Functional data analysis in phonetic research

Michele Gubian

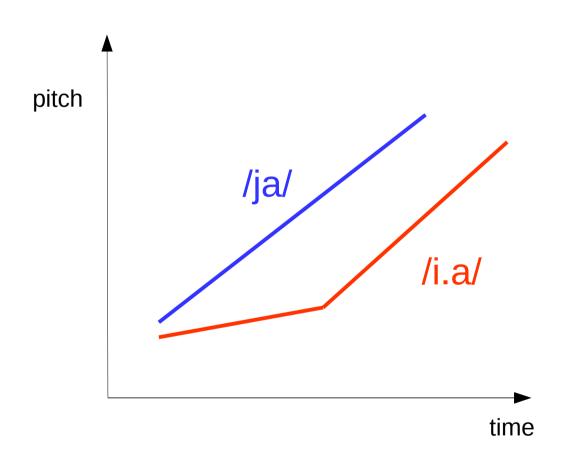
Institute of Phonetics and Speech Processing LMU Munich, Germany



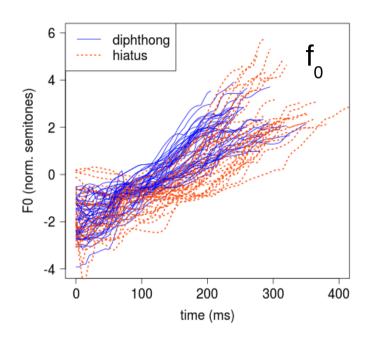


Vienna, February 2020

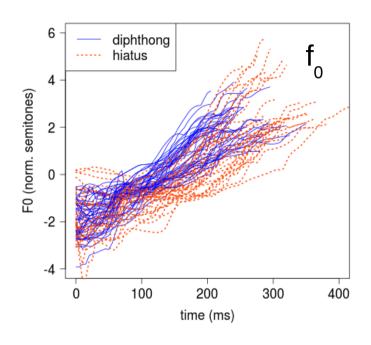
Alignment of rising pitch accents in Spanish



- European Spanish
- **Diphthong**: /ja/ e.g. *Emil<u>ia</u>na*
- **Hiatus** /i.a/ e.g. *p<u>ia</u>no*
- Rising pitch accent should align to syllabic structure



- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each



- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each

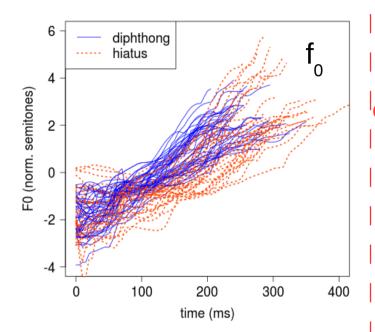


Genotimes: Genoti

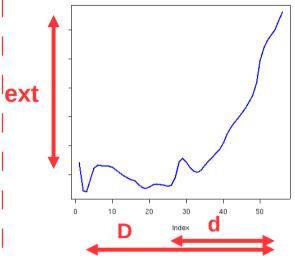
- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each

NUMBERS





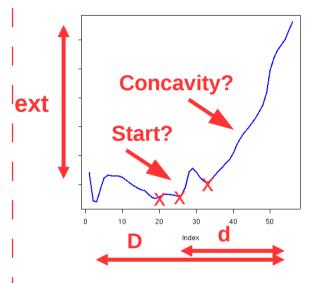
- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each



ext (st)	d/D	Cat.
5.3	0.9	D
4.6	0.7	H
		•••

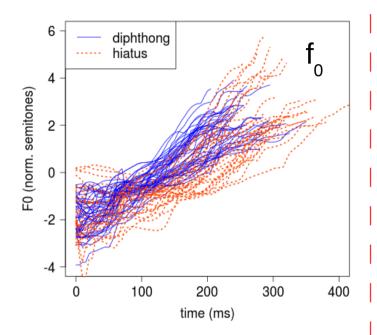
NUMBERS

- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each



ext (st)	d/D	Cat.
5.3	0.9	D
4.6	0.7	Н
	•••	

NUMBERS



- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each

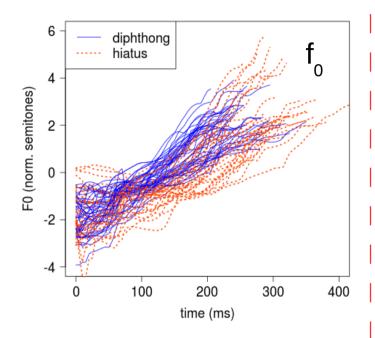


k0	k1	k2	•••
•••		•••	•••

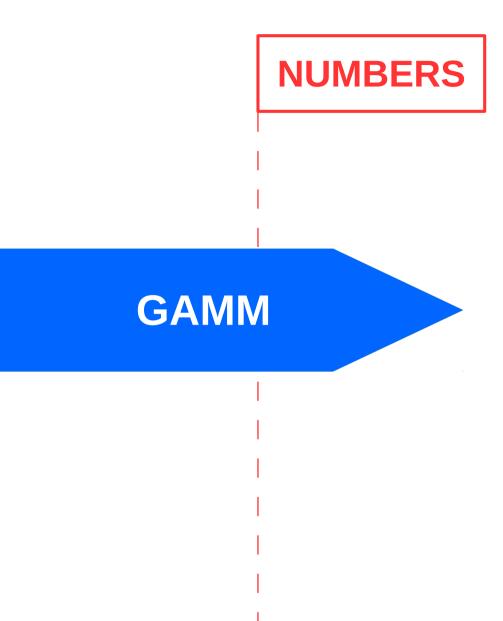
NUMBERS

DCT limitations

- DCT does not (easily) encode time-localised information, e.g. a small hump
- Typically only k0, k1 and k2 are used, which have a geometric interpretation (mean, slope, curvature)
- Extracting several k's brings up the need of PCA
- In general, not effective to encode long signals



- Read speech
- 9 participants
- 20 Diphthongs +20 Hiatuses each



GAMMs

PRO

- LMER directly on curves
- Good R packages (e.g. mgcv)
- Good tutorials (e.g. Wieling, Soskuthy)

CON

- No easy way to analyse multidimensional signals
- Computationally heavy
- LMER directly on curves :D

MISSION

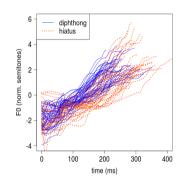
automate curve parametrisation

- Data driven
- Few parameters
 - Interpretable

Road map

CURVES

NUMBERS



Interpolate using a function basis

Dimensionality reduction tool

LMER

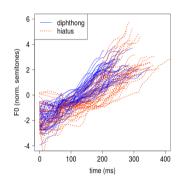
Data driven

- Few parameters
- Interpretable

Road map

CURVES

NUMBERS



Interpolate using a function basis

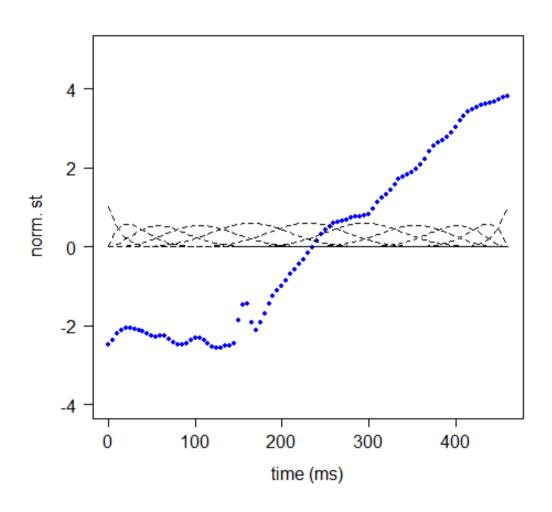
Dimensionality reduction tool

LMER

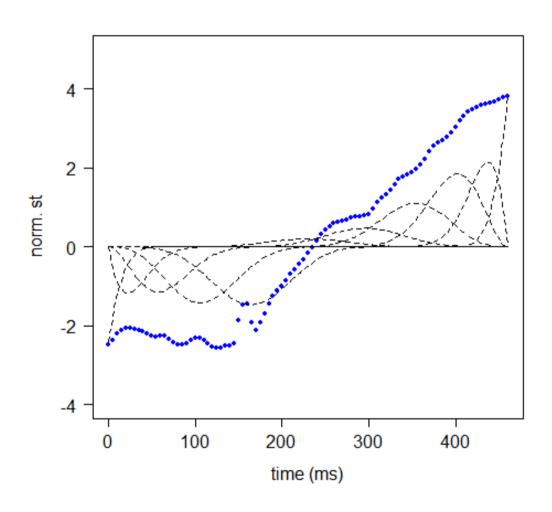
Data driven

- Few parameters
- Interpretable

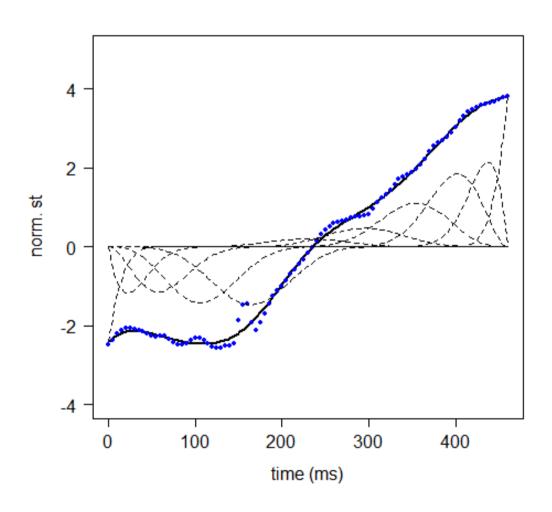
Interpolation with B-splines



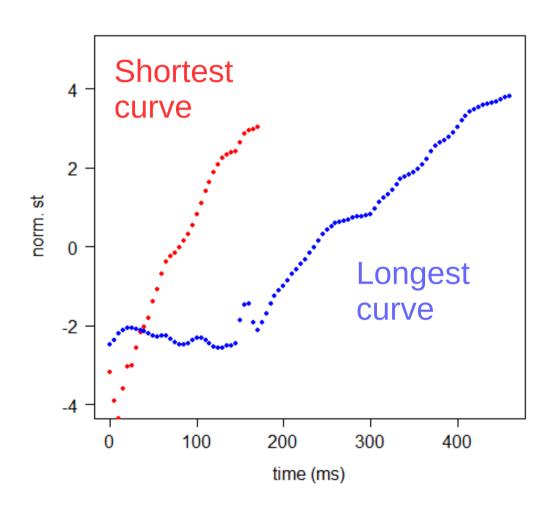
Interpolation with B-splines



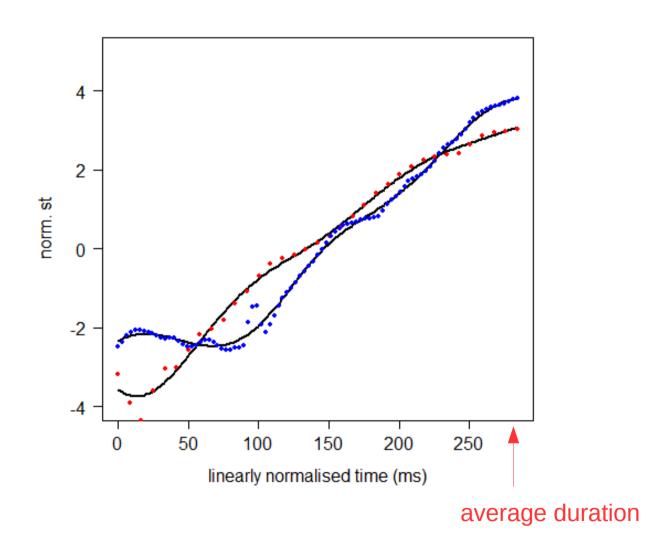
Interpolation with B-splines



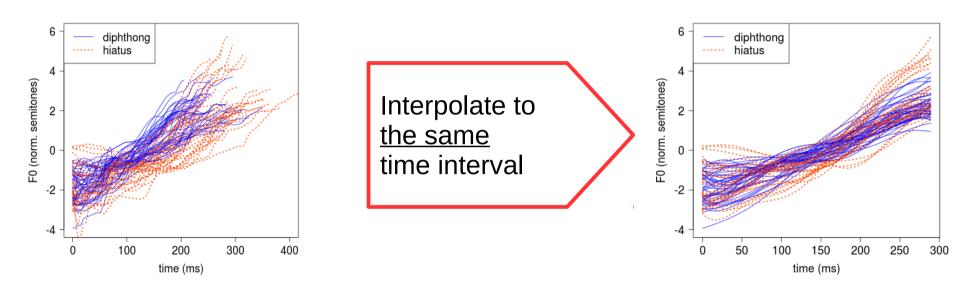
Different durations



Linear time normalisation



Linear time normalisation

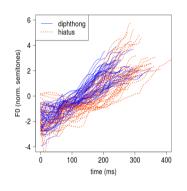


- We must use the same time interval
- This implies linear time normalisation
- Durations have to be reintroduced at the end of the analysis

Road map

CURVES

NUMBERS



Interpolate to the same time interval

Dimensionality reduction tool

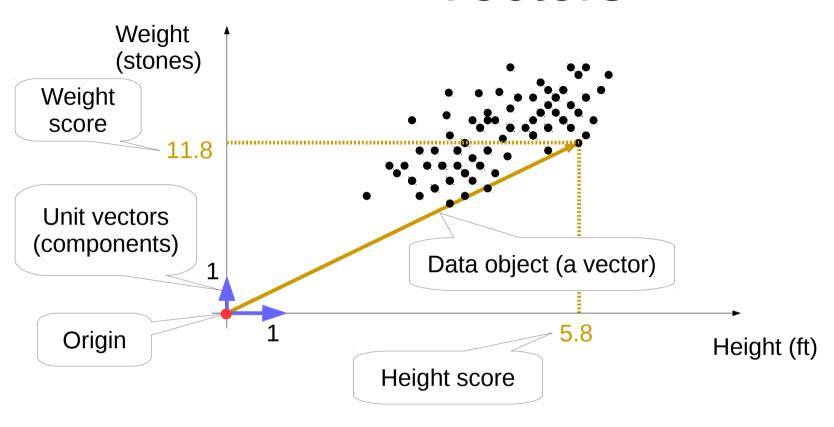
LMER

Data driven

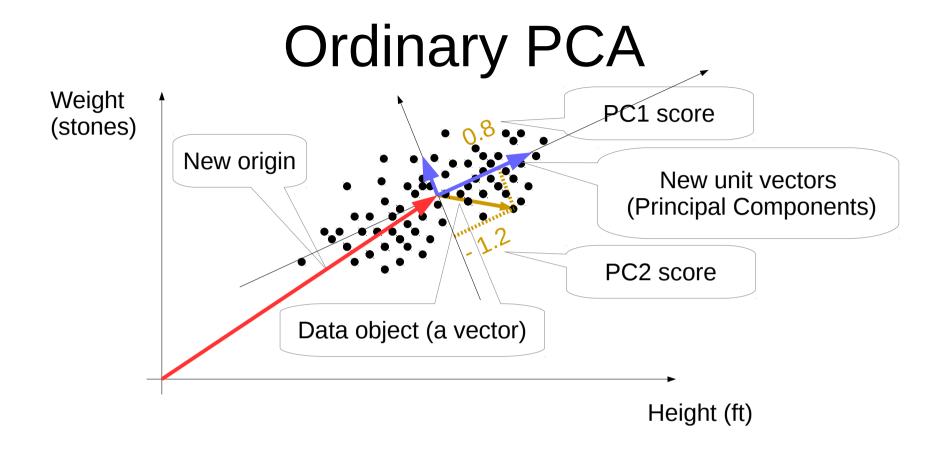
- Few parameters
- Interpretable

Introducing Functional PCA

Vectors

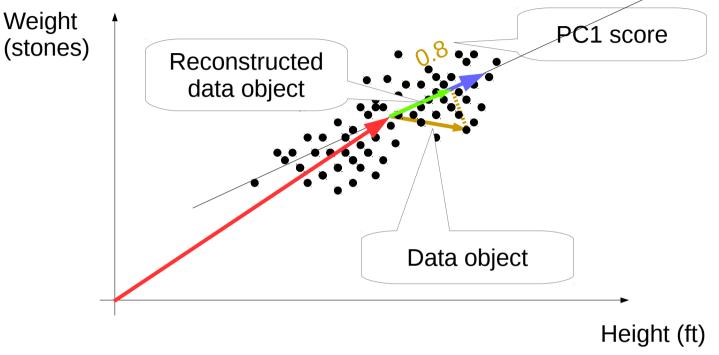


- Data objects and components are vectors
- From scores (numbers) we can reconstruct data objects (vectors)

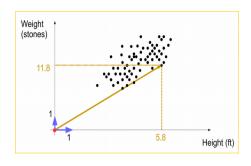


- PCA computes new origin and unit vectors which best suit the data
- From PC scores we can reconstruct data objects

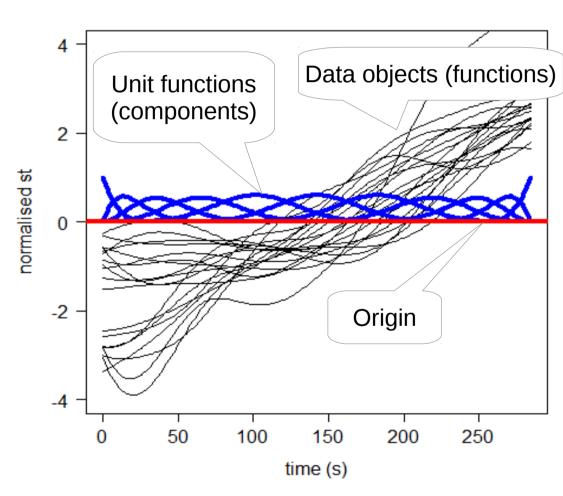
Dimensionality reduction



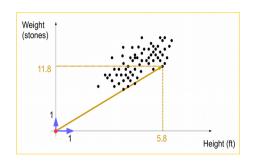
- We can use only part of the PCs
- This reduces the data dimensionality
- But introduces reconstruction errors too



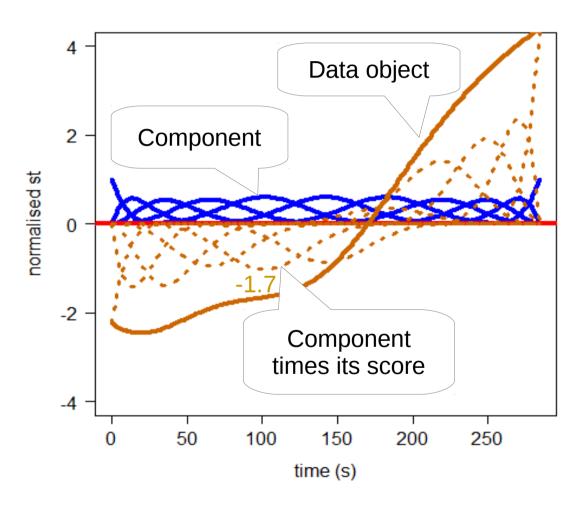
Functions (curves)



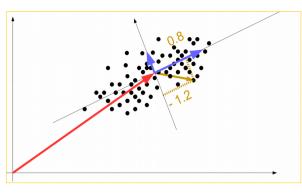
- Origin, components and data objects are functions
- Origin is a flat line
- Components are 11 B-spline curves



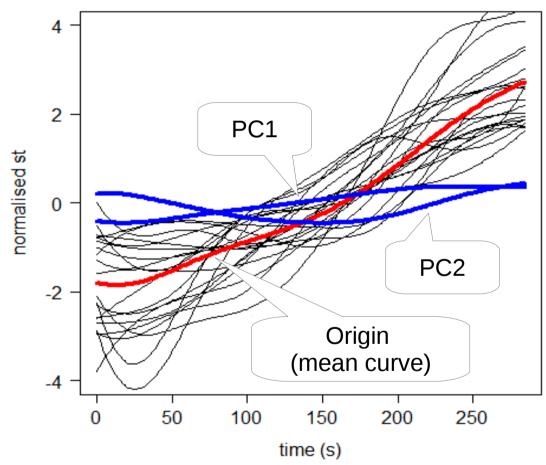
Functions (curves)



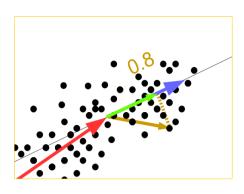
- Each of the 11 components is multiplied by a score
- These are summed together to obtain a data object



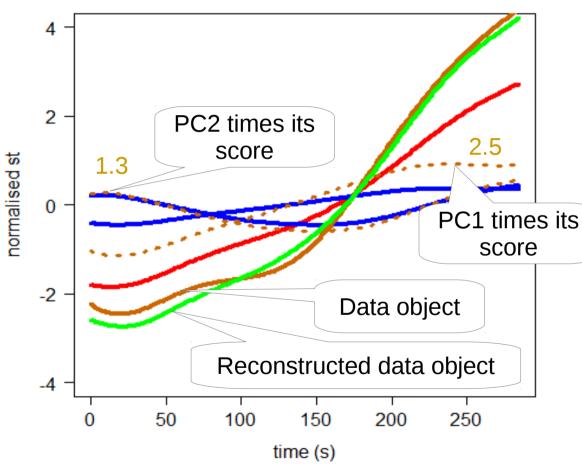
Functional PCA



 FPCA computes new origin and component functions which best suit the data

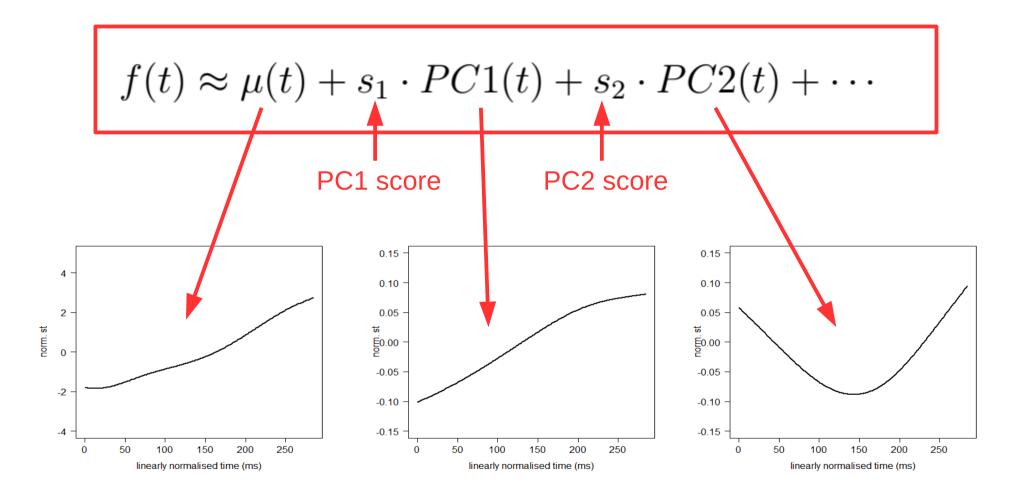


Functional PCA

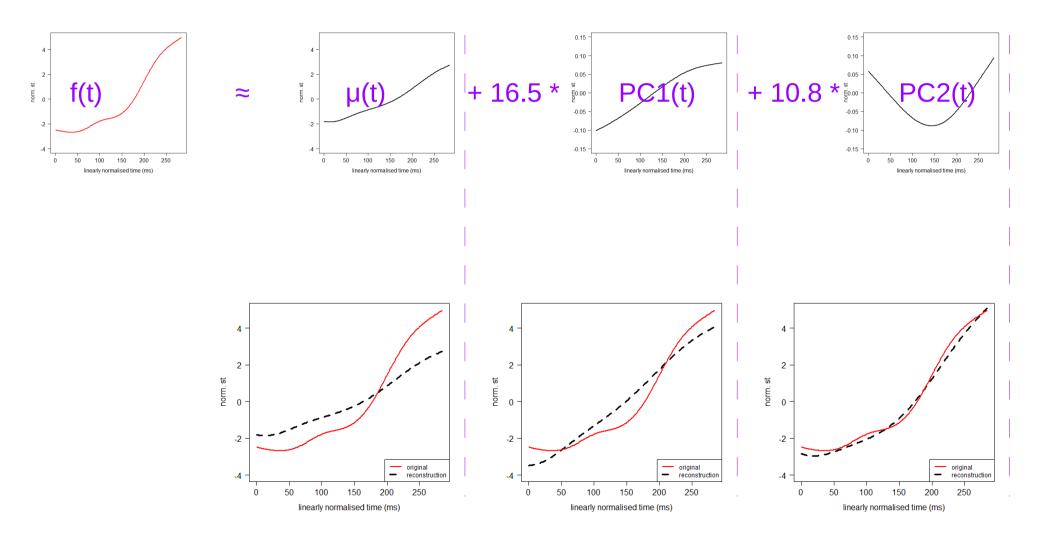


- The sum of origin (mean) curve + PCs times their scores gives an approx reconstruction of the original curve
- Dimensions from 11 (B-splines) down to 2 (PCs)

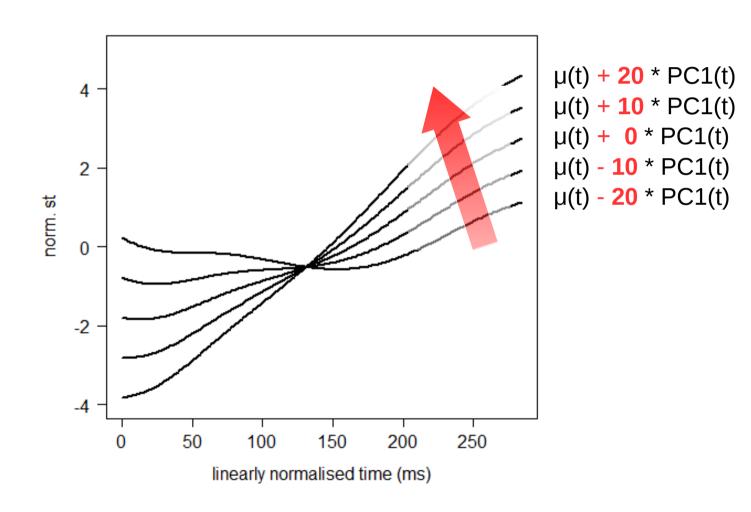
Functional PCs



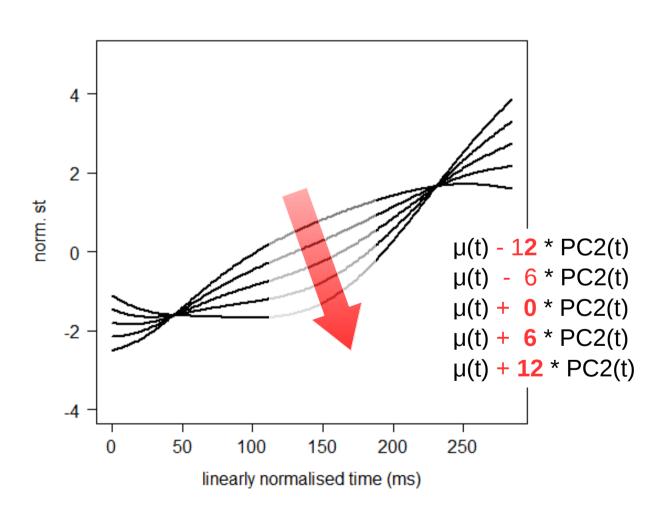
Curve reconstruction



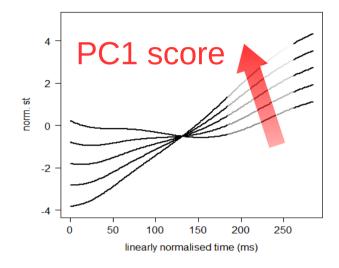
PC1 scores

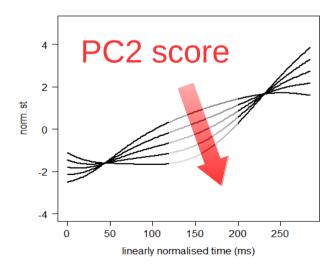


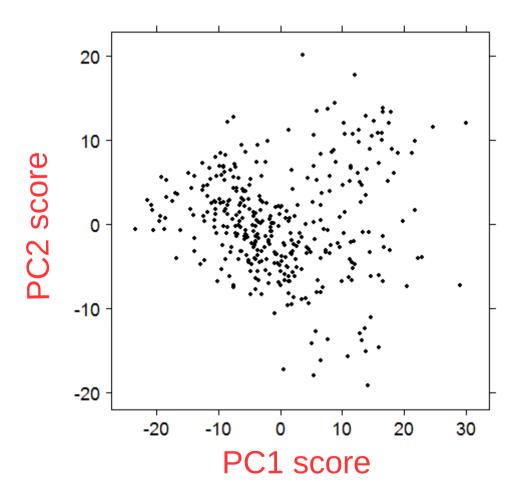
PC2 scores



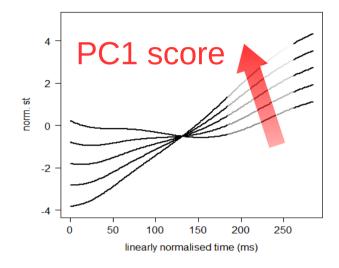
Curve parametrisation

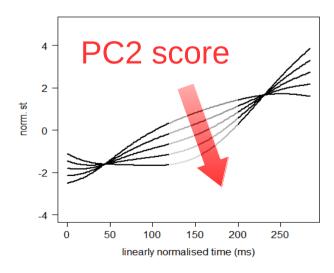


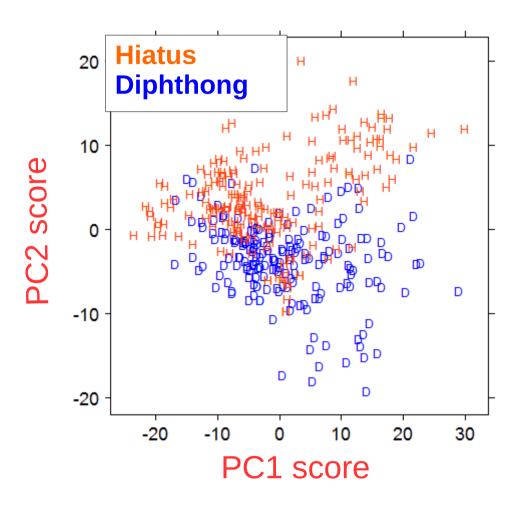




Curve parametrisation



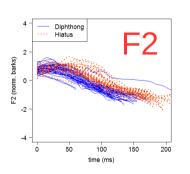


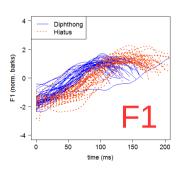


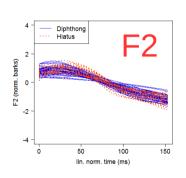
Multidimensional signals

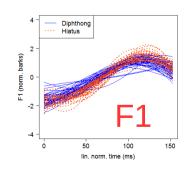
Formants

2D CURVES









FPCA

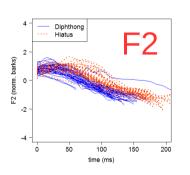


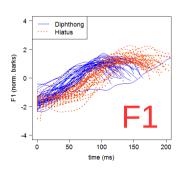
NUMBERS

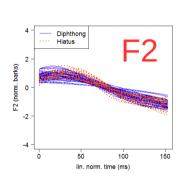
LMER

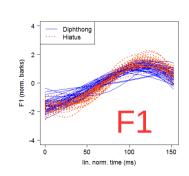
Formants

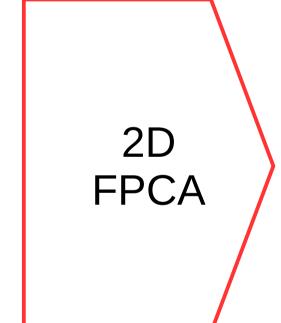
2D CURVES







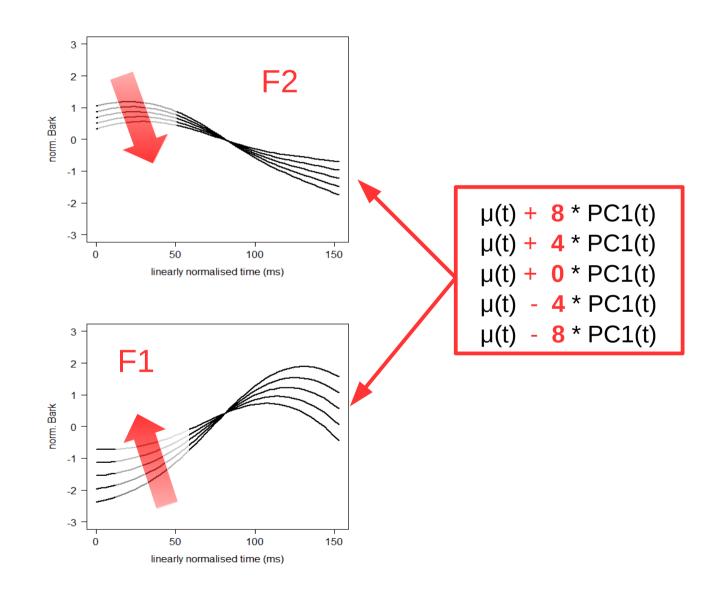




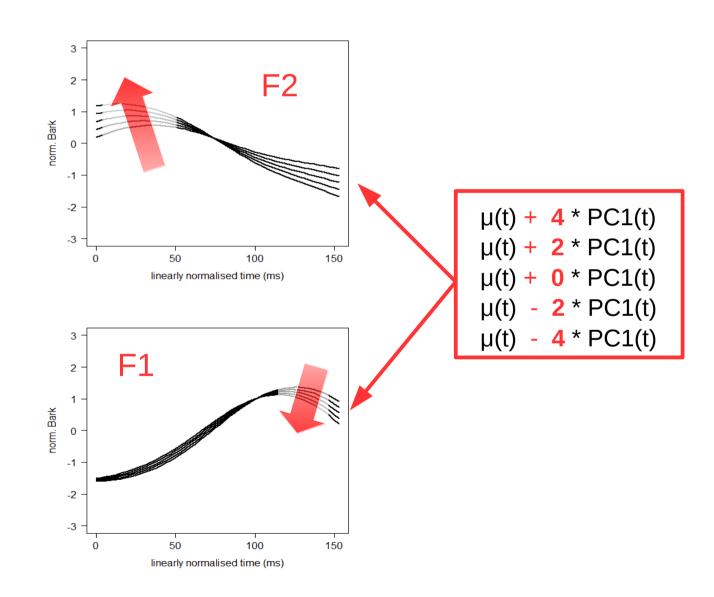
NUMBERS

LMER

PC1 scores

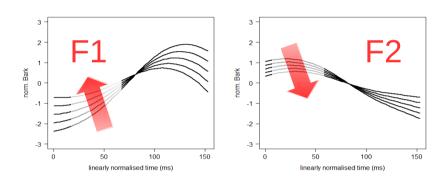


PC2 scores

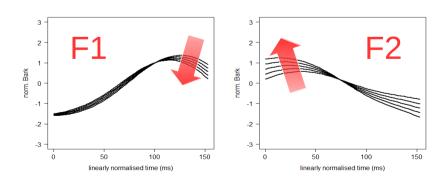


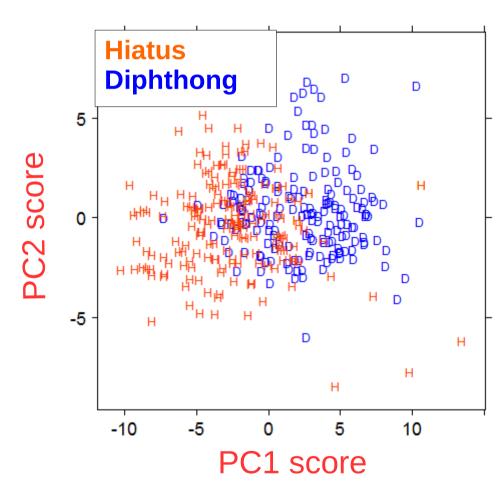
2D curve parametrisation

PC1 score



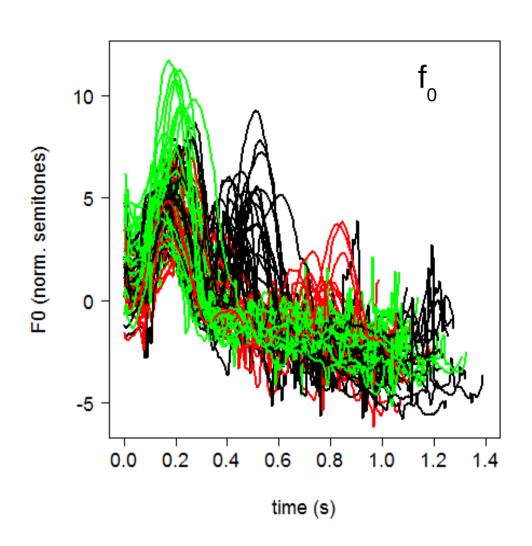
PC2 score





Long signals

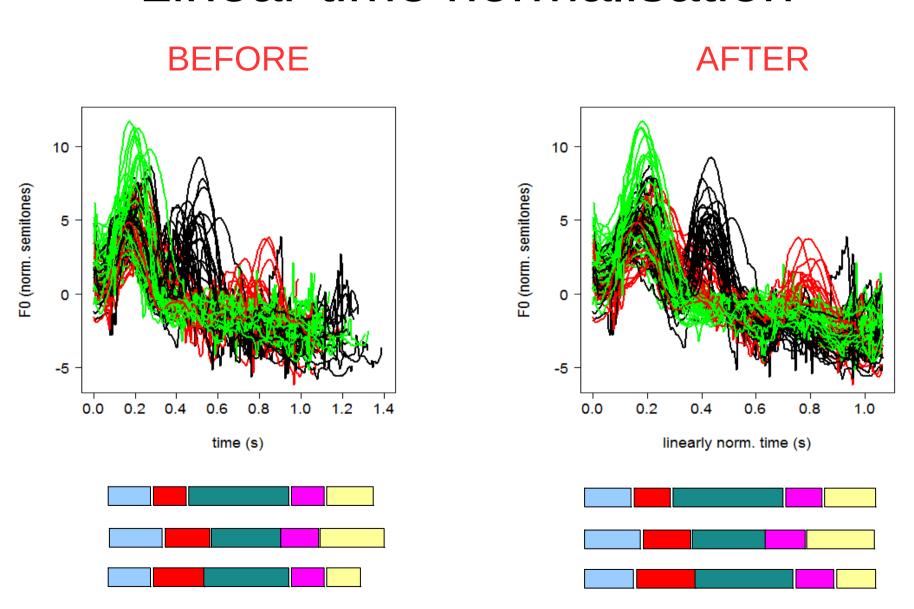
Many segments



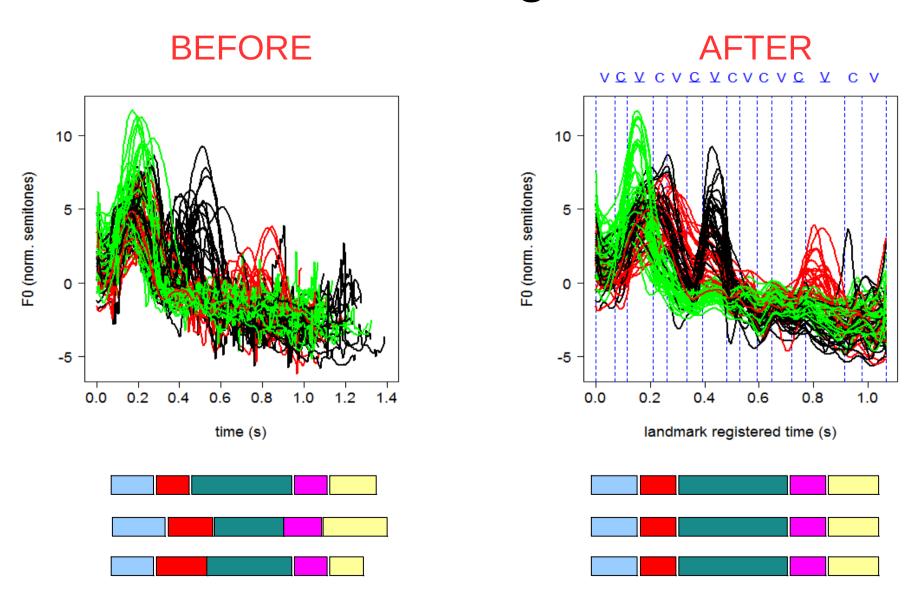
- Narrow focus in Neapolitan Italian
- Focus on
 Subject, Verb or Prop. Phrase
 Danilo vola da Roma
 (Danilo flies from Rome)
- 8 CV syllables
 first C was excluded (too short)
 VCVCV CV CV CV CV

... 15 segments!

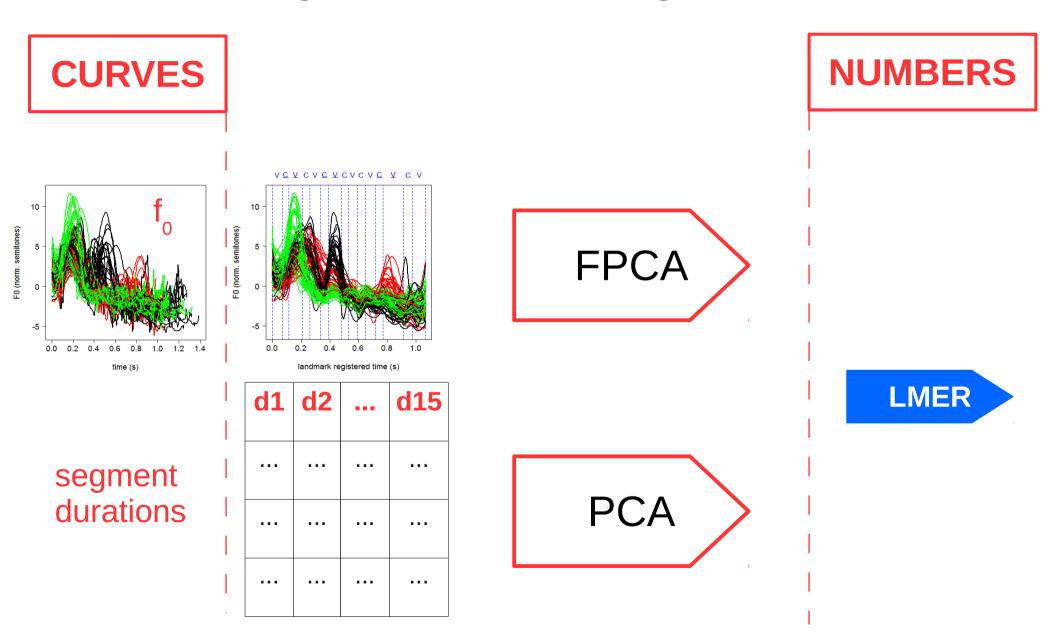
Linear time normalisation



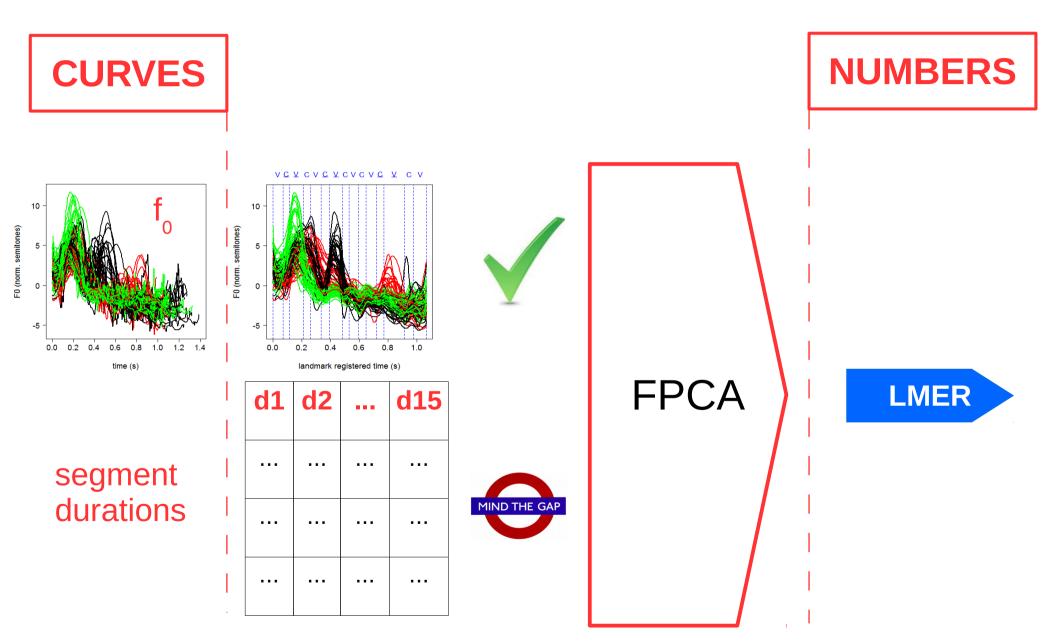
Landmark registration



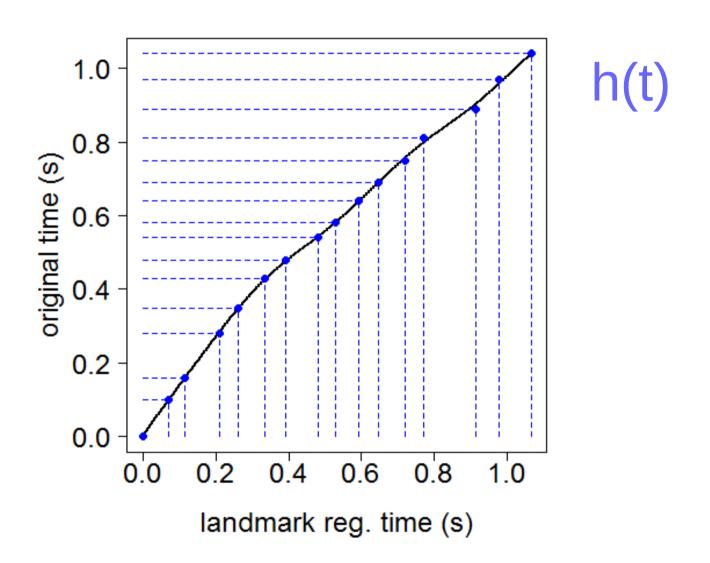
Using landmark registration



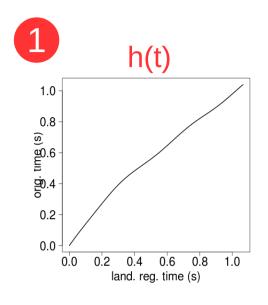
Using landmark registration

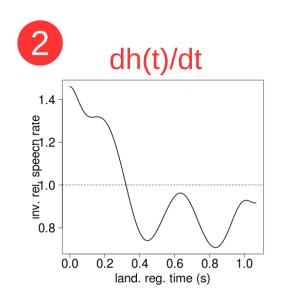


Inside landmark registration

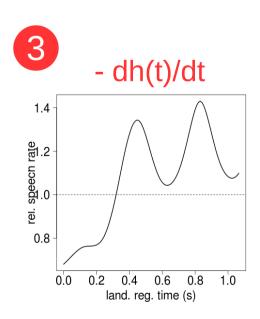


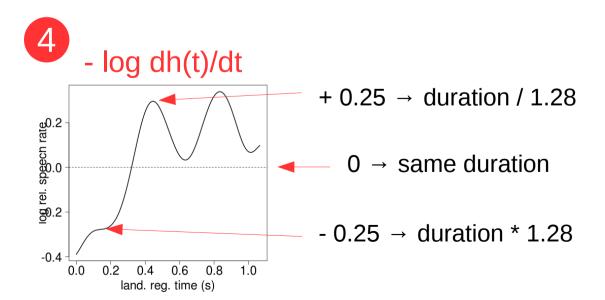
Relative log rate



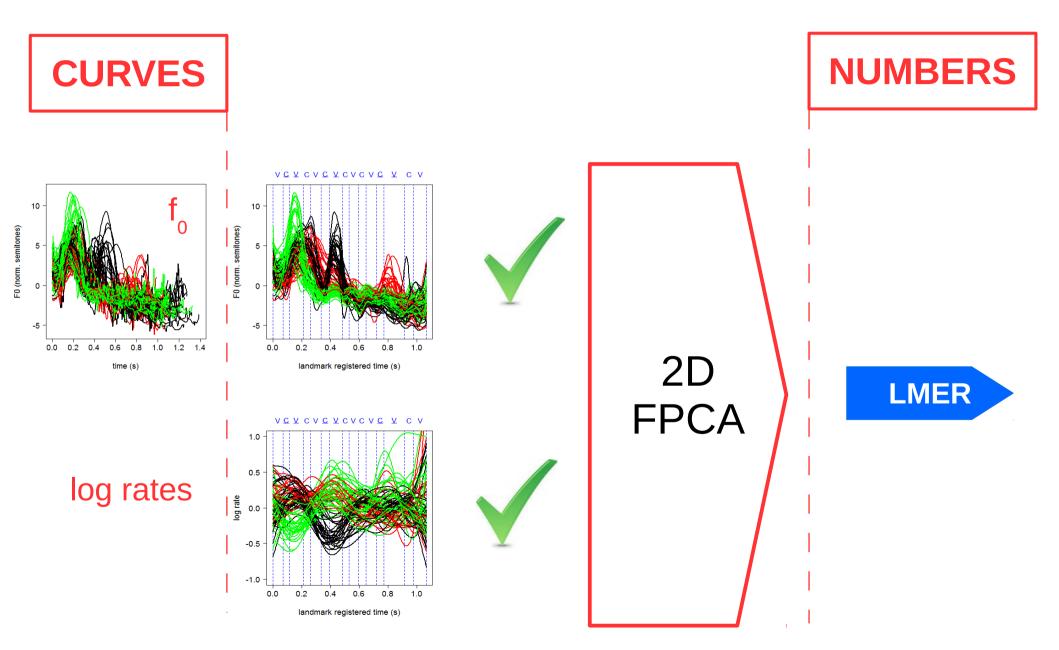




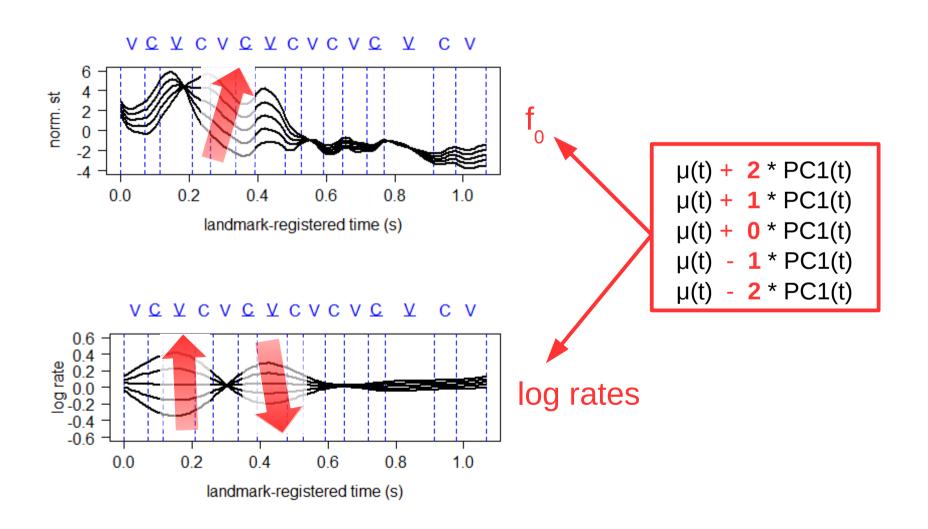




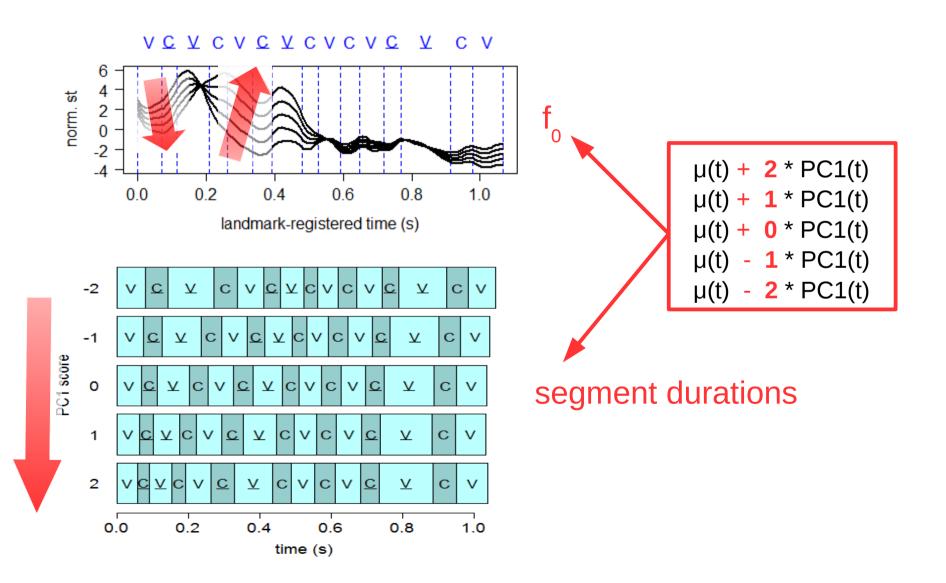
Using log rates



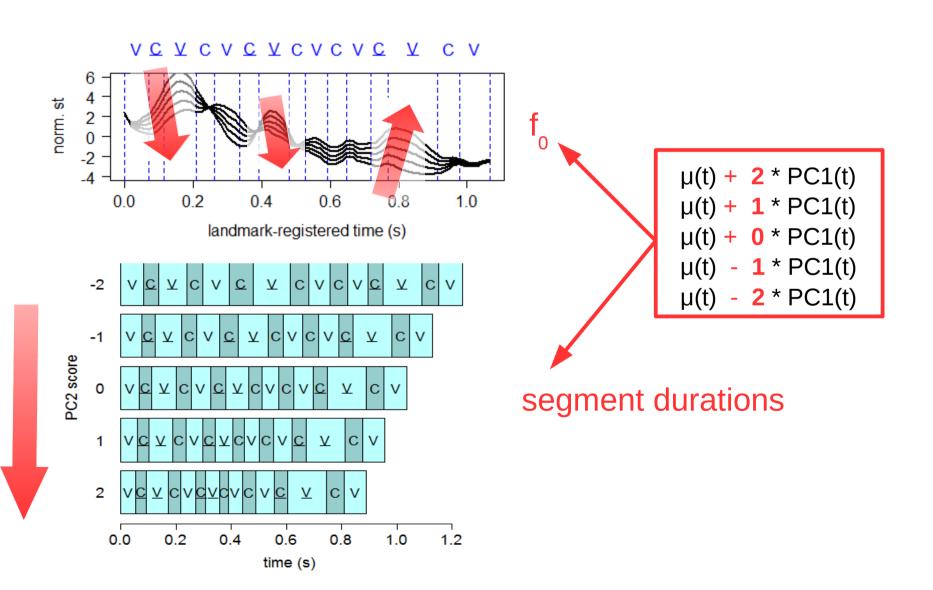
PC1 scores



PC1 scores

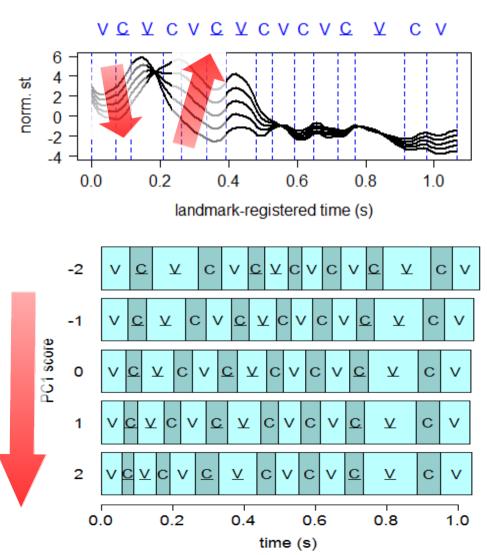


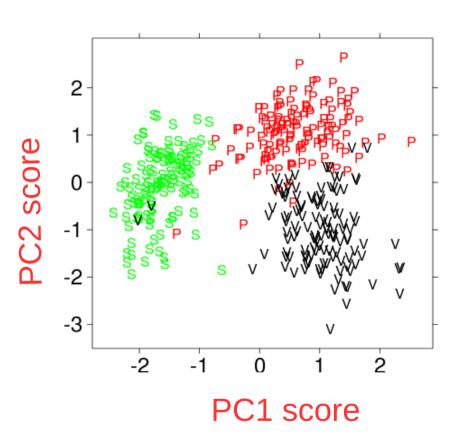
PC2 scores



multi-segment curve parametrisation

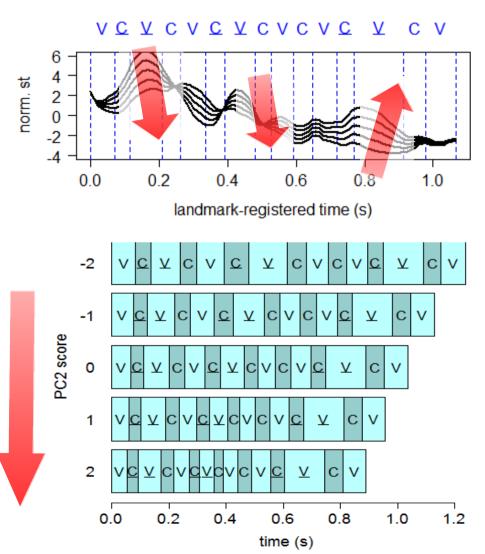
PC1 score

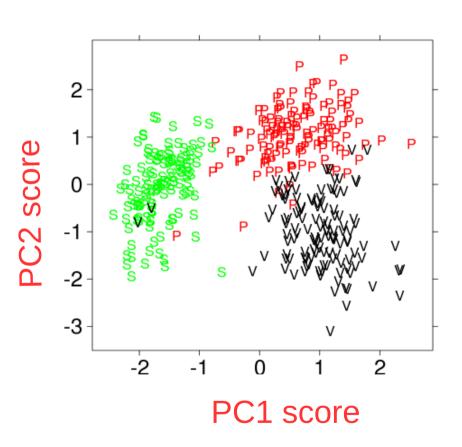




multi-segment curve parametrisation

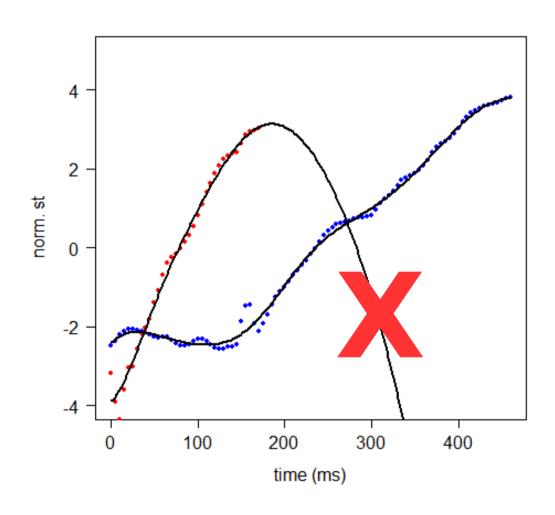
PC2 score



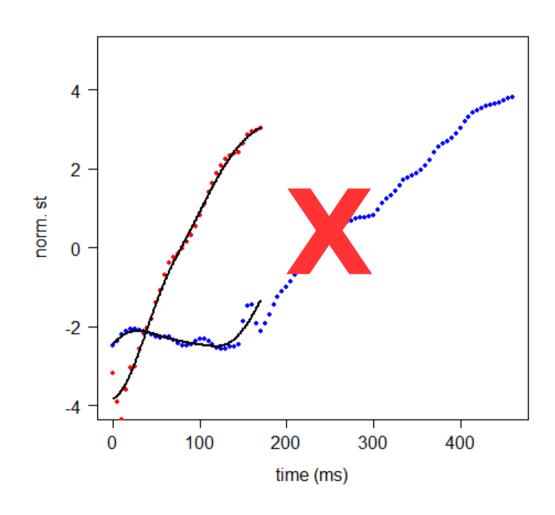


Extra slides

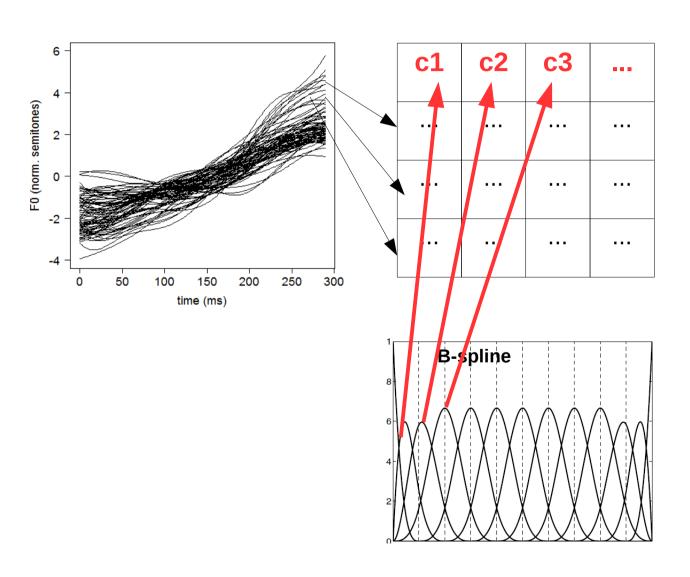
Take longest duration



Take shortest duration



Principal Component Analysis

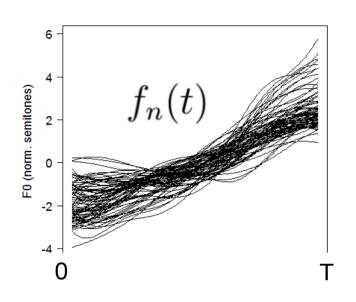




PCA limitations

- PCA does not use any explicit information related to the curve shapes or the B-splines shapes
- e.g. the sequence of coefficients c1, c2,.. reflects time adjacency of polynomial components, i.e. overlapping 'hills'

Functional PCA



$$\max \left\{ var_n \left(\int_0^T \frac{PC1(t)}{f_n(t)} f_n(t) dt \right) \right\}$$

subject to
$$\int_0^T PC1^2(t) = 1$$

7.....

- FPCA definition uses the input curves f_n(t)
- FPCA is independent of the B-splines used to smooth $f_n(t)$