

Backward Propagation

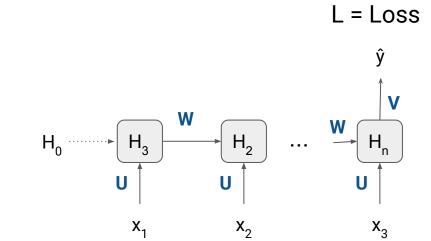
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• \partial L/\partial W = (\partial L/\partial \hat{y}) \cdot (\partial \hat{y}/\partial H_3) \cdot (\partial g(z_3)/\partial z_3)[H_2 + W((\partial g(z_2)/\partial z_2)[H_1 + W((\partial g(z_1)/\partial z_1)[H_0 + W(\partial H_0/\partial W)])])]
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• \partial L/\partial U = (\partial L/\partial \hat{y}) \cdot (\partial \hat{y}/\partial H_3) \cdot (\partial g(z_3)/\partial z_3)[x_3 + (W(\partial g(z_2)/\partial z_2) \cdot [x_2 + (W(\partial g(z_1)/\partial z_1) \cdot [x_1 + (\partial WH_0/\partial U)])])]
```



9L/3W

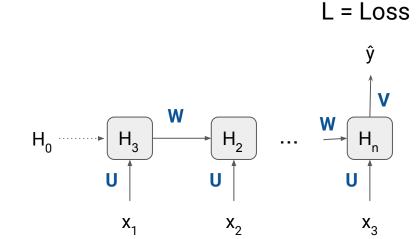
9L/3U





• $9\text{L}/9\text{M} \rightarrow 9\text{H}^{\text{u}}/9\text{M}$

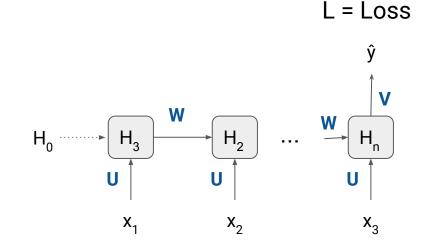
 $\bullet \quad 9\text{L}/9\text{L} \rightarrow 9\text{H}^{\text{u}}/9\text{L}$





• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W$

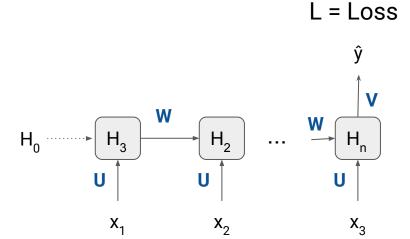
• $\partial L/\partial U \to \partial H_n/\partial U \to \partial H_{n-1}/\partial U$





• $\partial L/\partial W \to \partial H_n/\partial W \to \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

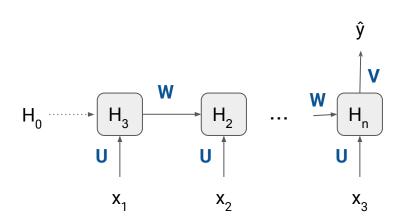
• $\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$





• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

• $\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$



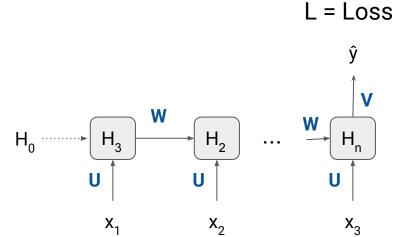


L = Loss

• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

• $\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$

• If gradients < 1



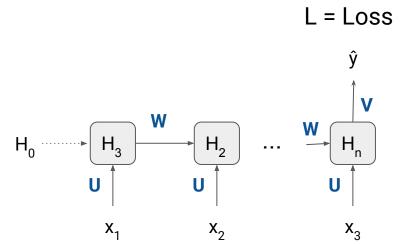


• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

•
$$\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$$

If gradients < 1

then **∂L/∂W** and **∂L/∂U** will be infinitesimally small





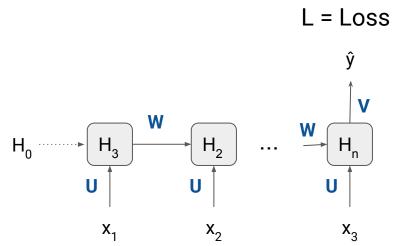
• $\partial L/\partial W \to \partial H_n/\partial W \to \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

•
$$\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$$

• If gradients < 1

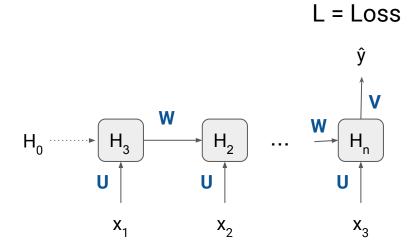
then **al**/**aw** and **al**/**au** will be infinitesimally small

$$(0.5)^10 = 0.00097$$





• $\partial L/\partial M \approx \partial L/\partial U \approx 0$

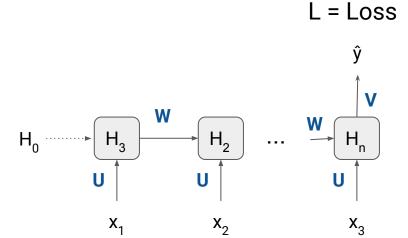




• $\partial L/\partial W \approx \partial L/\partial U \approx 0$

• $W = W - \alpha (\partial L/\partial W)$ $U = U - \alpha (\partial L/\partial U)$

updating weights

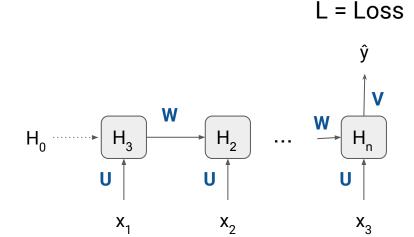




• $\partial L/\partial W \approx \partial L/\partial U \approx 0$

• $W = W - \alpha (\partial L/\partial W)$ $U = U - \alpha (\partial L/\partial U)$ updating weights

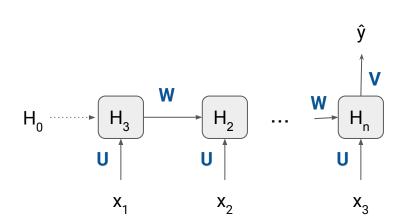
• $W_{\text{before}} \approx W_{\text{after}}$ $U_{\text{before}} \approx U_{\text{after}}$





• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

• $\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$





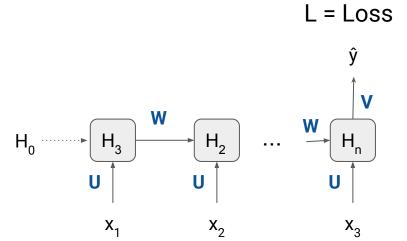
L = Loss

• $\partial L/\partial W \rightarrow \partial H_n/\partial W \rightarrow \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

• $\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$

If gradients > 1

then $\partial L/\partial W$ and $\partial L/\partial U$ are very large

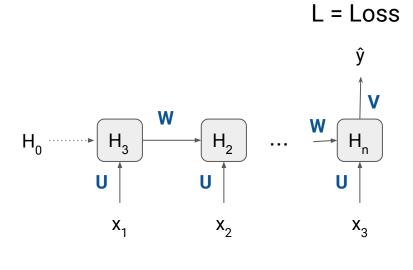




• $\partial L/\partial W \to \partial H_n/\partial W \to \partial H_{n-1}/\partial W \dots \partial H_0/\partial W$

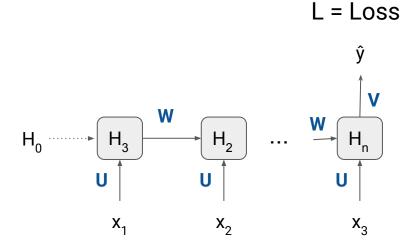
•
$$\partial L/\partial U \rightarrow \partial H_n/\partial U \rightarrow \partial H_{n-1}/\partial U \dots \partial H_0/\partial U$$

• If gradients > 1 then $\partial L/\partial W$ and $\partial L/\partial U$ are very large $(1.5)^10 = 57.665$





• $W = W - \alpha (\partial L/\partial W)$ $U = U - \alpha (\partial L/\partial U)$ updating weights





Vanishing Gradient

RNN does not perform well for long sentences



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books is



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books is
The writer of the books are



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books is
The writer of the books are

Exploding Gradient

Gradients are large



Vanishing Gradient

RNN does not perform well for long sentences

Eg: The writer of the books is
The writer of the books are

Exploding Gradient

- Gradients are large
- Poor predictions



How to mitigate exploding and vanishing gradients?



How to mitigate exploding and vanishing gradients?

Exploding Gradients

Gradient Clipping



How to mitigate exploding and vanishing gradients?

Exploding Gradients

Gradient Clipping

Threshold = 0.1

- if gradient > threshold, then gradient = threshold
- if gradient <= threshold, then gradient = gradient



How to mitigate exploding and vanishing gradients?

Exploding Gradients	Vanishing Gradients
Gradient Clipping	LSTM or GRU



Thank You

