

X-ray microscopy for thick biological specimens

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Abstract

We model the intensity fractions of beam components that are closely related to imaging quality for both X-ray and electron microscopy under the circumstance of a thick biological specimen. This not only allows one to gain a clear perspective on the variation of image contrast with sample thickness, but also leads us to compare the radiation dose caused by X-ray and electrons with the usage of phase contrast and energy filter, where X-ray is found to cause less radiation damage than electron microscopy when the specimen thickness is beyond 1–3 μm .

Keywords: X-ray, electron, thick specimen, radiation damage

1. Introduction

2. Theory and modeling

2.1. X-ray imaging

. The probability for a photon-matter interaction event (either scattering or photoionization) to occur over a fractional penetration depth dt can be expressed as

$$P = \sigma_i \rho dt \quad (1)$$

where σ_i is the scattering cross section for interaction event i , and ρ is the sample density. This report is concerned with interaction events subdivided into elastic (Rayleigh) scattering, inelastic (Compton) scattering, and photoionization, with their cross sections respectively represented by σ_{el} , σ_{inel} , and σ_{abs} . All cross section data are retrieved from *Xraylib*, a multi-platform database for X-ray-matter interactions [1]. To tidy

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up the narrative, we also denote

$$K_{\text{el}} = \sigma_{\text{el}}\rho \quad (2)$$

$$K_{\text{inel}} = \sigma_{\text{inel}}\rho \quad (3)$$

$$K_{\text{el},\text{in}} = \sigma_{\text{el}}(1 - \eta_{\text{el}})\rho \quad (4)$$

$$K_{\text{inel},\text{in}} = \sigma_{\text{inel}}(1 - \eta_{\text{inel}})\rho \quad (5)$$

$$K_{\text{out}} = \sigma_{\text{el}}\eta_{\text{el}}\rho + \sigma_{\text{inel}}\eta_{\text{inel}}\rho \quad (6)$$

$$K_{\text{abs}} = \sigma_{\text{abs}}\rho \quad (7)$$

where η_{el} and η_{inel} are the probabilities that a photon is scattered more than 90° (i.e., a photon that becomes undetectable, considering the case where an objective aperture is not present) in an elastic and inelastic scattering event, respectively. The two fractions can be found by integrating their corresponding differential scattering cross sections given by [2]

$$\frac{d\sigma_{\text{el}}}{d\Omega} = \frac{d\sigma_{\text{Th}}}{d\Omega} [F(x, Z)]^2 \quad (8)$$

$$\frac{d\sigma_{\text{inel}}}{d\Omega} = \frac{d\sigma_{\text{KN}}}{d\Omega} [S(x, Z)]^2 \quad (9)$$

where $d\Omega = 2\pi \sin\theta d\theta$ is the differential solid angle, and

$$\frac{d\sigma_{\text{Th}}}{d\Omega} = \frac{r_e^2}{2} (1 + \cos^2\theta) \quad (10)$$

$$\frac{d\sigma_{\text{KN}}}{d\Omega} = \frac{r_e^2}{2} \left[1 + k(1 - \cos\theta) \right]^{-2} \left[1 + \cos^2\theta + \frac{k^2(1 - \cos\theta)^2}{1 + k(1 - \cos\theta)} \right] \quad (11)$$

are the differential Thomson and Klein-Nishina cross sections as a function of scattering angle θ and relative incident energy $k = E/m_e c^2$, assuming unpolarized radiation, given by Hubbell [3]. The atomic form factor $F(x, Z)$ and the incoherent scattering function $S(x, Z)$, both taking the momentum transfer $x = \sin(\theta/2)/\lambda(\text{\AA})$ and atomic number Z as parameters, also following the definition by Hubbell, and are retrievable from *Xraylib*.

A series of differential equations of x-ray intensity in various categories as a function of penetration depth t can thereby be written [4]:

- The intensity component due to photons that do not undergo any interaction with the sample, I_{noscatt} , is given according to

$$dI_{\text{noscatt}} = -I_{\text{noscatt}}(K_{\text{inel}} + K_{\text{el}} + K_{\text{abs}})dt. \quad (12)$$

with initial condition $I_{\text{noscatt}}(0) = I_0$.

- The component of photons that undergo only one elastic scattering event and remain in the detectable angular range, I_{1el} , is given according to

$$dI_{\text{1el}} = I_{\text{noscatt}}K_{\text{el},\text{in}}dt - I_{\text{1el}}(K_{\text{inel}} + K_{\text{el}} + K_{\text{abs}})dt \quad (13)$$

with $I_{\text{1el}}(0) = 0$.

- For the component corresponding to photons undergoing multiple elastic scattering events yet still detectable, $I_{\text{el,plural}}$, the differential equation is

$$dI_{\text{el,plural}} = I_{\text{el}}K_{\text{el,in}}dt - I_{\text{el,plural}}(K_{\text{out}} + K_{\text{inel,in}} + K_{\text{abs}})dt \quad (14)$$

with $I_{\text{el,plural}}(0) = 0$.

- For photons that are scattered out of the detectable angular range (backscattered), either elastically or inelastically, the corresponding intensity contribution I_{out} satisfies

$$dI_{\text{out}} = (I_0 - I_{\text{out}} - I_{\text{abs}})K_{\text{out}}dt \quad (15)$$

with $I_{\text{out}}(0) = 0$.

- For photons that are absorbed via photoionization, the component I_{abs} satisfies

$$dI_{\text{abs}} = (I_0 - I_{\text{out}} - I_{\text{abs}})K_{\text{abs}}dt \quad (16)$$

with $I_{\text{abs}}(0) = 0$.

- The portion of detectable photons that do not undergo inelastic scattering, i.e., the summation of $I_{\text{noscatter}}$, I_{1el} , and $I_{\text{el,plural}}$, is denoted as $I_{\text{in,noinel}}$ and given by

$$dI_{\text{in,noinel}} = -I_{\text{in,noinel}}(K_{\text{inel,in}} + K_{\text{out}} + K_{\text{abs}}) \quad (17)$$

- Lastly, I_{inel} , the contribution of photons that undergo at least one inelastic scattering yet are still within the detectable angular range, is given in

$$dI_{\text{inel}} = I_{\text{in,noinel}}K_{\text{inel}}dt - I_{\text{inel}}(K_{\text{out}} + K_{\text{abs}})dt \quad (18)$$

with $I_{\text{inel}}(0) = 0$.

. Solutions to these differential equations yield

$$I_{\text{noscatter}} = I_0 e^{-(K_{\text{inel}}+K_{\text{el}}+K_{\text{abs}})t} \quad (19)$$

$$I_{\text{1el}} = I_0 K_{\text{el,in}} e^{-(K_{\text{inel}}+K_{\text{el}}+K_{\text{abs}})t} \quad (20)$$

$$= K_{\text{el,in}} t I_{\text{noscatter}}$$

$$I_{\text{el,plural}} = I_0 \left[e^{-(K_{\text{out}}+K_{\text{inel,in}}+K_{\text{abs}})t} - (1 + K_{\text{el,in}}t) e^{-(K_{\text{inel}}+K_{\text{el}}+K_{\text{abs}})t} \right] \quad (21)$$

$$I_{\text{out}} = \frac{I_0 K_{\text{out}}}{K_{\text{out}} + K_{\text{abs}}} \left[1 - e^{-(K_{\text{out}}+K_{\text{abs}})t} \right] \quad (22)$$

$$I_{\text{abs}} = \frac{I_0 K_{\text{abs}}}{K_{\text{out}} + K_{\text{abs}}} \left[1 - e^{-(K_{\text{out}}+K_{\text{abs}})t} \right] \quad (23)$$

$$I_{\text{in,noinel}} = I_0 e^{-(K_{\text{inel,in}}+K_{\text{out}}+K_{\text{abs}})t} \quad (24)$$

$$I_{\text{inel}} = I_0 \left[e^{-(K_{\text{out}}+K_{\text{abs}})t} - e^{-(K_{\text{inel,in}}+K_{\text{out}}+K_{\text{abs}})t} \right]. \quad (25)$$

It can be demonstrated that

$$I_{\text{noscatter}} + I_{\text{1el}} + I_{\text{el,plural}} + I_{\text{out}} + I_{\text{abs}} + I_{\text{inel}} = I_0. \quad (26)$$

. In the specific case of X-ray phase contrast imaging, more useful categories can be lined out based on the above results. Firstly, the photons that constitute the image signals are, in addition to non-scattered photons, those having undergone single elastic scattering with the scattering angle within in the range defined by the numerical aperture (NA). Here we consider an NA required for 1 μm resolution according to the Abbe criterion. The intensity of this portion of photons, $I_{\text{el,pc}}$, is related to I_{el} by

$$I_{\text{el,pc}} = I_{\text{el}} \frac{\int_0^{s(2\theta=\text{NA})} I(s) ds}{\int_{\text{forward}} I(s) ds} \quad (27)$$

where s is the momentum transfer of scattering, $s = 4\pi \sin(\theta)/\lambda$, 2θ is the scattering angle, and $I(s)$ is the scattering intensity as a function of s . The upper integral is over the s range stipulated by NA, while the lower is over the regime of forward scattering. We performed data fitting on the small angle X-ray scattering (SAXS) data of 80 different protein samples retrieved from Small Angle Scattering Biological Data Bank (SASBDB) [5] to parameterize $I(s)$, where the normalized Guinier's law

$$I(s) = \exp(-\frac{1}{3}R_g^2 s^2) \quad (28)$$

is applied to the portion with $s < 1.3/R_g$, while a polynomial approximation from the negative fourth to the zeroth order of s is used to model the high-angle portion. $s = 3.0$ is set as a cut-off point beyond which $I(s)$ is evaluated as 0 to take out the unphysical increasing part of the polynomial. This yields the integrable expression for $I(s)$ which can be plugged into Equation (27):

$$I(s) = \begin{cases} \exp(-1.396s^2) & 0 \leq s < 0.311 \\ 0.0168s^{-4} - 0.1514s^{-3} + 0.4397s^{-2} - 0.2441s - 1 + 0.0399 & 0.311 \leq s < 3.0 \\ 0 & s \geq 3.0. \end{cases} \quad (29)$$

Taking the $\pm 90^\circ$ -out-of-phase interfering amplitudes of I_{noscatt} and $I_{\text{el,pc}}$ yields the signal intensity:

$$I_{\text{signal}} = \sqrt{I_{\text{noscatt}} I_{\text{el,pc}}}. \quad (30)$$

Furthermore, if one assumes that inelastic and plural elastic scattering events completely randomize the direction of photons, then the intensity of photons of such kinds that are collected by the objective and thus contribute to the background of phase contrast imaging, $I_{\text{inel,pc}}$ and $I_{\text{el,plural,pc}}$, can be calculated from I_{inel} and $I_{\text{el,plural}}$ purely on geometric basis:

$$I_{\text{inel,pc}} = I_{\text{inel}} \frac{\pi(NA)^2}{2\pi} \quad (31)$$

$$I_{\text{el,plural,pc}} = I_{\text{el,plural}} \frac{\pi(NA)^2}{2\pi}. \quad (32)$$

The above equations are based on the assumption that the working distance is much larger than the dimension of the field of view so the offset of the scattering center to the axis is negligible.

2.2. Electron imaging

. It should be noted that electrons differ from X-ray in that they are never simply absorbed, which negates
 25 the presence of the absorption category. Moreover, now assuming that a typical objective aperture is present,
 one may make a general assumption on η_{el} based on a representative cutoff frequency of the aperture of s_0
 $= 4.12 \text{ nm}^{-1}$ proposed by Langmore and Smith [7]

$$\eta_{\text{el}} \approx 1 - \frac{s_0}{10}. \quad (33)$$

On the other hand, η_{inel} is simply assumed to be 0 as electron inelastic scattering is typically low-angle [8],
 so

$$K_{\text{out}} = \sigma_{\text{el}} \eta_{\text{el}} \rho \quad (34)$$

$$K_{\text{inel},\text{in}} = \sigma_{\text{inel}} \rho = K_{\text{inel}}. \quad (35)$$

Equations 19 to 25 are then rewritten as [4]

$$I_{\text{noscat}} = I_0 e^{-(K_{\text{inel}} + K_{\text{el}})t} \quad (36)$$

$$\begin{aligned} I_{\text{1el}} &= I_0 K_{\text{el},\text{in}} e^{-(K_{\text{inel}} + K_{\text{el}})t} \\ &= K_{\text{el},\text{in}} t I_{\text{noscat}} \end{aligned} \quad (37)$$

$$I_{\text{el},\text{plural}} = I_0 \left[e^{-(K_{\text{out}} + K_{\text{inel}})t} - (1 + K_{\text{el},\text{in}} t) e^{-(K_{\text{inel}} + K_{\text{el}})t} \right] \quad (38)$$

$$I_{\text{out}} = I_0 \left(1 - e^{-K_{\text{out}} t} \right) \quad (39)$$

$$I_{\text{in,noinel}} = I_0 e^{-(K_{\text{inel}} + K_{\text{out}})t} \quad (40)$$

$$I_{\text{inel}} = I_0 \left[e^{-K_{\text{out}} t} - e^{-(K_{\text{inel}} + K_{\text{out}})t} \right]. \quad (41)$$

2.3. Image contrast and radiation dose

. The categorization of X-ray and electron beam intensities would naturally shed light on the radiation dose
 done by probe beams to the specimen. In fact, the intensity breakdown is particularly useful for answering
 the dose question for electron imaging where absorption effect, which prevails in X-ray-matter interaction,
 is non-existent. As a paradigm scenario, we consider here a finer specimen model where protein features are
 dispersed as tablets in a layer of vitreous ice matrix with thickness t_f , embedded in the middle of vitreous
 ice with combined thickness t_b ($t_b \gg t_f$), such that the specimen has a total thickness $t = t_b + t_f$ (Figure 1).
 Jacobsen et al. [4] have provided a listing of equations describing the intensities of electrons passing through

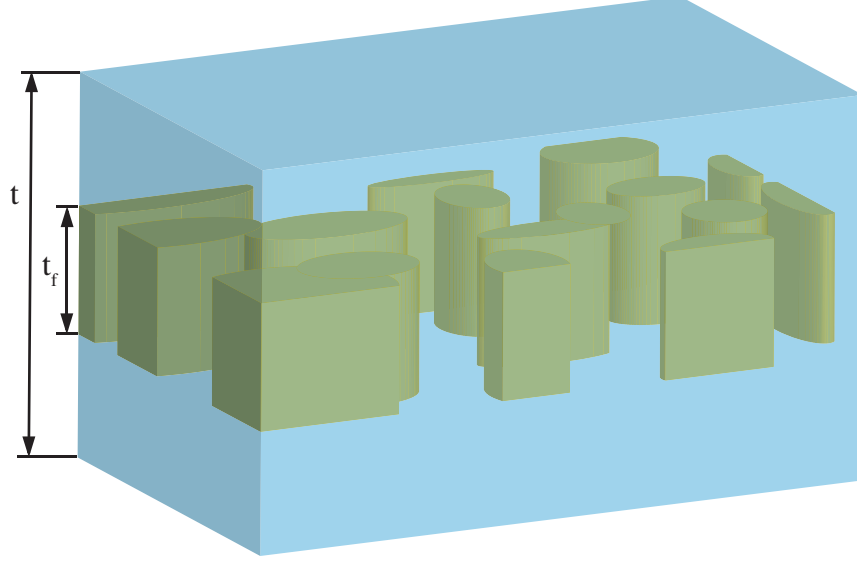


Figure 1: Schematic diagram of the hydrated specimen model adopted for contrast computation. Protein features are assumed to be tablets dispersed within a layer of thickness t_f , embedded in the middle of vitreous ice such that the total thickness is t . In a parallel beam scenario, probe beams (X-ray or electron) traveling in columns containing proteins constitute image signals, while those passing through ice-only columns form the background.

feature-containing columns (I_f) and matrix-only columns (I_b), respectively:

$$I_{\text{nosc},b} = I_0 e^{-(K_{\text{inel},b} + K_{\text{el},b})t} \quad (42)$$

$$\begin{aligned} I_{1\text{el},b} &= I_0 K_{\text{el},\text{in},b} e^{-(K_{\text{inel},b} + K_{\text{el},b})t} \\ &= K_{\text{el},\text{in},b} t I_{\text{nosc},b} \end{aligned} \quad (43)$$

$$I_{\text{in},\text{noinel},b} = I_0 e^{-(K_{\text{inel},b} + K_{\text{out},b})t} \quad (44)$$

$$I_{\text{el},\text{plural},b} = I_{\text{in},\text{noinel},b} - I_{\text{nosc},b} - I_{1\text{el},b} \quad (45)$$

$$I_{\text{in},b} = I_0 e^{-K_{\text{out},b}t} \quad (46)$$

$$I_{\text{inel},b} = I_{\text{in},b} - I_{\text{in},\text{noinel},b} \quad (47)$$

$$(48)$$

and

$$I_{\text{noscat},f} = I_0 e^{-(K_{\text{inel},b} + K_{\text{el},b})t_b} e^{-(K_{\text{inel},f} + K_{\text{el},f})t_f} \quad (49)$$

$$I_{\text{el},f} = (K_{\text{el},\text{in},b}t_b + K_{\text{el},\text{in},f}t_f)I_{\text{noscat},f} \quad (50)$$

$$I_{\text{el}/f,f} = K_{\text{el},\text{in},f}t_f I_{\text{noscat},f} \quad (51)$$

$$I_{\text{in},\text{noinel},f} = I_0 e^{-(K_{\text{out},b} + K_{\text{inel},b})t_b} e^{-(K_{\text{out},f} + K_{\text{inel},f})t_f} \quad (52)$$

$$I_{\text{el},\text{plural},f} = I_{\text{in},\text{noinel},f} - I_{\text{noscat},f} - I_{\text{el},f} \quad (53)$$

$$I_{\text{in},f} = I_0 e^{-K_{\text{out},b}t_b} e^{-K_{\text{out},f}t_f} \quad (54)$$

$$I_{\text{inel}} = I_{\text{in},f} - I_{\text{in},\text{noinel},f}. \quad (55)$$

$$(56)$$

. From the matrix-feature dichotomy, the signal and noise of the resultant image can be straightforwardly written as

$$S = N|I_f - I_b| \quad (57)$$

$$N = \sqrt{N} \sqrt{I_f + I_b} \quad (58)$$

where N is the number of probe particles per pixel. Consequently, the signal-to-noise ratio (SNR) is given by [2]

$$\begin{aligned} \text{SNR} &= \sqrt{N} \frac{I_f - I_b}{\sqrt{I_f + I_b}} \\ &= \sqrt{N} \Theta \end{aligned} \quad (59)$$

where Θ is the image contrast. For electron phase contrast imaging, this factor is expressed as

$$\Theta_{\text{e},\text{unfiltered}} = \frac{|I_{\text{in},\text{noinel},f} - I_{\text{in},\text{noinel},b}| + 2\sqrt{I_{\text{noscat},f}I_{\text{el}/f,f}}}{\sqrt{I_{\text{in},f} + I_{\text{in},b}}}. \quad (60)$$

If an energy filter is used to screen out inelastically scattered electrons, the factor is modified as

$$\Theta_{\text{e},\text{filtered}} = \frac{|I_{\text{in},\text{noinel},f} - I_{\text{in},\text{noinel},b}| + 2\sqrt{I_{\text{noscat},f}I_{\text{el}/f,f}}}{\sqrt{I_{\text{in},\text{noinel},f} + I_{\text{in},\text{noinel},b}}}. \quad (61)$$

. For X-ray, we only consider the case of Zernike phase contrast (ZPC), where phase-shifted X-ray beams interfere with a 90° -shifted reference beam. In this case, it would be more convenient to exploit the wave nature of X-ray and utilize the linear absorption coefficients, $\mu_f = 4\pi\beta_f/\lambda$ and $\mu_b = 4\pi\beta_b/\lambda$, and phase advances, $\eta_f = 2\pi\delta_f/\lambda$ and $\eta_b = 2\pi\delta_b/\lambda$, where $\beta_{f/b}$ and $\delta_{f/b}$ are terms in the complex refractive index $n = 1 - \delta - \beta$ respectively for feature and matrix, to write [9]

$$I_{\text{zpc},f} \approx I_0 e^{-\mu_b t_b} \left[1 + 4\pi(\delta_f - \delta_b) \frac{t_f}{\lambda} \right] \quad (62)$$

and

$$I_{\text{zpc},b} \approx I_0 e^{-\mu_b t_b}. \quad (63)$$

Equation 62 and 63 are based on the assumption that both materials are weak phase objects. Consequently, the contrast parameter for X-ray ZPC is given by

$$\Theta_{x,zpc} = 2\sqrt{2}\pi\frac{t_f}{\lambda}|\delta_f - \delta_b|\exp\left(\frac{-\mu_b t_b}{2}\right). \quad (64)$$

It should be noticed that $\mu = K_{\text{total}}$.

. According to the Rose criterion which states that a SNR of at least 5 is required for precise identification of image features, N should be

$$N = \frac{25}{\Theta^2}. \quad (65)$$

This leads us to write the specimen radiation dose in Gray (J/kg) for X-ray as

$$D_x = \frac{NEI_{\text{abs},f}}{\Delta^2\rho_f t_f} \quad (66)$$

where

$$I_{\text{abs},f} = I_{\text{noscat},b}(t_b/2)[1 - I_{\text{noscat},f}(t_f)] \quad (67)$$

$$= \exp\left(-K_{\text{total},b}\frac{t_b}{2}\right)\left[1 - \exp(-K_{\text{total},f}t_f)\right] \quad (68)$$

is the fraction of photons absorbed by the feature, E is the incident photon energy, Δ is the pixel size (which defines the resolution in scanning X-ray microscopy). and ρ_f is the feature density. In the case of electron, the radiation dose is contributed by inelastic scattering only:

$$D_e = \frac{N\langle E\rangle}{\Delta^2\Lambda_{\text{inel},f}\rho_f} \quad (69)$$

30 where $\Lambda_{\text{inel},f} = 1/K_{\text{inel},f}$ is the mean free path of electrons with regards to inelastic scattering in the feature material, and $\langle E\rangle$ is the expectation of energy deposition in an inelastic scattering event, evaluated from the electron energy-loss spectra (EELS) for ice as 46.0 eV and for protein as 37.5 eV [10].

3. Results and discussion

. For a general perception on the variation of X-ray and electron beam components with specimen thick-
 35 ness, we expediently assume the sample to be a homogeneous block of protein with a composition of $\text{H}_{48.6}\text{C}_{32.9}\text{N}_{8.9}\text{O}_{8.9}\text{S}_{0.6}$ and a dry density of 1.35 g/cm³, in order to emulate a biological specimen. This is the effective protein formula proposed by London through averaging over all 20 amino acids [6]. Figure 2 shows the intensity profiles relative to sample thickness at 5 keV, 10 keV, 20 keV, and 40 keV. For the former 3 energies simulated, absorption begins to dominate beyond a thickness of 0.05 cm, 0.5 cm, and 2 cm.
 40 At 40 keV, backscattered photons take over the dominant position due to the dramatic drop in photoionic absorption cross section (from 0.47 cm²/g at 20 keV to 0.05 cm²/g at 40 keV). In all cases, the fact that I_{signal} is several orders higher than $I_{\text{inel,pc}}$ and $I_{\text{el,plural,pc}}$ reveals that a high signal-to-background ratio is maintained. We should further point out that our assumption that used in calculating $I_{\text{inel,pc}}$ may lead to

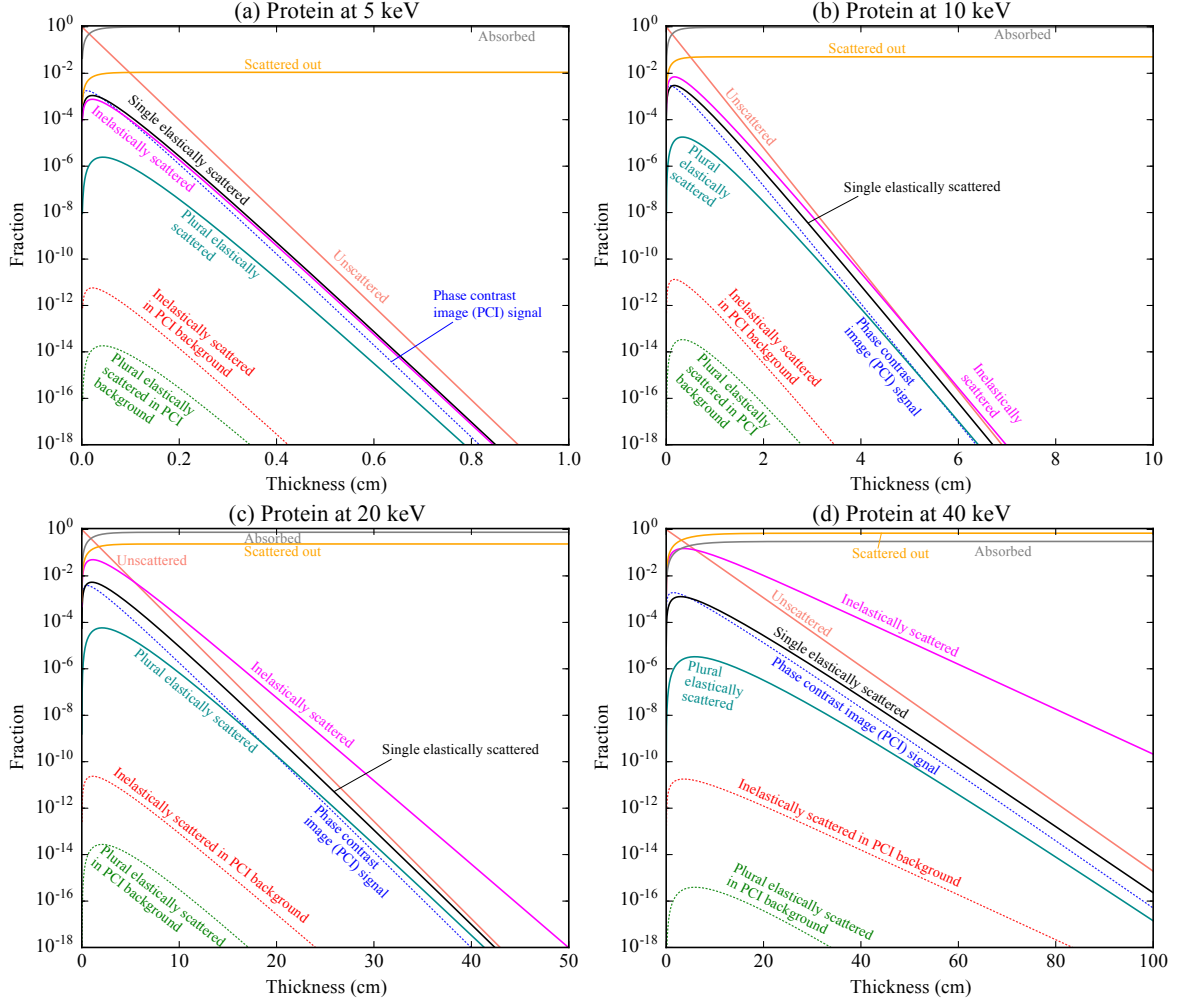


Figure 2: Normalized intensity profiles for X-ray in protein as a function of thickness at incident energy of (a) 5 keV, (b) 10 keV, (c) 20 keV, and (d) 40 keV.

a slight overestimation of this category, because the differential inelastic scattering cross section for X-ray is, unlike electrons, lower at both the 0° - and the 180° -end, so for the non-negligible portion of photons traveling in the primary beam direction before being inelastically scattered, the chance of entering the NA is exaggerated.

. In Figure 3 we show the simulation results for electrons. Based on the same model, Jacobsen et al. [4] studied the electron beam components in pure ice, which exhibits the same trend as in our case that the fraction of inelastically scattered electrons is larger and attenuates more slowly when the specimen thickness is on or beyond the order of 100 nm. Known as a drawback of electron imaging, the high chance of inelastic

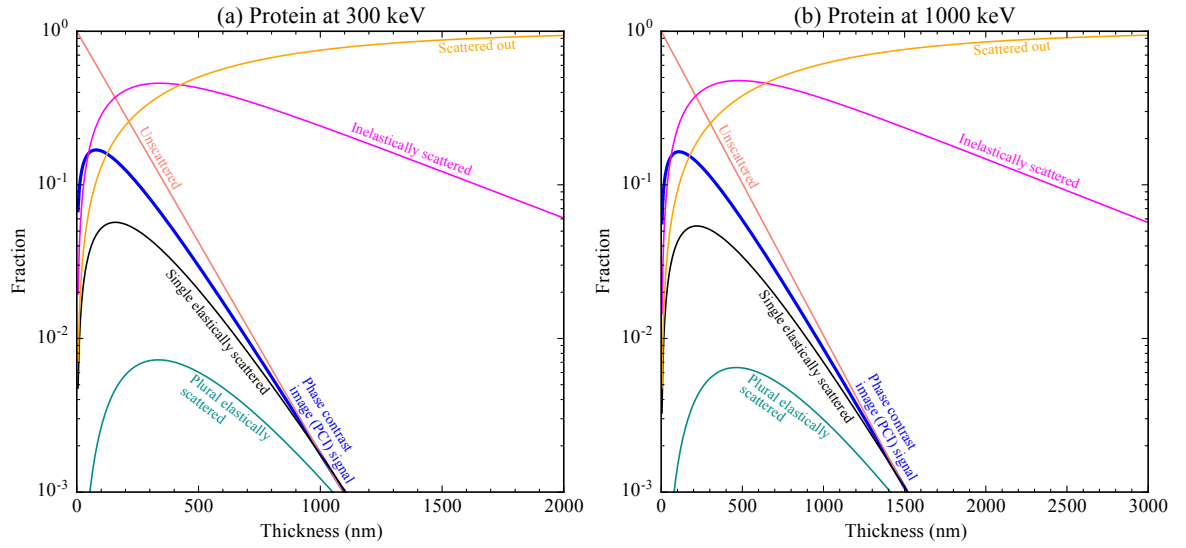


Figure 3: Normalized intensity profiles for electrons in vitreous ice as a function of thickness at incident energy of 300 keV. Reproduced from Jacobsen et al. (1998) with permission.

scattering degrades the optical transfer function (OTF), although the application of energy filters can large remove this undesirable effect.

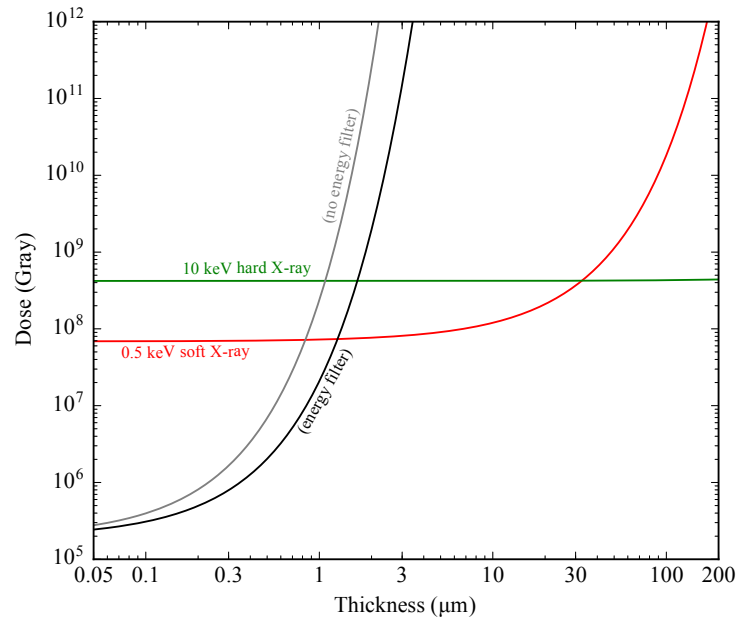


Figure 4: Radiation dose at varying specimen thickness for 0.5 keV soft X-ray and 10 keV hard X-ray, in comparison with 300 keV electrons, with and without energy filter. Reproduced from Jacobsen et al. (unpublished) with permission.

. To examine the image contrast and radiation dose as a function of specimen thickness, we visualize the
55 variation of radiation dose with the total thickness for a 10-nm-thick embedded protein layer, imaged with
using soft (500 eV) and hard (10 keV) X-ray and 300 keV electrons with and without energy filter for a
spatial resolution of 10 nm (Figure 4).

. The paradigm scenario illustrated here indicates a general tendency that soft X-ray produces lower radi-
ation dose than electrons. This advantage, however, is counterbalanced by the high spatial resolution that
60 electron microscopy can provide, and diminishes when the specimen thickness is on or beyond the order of 10
 μm . Increasing the energy of X-ray would effectively reduce the sensitivity of radiation dose to ice thickness.
Electron microscopy proves superiority for specimen thickness within the submicron regime; however, for
thickness beyond 1 μm , the ratio of multiple scattering or inelastic scattering over single elastic scattering
events begins to take off, which, on the other hand, remains steady for X-ray. Thus, when spatial resolution
65 is not a strict requirement, X-ray manifests to be a less intrusive technique for imaging biological specimens.

4. Conclusion

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