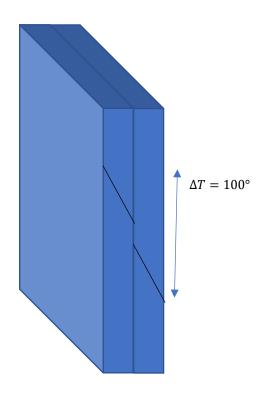
1) Two stainless steel plates 10 mm thick are subjected to a contact pressure of 1 atm under vacuum conditions for which there is an overall temperature **drop of 100**°C across the plates. What is the **heat flux through the plates**? What is the **temperature drop** across the contact plane? Hint: Use the contact conductance value in Table 2.1.

Stainless steel/stainless steel (evacuated interstices)

$$200 - 1,100$$



$$R_{t_{\text{equiv}}} = \frac{L}{kA} + \frac{1}{h_c A} + \frac{L}{kA}$$

x R1 Rconect R2

$$k := 13.8$$

$$k \coloneqq 13.8 \tag{1}$$

h[steelEvac] := 200

$$h_{steelEvac} := 200 \tag{2}$$

$$L := .01$$

$$L := 0.01 \tag{3}$$

$$R[contact] := \frac{1}{h[steelEvac]}$$

$$R_{contact} := \frac{1}{200} \tag{4}$$

$$R[s] := \frac{L}{k}$$

$$R_{s} := 0.0007246376812 \tag{5}$$

$$R[total] := 2 \cdot R[s] + R[contact]$$

$$R_{total} := 0.006449275362$$
 (6)

DeltaT := 100

$$DeltaT := 100 \tag{7}$$

$$R_{total} := 0.002242424242$$
 (8)

$$q := \frac{DeltaT}{R[total]}$$

$$q := 15505.61798$$
 (9)

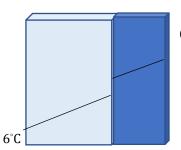
$$solve\left(q = \frac{T}{R[contact]}, T\right)$$

$$77.52808990$$
(10)

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2) A stainless steel (AISI 304) tube used to transport a chilled pharmaceutical has an inner diameter of 36 mm and a wall thickness of 2 mm. The pharmaceutical and ambient air are at temperatures of 6°C and 23°C, respectively, while the corresponding inner and outer convection coefficients are 400 W/m²-K and 6 W/m²-K, respectively.

(a) What is the heat gain per unit length [W/m]?



Outside 23°C



$$h_{inner} := 400 \tag{1}$$

$$h[outter] := 6$$

$$outter := 6 \tag{2}$$

$$r[outter] := \frac{.036}{2} + 0.002$$

$$r_{outter} := 0.020000000000$$

$$r[inner] := \frac{.036}{2}$$

$$r_{outter} := 0.020000000000$$
 (3)

$$r[inner] := \frac{.036}{2}$$

$$r_{inner} := 0.01800000000$$
 (4)

$$h[\mathit{cil}] := 13.8 \;\; \#\mathit{back} \; \mathit{of} \; \mathit{the} \; \mathit{book}$$

$$h_{cil} := 13.8$$
 (5)

(6)

(8)

$$\begin{split} R[\mathit{contact}] &:= \frac{\left(\ln\left(\frac{r[\mathit{outter}]}{r[\mathit{inner}]}\right)\right)}{(2 \cdot \mathrm{Pi} \cdot h[\mathit{cil}])} \\ R_{\mathit{contact}} &:= 0.001215119338 \end{split}$$

$$R_{contact} := 0.001215119338$$

$$R[pharm] := evalf\left(\frac{1}{h[inner] \cdot r[inner] \cdot 2 \cdot Pi}\right)$$

$$R_{abane} := 0.02210485320 \tag{7}$$

$$R[pharm] := evalf\left(\frac{1}{h[inner] \cdot r[inner] \cdot 2 \cdot Pi}\right)$$

$$R_{pharm} := 0.02210485320 \tag{7}$$

$$R[steel] := evalf\left(\frac{1}{h[outter] \cdot r[outter] \cdot 2 \cdot Pi}\right)$$

$$R_{steel} := 1.326291192 \tag{8}$$

$$R[total] := evalf(R[pharm] + R[contact] + R[steel])$$

$$R_{total} := 1.349611165$$
 (9)

$$Delta_T := 23 - 6$$

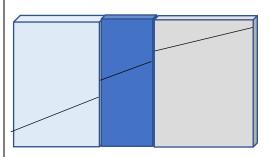
$$Delta_T := 17$$
(10)

$$q[prime] := \frac{Delta_T}{R[total]}$$

$$q_{prime} := 12.59622063$$
 (11)

18mm

(b) What is the heat gain per unit length if a 10 mm thick layer of calcium silicate insulation ($k_{ins} = 0.05 \text{ W/m-K}$) is applied to the outside of the tube?



$$R[contactSC] := \frac{\left(\ln\left(\frac{\frac{0.036}{2} + 0.012}{\frac{0.036}{2} + 0.01}\right)\right)}{(2 \cdot \text{Pi} \cdot 0.05)}$$

$$R_{contactSC} := 0.2196111294$$
 (9)

$$R[calcium] := \frac{1}{2 \cdot \text{Pi} \cdot (0.0180 + 0.02) \cdot 6}$$

$$R_{calcium} := 0.6980479960$$
 (10)

$$R[total] := evalf(R[pharm] + R[contact] + R[steel] + R[contactSC] + R[calcium])$$

$$R_{total} := 2.267270290$$
 (11)

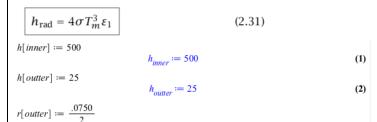
$$Delta_T := 23 - 6$$

$$Delta_T := 17 \tag{12}$$

$$q[prime] := \frac{Delta_T}{R[total]}$$

$$q_{min} := 7.498003249$$
(13)

3) Steam at a temperature of 250°C flows through a steel pipe (AISI 1010) of 60 mm inner diameter and 75 mm outer diameter. The convection coefficient between the steam and the inner surface of the pipe is 500 W/m²-K, while that between the outer surface of the pipe and the surroundings is 25 W/m²-K. The pipe emissivity is 0.8, and the temperature of the air and surroundings is 20°C. What is the heat loss per unit length of pipe?



$$r_{outter} := 0.03750000000$$
 (3)

$$r[inner] := .030$$
 $r_{inner} := 0.030$ (4)

$$h[cil] := 64$$
 #back of the book
$$h_{cil} := 64$$
(5)

$$R[contactSeS] := \frac{\left(\ln\left(\frac{r[outter]}{r[inner]}\right)\right)}{(2 \cdot \text{Pi} \cdot h[cil])}$$

$$R_{contactSeS} := 0.0005549124875$$
(6)

$$R[steam] := evalf\left(\frac{1}{h[inner] \cdot r[inner] \cdot 2 \cdot Pi}\right)$$

$$R_{steam} := 0.01061032954$$
(7)

$$R[steel] := evalf \left(\frac{1}{h[outter] \cdot r[outter] \cdot 2 \cdot Pi} \right)$$

$$R_{eval} := 0.1697652726$$
(8)

epsilon := 0.8
$$\epsilon := 0.8 \tag{9}$$

$$T := 135 \# 20 + 273$$

$$T := 135 \tag{10}$$

$$\sigma := 5.67000000010^{-8} \tag{11}$$

 $sigma := 5.67 \cdot 10^{-8}$

$$h[rad] := 4 \cdot \text{sigma} \cdot T^3 \cdot \text{epsilon}$$

$$h_{rad} := 0.4464104400$$
(12)

$$R[rad] := \frac{1}{2 \cdot \text{Pi} \cdot h[rad]}$$

$$R_{end} := 0.3565215524$$
(13)

$$R[total] := evalf\Big(R[steam] + R[contactSeS] + \Big(R[steel]^{-1} + R[rad]^{-1}\Big)^{-1}\Big)$$

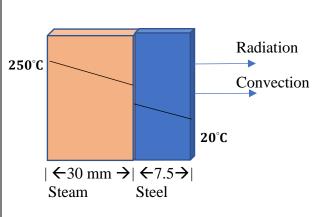
$$R_{total} := 0.1261690301$$
(14)

$$Delta_T := 250 - 20$$

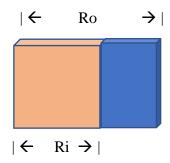
$$Delta_T := 230$$
(15)

$$q[prime] := \frac{Delta_T}{R[total]}$$

$$q_{prime} := 1822.951320$$
 (16)



4) A **spherical** shell of inner and outer radii of r_i and r_o , respectively, is filled with a heat-generating material that provides for a uniform **volumetric generation rate** (W/m³) of \mathbf{q} . The outer surface of the shell is exposed to a fluid having a temperature \mathbf{T}_{∞} and a convection coefficient \mathbf{h} . Obtain an expression for the **steady-state temperature** distribution $\mathbf{T}(\mathbf{r})$ in the shell, expressing you results in terms of \mathbf{r}_i , \mathbf{r}_o , \mathbf{q} , \mathbf{h} , \mathbf{T}_{∞} , and the thermal **conductivity** \mathbf{k} of the shell material.



With the help for Mcklane G.

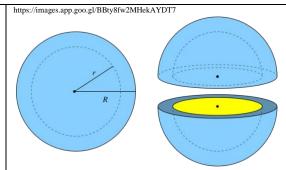
$$\frac{K}{r^2} \frac{d}{dr} \left(r^2 \frac{dt}{dr} \right) = 0$$

$$\frac{d}{dr} \left(r^2 \frac{dt}{dr} \right) = 0$$

$$\int \frac{d}{dr} \left(r^2 \frac{dt}{dr} \right) = 0$$

$$r^2 \frac{dT}{dr} + C_1 = 0$$

$$\frac{dt}{dr} = -\frac{C_1}{r^2}$$
Integrate:
$$T(r) = \frac{C_1}{r} + C_2$$



1st Apply Boundary conditions for q

$$-k\frac{dT}{dr}|_{r=r_i} = q = \frac{\dot{q}V}{A}$$
$$-k\left(-\frac{c_i}{r_i}\right) = \dot{q}\frac{V}{A}$$
$$C_1 = \dot{q}V\frac{r_i^2}{kA} = \dot{q}\frac{r_i^3}{Ak}$$

2nd Convective

$$\begin{aligned} -k \frac{dT}{dr}|_{r=r_0} &= h(T_o - T_{oo}) \\ -k \left(-\frac{qr^2}{3kr_o^2} \right) &= h \left(\frac{qr^2}{3kr_o^2} + C_2 - T_{oo} \right) \\ \frac{\dot{q}r^2}{3r_o^2} &= h \frac{r^2}{3kr_o^2} + h C_2 - h T_{oo} \end{aligned}$$

$$T(r) := \frac{\dot{q}r_i^3}{3k} \left[\frac{1}{r} - \frac{1}{r_o} \right] + \frac{\dot{q}r_i^3}{3hr_o^2} + T_{oo}$$

5. The exposed surface (x = 0) of a plane wall of thermal conductivity k is subjected to microwave radiation that causes volumetric heating to vary as

$$\dot{q}(x) = \dot{q}_o \left(1 - \frac{x}{L} \right) \tag{1}$$

where \mathbf{q}^{\cdot}_{0} (W/m³) is a constant. The boundary at $\mathbf{x} = \mathbf{L}$ is perfectly insulated, while the exposed surface is maintained at a constant temperature \mathbf{T}_{0} . Determine the temperature distribution $\mathbf{T}(\mathbf{x})$ in terms of \mathbf{x} , \mathbf{L} , \mathbf{k} , \mathbf{q}^{\cdot}_{0} , and \mathbf{T}_{0} .

We the help of Braedin B.

$$\frac{d^2T}{dx^2} + \frac{q(x)}{k} = 0$$

$$\frac{d^2T}{dx^2} + \frac{q\left(1 - \frac{x}{L}\right)}{k} = 0$$

$$\frac{dT}{dx} + \frac{q_o x}{k} - \frac{q_o x^2}{6 k L} = C_1 x + C_2$$

If x = 0 and T = To

$$T(0) + \frac{q_0(0)^2}{2k} - \frac{q_0(0)^3}{6kL} = C_1 + C_2$$

$$C_2 = T_0$$

If x = L dt/dx = 0

$$C_1 = q_o x^2$$

$$T(x) := T_o + \frac{q_o L x}{2k} (1 - \frac{x}{L} + \frac{1}{3} * \frac{x^2}{L^2})$$

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6) A long cylindrical rod of diameter $200 \ mm$ with thermal conductivity of $0.5 \ W/m$ -K experiences uniform volumetric heat generation of $24,000 \ W/m^3$. The rod is encapsulated by a circular sleeve having an outer diameter of $400 \ mm$ and a thermal conductivity of $4 \ W/m$ -K. The outer surface of the sleeve is exposed to a cross flow of air at $27^{\circ}C$ with a convection coefficient of $25 \ W/m^2$ -K.

(a) Find the temperature at the interface between the rod and sleeve and on the outer surface.

$$k[s] := 4$$

$$k_s := 4 \tag{1}$$

$$r[s] := 0.2$$

$$r_s := 0.2 \tag{2}$$

$$r[r] := 0.1$$

$$r_r := 0.1 \tag{3}$$

$$\underline{R}[cond] := \frac{\ln\left(\frac{r[s]}{r[r]}\right)}{2 \cdot \text{Pi} \cdot k[s]}$$

$$R_{cond} := 0.02757945001$$
(4)

$$h := 25$$

$$h := 25 \tag{5}$$

$$A[outSerf] := 2 \cdot Pi \cdot r[s]$$

$$A_{outSerf} := 1.256637062$$
(6)

$$R[convect] := \frac{1}{h \cdot A[outSerf]}$$

$$R_{convect} := 0.03183098860$$
 (7)

$$R[pimeTot] := R[convect] + R[cond]$$

 $R_{pimeTot} := 0.05941043861$ (8)

$$R_{pimeTot} := \frac{0.05941043861}{L} \tag{9}$$

$$q := 24000$$

$$q := 24000$$
 (10)

$$T[infn] := 27$$
 $T_{infn} := 27$ (11)

$$solve\left(q \cdot \text{Pi} \cdot r[r]^2 = \frac{T[x] - T[infn]}{R[pimeTot]}, T[x]\right)$$

$$71.79441540 \tag{12}$$

(b) What is the temperature at the center of the rod?

$$k[s] := 4$$

$$k_s := 4 \tag{1}$$

$$r[s] := 0.2$$
 $r_s := 0.2$ (2)

$$r[r] := 0.1$$
 (3)

$$R[cond] := \frac{\ln\left(\frac{r[s]}{r[r]}\right)}{2 \cdot \text{Pi} \cdot k[s]}$$

$$R_{cond} := 0.02757945001 \tag{4}$$

$$h := 25$$

$$h := 25 \tag{5}$$

$$A[outSerf] := 2 \cdot \text{Pi} \cdot r[s]$$

$$A_{outSerf} := 1.256637062$$
(6)

$$R[convect] := \frac{1}{h \cdot A[outSerf]}$$

$$R_{convect} := 0.03183098860$$
 (7)

$$R[pimeTot] := R[convect] + R[cond]$$

 $R_{pimeTot} := 0.05941043861$ (8)

$$R_{pimeTot} := \frac{0.05941043861}{L} \tag{9}$$

$$q := 24000$$

$$q := 24000 \tag{10}$$

$$T[infn] := 27$$

$$T_{infn} := 27$$
(11)

$$solve\left(q \cdot \operatorname{Pi} \cdot r[s]^{2} = \frac{T[x] - T[\inf n]}{R[\operatorname{pimeTot}]}, T[x]\right)$$

$$206.1776616 \tag{12}$$

7) Radioactive waste (k_{rw} = 20 W/m-K) is stored in a spherical, stainless steel (k_{ss} = 15 W/m-K) container of inner and outer radii of r_i = 0.5 m and r_o = 0.6 m, respectively. Heat is generated volumetrically within the waste at a uniform rate of q = 10^5 W/m³, and the outer surface of the container is exposed to a water flow for which h = 1000 W/m²-K and T_{∞} = 25° C.

(a) Evaluate the steady-state outer surface temperature of the container, $T_{s,o}$.

$$r[s] := 0.6$$
 $r_s := 0.6$ (1)

$$r[r] := 0.5$$
 $r_r := 0.5$ (2)

$$h := 1000$$

$$h := 1000 \tag{3}$$

$$R[outSerf] := \frac{1}{4 \cdot \text{Pi} \cdot r[s]^2 \cdot h}$$

$$R_{outSerf} := 0.0002210485320$$
 (4)

$$q[dot] := 10^5$$
 $q_{dot} := 100000$ (5)

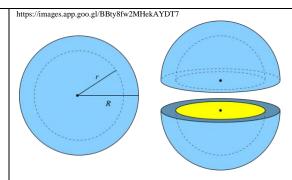
$$T[infin] := 25$$

$$T_{infin} := 25$$
(6)

$$solve\left(q[dot] = \frac{T[ss] - T[infin]}{R[outSerf]}, T[ss]\right)$$

$$47.10485320 \tag{7}$$

(c) Obtain an expression for the temperature distribution, T(r) in the radioactive waste. Evaluate the temperature at r=0.



(b) Evaluate the steady-state inner surface temperature of the container, $T_{s,i}$.