

# Quantum Tunneling Calculator

A COMPUTATIONAL SIMULATION OF QUANTUM TUNNELING

**PROJECT AIM:**

- TO DEMONSTRATE QUANTUM TUNNELING USING SCHRÖDINGER EQUATION
- TO VISUALIZE WAVE FUNCTION AND TUNNELING PROBABILITY

# Quantum Tunneling – Physical Background

- ▶ In quantum mechanics, particles behave as waves
- ▶ A particle can penetrate a potential barrier even if  $E < V_0$
- ▶ • This phenomenon is forbidden in classical mechanics

Equation:

- ▶ 
$$-(\hbar^2/2m) \frac{d^2\psi}{dx^2} + V(x)\psi = E\psi$$

# Outputs of the Tunneling Calculator

- ▶ Transmission (Tunneling) Probability
- ▶ Wave function  $\psi(x)$
- ▶ Probability Density  $|\psi(x)|^2$
- ▶ Rectangular Potential Barrier
- ▶ Transmission Probability:
- ▶  $T = [1 + (V_0^2 \sinh^2(\kappa L)) / (4E(V_0 - E))]^{-1}$

# How the Code Works

- ▶ User inputs: Energy, Barrier Height, Barrier Width
- ▶ Unit conversion to SI units (eV  $\rightarrow$  J, nm  $\rightarrow$  m)
- ▶ Solution of Schrödinger equation

## **Key Parameters:**

- ▶  $k = \sqrt{2mE}/\hbar$
- ▶  $\kappa = \sqrt{2m(V_0 - E)}/\hbar$
- ▶ Wave function constructed in three regions

# Applications

- ▶ Shows clear difference between classical and quantum physics
- ▶ Exponential decay of wave function inside barrier
- ▶ Finite transmission confirms tunneling

## **Applications of Quantum Tunneling:**

- ▶ Scanning Tunneling Microscope (STM)
- ▶ Flash memory devices
- ▶ Nuclear fusion and alpha decay