d years old!", "Nina", 22)
```

In C, the type (and number) of parameters passed to this function are dependent on the first parameter (the format string).

To do a similar thing in Haskell, we would like to use a richer type that allows us to define a function whose subsequent parameter is determined by the first.

Our format strings are indexed by a tuple type containing all of the types of the %directives used.

"Hello %s You are %d years old!"

is written:

```
L "Hello" $ Str $ L " You are "
$ Dec $ L " years old!" End
```

```
printf :: Format ts -> ts -> IO ()
printf End () =
    pure () -- type is ()
printf (Str fmt) (s,ts) =
    do putStr s; printf fmt ts -- type is (String, ...)
printf (Dec fmt) (i,ts) =
    do putStr (show i); printf fmt ts -- type is (Int,..)
printf (L s fmt) ts =
    do putStr s; printf fmt ts
```

Exercise 5

Vectors

Define a natural number kind to use on the type level:

```
data Nat = Z | S Nat
```

Our length-indexed list can be defined, called a Vec:

```
{-# LANGUAGE DataKinds #-}
data Vec (a :: *) :: Nat -> * where
  Nil :: Vec a Z
  Cons :: a -> Vec a n -> Vec a (S n)
```

The functions hd and tl can be total:

```
hd :: Vec a (S n) -> a
hd (Cons x xs) = x
tl :: Vec a (S n) -> Vec a n
tl (Cons x xs) = xs
```

Exercise 5

Vectors, continued

Our map for vectors is as follows:

```
mapVec :: (a -> b) -> Vec a n -> Vec b n
mapVec f Nil = Nil
mapVec f (Cons x xs) = Cons (f x) (mapVec f xs)
```

Properties

Using this type, it's impossible to write a mapVec function that changes the length of the vector.

Properties are verified by the compiler!

Appending Vectors

Example (Problem)

```
appendV :: Vec a m -> Vec a n -> Vec a ???
```

We want to write m + n in the ??? above, but we do not have addition defined for kind Nat.

We can define a normal Haskell function easily enough:

```
plus :: Nat -> Nat -> Nat
plus Z y = y
plus (S x) y = S (plus x y)
```

This function is not applicable to type-level Nats, though.

 \Rightarrow we need a type level function.

Type Families

Type level functions, also called *type families*, are defined in Haskell like so:

Concatenating Vectors

Example (Problem)

```
concatV :: Vec (Vec a m) n -> Vec a ???
```

We want to write m * n in the ??? above, but we do not have times defined for kind Nat.

Filtering Vectors

Example (Problem)

```
filterV :: (a -> Bool) -> Vec a n -> Vec a ???
```

What is the size of the result of filter?

Filtering Vectors

Example (Problem)

```
filterV :: (a -> Bool) -> Vec a n -> [a]
```

We do not know the size of the result.

We can use our type family to define concatV:

Homework

- Assignment 2 is released. The deadline has been extended; it is now due on Wednesday 4th August, 6 PM (in 12 days).
- Week 7's quiz is due on today. Make sure you submit your answers.
- The sixth programming exercise is due by the start of my next lecture (in 7 days).
- This week's quiz is also up, it's due Friday next week at 6pm (in 7 days).

Consultations

- Consultations will be made on request. Ask on course forum or email cs3141@cse.unsw.edu.au.
- If there is a consultation it will be announced on the course forum with a link a room number for Hopper.
- Make sure to join the queue on Hopper. Be ready to share your screen with REPL (ghci or stack repl) and editor set up.