

Quantum Tunneling Calculator

A COMPUTATIONAL SIMULATION OF QUANTUM
TUNNELING

PROJECT AIM:

- TO DEMONSTRATE QUANTUM TUNNELING USING SCHRODINGER EQUATION
- TO VISUALIZE WAVE FUNCTION AND TUNNELING PROBABILITY

Quantum Tunneling – Physical Background

- ▶ In quantum mechanics, particles behave as waves
- ▶ A particle can penetrate a potential barrier even if $E < V_0$
- ▶ • This phenomenon is forbidden in classical mechanics

Equation:

- ▶ $-(\hbar^2/2m) d^2\psi/dx^2 + V(x)\psi = E\psi$

Outputs of the Tunneling Calculator

- ▶ Transmission (Tunneling) Probability
- ▶ Wave function $\psi(x)$
- ▶ Probability Density $|\psi(x)|^2$
- ▶ Rectangular Potential Barrier
- ▶ Transmission Probability:
- ▶ $T = [1 + (V_0^2 \sinh^2(\kappa L)) / (4E(V_0 - E))]^{-1}$

How the Code Works

- ▶ User inputs: Energy, Barrier Height, Barrier Width
- ▶ Unit conversion to SI units ($eV \rightarrow J$, $nm \rightarrow m$)
- ▶ Solution of Schrödinger equation

Key Parameters:

- ▶ $k = \sqrt{(2mE)/\hbar}$
- ▶ $\kappa = \sqrt{(2m(V_0 - E))/\hbar}$
- ▶ Wave function constructed in three regions

Applications

- ▶ Shows clear difference between classical and quantum physics
- ▶ Exponential decay of wave function inside barrier
- ▶ Finite transmission confirms tunneling

Applications of Quantum Tunneling:

- ▶ Scanning Tunneling Microscope (STM)
- ▶ Flash memory devices
- ▶ Nuclear fusion and alpha decay