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$$= e^{-Z} \frac{1 - P}{P} \xrightarrow{\text{Inverse}} e^Z \frac{P}{1 - P}$$

Odds Ratio in Logistic Regression

$$\begin{aligned} &= \frac{e^z \cdot \frac{P}{1-P}}{\quad} \xrightarrow{\text{Take Log}} \log(e^z) \cdot \log\left(\frac{P}{1-P}\right) \end{aligned}$$

Odds Ratio in Logistic Regression

$$\begin{aligned} &= \boxed{e^z \frac{P}{1 - P}} \xrightarrow{\text{Take Log}} \log(e^z) \log\left(\frac{P}{1 - P}\right) \\ &= Z \log\left(\frac{P}{1 - P}\right) \end{aligned}$$

Odds Ratio in Logistic Regression

$$= e^z \frac{P}{1 - P}$$

Take Log



$$= \log(e^z) \quad \log\left(\frac{P}{1 - P}\right)$$

$$= Z \quad \log\left(\frac{P}{1 - P}\right)$$

$$= \beta X + b \quad \log\left(\frac{P}{1 - P}\right)$$

Odds Ratio in Logistic Regression

$$\beta X + b = \log \left(\frac{P}{1 - P} \right)$$

$$\text{Odds Ratio} = \frac{P}{1 - P}$$