

## 1 Attribute Type

Answer: interval

## 2 Missing values

Answer:

- Eliminate data objects with missing values
- Estimate missing values
- Ignore missing values during data analysis

## 3 Jaccard coefficient

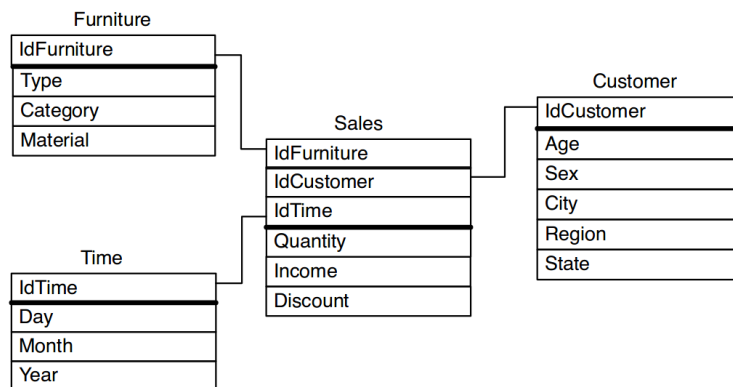
Answer: 0.5

## 4 CityBlock distance

Answer: 5

## 5 Modeling

Answer:



## 6 OLAP

Answer:

- {Month, ItemName, City}: Yes, after roll-up from ItemName to Brand

- {Month, Brand, Country}: No, cannot retrieve city in the query
- {Year, Brand, City}: No, cannot retrieve month and city in the query
- {ItemName, City} where year = 2016: No, cannot retrieve the specified month in the query

## 7 Apriori Algorithm

Answer:

1) Applying Apriori

Pass(k)	Candidate k-itemsets and their support	Frequent k-itemsets
k=1	{H}(4), {B}(2), {K}(2), {C}(3), {I}(4)	{H}, {B}, {K}, {C}, {I}
k=2	{H, B}(2), {H, K}(1), {H, C}(2), {H, I}(2), {B, K}(1), {B, C}(0), {B, I}(0), {K, C}(0), {K, I}(1), {C, I}(3)	{H, B}, {H, C}, {H, I}, {C, I}
k=3	{H, C, I}(2)	{H, C, I}
k=4	{}	

2)

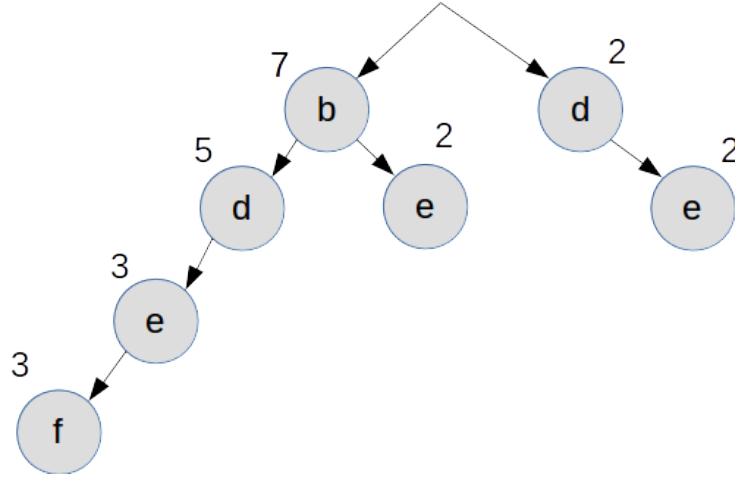
- {H}  $\rightarrow$  {C, I} (confidence=2/4=0.5)
- {C}  $\rightarrow$  {H, I} (confidence=2/3=0.66)
- {I}  $\rightarrow$  {H, C} (confidence=2/4=0.5)
- {H, C}  $\rightarrow$  {I} (confidence=2/2=1)
- {H, I}  $\rightarrow$  {C} (confidence=2/2=1)
- {C, I}  $\rightarrow$  {H} (confidence=2/3=0.66)

Therefore, the four qualified association rules are {C}  $\rightarrow$  {H, I}, {H, C}  $\rightarrow$  {I}, {H, I}  $\rightarrow$  {C}, and {C, I}  $\rightarrow$  {H}.

## 8 FP-growth

Answer:

1)



2)

Item	Conditional sub-database	Conditional FP-tree	Frequent Item sets
f	$\{\{b,d,e\}:3\}$	$\langle b : 3, d : 3, e : 3 \rangle$	$\{f\}:3, \{b,f\}:3, \{d,f\}:3, \{e,f\}:3, \{b,d,f\}:3, \{b,e,f\}:3, \{d,e,f\}:3, \{b,d,e,f\}:3$
e	$\{\{b,d\}:3, \{b\}:2, \{d\}:2\}$	$\langle b : 5, d : 3 \rangle, \langle d : 2 \rangle$	$\{e\}:7, \{d,e\}:5, \{b,e\}:5$
ed	$\{\{b\}:3\}$	$b:3$	$\{b,d,e\}:3$
(eb	empty	empty)	
d	$\{\{b\}:5\}$	$b:5$	$\{d\}:7, \{b,d\}:5$
b	empty	empty	$\{b\}:7$

## 9 K-means clustering

Step 1a: compute squared Euclidean distances between data points and mean vectors

	$m_1 = (2, 0)$	$m_2 = (3, 4)$
$x^{(1)} = (0, 3)$	$(0-2)^2 + (3-0)^2 = 13$	$(0-3)^2 + (3-4)^2 = 10$
$x^{(2)} = (1, 4)$	$(1-2)^2 + (4-0)^2 = 17$	$(1-3)^2 + (4-4)^2 = 4$
$x^{(3)} = (3, 1)$	$(3-2)^2 + (1-0)^2 = 2$	$(3-3)^2 + (1-4)^2 = 9$
$x^{(4)} = (4, 2)$	$(4-2)^2 + (2-0)^2 = 8$	$(4-3)^2 + (2-4)^2 = 5$
$x^{(5)} = (5, 1)$	$(5-2)^2 + (1-0)^2 = 10$	$(5-3)^2 + (1-4)^2 = 13$

Pick the smallest in each row, which results that  $x^{(1)}$ ,  $x^{(2)}$ , and  $x^{(4)}$  belong to Cluster 2, and  $x^{(3)}$ , and  $x^{(5)}$  belong to Cluster 1

Step 1b: update mean vectors

$$m_1 = (x^{(3)} + x^{(5)})/2 = ((3, 1) + (5, 1))/2 = (4, 1)$$

$$m_2 = (x^{(1)} + x^{(2)} + x^{(4)})/3 = ((0, 3) + (1, 4) + (4, 2))/3 = (5/3, 3) \text{ or } (1.67, 3)$$

Step 2a: compute squared Euclidean distances between data points and mean vectors

	$m_1 = (4, 1)$	$m_2 = (5/3, 3)$
$x^{(1)} = (0, 3)$	$(0-4)2+(3-1)2=20$	$(0-5/3)2+(3-3)2=2+7/9$ (or 2.78)
$x^{(2)} = (1, 4)$	$(1-4)2+(4-1)2=18$	$(1-5/3)2+(4-3)2=1+4/9$ (or 1.44)
$x^{(3)} = (3, 1)$	$(3-4)2+(1-1)2=1$	$(3-5/3)2+(1-3)2=5+7/9$ (or 5.78)
$x^{(4)} = (4, 2)$	$(4-4)2+(2-1)2=1$	$(4-5/3)2+(2-3)2=6+4/9$ (or 6.44)
$x^{(5)} = (5, 1)$	$(5-4)2+(1-1)2=1$	$(5-5/3)2+(1-3)2=15+1/9$ (or 15.11)

Pick the smallest in each row, which results that  $x^{(1)}$  and  $x^{(2)}$  belong to Cluster 2, and  $x^{(3)}$ ,  $x^{(4)}$ , and  $x^{(5)}$  belong to Cluster 1

Step 2b: update mean vectors

$$m_1 = (x(3) + x(4) + x(5))/3 = ((3, 1) + (4, 2) + (5, 1))/3 = (4, 4/3) \text{ or } (4, 1.33)$$

$$m_2 = (x(1) + x(2))/2 = ((0, 3) + (1, 4))/2 = (0.5, 3.5)$$

Step 3a: compute squared Euclidean distances between data points and mean vectors

	$m_1 = (4, 4/3)$	$m_2 = (1/2, 7/2)$
$x^{(1)} = (0, 3)$	$(0-4)2+(3-4/3)2=18+7/9$ (or 18.78)	$(0-0.5)2+(3-3.5)2=0.5$
$x^{(2)} = (1, 4)$	$(1-4)2+(4-4/3)2=16+1/9$ (or 16.11)	$(1-0.5)2+(4-3.5)2=0.5$
$x^{(3)} = (3, 1)$	$(3-4)2+(1-4/3)2=1+1/9$ (or 1.11)	$(3-0.5)2+(1-3.5)2=12.5$
$x^{(4)} = (4, 2)$	$(4-4)2+(2-4/3)2=4/9$ (or 0.44)	$(4-0.5)2+(2-3.5)2=14.5$
$x^{(5)} = (5, 1)$	$(5-4)2+(1-4/3)2=1+1/9$ (or 1.11)	$(5-0.5)2+(1-3.5)2=26.5$

Pick the smallest in each row, which results that  $x^{(1)}$  and  $x^{(2)}$  belong to Cluster 2, and  $x^{(3)}$ ,  $x^{(4)}$ , and  $x^{(5)}$  belong to Cluster 1.

Since there is no change in the cluster assignment, the algorithm ends and outputs

$$m_1 = (4, 4/3) \text{ or } (4, 1.33)$$

$$m_2 = (0.5, 3.5)$$

$$\text{Cluster}(x^{(1)})=2$$

$$\text{Cluster}(x^{(2)})=2$$

$$\text{Cluster}(x^{(3)})=1$$

$$\text{Cluster}(x^{(4)})=1$$

$$\text{Cluster}(x^{(5)})=1$$

## 10 DBSCAN pros and cons

Answer:

- Data is high-dimensional
- Data has varying densities

## 11 Cross-validation

Purpose of cross validation. One of the following answers or the like is acceptable:

- Cross-validation can be used to evaluate the performance of a supervised model (e.g. a classifier or regressor)
- Cross-validation is any of various similar model validation techniques for assessing how the results of a statistical analysis will generalize to an independent data set.
- Cross-validation can be used to tune hyper-parameters in algorithms or models

Cross validation procedure. It requires the following parts in the answer

- has explained training/validation/test sets
- has correctly show K-fold rotation steps

## 12 Decision tree

Answer:

1)

$$\text{Entropy}(p) = -\frac{3}{8} \cdot \log_2 \frac{3}{8} - \frac{5}{8} \cdot \log_2 \frac{5}{8} \approx 0.9544$$

If using "NotHeavy" for root splitting,

$$\sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = \frac{5}{8} \left( -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} \right) + \frac{3}{8} \left( -\frac{1}{3} \log_2 \frac{1}{3} - \frac{2}{3} \log_2 \frac{2}{3} \right) \approx 0.9512$$

$$\text{GAIN}_{\text{NotHeavy}} = \text{Entropy}(p) - \sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = 0.0032$$

If using "Smelly" for root splitting,

$$\sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = \frac{3}{8} \left( -\frac{1}{3} \log_2 \frac{1}{3} - \frac{2}{3} \log_2 \frac{2}{3} \right) + \frac{5}{8} \left( -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} \right) \approx 0.9512$$

$$\text{GAIN}_{\text{Smelly}} = \text{Entropy}(p) - \sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = 0.0032$$

If using "Spotted" for root splitting,

$$\sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = \frac{3}{8} \left( -\frac{1}{3} \log_2 \frac{1}{3} - \frac{2}{3} \log_2 \frac{2}{3} \right) + \frac{5}{8} \left( -\frac{2}{5} \log_2 \frac{2}{5} - \frac{3}{5} \log_2 \frac{3}{5} \right) \approx 0.9512$$

$$\text{GAIN}_{\text{Spotted}} = \text{Entropy}(p) - \sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = 0.0032$$

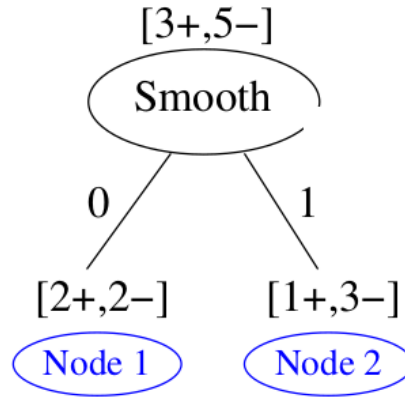
If using "Smooth" for root splitting,

$$\sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = \frac{4}{8} \left( -\frac{1}{4} \log_2 \frac{1}{4} - \frac{3}{4} \log_2 \frac{3}{4} \right) + \frac{4}{8} \left( -\frac{2}{4} \log_2 \frac{2}{4} - \frac{2}{4} \log_2 \frac{2}{4} \right) \approx 0.9056$$

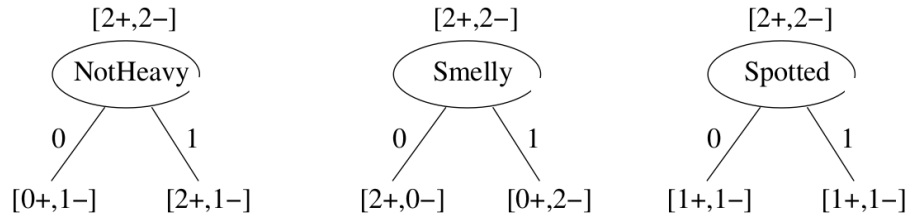
$$\text{GAIN}_{\text{Smooth}} = \text{Entropy}(p) - \sum_{i=1}^k \frac{n_i}{n} \text{Entropy}(i) = 0.0488$$

So we should use "Smooth" for the root splitting because its GAIN is the largest.

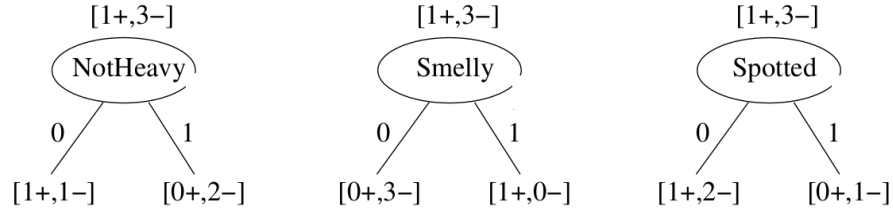
2)



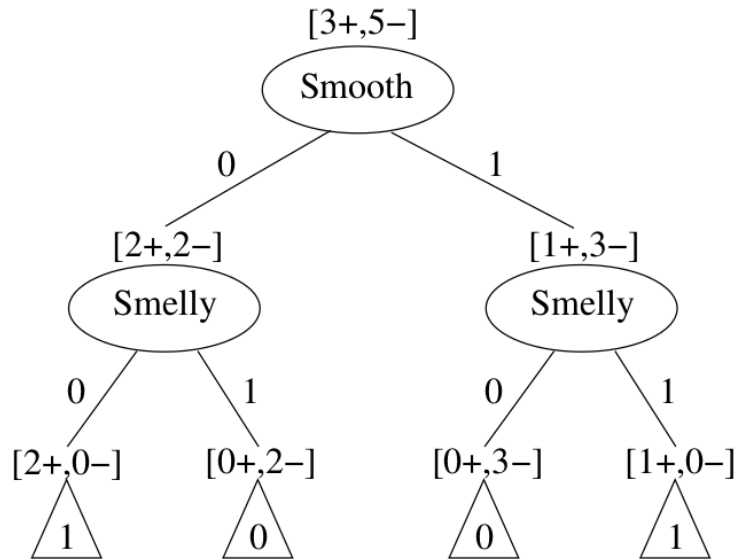
**Node 1:** Smooth = 0



**Node 2: Smooth = 1**



It can be seen that after splitting with “Smooth” and then “Smelly”, all training samples have been classified. The Entropy after the two-level decision becomes zero (i.e. giving the maximum GAIN). The GAINs using other features are smaller. Therefore the resulting decision tree is



3)

- For U: Smooth = 1, Smelly = 1  $\Rightarrow$  Edible = 1
- For V: Smooth = 1, Smelly = 1  $\Rightarrow$  Edible = 1
- For W: Smooth = 0, Smelly = 1  $\Rightarrow$  Edible = 0