

Advanced Algorithms & Data Structures

Assignment 1

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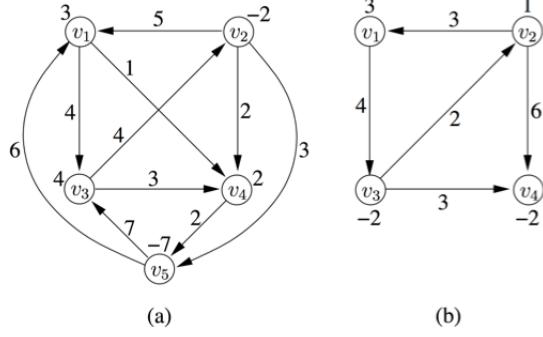
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1 b -flow

Find for each of the two graphs in Figure 1, a b -flow for the graph or argue that the graph has no b -flow



For a directed graph $G = (V, E)$. For each vertex $v \in V$ let $\delta^+(v)$ be the set of outgoing edges from v and $\delta^-(v)$ be the set of incoming edges to v .

Given is that each a b -flow under the following constraints

$$\sum_{e \in \delta^-(v)} x_e - \sum_{e \in \delta^+(v)} x_e = b_v, \forall v \in V \quad (1)$$

$$0 \leq x_e \leq u_e, \forall e \in E \quad (2)$$

Given these constraints we find that the following b -flows exist for graph (a)

$$\delta(v_2v_4) = 2$$

$$\delta(v_5v_3) = 4$$

$$\delta(v_5v_1) = 3$$

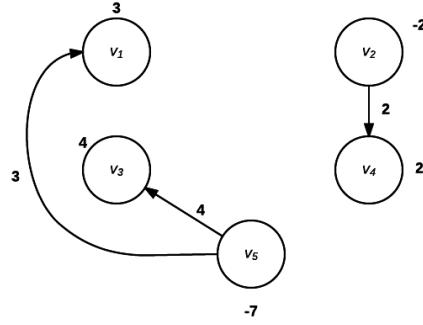


Figure 1: Graph 1A b -flow

We find that there is no b -flow in graph (b) as there is no outgoing edge from v_4 and we do not allow for negative flows. Thus only some of the nodes can satisfy equations (1) and (2) resulting in no existing b -flow.

2 Rectilinear Planar Embedding

2.1 Exercise 2.1

Table 1 shows the values for x_{vf} that correspond to Figure 3 from the Assignment Document.

x_{vf}	a	b	c	d	e
v_1	0	1	1	0	0
v_2	0	0	1	1	0
v_3	1	0	1	1	1
v_4	0	0	0	-1	1
v_5	1	0	0	0	-1
v_6	1	1	0	1	1
v_7	0	0	0	0	0

Table 1: x_{vf} values for Figure 3 in Assignment Document

Table 2 shows the values for z_{fg} that correspond to Figure 3 from the Assignment Document. There are 13 break-points in this graph.

z_{fg}	a	b	c	d	e
a	-	0	0	0	0
b	2	-	1	1	0
c	1	1	-	0	0
d	0	1	0	-	
e	4	0	0	0	-

Table 2: z_{fg} values for Figure 3 in Assignment Document

We are asked to draw a rectilinear layout of graph 2(a) from the assignment description

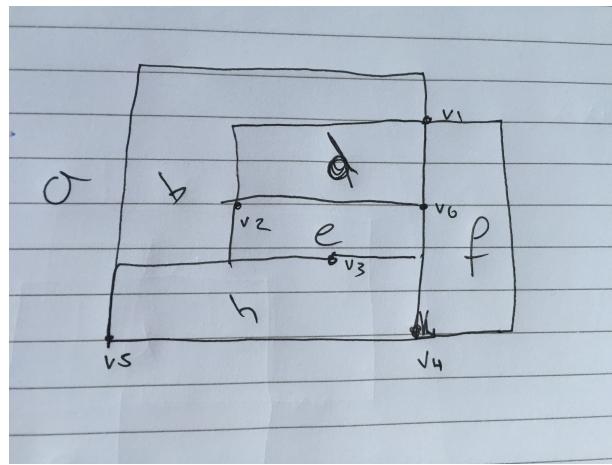


Figure 2: Rectilinear drawing of Graph 2(a) in assignment desc

2.2 Exercise 2.2

Let f_e be the external boundary cycle and B be the set of all boundaries. Inner turns (from x to y) are denoted by z_{xy} and outer turns (from y to x) are denoted by zyx .

$$\forall f \in B \ f_e : \sum_v x_{vf_e} + \sum_{b \in B \setminus f_e} f_b - \dots = -4 \quad (3)$$

$$\sum_v x_{vf} + \sum_{b \in B \setminus f_e} f_b - \dots = 4 \quad (4)$$