

- Breadth-First Search (BFS)

- Queue ADT

Ring buffer : Implementation technique  
for queues.

Queue  $\langle T \rangle$

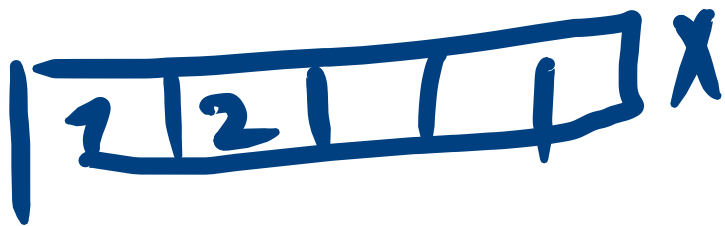
FIFO ~ First-in First-out

is.empty( $q$ )

enqueue( $q, e$ )  $\rightarrow$  adds elt to queue

dequeue( $q$ )  $\rightarrow$  returns the earliest element in the queue and removes it.

# Array Implementation of Queue



front back

$e(3)$

$e(1)$

$e(2)$

$d() \rightarrow 3$

$\leftarrow e() \text{ \& } d() \text{ are}$   
now  $O(1)$  operations.



$e(3)$   
 $e(4)$



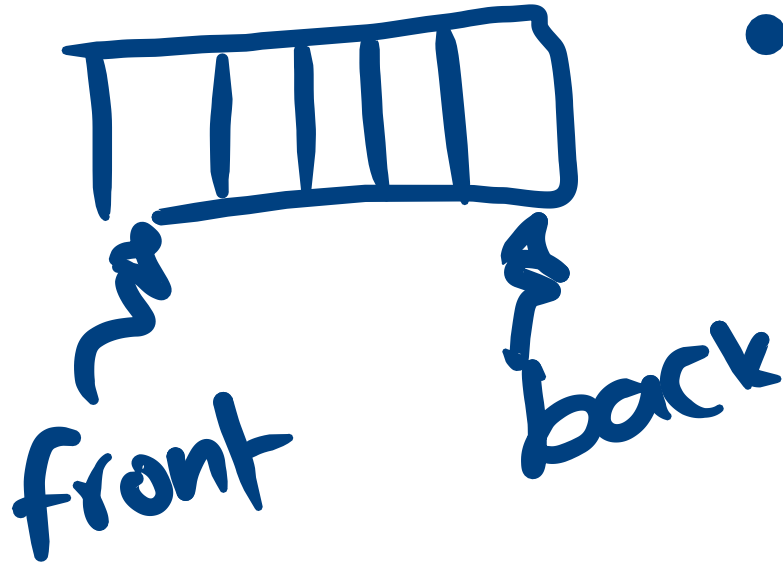
$d()$

$d()$

$d()$

front back

How to solve? Imagine first elt of array follows the last.  
(Ring buffer)



• len of the queue.

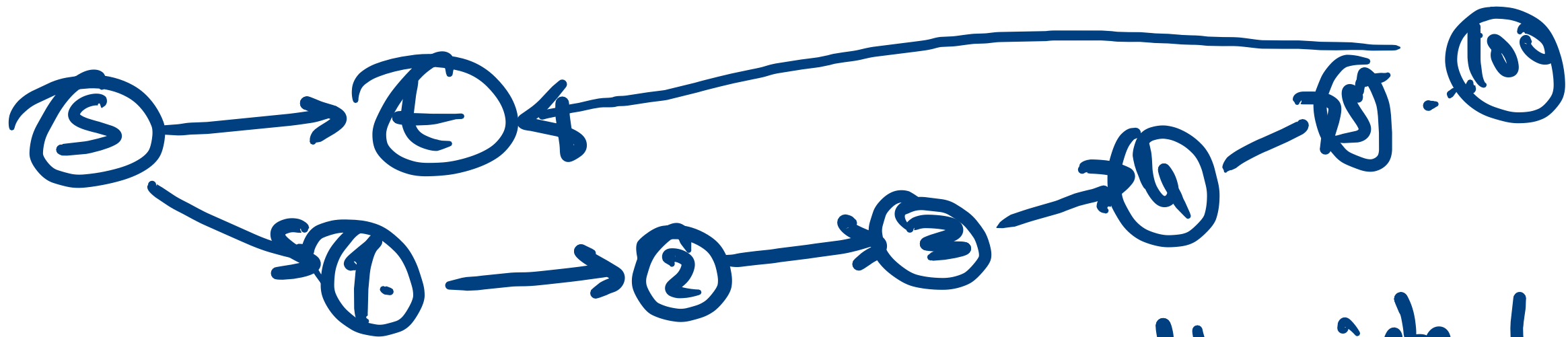
Why BFS?

8-Puzzle

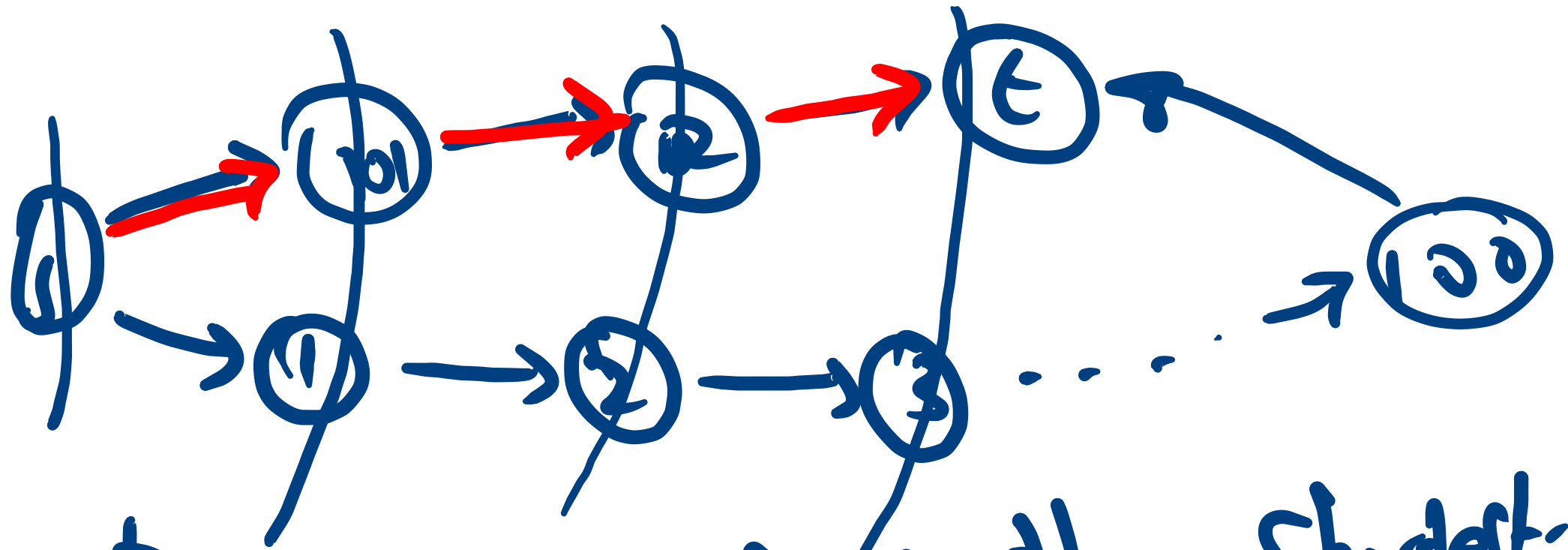
$G = (V = \text{Board state})$

$E = \leq 4 \text{ neighbors/board state}$

Why not a DFS to find a path to the solution?



DFS may find long paths instead of short paths.

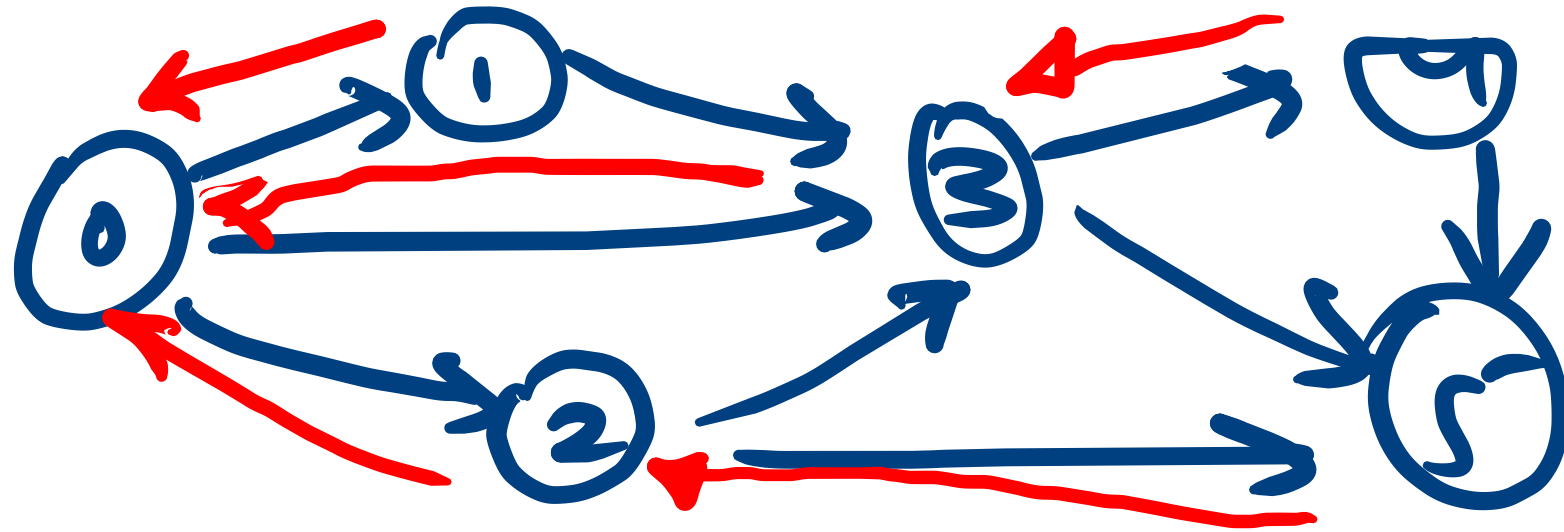


BFS would find the Shortest-path  
from  $s$  to  $t$ .

BFS is obtained by switching  
Stack in DFS with a queue.



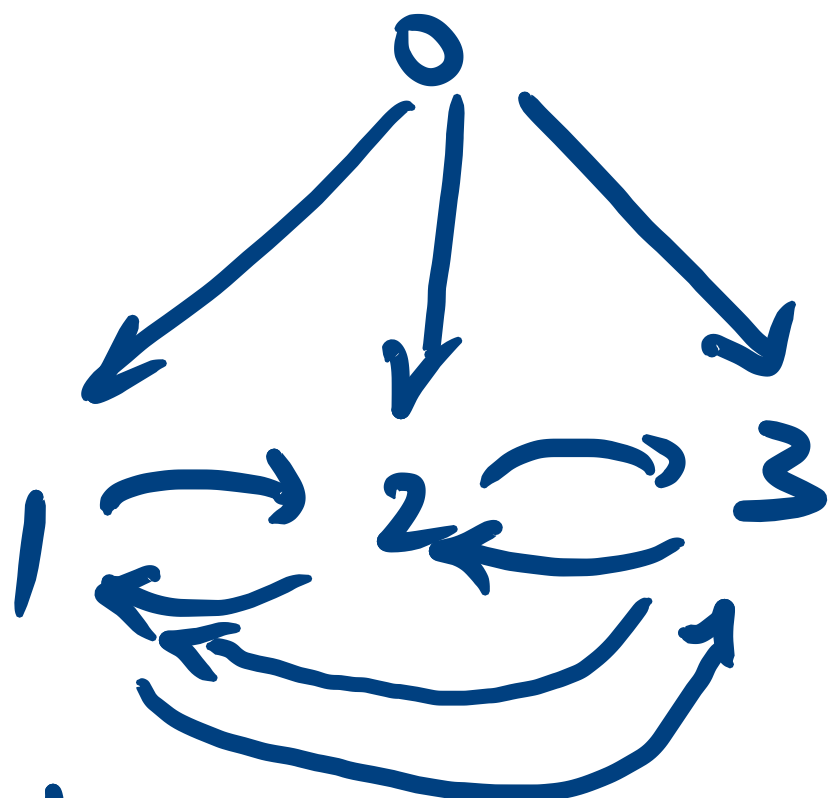
See notes on my webpage for BFS



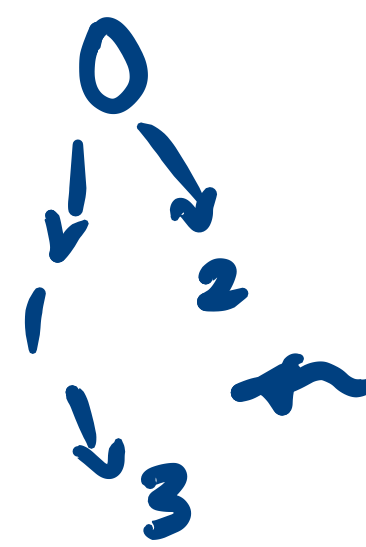
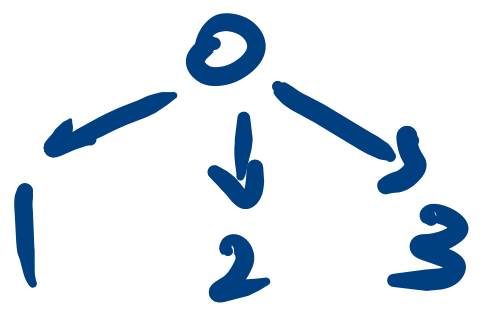
$q \leftarrow \{0\}$   
 $P[v] \leftarrow v \quad v \in 0..5$

4)  $u \leftarrow 3$   
 $V[u] \leftarrow \text{true}$   
 $P[u] \leftarrow 3$   
 $e(u)$

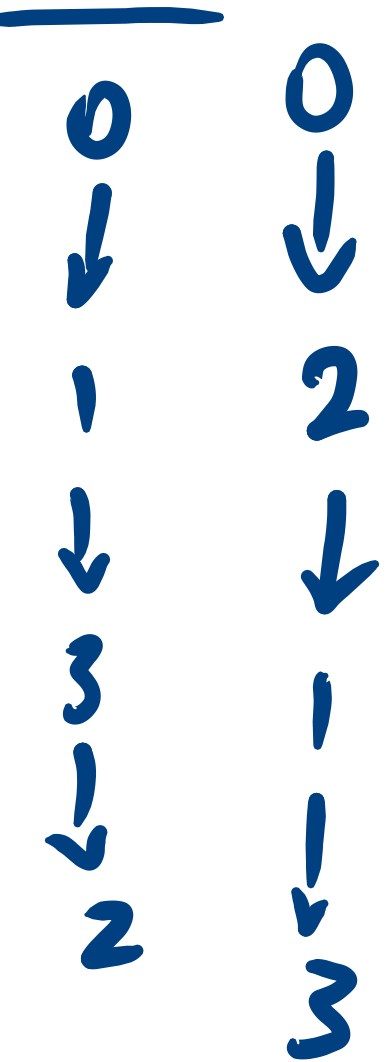
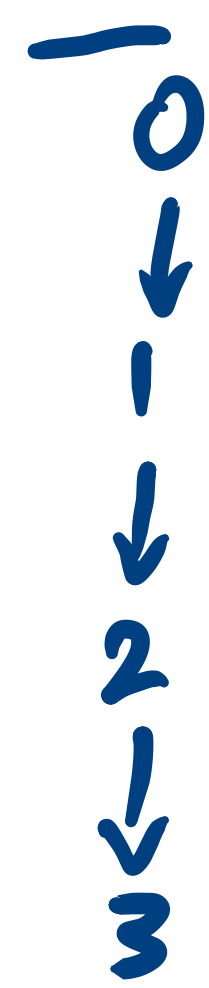
1:  $V[0] \leftarrow \text{true}$   
 $e(1)$   
 $e(2)$   
 $e(3)$   
 $q \leftarrow 1 \ 2 \ 3$   
 $V[1..3] \leftarrow \text{true}$   
 $P[1..3] \leftarrow 0$   
  
 2:  $u \leftarrow 1$   
 3:  $u \leftarrow 2$   
 $e(5)$   
 $V[5] \leftarrow \text{true}$   
 $P[5] \leftarrow 2$



BFS tree



DFS trees



Not DFS tree.  
Not BFS tree.

DFS

- Explore From the latest visited vertex  $\Rightarrow$  Stack.

BFS.

Explore from the earliest (closest) visited vertex  $\Rightarrow$  queue.