

In[14]:=

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(* All atomic units *)
μ = 1835;
mP = 1836; (* Proton mass *)
hbar = 1;
c = 137 ;(*SpeedOfLight, atomic units*)
(* 1 kelvin[K]=8.61732814974056E-05 electron-volt[eV]*)
(* 1 Hartree = 27.2114eV *)
R0 = 0.01; (* Min distance between nuclei, atomic units*)

(* Potential tables for the gerade and ungerade case *)
vSg1Data =
  Import["~/Work/Physics-Thesis/thesis-2/ZelimirOverleaf/MathematicaCodeFinal/
    gerade1sV2.mx"];
vSu1Data =
  Import["~/Work/Physics-Thesis/thesis-2/ZelimirOverleaf/MathematicaCodeFinal/
    ungerade1sV2.mx"];

(* Max value of R for calculation *)
maxR = 50;

(*vSg1Data = Prepend[vSg1Data,{0,-8.0, 10100,25.8,0,.11}];
vSu1Data=Prepend[vSu1Data,{0,-0.889, 10100,25.81,0.041}];*)

(* Interpolatte the potential *)
vGerade := Interpolation[Transpose[{vSg1Data[[All, 1]], vSg1Data[[All, 3]]}]];
vUngerade := Interpolation[Transpose[{vSu1Data[[All, 1]], vSu1Data[[All, 3]]}]];

(* Calogero's differential equation to compute the phase shift delta *)
deltaPrime[vPotential_, r_, k_, m_, delta_] := Module[{Jm, Ym, psi},
  Jm = BesselJ[m, k * r];
  Ym = BesselY[m, k * r];
  psi = Jm * Cos[delta] - Ym * Sin[delta];
  -vPotential[r] * psi^2 / k
];

(* Calogero's method to compute the phase shift delta *)
delta[deltaPrime_, vPotential_, k_, m_] := Module[{solDelta, deltaEq, deltaFinal},
  (* Calogero *)
  solDelta = NDSolve[
    {deltaEq'[r] == deltaPrime[vPotential, r, k - vPotential[50], m, deltaEq[r]],
    deltaEq[0.01] == 0}, deltaEq, {r, 20, 50}];
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deltaFinal = deltaEq[50] /. solDelta[[1]] // N;

deltaFinal
];

(* some constants for reference *)
(* 1Kelvin = 7.733675709525194`*^-7 Hartree *)
(* 1 a0 (Bohr radius = 5.29177210544*10-11m
    1 barn = 10-28
    1 a02=5.29177210544`*^-22 = 5.29177210544`*^6 barn
    *)
(* Scattering at around room temperature, 270-310K *)
(* kB = 3.167*10-6 EH/T (Boltzman) *)
(* k =  $\sqrt{\frac{2mE}{\hbar}}$  *)
(* 1 EH=3.1577464 x 105 K *)
(* 270K = 0.000855 EH => k = 0.0413531175145633 *)
(* 300K = 0.00095 EH => k = 0.0435900132315404 *)
;

(* Compute deltas for the gerade and ungerade case *)
deltaGer[k_,m_] := delta[deltaPrime,vGerade,k,m];
deltaUng[k_,m_] := delta[deltaPrime,vUngerade,k,m];

diff[k_,m_] := deltaGer[k,m] - deltaUng[k,m];

Plot[diff[(k2)*3.1577464*5 /2, 0], {k,270,300},
  AxesLabel->{"T Temperature (K)","Phase Shift Ger, Ung"},
  PlotLabel->"Phase Shift Gerade & Ungerade vs Temperature (K)"]

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eps[m_] := If[ m == 0, 1, 2];

m = 0;
(* Scattering length *)

$$\lambda[k_, m_] := \frac{4}{k} \text{Sum}[\text{eps}[i] (\text{Sin}[\text{deltaGer}[k, i] - \text{deltaUng}[k, i]])^2, \{i, 0, m\}];$$


allLambda[m_] := Table[{k,  $\lambda[k, m]$ }, {k, 0.0413, 0.04359, 0.0001}];

(* Cross section in atomic units *)
scatteringLength := allLambda[m];

(* temp in Kelvins *)
scatteringLengthK := Transpose[
  {(scatteringLength[[All, 1]]^2) * 3.1577464*^5 / 2, scatteringLength[[All, 2]]}];

f = Interpolation[scatteringLengthK, InterpolationOrder → 2];

Plot[f[x],
  {x, scatteringLengthK[[1, 1]], scatteringLengthK[[Length[scatteringLength], 1]]},
  Epilog → Point[scatteringLength], AxesLabel → {"T Temperature (K)", " $\lambda$  (a.u.)"},
  PlotLabel → "Scattering Length (a.u.) vs Temperature (K)"]

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