

1. Water enters a tube at 27°C with a **flow rate of 450 kg/h.** The heat transfer from the tube wall to the fluid is given as q_s (W/m) = ax , where the **coefficient a is 20 W/m^2** and x (m) is the axial distance from the tube entrance.

1. (a) Beginning with a properly defined differential control volume in the tube, derive an expression for the temperature distribution $T_m(x)$ of the water.

$$q_{\text{prime}} := a \cdot x$$

$$q_{\text{prime}} := a \cdot x \quad (1)$$

$$\dot{m} := 450$$

$$\dot{m} := 450 \quad (2)$$

$$T_{mi} := 27$$

$$T_{mi} := 27 \quad (3)$$

$$\# \text{Energy in} + = \text{Energy out} -$$

$$\dot{m} \cdot C_p \cdot T_m = a \cdot x \, dx + \dot{m} \cdot C_p \cdot T_m + \dot{m} \cdot C_p \cdot dT_m$$

$$0 \cdot C_p \cdot T_m = a \, dx \, x + 450 \, C_p \, T_m + 450 \, C_p \, dT_m \quad (4)$$

$$0 = a \cdot x \, dx + \dot{m} \cdot C_p \cdot dT_m$$

$$0 = a \, dx \, x + 450 \, C_p \, dT_m \quad (5)$$

$$a \cdot x \, dx = \dot{m} \cdot C_p \cdot dT_m$$

$$a \, x \, dx = 450 \, C_p \, dT_m \quad (6)$$

$$\int_0^x a \cdot x \, dx \int_{T_{mi}}^{T_{mf}} T_m \, dx$$

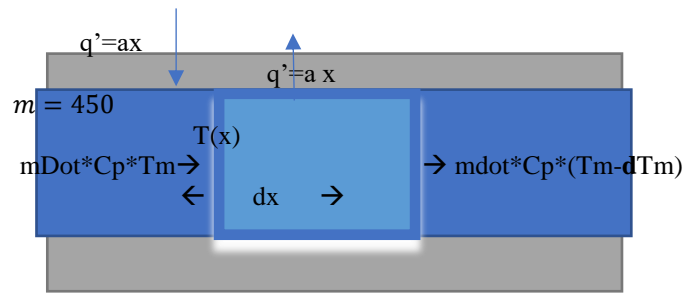
$$\frac{1}{900} \frac{a x^2}{C_p} + C = T_m(x) \quad (7)$$

$$\frac{1}{900} \frac{a x^2}{C_p} + 27 = T_m(0)$$

$$\frac{1}{900} \frac{a x^2}{C_p} + 27 = T_m(0) \quad (8)$$

$$\#a$$

$$\frac{1}{2 \cdot \dot{m} \cdot C_p} \frac{a x^2}{C_p} + 27$$



- (b) What is the mean outlet temperature of the water for a heated section of 30 m long?

$$x := 30$$

$$x := 30 \quad (10)$$

$$C_p := 4181$$

$$C_p := 4181 \quad (11)$$

$$a := 20$$

$$a := 20 \quad (12)$$

$$\dot{m} := \frac{\dot{m}}{3600}$$

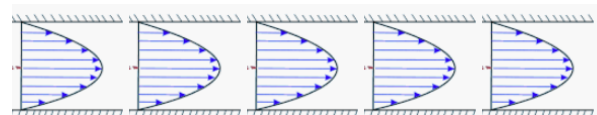
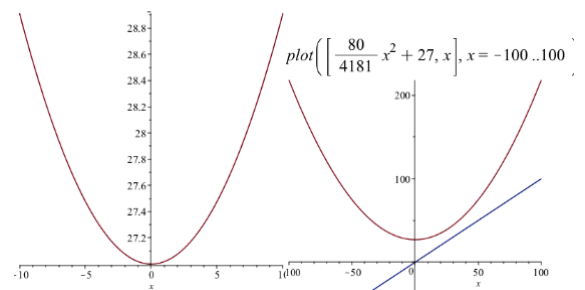
$$\dot{m} := \frac{1}{8} \quad (13)$$

$$\text{evalf}\left(\frac{1}{2 \cdot \dot{m}} \frac{a x^2}{C_p} + 27\right)$$

$$44.22076058 \quad (14)$$

44.22076058 Degrees C

- (c) Sketch the mean fluid temperature, $T_m(x)$, and the tube wall temperature, $T_s(x)$, as a function of distance along the tube for fully developed and developing flow conditions.



(d) What value of a uniform wall heat flux, q'' (instead of $q' = ax$), would provide the same fluid ss outlet temperature as that determined in part (b)? For this type of heating, repeat part (c).

$$q_s[dubPrime] := \frac{\left(\frac{\dot{m}}{3600} \cdot C_p \cdot (44.22076058 - 27) \right)}{\pi \cdot D \cdot 30}$$

$$q_{s,dubPrime} := \frac{95.49296585}{D}$$

$$q_s'' = 95.4929/D \text{ KL/m}^2$$

2. SAE 30 oil ($k = 0.15 \text{ W/m-K}$) is heated by flowing through a circular tube of diameter $D = 50 \text{ mm}$ and length $L = 25 \text{ m}$ and whose surface is maintained at 150°C . If the flow rate and inlet temperature of the oil are 0.5 kg/s and 20°C , what is the outlet temperature $T_{m,o}$? What is the total heat transfer rate q for the tube?

$$d := \text{evalf}\left(\frac{50}{1000}\right) \quad d := 0.05000000000 \quad (1)$$

$$L := 25 \quad L := 25 \quad (2)$$

$$\dot{m} := 0.5 \quad \dot{m} := 0.5 \quad (3)$$

$$k = 0.15 \text{ W/m-K} \quad \frac{69}{500} = 0.15 \quad (4)$$

$$T[s] := 150 \quad T_s := 150 \quad (5)$$

$$T[m] := 20 \quad T_m := 20 \quad (6)$$

$$T_m := \frac{T[m] + T[s]}{2} + 273 \quad T_m := 358 \quad (7)$$

$$\# @350 \text{ K, find properties for the oil} \quad \rho := 852 \quad \rho := 852 \quad (8)$$

$$C_p := 2130 \quad C_p := 2130 \quad (9)$$

$$\text{nu} := 37 \quad \nu := 37 \quad (10)$$

$$\mu := 0.032 \quad \mu := 0.032 \quad (11)$$

$$k := 138 \cdot 10^{-3} \quad k := \frac{69}{500} \quad (12)$$

$$Pr := 490 \quad Pr := 490 \quad (13)$$

$$\text{Ren}[p] := \text{evalf}\left(\frac{4 \cdot \dot{m}}{\pi \cdot d \cdot \mu}\right) \quad \text{Ren}_p := 397.8873578 \quad (14)$$

$$x[s] := 0.05 \cdot d \cdot \text{Ren}[p] \cdot Pr \quad x_s := 487.4120133 \quad (15)$$

$$0.05 \cdot d \cdot \text{Ren}[p] \quad 0.9947183945 \quad (16)$$

$$hBar := 2131 \quad hBar := 2131 \quad (17)$$

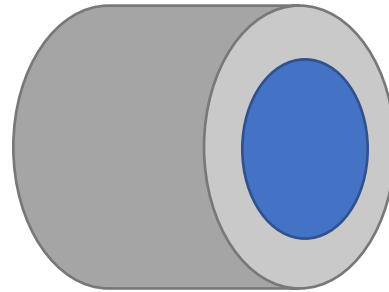
$$T[mo] := T[s] - (T[s] - T[m]) \cdot \exp\left(-\frac{\pi \cdot d \cdot L}{\dot{m} \cdot C_p} hBar\right) \quad T_{mo} := 149.9497193 \quad (18)$$

$$Nus := 3.657 + \frac{\left(0.0668 \cdot \left(\frac{d}{L}\right) \cdot \text{Ren}[p] \cdot Pr\right)}{\left(1 + 0.04 \cdot \left(\left(\frac{d}{L}\right) \cdot \text{Ren}[p] \cdot Pr\right)^{\frac{2}{3}}\right)} \quad Nus := 11.96572707 \quad (19)$$

$$K[f] := 0.138 \quad K_f := 0.138 \quad (20)$$

$$h := \frac{Nus \cdot K[f]}{d} \quad h := 33.02540672 \quad (21)$$

$$h := 33.02540672 \text{ W/m}^2\text{K}$$



#Find the total Heat Transfer

$$T[mo] := 34.88 \quad T_{mo} := 34.88 \quad (22)$$

$$q := \dot{m} \cdot C_p \cdot (T[mo] - T[m]) \quad q := 15847.200 \quad (23)$$

$$15847.200 \text{ W}$$

3. To cool a summer home without using a vapor-compression refrigeration cycle, air is routed through a plastic pipe ($k = 0.15 \text{ W/m}\cdot\text{K}$, $D_i = 0.15 \text{ m}$, $D_o = 0.17 \text{ m}$) that is submerged in an adjoining body of water. The water temperature is nominally at $T_{\infty} = 17^\circ\text{C}$, and a convection coefficient of $h_o = 1500 \text{ W/m}^2\cdot\text{K}$ is maintained at the outer surface of the pipe. If air from the home enters the pipe at a temperature of $T_{m,i} = 29^\circ\text{C}$ and a volumetric flow rate of $\dot{V}_i = 0.025 \text{ m}^3/\text{s}$, what pipe length is needed to provide a discharge temperature of $T_{m,o} = 21^\circ\text{C}$?

#prob 3

$$D_i := 0.15$$

$$D_i := 0.15 \quad (1)$$

$$D_o := 1.7$$

$$D_o := 1.7 \quad (2)$$

$$T_{m,i} := 29$$

$$T_{m,i} := 29 \quad (3)$$

$$\dot{V}_i := 0.025 \frac{\text{m}^3}{\text{s}}$$

$$\dot{V}_i := 0.025 \quad (4)$$

$$h := 1500$$

$$h := 1500 \quad (5)$$

$$T[\infty] := 17$$

$$T_{\infty} := 17 \quad (6)$$

$$T_{m,o} := 21$$

$$T_{m,o} := 21 \quad (7)$$

$$k := 0.15$$

$$k := 0.15 \quad (8)$$

#using page 730

$$\rho := 1.177$$

$$\rho := 1.177 \quad (9)$$

$$C_p := 1007$$

$$C_p := 1007 \quad (10)$$

$$\mu := 1.857 \cdot 10^{-5}$$

$$\mu := 0.00001857000000 \quad (11)$$

$$\nu := 1.578$$

$$\nu := 1.578 \quad (12)$$

$$K := 0.02623$$

$$K := 0.02623 \quad (13)$$

$$\alpha := 2.213$$

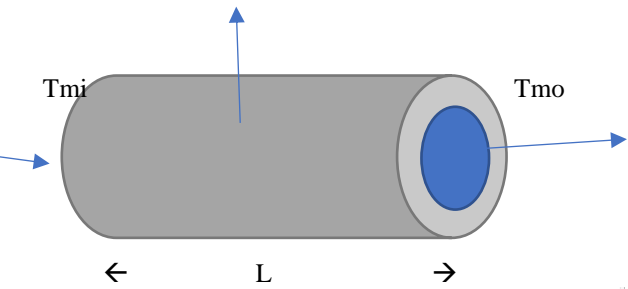
$$\alpha := 2.213 \quad (14)$$

$$Pr := 0.713$$

$$Pr := 0.713 \quad (15)$$

$$\dot{m} := \rho \cdot \dot{V}_i$$

$$\dot{m} := 0.029425 \quad (16)$$



$$Re_n[d] := \frac{4 \cdot \dot{m} \cdot \rho}{\pi \cdot D_i \cdot \mu} \quad Re_n[d] := 13450.03540 \quad (17)$$

$$R[tot] := \frac{1}{h \cdot \pi \cdot A \cdot L} + \frac{\ln\left(\frac{D_o}{D_i}\right)}{2 \cdot \pi \cdot L \cdot K} + \frac{1}{h_o \cdot \pi \cdot D_o \cdot L} \quad (18)$$

$$R_{tot} := \frac{1}{1500 \pi A L} + \frac{14.73077134}{L} + \frac{0.1872411095}{h_o L}$$

$$hi := \frac{K}{D_i} \cdot 0.073 \cdot Re_n[d]^{\frac{4}{5}} \cdot Pr^{0.3} \quad hi := 23.17050464 \quad (19)$$

$$(U_{as})^{-1} = \frac{1}{h \cdot \pi \cdot A \cdot L} + \frac{\ln\left(\frac{D_o}{D_i}\right)}{2 \cdot \pi \cdot L \cdot K} + \frac{1}{h \cdot \pi \cdot D_o \cdot L} \quad (20)$$

$$\frac{1}{U_{as}} = 2.174 L$$

$$\text{solve}\left(\frac{T[\infty] - T_{m,o}}{T[\infty] - T_{m,i}} = \frac{1}{3} \cdot \exp\left(-\frac{2.174 L}{0.0289 \cdot 1007}\right), L\right) \quad L := 14.73 \quad (21)$$

14.73 m

4. Air at $4 \times 10^{-4} \text{ kg/s}$ and 27°C enters a triangular duct that is **20 mm** on a side and **2 m long**. The duct surface is maintained at 100°C . Assuming fully developed flow throughout the duct, determine the air **outlet temperature**.

#prob4

$$T_i := 27$$

$$T_i := 27$$

(1)

$$T_{\text{mean}} := \frac{(27 + 100)}{2}$$

$$T_{\text{mean}} := \frac{127}{2}$$

(2)

$$k := 0.02833$$

$$k := 0.02833$$

(3)

$$\text{nu} := 1.93 \cdot 10^{-5}$$

$$\nu := 0.00001930000000$$

(4)

$$\text{Pr} := 0.712$$

$$\text{Pr} := 0.712$$

(5)

$$\rho := 1.05$$

$$\rho := 1.05$$

(6)

$$D_i := \text{evalf}\left(\frac{\left(4 \cdot \frac{\sqrt{3}}{4} (20 \cdot 10^{-3})^2\right)}{3 \cdot 20 \cdot 10^{-3}}\right)$$

$$D_i := 0.01154700539$$

(7)

$$V := 2.2$$

$$V := 2.2$$

(8)

$$\text{Ren} := \frac{V \cdot D_i}{\text{nu}} \# \text{Laminor}$$

$$\text{Ren} := 1316.238956$$

(9)

$$\dot{m} := \text{evalf}\left(1.05 \cdot \frac{\sqrt{3}}{4} (20 \cdot 10^{-3})^2 \cdot \text{nu}\right)$$

$$\dot{m} := 3.510000962 \cdot 10^{-9}$$

(10)

$$\text{Nus} := 0.664 \cdot \text{Ren}^{\frac{1}{2}} \cdot \text{Pr}^{\frac{1}{3}}$$

$$\text{Nus} := 21.51107497$$

(11)

$$\text{solve}\left(\text{Nus} = \frac{h \cdot \rho}{k}, h\right)$$

$$0.5803892895$$

(12)

$$\text{solve}(Q := \dot{m} \cdot C_p \cdot (T_o - T_i), T_o)$$

$$Q := 462$$

(13)

$$T_o := 1175.11$$

$$T_o := 1175.11$$

(14)

1175.11 degrees C

