

Classification (Short Version)

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Classification

- To learn more



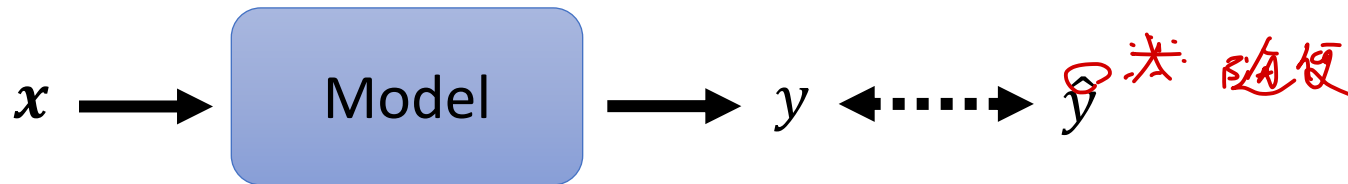
<https://youtu.be/fZAZUYEeIMg>
(in Mandarin)



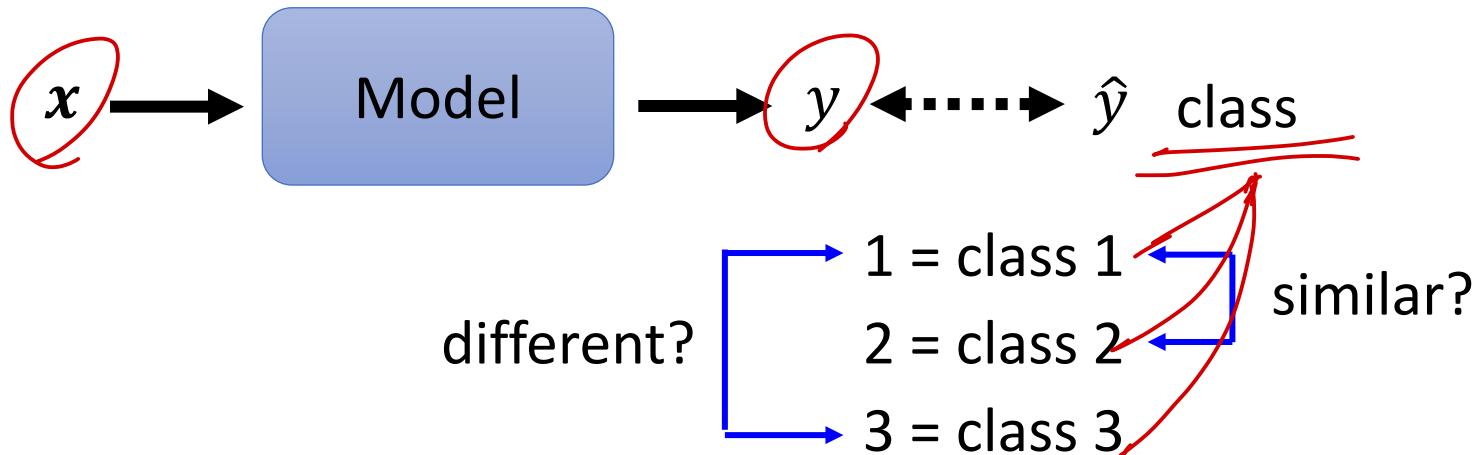
<https://youtu.be/hSXFuypLukA>
(in Mandarin)

Classification as Regression?

- ★ Regression

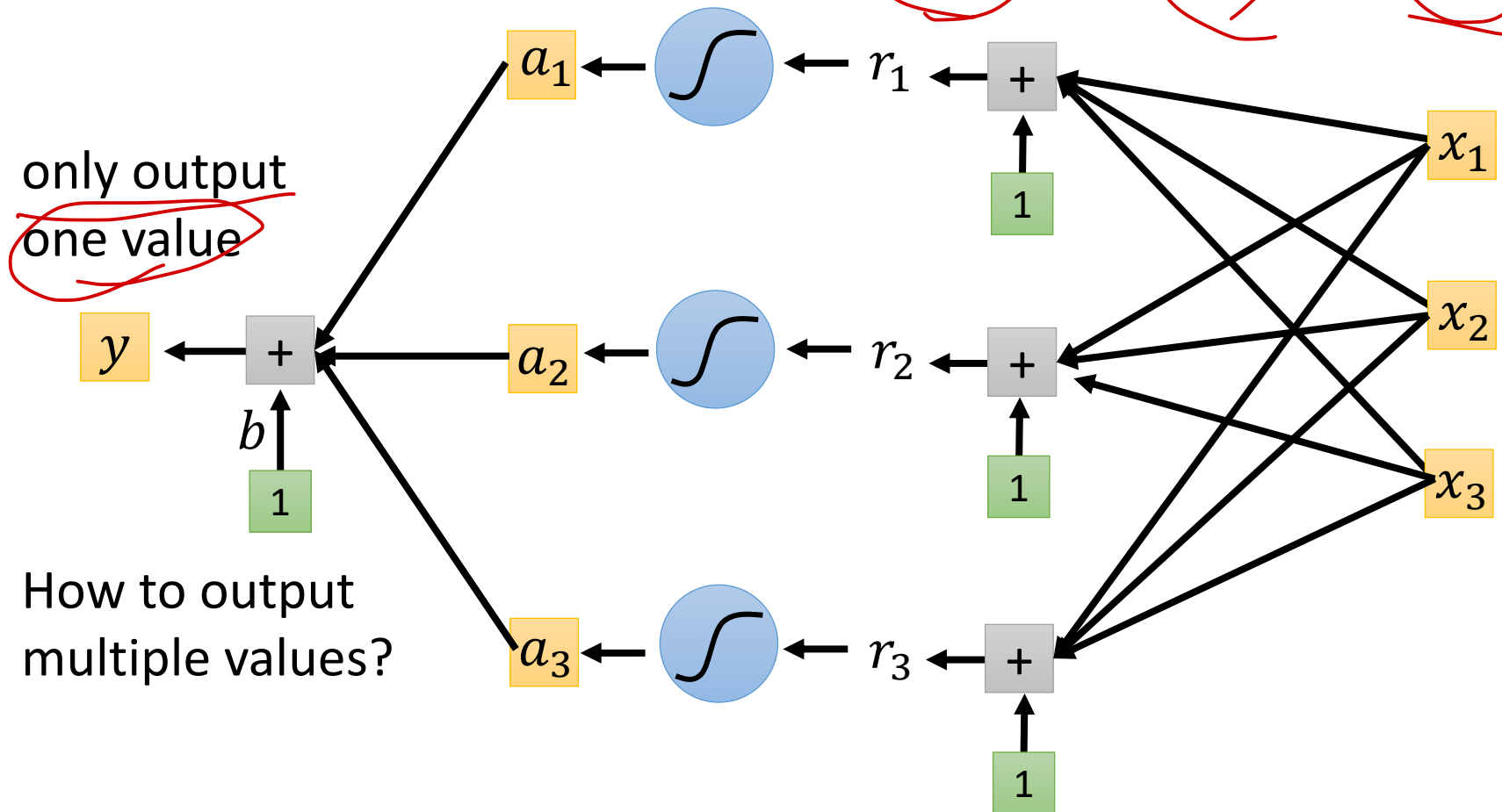


- Classification as regression?

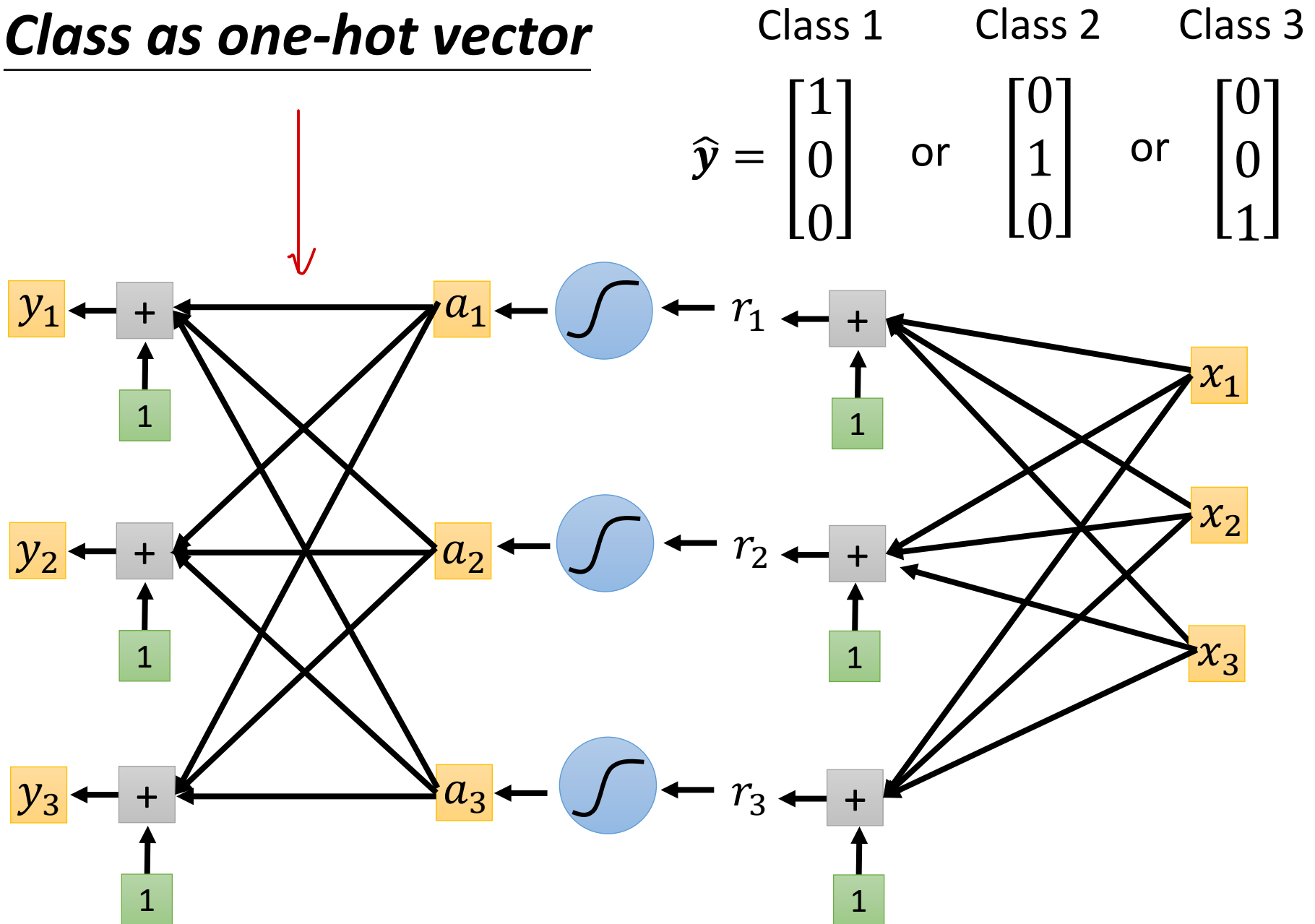


Class as one-hot vector

Class 1 $\hat{y} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$ or Class 2 $\begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$ or Class 3 $\begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$



Class as one-hot vector



Regression

label

$$\hat{y} \longleftrightarrow y = b + c^T \sigma(b + W x)$$

feature

Classification

feature

$$y = b' + W' \sigma(b + W x)$$

label

$$\hat{y} \longleftrightarrow y' = \text{softmax}(y)$$

0 or 1

Make all values between 0 and 1

Can have any value

normalize \rightarrow $\frac{1}{1+e^{-x}}$

Handwritten notes: 向量 (vector) above y ; 通过 (pass) and 归一化 (normalization) with arrows pointing to the softmax function.

Soft-max

$$y'_i = \frac{\exp(y_i)}{\sum_j \exp(y_i)}$$

$$\blacksquare 1 > y'_i > 0$$

$$\blacksquare \sum_i y'_i = 1$$

How about binary classification? ☺

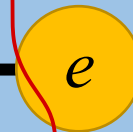
$0-1$]

Softmax

0.88

y'_1

20



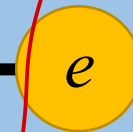
y_1

3

0.12

y'_2

2.7



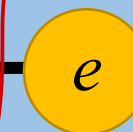
y_2

1

≈ 0

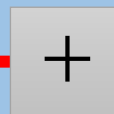
y'_3

0.05



y_3

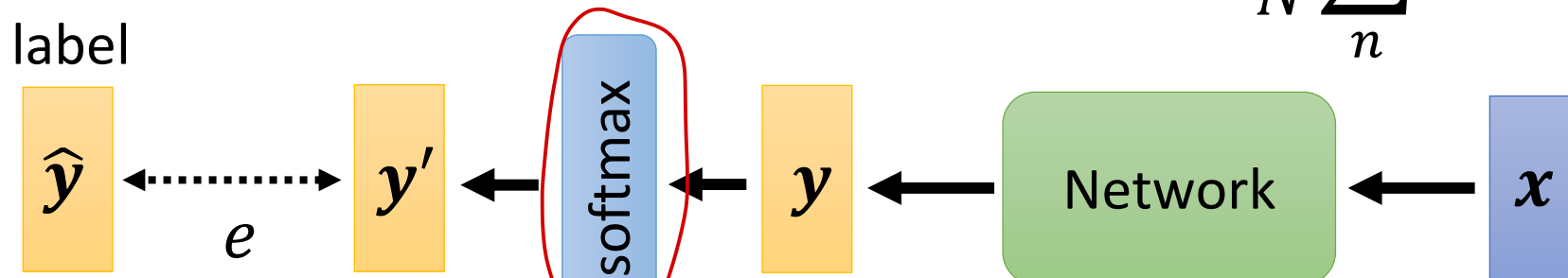
-3



logit

Loss of Classification

$$L = \frac{1}{N} \sum_n e_n$$



Mean Square Error (MSE)

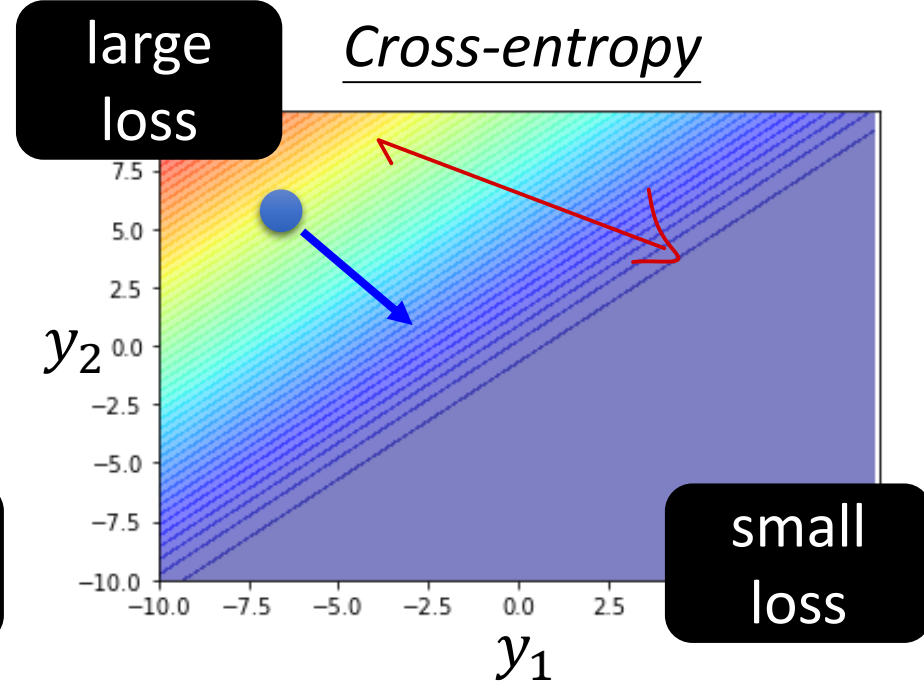
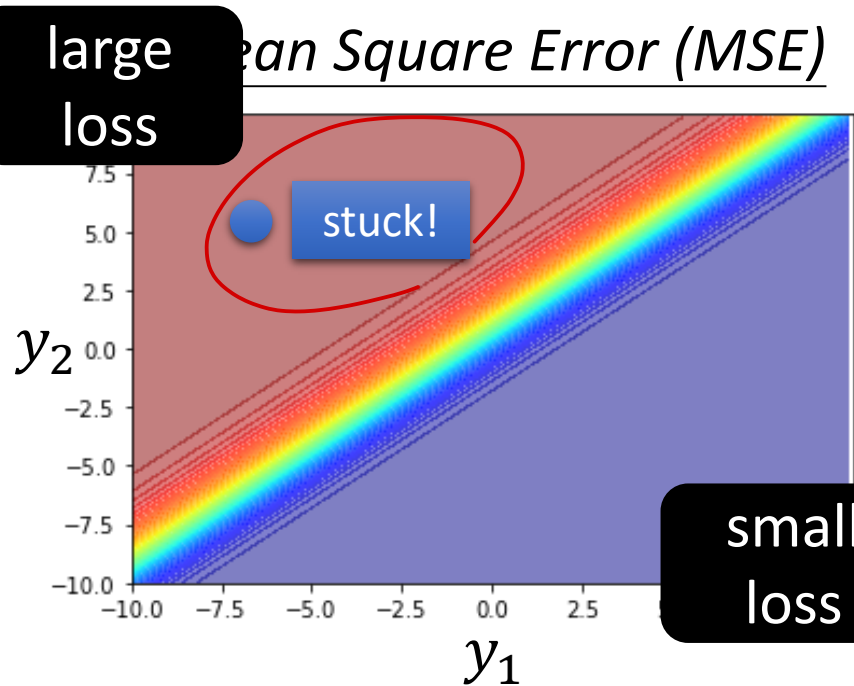
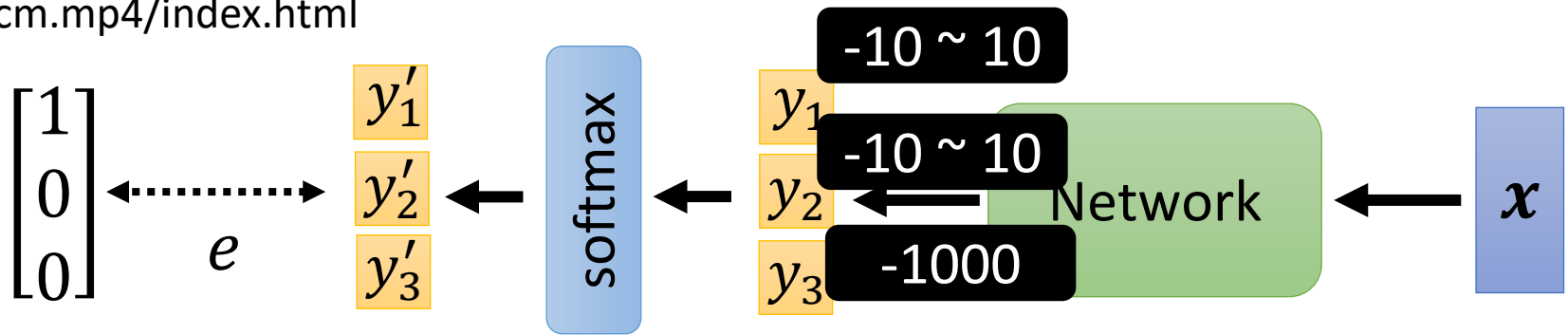
$$e = \sum_i (\hat{y}_i - y'_i)^2$$

Cross-entropy

$$e = - \sum_i \hat{y}_i \ln y'_i$$



Minimizing cross-entropy is equivalent to **maximizing likelihood**.



Changing the loss function can change the difficulty of optimization.