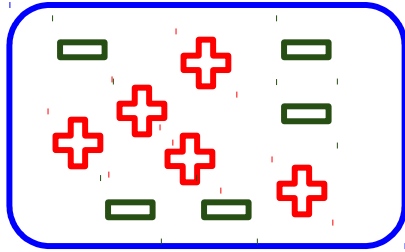


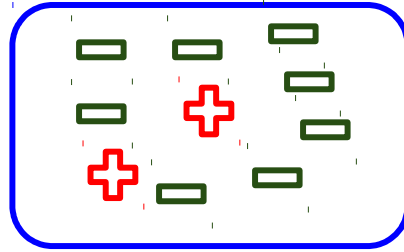
# How to select best split point in Decision Trees?

# Information Gain

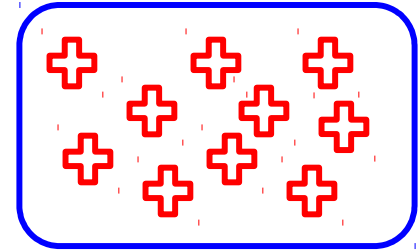
# Information Gain



Node  
1

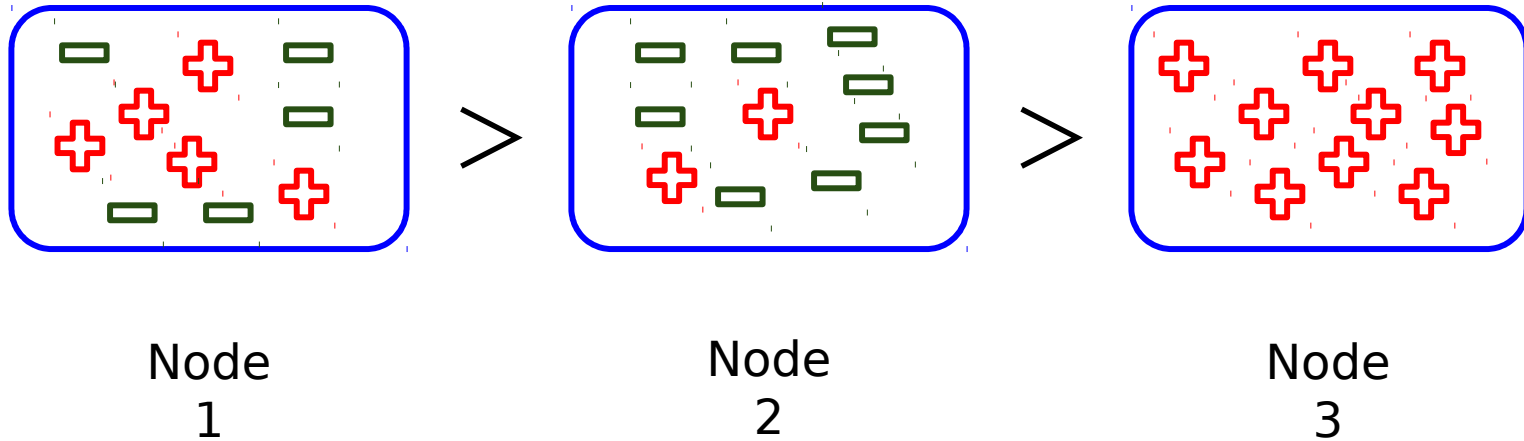


Node  
2



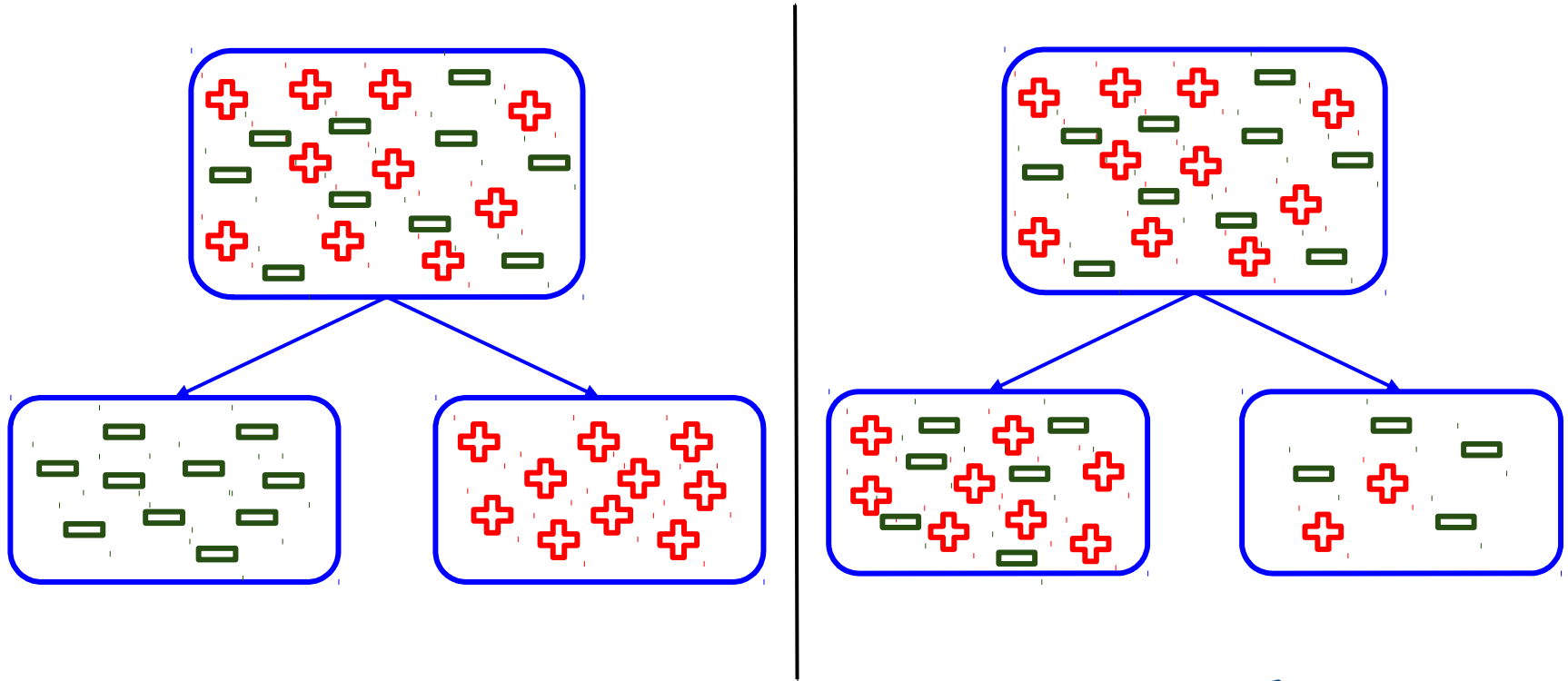
Node  
3

# Information Gain



Information required to describe the  
node

# Information Gain



# Information Gain

$$\text{Information Gain} = 1 - \text{Entropy}$$

# Information Gain

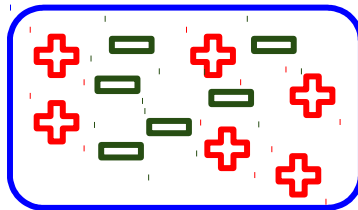
## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$

# Information Gain

## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$

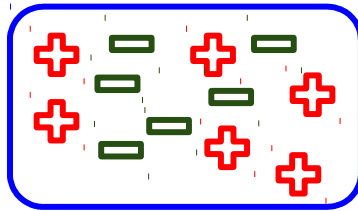




# Information Gain

## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$



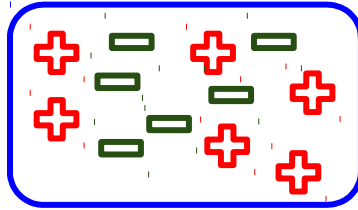
% Play = 0.50

% Not play = 0.50

# Information Gain

## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$



% Play = 0.50

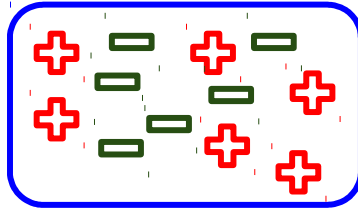
% Not play = 0.50

$$\text{Entropy} = - (0.5) * \log_2(0.5) - (0.5) * \log_2(0.5)$$

# Information Gain

## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$



% Play = 0.50

% Not play = 0.50

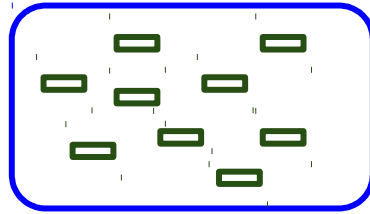
$$\text{Entropy} = - (0.5) * \log_2(0.5) - (0.5) * \log_2(0.5)$$

$$= 1$$

# Information Gain

## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$



% Play = 0

% Not play = 1

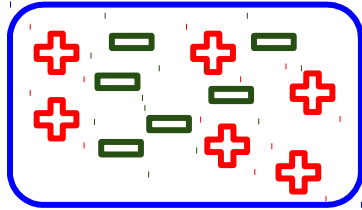
$$\text{Entropy} = - (0) * \log_2(0) - (1) * \log_2(1)$$

$$= 0$$

# Information Gain

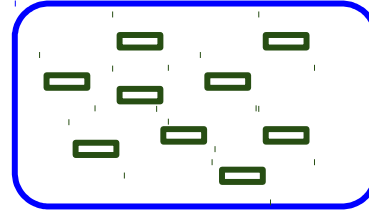
## Entropy

$$- p_1 * \log_2 p_1 - p_2 * \log_2 p_2 - p_3 * \log_2 p_3 - \dots - p_n * \log_2 p_n$$



% Play = 0.50  
% Not play = 0.50

Entropy = 1



% Play = 0  
% Not play = 1

Entropy = 0

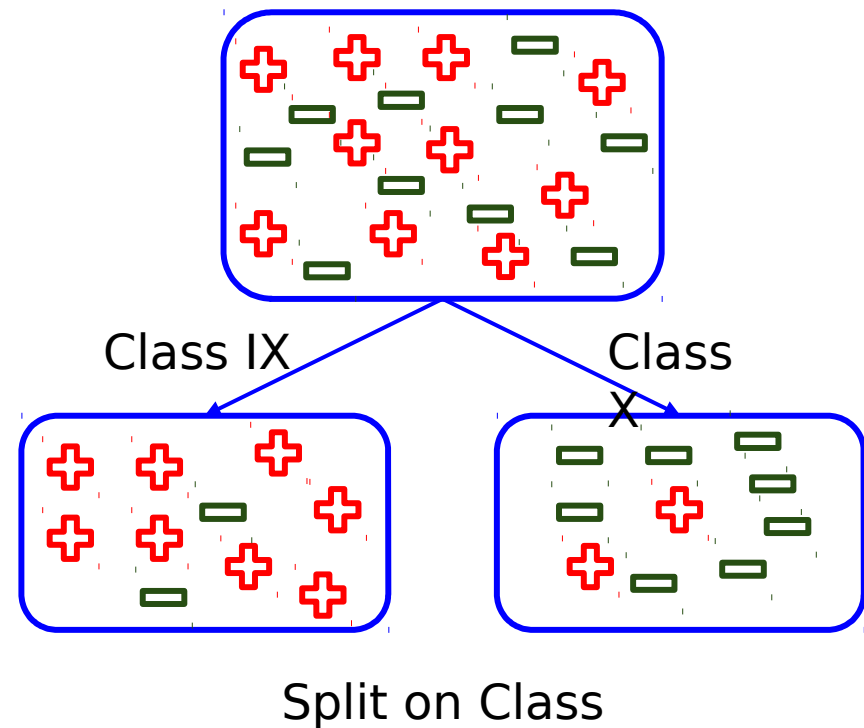
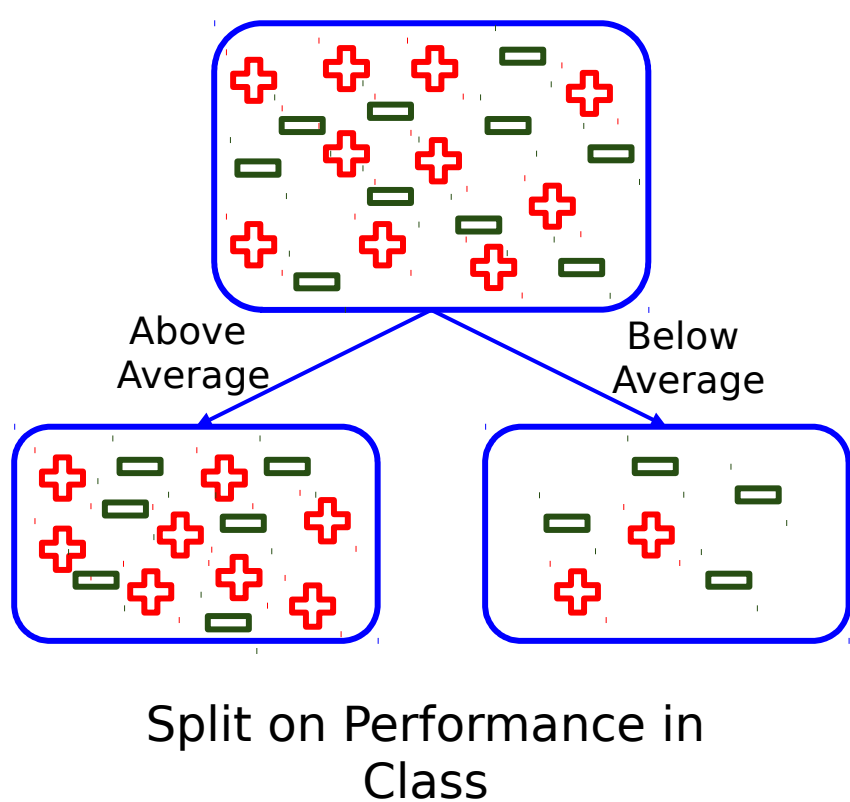
# Properties of Entropy

- Works only with categorical targets
- Lesser the Entropy, higher the homogeneity of nodes

# Steps to calculate Entropy for a split

- Calculate the entropy of the parent node
- Calculate the entropy of each child node
- Calculate the weighted average entropy of the split

# Steps to calculate Entropy for a split





# Steps to calculate Entropy for a split

**Split on Performance in  
Class**

# Steps to calculate Entropy for a split

## Split on Performance in Class

- Entropy for Parent node:

$$-(0.5) \cdot \log_2(0.5) - (0.5) \cdot \log_2(0.5) = 1$$

- Entropy for sub-node Above Average:

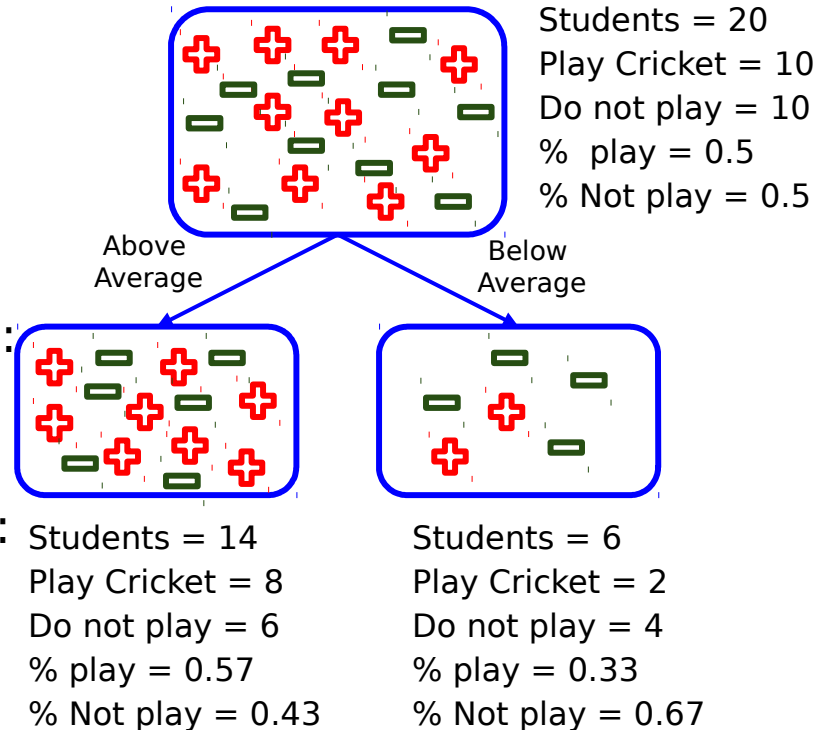
$$-(0.57) \cdot \log_2(0.57) - (0.43) \cdot \log_2(0.43) = 0.98$$

- Entropy for sub-node Below Average:

$$-(0.33) \cdot \log_2(0.33) - (0.67) \cdot \log_2(0.67) = 0.91$$

- Weighted Entropy: Performance in Class:

$$(14/20) \cdot 0.98 + (6/20) \cdot 0.91 = 0.959$$



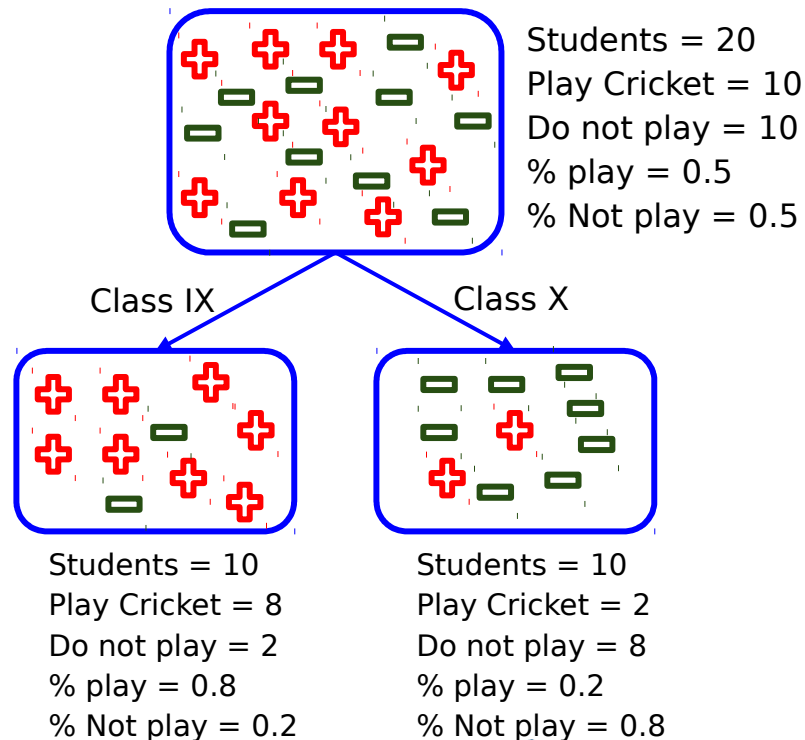
# Steps to calculate Entropy for a split

## **Split on Class**

# Steps to calculate Entropy for a split

## Split on Class

- Entropy for Parent node:  
 $-(0.5) \cdot \log_2(0.5) - (0.5) \cdot \log_2(0.5) = 1$
- Entropy for sub-node Class IX:  
 $-(0.8) \cdot \log_2(0.8) - (0.2) \cdot \log_2(0.2) = 0.722$
- Entropy for sub-node Class X:  
 $-(0.2) \cdot \log_2(0.2) - (0.8) \cdot \log_2(0.8) = 0.722$
- Weighted Entropy: Class:  
 $(10/20) \cdot 0.722 + (10/20) \cdot 0.722 = 0.722$



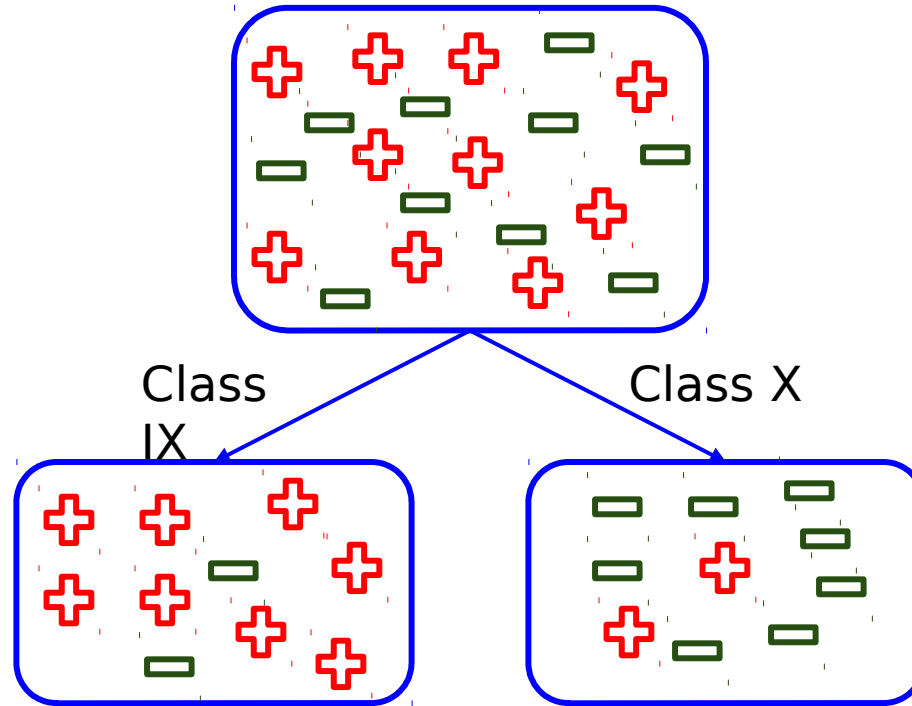
# Steps to calculate Entropy for a split

Split	Entropy	Information Gain
Performance in Class	0.959	0.041
Class	0.722	0.278

# Steps to calculate Entropy for a split

Split	Entropy	Information Gain
Performance in Class	0.959	0.041
Class	0.722	0.278

# Steps to calculate Entropy for a split



Split on Class

Thank  
You!