

1. The function F above satisfies the conclusion of Rolle's Theorem in the interval $[a, b]$ because

- I. F is continuous.
- II. F is differentiable on (a, b) .
- III. $F(a) = F(b) = 0$.

- A) I only
- B) II only
- C) I and III only
- D) I, II, and III
- E) F does not satisfy Rolle's Theorem

2. If $Q(x) = (3x + 2)^3$, then the third derivative of Q at $x = 0$ is

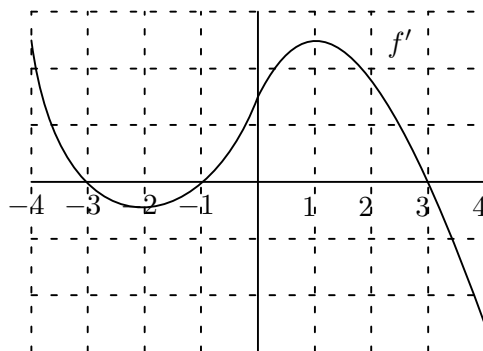
- A) 0
- B) 9
- C) 54
- D) 162
- E) 224

3. If a function g is differentiable on the interval $[-4, 4]$, then which of the following statements is true?

- A) g is not continuous on $[-5, 5]$.
- B) g is not differentiable on $[-5, 5]$.
- C) $g'(c) = 0$ for some c in $[-4, 4]$.
- D) The conclusion of the Mean Value Theorem applies to g .
- E) None of the above statements are true.

4. The value of c guaranteed to exist by the Mean Value Theorem for $f(x) = x^2$ in the interval $[0, 3]$ is

- A) 1
 - B) 2
 - C) $\frac{3}{2}$
 - D) $\frac{1}{2}$
 - E) None of these
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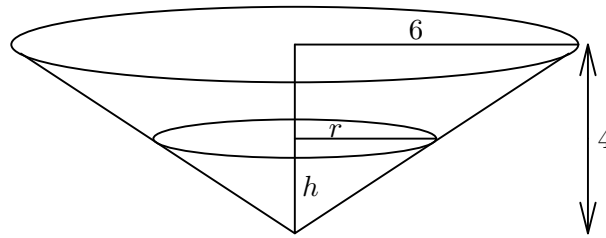
5. The graph of the derivative of a function f is shown above. Which of the following are true about the original function f ?

- I. f is increasing on the interval $(-2, 1)$.
- II. f is continuous at $x = 0$.
- III. f has an inflection point at $x = -2$.

- A) I only
 - B) II only
 - C) III only
 - D) II and III only
 - E) I, II, and III
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6. Two particles move along the x -axis and their positions at time $0 \leq t \leq 2\pi$ are given by $x_1 = \cos t$ and $x_2 = e^{(t-3)/2} - 0.75$. For how many values of t do the two particles have the same velocity?

- A) 0
- B) 1
- C) 2
- D) 3
- E) 4



7. The conical reservoir shown above has diameter 12 feet and height 4 feet. Water is flowing into the reservoir at the constant rate of 10 cubic feet per minute. At the instant when the surface of the water is 2 feet above the vertex, the water level is rising at the rate of

- A) 0.177 ft per min
- B) 0.354 ft per min
- C) 0.531 ft per min
- D) 0.708 ft per min
- E) 0.885 ft per min

8. The position of a particle moving on the x -axis, starting at time $t = 0$, is given by $x(t) = (t - a)^3(t - b)$, where $0 < a < b$. Which of the following statements are true?

- I. The particle is at a positive position on the x -axis at time $t = \frac{a+b}{2}$.
- II. The particle is at rest at time $t = a$.
- III. The particle is moving to the right at time $t = b$.

- A) I only
- B) II only
- C) III only
- D) I and II only
- E) II and III only

9. Let the function f be differentiable on the interval $[0, 2.5]$ and define g by $g(x) = f(f(x))$. Use the table below to estimate $g'(1)$.

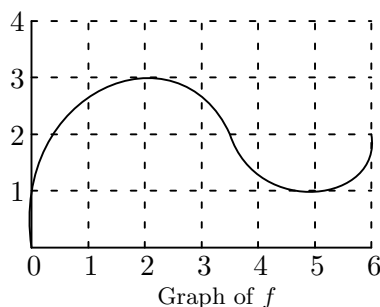
x	0.0	0.5	1.0	1.5	2.0	2.5
$f(x)$	1.7	1.8	2.0	2.4	3.1	4.4

- A) 0.8
- B) 1.2
- C) 1.6
- D) 2.0
- E) 2.4

10. Which of the following are true about a particle that starts at $t = 0$ and moves along a number line if its position at time t is given by $s(t) = (t - 2)^3(t - 6)$?

- I. The particle is moving to the right for $t > 5$.
- II. The particle is at rest at $t = 2$ and $t = 6$.
- III. The particle changes direction at $t = 2$.

- A) I only
- B) II only
- C) III only
- D) I and III only
- E) None are true.



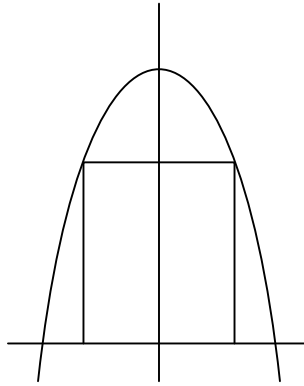
11. The graph of the function f is shown above. Which of the following statements are true?

- I. $\lim_{h \rightarrow 0} \frac{f(2+h) - f(2)}{h} = f'(5)$.
- II. $\frac{f(5) - f(2)}{5 - 2} = \frac{2}{3}$.
- III. $f''(1) \leq f''(5)$.

- A) I and II only
- B) I and III only
- C) II and III only
- D) I, II, and III
- E) None of these

12. If $x^2 - y^2 = 25$, then $\frac{d^2y}{dx^2} =$

- A) $-\frac{x}{y}$
- B) $\frac{5}{y^2}$
- C) $-\frac{x^2}{y^3}$
- D) $-\frac{25}{y^3}$
- E) $\frac{4}{y^3}$



13. A rectangle with one side on the x -axis has its upper vertices on the graph of $y = 4 - x^2$, as shown in the figure above. What is the maximum area of the rectangle?

- A) 1.155
- B) 1.855
- C) 3.709
- D) 6.158
- E) 12.316

14. Let f be a twice-differentiable function of x such that, when $x = c$, f is decreasing, concave up, and has an x -intercept. Which of the following is true?

- A) $f(c) < f'(c) < f''(c)$
- B) $f(c) < f''(c) < f'(c)$
- C) $f'(c) < f(c) < f''(c)$
- D) $f'(c) < f''(c) < f(c)$
- E) $f''(c) < f(c) < f'(c)$

15. If $f'(x) = \arctan(x^3 - x)$, at how many points is the tangent line to the graph of $f(x)$ parallel to the line $y = 2x$?

- A) None
- B) 1
- C) 2
- D) 3
- E) Infinitely many