

EXPERIMENT No.4

FORMATION OF BUS ADMITTANCE MATRIX

Aim

To formulate a Y- Bus using two-dimensional matrix by step by step method, develop a computer program and implement on four bus system.

Software Platform

Scilab

Theory

The Y-bus /Z-bus matrix constitutes the models of the passive portions of the power network. Y-bus matrix is often used in solving load flow problems. It has gained widespread applications owing to its simplicity of data preparation and the ease with which the bus admittance matrix can be formed and modified for network changes. Of course, sparsity is one of its greatest advantages as it heavily reduces computer memory and time requirements. In short circuit analysis, the generator and transformer impedances must also be taken into account. In contingency analysis, the shunt elements are neglected, while forming the Z-bus matrix, which is used to compute the outage distribution factors. This can be easily obtained by inverting the Y-bus matrix. The impedance matrix is a full matrix and is most useful for short circuit studies. Initially, the Y-bus matrix is formed by considering line data only. After forming the Y-bus matrix, the modified Y-bus matrix is formed by adding the generator and transformer admittances to the respective diagonal elements and is inverted to form the Z-bus matrix.

The performance equation for a n-bus system in terms of admittance matrix can be written as,

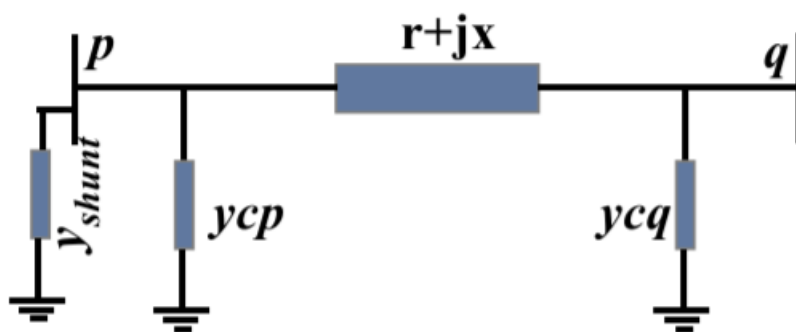
$$\begin{pmatrix} Y_{11} & Y_{12} & \cdots & Y_{1N} \\ Y_{21} & Y_{22} & \cdots & Y_{2N} \\ \vdots & \ddots & \cdots & \vdots \\ Y_{NN} & Y_{N2} & \cdots & Y_{NN} \end{pmatrix} * \begin{pmatrix} V_1 \\ V_2 \\ \vdots \\ V_N \end{pmatrix} = \begin{pmatrix} I_1 \\ I_2 \\ \vdots \\ I_N \end{pmatrix}$$

$$\mathbf{I} = \mathbf{Y}_{bus} \cdot \mathbf{V}$$

The admittances $Y_{11}, Y_{22}, \dots, Y_{nn}$ are called the self-admittances at the nodes and all other admittances are called the mutual admittances of the nodes.

Inspection method

The admittance matrix can be formed from the parameters of system components. A diagonal element Y_{pp} is the sum of all admittances connected to the p th bus. An off-diagonal element Y_{pq} is the negative sum of the all admittances directly connected between p th and q th buses.



π -model of transmission line

We start with $[Y_{bus}]$ array initially set to zero. The dimensions of $[Y_{bus}]$ are $n \times n$ bus, where 'n' is the number of buses (or the total no. of nodes, including reference node). Consider an element having admittance y_{pq} connected between buses p and q . Four entries in Y_{bus} are affected: Y_{pp} , Y_{qq} , Y_{pq} and Y_{qp} . We modify these entries as below,

$$Y_{pp,new} = Y_{pp,old} + y_{pq} + y_{cp} \quad (1.1a)$$

$$Y_{qq,new} = Y_{qq,old} + y_{qp} + y_{cq} \quad (1.1b)$$

$$Y_{pq,new} = Y_{pq,old} - y_{pq} \quad (1.1c)$$

$$Y_{qp,new} = Y_{qp,old} - y_{qp} \quad (1.1d)$$

We add the elements one by one and modify the entries of $[Y_{bus}]$ as per equations (1.1). If an element is connected from i th bus to reference, only entry Y_{pp} is affected.

Program

Problem 1

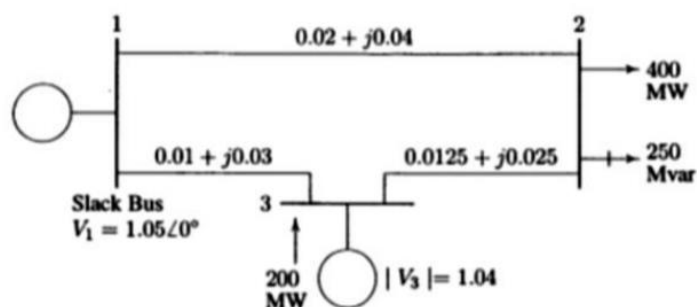
Form the Y Bus for the system shown in figure by step by step method.

Line No. (k)	From Bus $l_p(k)$	To Bus $l_q(k)$	Line Impedance	y_{cp}	y_{cq}
1	1	2	$0.01 + j0.04$	$j0.08$	$j0.08$
2	1	3	$0 + j0.1$	0	0
3	2	3	$0.04 + j0.16$	$j0.09$	$j0.09$
4	2	5	$0.06 + j0.18$	$j0.08$	$j0.08$
5	2	5	$0.06 + j0.18$	$j0.08$	$j0.08$
6	3	4	$0 + j0.1$	0	0
7	4	5	$0.1 + j0.3$	0	0

$y_{shunt}(i)$	0	0	0	0	$j0.3$
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Problem 2

For the network shown in figure, determine the bus admittance matrix .



Sample Program (All)

```
1. clc;
2. clear;
3. //input
4. buses=input("Enter the number of buses:")
5. line=input("Enter the number of lines:")
6. Ybus=zeros(buses,buses)
7. net_data=zeros(line,6)
8. Yshunt=zeros(1,buses)
9. row=list()
10. for i=1:line
11. row(i)=string(i)
12. end
13. row=list2vec(row)
14. sh_col=list()
15. for i=1:buses
16. sh_col(i)="Bus"+string(i)
17. end
18. sh_col=list2vec(sh_col)
19. column=['From Bus';'To Bus';'Line res';'Line
    imp';'ycp';'ycq']
20. net_data=x_mdialog("Network
    Data",row,column,string(net_data))
21. Yshunt=x_mdialog("Shunt
    Admittance","Yshunt",sh_col,string(Yshunt))
22. net_data=resize matrix(net_data,-1,-1,"constant")
23. Yshunt=resize matrix(Yshunt,-1,-1,"constant")
24. //Extraction
25. from=net_data(:,1)
26. to=net_data(:,2)
27. z=(net_data(:,3)+net_data(:,4)*%i)
28. ycp=net_data(:,5)*%i
29. ycq=net_data(:,6)*%i
30. Yshunt=Yshunt*%i
31. //logic
32. for i=1:line
33. p=from(i)
34. q=to(i)
35. Ybus(p,p)=Ybus(p,p)+1/z(i)+ycp(i)
36. Ybus(q,q)=Ybus(q,q)+1/z(i)+ycq(i)
37. Ybus(p,q)=Ybus(p,q)-1/z(i)
38. Ybus(q,p)=Ybus(q,p)-1/z(i)
39. end
40. for i=1:buses
41. Ybus(i,i)=Ybus(i,i)+Yshunt(i)
42. end
43. //display
44. x_matrix('The Bus Admittance Matrix',Ybus)
45. disp("The Bus Admittance Matrix")
46. disp(Ybus)
```

Sample Output-1

Enter the number of buses:5

Enter the number of lines:7

Scilab Multiple Values Request

Network Data

	From Bus	To Bus	Line res	Line imp	ycp	ycq
1	1	2	0.01	0.04	0.08	0.08
2	1	3	0	0.1	0	0
3	2	3	0.04	0.16	0.09	0.09
4	2	5	0.06	0.18	0.08	0.08
5	2	5	0.06	0.18	0.08	0.08
6	3	4	0	0.1	0	0
7	4	5	0.1	0.3	0	0

OK Cancel

Scilab Multiple Values Request

Shunt Admittance

	Bus1	Bus2	Bus3	Bus4	Bus5
Yshunt	0	0	0	0	0.3

OK Cancel

Scilab Input Value Request

The Bus Admittance Matrix

```
[5.8823529- $\text{i}$ *33.449412, -5.8823529+ $\text{i}$ *23.529412,  $\text{i}$ *10, 0, 0  
-5.8823529+ $\text{i}$ *23.529412, 10.686275- $\text{i}$ *39.081765, -1.4705882+ $\text{i}$ *5.8823529, 0, -3.3333333+ $\text{i}$ *10  
 $\text{i}$ *10, -1.4705882+ $\text{i}$ *5.8823529, 1.4705882- $\text{i}$ *25.792353,  $\text{i}$ *10, 0  
0, 0,  $\text{i}$ *10, 1- $\text{i}$ *13, -1+ $\text{i}$ *3  
0, -3.3333333+ $\text{i}$ *10, 0, -1+ $\text{i}$ *3, 4.3333333- $\text{i}$ *12.54]
```

OK Cancel

Enter the number of buses:5

Enter the number of lines:7

"The Bus Admittance Matrix"

5.8823529 - 33.449412i	-5.8823529 + 23.529412i	0.	+ 10.i	0. + 0.i	0.	+ 0.i
-5.8823529 + 23.529412i	10.686275 - 39.081765i	-1.4705882 + 5.8823529i		0. + 0.i	-3.3333333 + 10.i	
0.	+ 10.i	-1.4705882 + 5.8823529i	1.4705882 - 25.792353i	0. + 10.i	0.	+ 0.i
0.	+ 0.i	0.	+ 0.i	0.	+ 10.i	1. - 13.i
0.	+ 0.i	-3.3333333 + 10.i	0.	+ 0.i	-1. + 3.i	4.3333333 - 12.54i

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Sample Output – 2

Enter the number of buses:3

Enter the number of lines:3

Scilab Multiple Values Request



Network Data

	From Bus	To Bus	Line res	Line imp	ycp	ycq
1	1	2	0.02	0.04	0	0
2	1	3	0.01	0.03	0	0
3	2	3	0.0125	0.025	0	0

OK Cancel

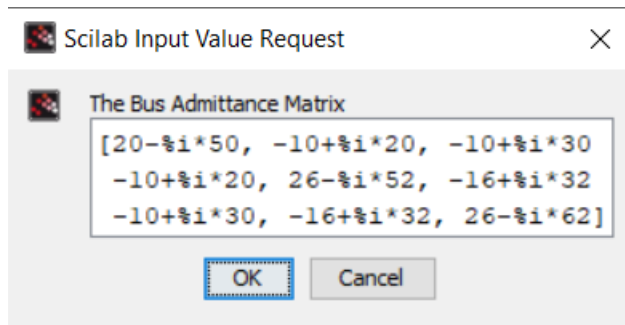
Scilab Multiple Values Request



Shunt Admittance

	Bus1	Bus2	Bus3
Yshunt	0	0	0

OK Cancel



"The Bus Admittance Matrix"

```
20. - 50.i   -10. + 20.i   -10. + 30.i  
-10. + 20.i   26. - 52.i   -16. + 32.i  
-10. + 30.i  -16. + 32.i   26. - 62.i
```

Result

The Y- bus matrix was formed for the given system by step by step method and the results were verified by manual calculation.