The braids package: codebase

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v2.2 from 2022/10/26

1 Introduction

This is a package for drawing braid diagrams using PGF/TikZ. Its inspiration was a question and answer on the website http://tex.stackexchange.com.

2 History

- v1.0 First public release.
- v1.1 Added ability to configure the gap size, the control points, and the "nudge". Added ability to add labels to strands between crossings.
- v2 Reimplemented as TikZ library rather than a standalone package.

3 Implementation

Issue a notice that this is a depreciated version of the braids package.

- 1 \PackageWarning{braids}{%
- This package has been reimplemented as a TikZ library; if starting with a fresh document,
- 3 **}**%

\ge@addto@macro

This is an expanded version of \g@addto@macro. Namely, it adds the *expansion* of the second argument to the first.

- 4 \long\def\ge@addto@macro#1#2{%
- \begingroup
- $\label{lem:condition} $$ \toks@\exp{\toks@expandafter}\exp{\toks@expandafter}_1#2}\%$$
- 7 \xdef#1{\the\toks@}%
- 8 \endgroup}

 $(End\ definition\ for\ \ge@addto@macro.)$

\braid This is the user command. We start a group to ensure that all our assignments are local, and then call our initialisation code. The optional argument is for any keys to be set.

- 9 \newcommand{\braid}[1][]{%
- 10 \begingroup
- 11 \braid@start{#1}}

(End definition for \braid. This function is documented on page ??.)

\braid@process

This is the token swallower. This takes the next token on the braid specification and passes it to the handler command (in the macro \braid@token) which decides what to do next. (Incidentally, the code here is heavily influenced by TikZ. That's probably not very surprising.)

```
12 \def\braid@process{%
13 \afterassignment\braid@handle\let\braid@token=%
14 }
(End definition for \braid@process.)
```

\braid@process@start

This is a variant of \braid@process which is used at the start where we might have a few extra bits and pieces before the braid itself starts. Specifically, we test for the at and (name) possibilities.

```
15 \def\braid@process@start{%
16 \afterassignment\braid@handle@start\let\braid@token=%
17 }
```

 $(End\ definition\ for\ \ braid@process@start.)$

\braid@handle@start

This is the handler in use at the start. It looks for the tokens a or (which (might) signal the start of an at (coordinate) or (name). If we get anything else (modulo spaces) we decide that we've reached the end of the initialisation stuff and it is time to get started on the braid itself.

```
18 \def\braid@handle@start{%
19 \let\braid@next=\braid@handle
```

o \ifx\braid@token a

We got an a so we might have an at (coordinate)

22 \else

23 \ifx\braid@token(%)

We got an (so we have a name

```
24 \iffalse)\fi %Indentation hack!
25 \let\braid@next=\braid@assign@name
```

26 \else

27 \ifx\braid@token\@sptoken

Space; boring, redo from start

 $(End\ definition\ for\ \verb|\braid@handle@start|.)$

\braid@handle

This is the main handler for parsing the braid word. It decides what action to take depending on what the token is. We have to be a bit careful with catcodes, some packages set; and | to be active. We should probably also be careful with ^ and _.

```
34 \let\braid@semicolon=;
```

35 \let\braid@bar=|

37 \let\braid@next=\braid@process

Start by checking our catcodes to see what we should check against

- 38 \ifnum\the\catcode'\;=\active
- 39 \expandafter\let\expandafter\braid@semicolon\tikz@activesemicolon
- 40 \fi
- 41 \ifnum\the\catcode'\|=\active
- 42 \expandafter\let\expandafter\braid@bar\tikz@activebar
- 43 \f:
- 44 \ifx\braid@token\braid@semicolon

Semicolon, means that we're done reading our braid. It's time to render it.

- 45 \let\braid@next=\braid@render
- 46 \else
- 47 \ifx\braid@token^

Superscript character, the next token tells us whether it's an over-crossing or an under-crossing.

- 48 \let\braid@next=\braid@sup
- 49 \else
- 50 \ifx\braid@token_

Subscript character, the next token tells us which strands cross.

- 51 \let\braid@next=\braid@sub
- 52 \else
- 53 \ifx\braid@token-

Hyphen, this is so that we can have more than one crossing on the same level.

- 54 \braid@increase@levelfalse
- 55 \else
- 56 \ifx\braid@token1%

1: this means the "identity" crossing, so no crossing here. Increase the level, unless overriden, and add to the label.

- 57 \ifbraid@increase@level
- 58 \stepcounter{braid@level}
- 59 **\fi**
- 60 \braid@increase@leveltrue
- \ge@addto@macro\braid@label{\braid@token}%
- 62 \else
- 63 \ifx\braid@token[%

Open bracket, this means we have some more options to process.

- 64 \let\braid@next=\braid@process@options
- 65 \else
- 66 \ifx\braid@token\braid@bar

Bar, this tells us that we want a "floor" at this point.

- 67 \edef\braid@tmp{,\expandafter\the\value{braid@level}}%
- \ge@addto@macro\braid@floors\braid@tmp%
- 69 \else
- 70 \ifx\braid@token\bgroup

Begin group, which we reinterpret as begining a scope.

- 71 \braid@beginscope
- 72 \else
- 73 \ifx\braid@token\egroup

```
\braid@endscope
                         75
                              \ifx\braid@token\braid@olabel@strand
                         76
                               \let\braid@next=\braid@olabel@strand
                         77
                         78
                              \ifx\braid@token\braid@clabel@strand
                               \let\braid@next=\braid@clabel@strand
                       Otherwise, we add the token to the braid label.
                              \ge@addto@macro\braid@label{\braid@token}%
                              \fi
                              \fi
                              \fi
                              \fi
                              \fi
                              \fi
                              \fi
                              \fi
                         91
                             \fi
                              \fi
                         93
                              \braid@next%
                         95 }
                       (End definition for \braid@handle.)
 \braid@maybe@locate If we got an a token in the \braid@handle@start then it might mean we're looking
                       at at (coordinate) or it might mean that the user has decided to use a as the braid
                       parameter. So we examine the next token for a t.
                         96 \def\braid@maybe@locate{%
                             \afterassignment\braid@@maybe@locate\let\braid@token=%
                         98 }
                       (End\ definition\ for\ \verb+\braid@maybe@locate.)
\braid@@maybe@locate
                       This is where we test for t and act appropriately.
                         99 \def\braid@@maybe@locate{%
                              \let\braid@next=\braid@handle
                              \ifx\braid@token t
                               \let\braid@next=\braid@find@location
                              \fi
                              \braid@next%
                        105 }
                       (End definition for \braid@@maybe@locate.)
\braid@find@location This macro starts us looking for a coordinate.
                         106 \def\braid@find@location{%
                              \afterassignment\braid@@find@location\let\braid@token=%
                        108 }
                       (End definition for \braid@find@location.)
```

End group, which ends the scope

```
\braid@@find@location This is the test for the start of a coordinate. If we get a ( that means we've reached the
                         coordinate. A space means "carry on". Anything else is a (non-fatal) error.
                           109 \def\braid@@find@location{%
                                \let\braid@next=\braid@location@error
                                \ifx\braid@token(%)
                                 \let\braid@next=\braid@locate
                           112
                                \else
                                \ifx\braid@token\@sptoken
                           114
                                 \let\braid@next=\braid@find@location
                           115
                           116
                           117
                                \fi
                                \braid@next%
                           118
                           119 }
                         (End definition for \braid@@find@location.)
\braid@location@error This is our error message for not getting a location.
                           120 \def\braid@location@error{%
                                \PackageWarning{braids}{Could not figure out location for braid}%
                                \braid@process@start%
                           122
                           123 }
                          (End definition for \braid@location@error.)
         \braid@locate If we reached a ( when looking for a coordinate, everything up to the next ) is that
                         coordinate. Then we parse the coordinate and call the relocation macro.
                           124 \def\braid@locate#1){%
                                \tikz@scan@one@point\braid@relocate(#1)%
                           126 }
                          (End definition for \braid@locate.)
       \braid@relocate
                         This is the macro that actually does the relocation.
                           127 \def\braid@relocate#1{%
                                #1\relax
                           128
                                \advance\pgf@x by -\braid@width
                           129
                                \pgftransformshift{\pgfqpoint{\pgf@x}{\pgf@y}}
                                \braid@process@start%
                           132 }
                         (End definition for \braid@relocate.)
    \braid@assign@name
                         This macro saves our name.
                           133 \def\braid@assign@name#1){%
                                \def\braid@name{\#1}\%
                                \braid@process@start%
                           135
                          (End definition for \braid@assign@name.)
                         The intention of this macro is to allow setting of style options mid-braid. (At present,
\braid@process@options
                          this wouldn't make a lot of sense.)
                           137 \def\braid@process@options#1]{%
                                  \tikzset{#1}%
                                \braid@process%
                           139
```

140 }

(End definition for \braid@process@options.)

The next macros handle the actual braid elements. Everything has to have a subscript, but the superscript is optional and can come before or after the subscript.

```
This handles braid elements of the form a^{-1}_2.
\braid@sup
               141 \def\braid@sup#1_#2{%
                    \g@addto@macro\braid@label{_{#2}^{#1}}%
                    \braid@add@crossing{#2}{#1}%
               144 }
              (End definition for \braid@sup.)
 \braid@sub
               145 % This handles braid elements of the form \Verb+a_1+ or \Verb+a_1^{-1}+.
               146 \def\braid@sub#1{%
                    \@ifnextchar^{\braid@@sub{#1}}%
                    \label{$\{\S@addto@macro\braid@label{$\{\#1\}\}$} hraid@add@crossing{$\#1\}$}}
               149 }
              (End definition for \braid@sub.)
\braid@@sub Helper macro for \braid@sub.
               150 \def\braid@@sub#1^#2{%
                    \g@addto@macro\braid@label{_{#1}^{#2}}%
                    \braid@add@crossing{#1}{#2}%
               153 }
              (End definition for \braid@@sub.)
             Remember what 1 looks like for testing against.
  \braid@ne
               154 \def\braid@ne{1}
              (End definition for \braid@ne.)
             This is the macro which adds the crossing to the current list of strands. The strands are
```

\braid@add@crossing

stored as soft paths (see the TikZ/PGF documentation). So this selects the right strands and then extends them according to the crossing type.

155 \def\braid@add@crossing#1#2{%

Our crossing type, which is #2, is one of 1 or -1. Our strands are #1 and #1+1.

```
\edef\braid@crossing@type{#2}%
     \edef\braid@this@strand{#1}%
157
```

\pgfmathtruncatemacro{\braid@next@strand}{#1+1}

Increment the level counter, if requested. The controls whether the crossing is on the same level as the previous one or is one level further on.

```
\ifbraid@increase@level
159
     \stepcounter{braid@level}
160
161
```

Default is to request increment so we set it for next time.

\braid@increase@leveltrue

Now we figure out the coordinates of the crossing. (\braid@tx,\braid@ty) is the top-left corner (assuming the braid flows down the page). (\braid@nx,\braid@ny) is the bottom-right corner (assuming the braid flows down the page). We start by setting (\braid@tx,\braid@ty) according to the level and strand number, then shift \braid@ty by \braid@eh which is the "edge height" (the little extra at the start and end of each strand). Then from these values, we set (\braid@nx,\braid@ny) by adding on the appropriate amount. The heights \braid@cy and \braid@dy are for the control points for the strands as they cross. They're actually the same height, but using two gives us the possibility of changing them independently in a later version of this package. Lastly, we bring \braid@ty and \braid@ny towards each other just a little so that there is "clear water" between subsequent crossings (makes it look a bit better if the same strand is used in subsequent crossings).

```
\braid@tx=\braid@this@strand\braid@width
163
     \braid@ty=\value{braid@level}\braid@height
164
     \advance\braid@ty by \braid@eh
165
     \braid@nx=\braid@tx
166
     \braid@ny=\braid@ty
167
     \advance\braid@nx by \braid@width
     \advance\braid@ny by \braid@height
     \advance\braid@ty by \braid@nf\braid@height
170
     \advance\braid@ny by -\braid@nf\braid@height
171
     \braid@cy=\braid@ty
     \braid@dy=\braid@ny
173
     \advance\braid@cy by \braid@cf\braid@height
174
     \advance\braid@dy by -\braid@cf\braid@height
175
```

Now we try to find a starting point for the strand ending here. We might not have used this strand before, so it might not exist.

```
76 \expandafter\let\expandafter\braid@this@path@origin%
```

177 \csname braid@strand@\braid@this@strand @origin\endcsname

If we haven't seen this strand before, that one will be \relax.

```
178 \ifx\braid@this@path@origin\relax
```

Haven't seen this strand before, so initialise it. Record the initial position of the strand.

179 \let\braid@this@path@origin\braid@this@strand

Start a new soft path.

```
\pgfsyssoftpath@setcurrentpath{\@empty}
```

\pgfpathmoveto{\pgfpoint{\braid@tx}{0pt}}

Save the path as \braid@this@path.

```
\pgfsyssoftpath@getcurrentpath{\braid@this@path}
```

183 **\els**e

We have seen this before, so we simply copy the associated path in to \braid@this@path.

```
\expandafter\let\expandafter\braid@this@path%
```

- \csname braid@strand@\braid@this@path@origin\endcsname
- 186 \fi

Now we do the same again with the other strand in the crossing.

- \expandafter\let\expandafter\braid@next@path@origin%
- \csname braid@strand@\braid@next@strand @origin\endcsname
- 189 \ifx\braid@next@path@origin\relax
- 190 \let\braid@next@path@origin\braid@next@strand

```
191 \pgfsyssoftpath@setcurrentpath{\@empty}
192 \pgfpathmoveto{\pgfpoint{\braid@nx}{0pt}}
193 \pgfsyssoftpath@getcurrentpath{\braid@next@path}
194 \else
195 \expandafter\let\expandafter\braid@next@path%
196 \csname braid@strand@\braid@next@path@origin\endcsname
197 \fi
```

Now that we have the paths for our two strands, we extend them to the next level. We start by selecting the first path.

\pgfsyssoftpath@setcurrentpath{\braid@this@path}

Draw a line down to the current level, note that this line is always non-trivial since we shifted the corners of the crossing in a little.

\pgfpathlineto{\pgfqpoint{\braid@tx}{\braid@ty}}

Curve across to the next position. Depending on the crossing type, we either have a single curve or we have to break it in two. Our gap is to interrupt at times determined by the gap key.

We're on the overpass, so just one curve needed.

```
203 \pgfpathcurveto{\pgfqpoint{\braid@tx}{\braid@cy}}%
204 {\pgfqpoint{\braid@nx}{\braid@dy}}%
205 {\pgfqpoint{\braid@nx}{\braid@ny}}
206 \else
```

We're on the underpass, so we need to interrupt our path to allow the other curve to go past.

```
\pgfpathcurvebetweentimecontinue{0}{\braid@gst}%
207
     {\pgfqpoint{\braid@tx}{\braid@ty}}%
208
     {\pgfqpoint{\braid@tx}{\braid@cy}}%
209
     {\pgfqpoint{\braid@nx}{\braid@dy}}%
     {\pgfqpoint{\braid@nx}{\braid@ny}}%
     \pgfpathcurvebetweentime{\braid@gend}{1}%
     {\pgfqpoint{\braid@tx}{\braid@ty}}%
     {\bf \{\pgfqpoint{\bf \{\braid@tx\}{\bf \{\braid@cy\}}}\%}
     {\pgfqpoint{\braid@nx}{\braid@dy}}%
215
     {\pgfqpoint{\braid@nx}{\braid@ny}}
216
217 \fi
```

We're done with this path, so now we save it.

\pgfsyssoftpath@getcurrentpath{\braid@this@path}\ Now do the same with the second path.

```
pgfsyssoftpath@setcurrentpath{\braid@next@path}
pgfpathlineto{\pgfqpoint{\braid@nx}{\braid@ty}}

pgfpathlineto{\pgfqpoint{\braid@over@cross}
pgfpathcurvebetweentimecontinue{0}{\braid@gst}%

pgfqpoint{\braid@nx}{\braid@ty}}%

pgfqpoint{\braid@nx}{\braid@cy}}%

pgfqpoint{\braid@tx}{\braid@dy}}%

pgfqpoint{\braid@tx}{\braid@dy}}%

pgfqpoint{\braid@tx}{\braid@ny}}

pgfpathcurvebetweentime{\braid@gnd}{1}%
```

```
{\pgfqpoint{\braid@nx}{\braid@ty}}%
      {\pgfqpoint{\braid@nx}{\braid@cy}}%
 229
      {\pgfqpoint{\braid@tx}{\braid@dy}}%
 230
      {\pgfqpoint{\braid@tx}{\braid@ny}}
 231
 232
      \pgfpathcurveto{\pgfqpoint{\braid@nx}{\braid@cy}}%
      {\pgfqpoint{\braid@tx}{\braid@dy}}%
 234
      {\pgfqpoint{\braid@tx}{\braid@ny}}
 235
 236
      \pgfsyssoftpath@getcurrentpath{\braid@next@path}
 237
Now save the paths to their proper macros again.
      \expandafter\let%
      \csname braid@strand@\braid@this@path@origin \endcsname%
 239
      \braid@this@path
      \expandafter\let%
 241
      \csname braid@strand@\braid@next@path@origin \endcsname%
 242
      \braid@next@path
 243
Now update the origins
      \expandafter\let%
 244
      \csname braid@strand@\braid@this@strand @origin\endcsname%
 245
 246
      \braid@next@path@origin
 247
      \expandafter\let%
      \csname braid@strand@\braid@next@strand @origin\endcsname%
 248
      \braid@this@path@origin
increment the strand counter, if necessary
      \pgfmathparse{\value{braid@strands} < \braid@next@strand ?</pre>
 250
         "\noexpand\setcounter{braid@strands}{\braid@next@strand}" : ""}
 251
      \pgfmathresult
 252
And merrily go on our way with the next bit of the braid specification.
      \braid@process%
(End definition for \braid@add@crossing.)
```

\braid@olabel@strand

This macro allows us to label a strand just before a crossing. The first argument is the strand number at that particular crossing and the second is the label. We also save the current height. This version takes the strand number as meaning the *original* ordering.

```
\newcommand{\braid@olabel@strand}[3][]{%
      \edef\braid@tmp{{\the\value{braid@level}}}%
 256
      \expandafter\ifx\csname braid@strand@#2@origin\endcsname\relax
 257
      \g@addto@macro\braid@tmp{{#2}}%
      \else
      \edef\braid@tmpa{{\csname braid@strand@#2@origin\endcsname}}%
      \ge@addto@macro\braid@tmp{\braid@tmpa}%
 262
      \g@addto@macro\braid@tmp{{#3}{#1}}%
 263
      \ge@addto@macro{\braid@strand@labels}{\braid@tmp}%
 264
      \braid@process%
 265
 266 }
(End definition for \braid@olabel@strand.)
```

```
This macro allows us to label a strand just before a crossing. The first argument is the
        \braid@clabel@strand
                                strand number at that particular crossing and the second is the label. We also save the
                                current height. This version takes the strand number as meaning the current ordering.
                                  267 \newcommand{\braid@clabel@strand}[3][]{%
                                       \edef\braid@tmp{{\the\value{braid@level}}}%
                                       \g@addto@macro\braid@tmp{{#2}{#3}{#1}}%
                                       \ge@addto@macro{\braid@strand@labels}{\braid@tmp}%
                                       \braid@process%
                                 271
                                 272 }
                                (End definition for \braid@clabel@strand.)
          \braid@floors@trim The list of floors, if given, will start with a superfluous comma. This removes it.
                                 273 \def\braid@floors@trim,{}
                                (End definition for \braid@floors@trim.)
         \braid@render@floor This is the default rendering for floors: it draws a rectangle.
                                 274 \def\braid@render@floor{%
                                         \draw (\floorsx,\floorsy) rectangle (\floorex,\floorey);
                                 275
                                 276 }
                                (End definition for \braid@render@floor.)
 \braid@render@strand@labels
                                This starts rendering the labels on the strands at the crossings.
                                 277 \def\braid@render@strand@labels#1{%
                                 278
                                       \def\braid@tmp{#1}%
                                 279
                                       \ifx\braid@tmp\pgfutil@empty
                                      \let\braid@next=\pgfutil@gobble
                                 280
                                 281
                                 282
                                      \let\braid@next=\braid@@render@strand@labels
                                      \fi
                                       \braid@next{#1}%
                                 284
                                 285 }
                                (End definition for \braid@render@strand@labels.)
                                This is the actual renderer.
\braid@@render@strand@labels
                                 286 \def\braid@@render@strand@labels#1#2#3#4{%
                                       \begingroup
                                 287
                                       \pgfscope
                                 288
                                       \let\tikz@options=\pgfutil@empty
                                 289
                                       \let\tikz@mode=\pgfutil@empty
                                 290
                                       \let\tik@transform=\pgfutil@empty
                                 291
                                       \let\tikz@fig@name=\pgfutil@empty
                                 292
                                       \tikzset{/pgf/braid/strand label,#4}%
                                 293
                                       \braid@nx=#2\braid@width
                                       \braid@ny=#1\braid@height
                                       \advance\braid@ny by \braid@eh
                                 296
                                       \advance\braid@ny by \braid@height
                                 297
                                       \pgftransformshift{\pgfqpoint{\braid@nx}{\braid@ny}}%
                                 298
                                       \tikz@options
                                 299
                                       \setbox\pgfnodeparttextbox=\hbox%
                                 300
```

\bgroup%

```
\tikzset{every text node part/.try}%
302
     \ifx\tikz@textopacity\pgfutil@empty%
303
304
     \pgfsetfillopacity{\tikz@textopacity}%
305
     \pgfsetstrokeopacity{\tikz@textopacity}%
306
307
     \pgfinterruptpicture%
308
     \tikz@textfont%
309
     \ifx\tikz@text@width\pgfutil@empty%
310
     \else%
311
     \begingroup%
312
     \pgfmathsetlength{\pgf@x}{\tikz@text@width}%
313
     \pgfutil@minipage[t]{\pgf@x}\leavevmode\hbox{}%
314
     \tikz@text@action%
315
316
     \tikz@atbegin@node%
317
     \bgroup%
318
     \aftergroup\unskip%
319
     \ifx\tikz@textcolor\pgfutil@empty%
     \pgfutil@colorlet{.}{\tikz@textcolor}%
322
     \fi%
323
     \pgfsetcolor{.}%
324
     \setbox\tikz@figbox=\box\pgfutil@voidb@x%
325
     \tikz@uninstallcommands%
326
     \tikz@halign@check%
327
     \ignorespaces%
328
     #3
329
     \egroup
330
     \tikz@atend@node%
331
     \ifx\tikz@text@width\pgfutil@empty%
332
     \else%
333
     \pgfutil@endminipage%
334
     \endgroup%
335
     \fi%
336
     \endpgfinterruptpicture%
337
     \egroup%
338
339
      \ifx\tikz@text@width\pgfutil@empty%
340
       \else%
         \pgfmathsetlength{\pgf@x}{\tikz@text@width}%
341
         \wd\pgfnodeparttextbox=\pgf@x%
342
343
       \fi%
       \ifx\tikz@text@height\pgfutil@empty%
344
       \else%
345
         \pgfmathsetlength{\pgf@x}{\tikz@text@height}%
346
         \ht\pgfnodeparttextbox=\pgf@x%
347
348
       \ifx\tikz@text@depth\pgfutil@empty%
349
350
351
         \pgfmathsetlength{\pgf@x}{\tikz@text@depth}%
352
         \dp\pgfnodeparttextbox=\pgf@x%
353
       \fi%
     \pgfmultipartnode{\tikz@shape}{\tikz@anchor}{\tikz@fig@name}{%
354
       {\begingroup\tikz@finish}%
355
```

```
356 }%
357 \endpgfscope
358 \endgroup
359 \braid@render@strand@labels%
360 }
```

 $(End\ definition\ for\ \ braid@@render@strand@labels.)$

\braid@render

This is called at the end of the braid and it renders the braids and floors according to whatever has been built up up to now.

```
361 \def\braid@render{
```

Check for floors since we do them first.

- 362 \ifx\braid@floors\@empty
- 363 \else

Have some floors, start a scope and prepare to render them.

hgfsys@beginscope

Clear the path (just to be sure).

365 \pgfsyssoftpath@setcurrentpath{\empty}

Trim the initial comma off the list of floors.

366 \edef\braid@floors{\expandafter\braid@floors@trim\braid@floors}

Initialise our horizontal coordinates.

- 367 \braid@tx=\braid@width
- 368 \advance\braid@tx by \braid@eh
- \braid@nx=\value{braid@strands}\braid@width
- 370 \advance\braid@nx by -\braid@eh

Loop over the list of floors.

```
371 \foreach \braid@f in \braid@floors {
372 \pgfsys@beginscope
```

Figure out the vertical coordinates for the current floor.

- 373 \braid@ty=\braid@f\braid@height
- 374 \advance\braid@ty by \braid@eh
- 375 \advance\braid@ty by \braid@height
- 376 \braid@ny=\braid@ty
- 377 \advance\braid@ny by \braid@height

Save the coordinates for use in the floor rendering macro.

```
\def\floorsx{\the\braid@tx}
def\floorsy{\the\braid@ty}
def\floorex{\the\braid@nx}
def\floorey{\the\braid@ny}
let\tikz@options=\pgfutil@empty
```

Load general floor style options.

\expandafter\tikzset\expandafter{\braid@floors@style}

Load any style options specific to this floor. We're actually offset by 2 from what the user thinks the floor level is.

\pgfmathtruncatemacro{\braid@ff}{\braid@f+2}

Load the relevant floor style, if it exists.

- \expandafter\let\expandafter\braid@floor@style%
- \csname braid@options@floor@\braid@ff\endcsname
- 387 \ifx\braid@floor@style\relax
- 388 \else

There is a floor style for this level, so process it.

- \expandafter\tikzset\expandafter{\braid@floor@style}%
- 390 \fi

The \tikzset just parses the options, we need to call \tikz@options to actually set them.

391 \tikz@options

Now we call the rendering code.

392 \braid@render@floor

Done! End the scope for this floor and go again.

- 393 \pgfsys@endscope
- 394 }

Done rendering floors, end the scope.

- 395 \pgfsys@endscope
- 396 \fi

Finished with floors (if we had them), now get on with the strands.

- 397 \stepcounter{braid@level}
- 398 \foreach \braid@k in {1,...,\value{braid@strands}} {

Start a local scope to ensure we don't mess with other braids

399 \pgfsys@beginscope

Default is to draw each braid

- 400 \tikz@mode@drawtrue%
- 401 \let\tikz@mode=\pgfutil@empty
- 402 \let\tikz@options=\pgfutil@empty

(x,y) coordinates of bottom of strand

- 403 \braid@tx=\braid@k\braid@width
- \braid@ty=\value{braid@level}\braid@height
- 405 \advance\braid@ty by 2\braid@eh

Try to find the starting point of this strand

- 406 \expandafter\let\expandafter\braid@path@origin%
- 407 \csname braid@strand@\braid@k @origin\endcsname
- 408 \ifx\braid@path@origin\relax

If that doesn't exist, we'll just draw a straight line so we move to the top of the current position

- 409 \pgfsyssoftpath@setcurrentpath{\@empty}
- 410 \pgfpathmoveto{\pgfqpoint{\braid@tx}{Opt}}
- 411 \let\braid@path@origin\braid@k
- 412 \else

If the path does exist, we load it

- 413 \expandafter\let\expandafter\braid@path%
- \csname braid@strand@\braid@path@origin\endcsname
- 415 \pgfsyssoftpath@setcurrentpath{\braid@path}
- 416 **\fi**

```
Extend the path to the bottom
        \pgflineto{\pgfqpoint{\braid@tx}{\braid@ty}}
Load common style options
        \expandafter\tikzset\expandafter{\braid@style}
Load any style options specific to this strand
        \expandafter\let\expandafter\braid@style%
 419
        \csname braid@options@strand@\braid@path@origin\endcsname
 420
        \ifx\braid@style\relax
 421
        \else
 422
        \expandafter\tikzset\expandafter{\braid@style}
 423
        \fi
 424
    \braid@options
 425
        \tikz@mode
 426
        \tikz@options
 427
This is the command that actually draws the strand.
          \edef\tikz@temp{\noexpand\pgfusepath{%
              \iftikz@mode@draw draw\fi%
 429
          }}%
 430
          \tikz@temp
 431
If our braid has a name, we label the ends of the strand.
 432 \ifx\braid@name\pgfutil@empty
 433 \else
Label the ends of the strand.
 434 \coordinate (\braid@name-\braid@path@origin-e) at (\braid@tx,\braid@ty);
 435 \coordinate (\braid@name-rev-\braid@k-e) at (\braid@tx,\braid@ty);
 436 \braid@nx=\braid@path@origin\braid@width
 437 \coordinate (\braid@name-\braid@path@origin-s) at (\braid@nx,Opt);
 438 \coordinate (\braid@name-rev-\braid@k-s) at (\braid@nx,0pt);
 439 \fi
Done with this strand, close the scope and do the next one.
       \pgfsys@endscope
 441
If our braid has a name, we also want to label the centre.
        \ifx\braid@name\pgfutil@empty
 443
        \else
 444
        \braid@tx=\value{braid@strands}\braid@width
        \braid@ty=\value{braid@level}\braid@height
 445
        \advance\braid@ty by 2\braid@eh
 446
        \advance\braid@tx by \braid@width
 447
        \braid@tx=.5\braid@tx
 448
        \braid@ty=.5\braid@ty
 449
        \coordinate (\braid@name) at (\braid@tx,\braid@ty);
 450
Now we label the strands if needed.
      \ifx\braid@strand@labels\pgfutil@empty
 452
 453
       \expandafter\braid@render@strand@labels\braid@strand@labels{}%
 454
```

```
All done now, close the scope and end the group (which was opened right at the start).
```

456 \pgfsys@endscope

457 \endgroup}

(End definition for \braid@render.)

\braid@start

This starts off the braid, initialising a load of stuff. We start a PGF scope, set the level to -1, the label, floors, and name to empty, process any options we're given, and save certain lengths for later use.

```
\def\braid@start#1{%
      \pgfsys@beginscope
      \setcounter{braid@level}{-1}%
      \let\braid@label\@empty
 461
      \let\braid@strand@labels\@empty
      \let\braid@floors\@empty
 463
      \let\braid@name\empty
 464
      \let\clabel=\braid@clabel@strand
 465
      \let\olabel=\braid@olabel@strand
 466
      \pgfkeys{/pgf/braid/.cd,#1}%
 467
      \ifbraid@strand@labels@origin
 468
      \let\label=\braid@olabel@strand
      \else
 470
 471
      \let\label=\braid@clabel@strand
 472
      \fi
      \let\braid@options\tikz@options
 473
      \tikz@transform
 474
      \setcounter{braid@strands}{%
 475
        \pgfkeysvalueof{/pgf/braid/number of strands}}%
 476
      \braid@width=\pgfkeysvalueof{/pgf/braid/width}%
 477
      \braid@height=\pgfkeysvalueof{/pgf/braid/height}%
 478
      \braid@eh=\pgfkeysvalueof{/pgf/braid/border height}%
      \pgfkeysgetvalue{/pgf/braid/control factor}{\braid@cf}%
      \pgfkeysgetvalue{/pgf/braid/nudge factor}{\braid@nf}%
      \braid@height=-\braid@height
 482
      \braid@eh=-\braid@eh
      \braid@increase@leveltrue
      \braid@process@start
 485
 486 }
(End definition for \braid@start.)
    These are the lengths we'll use as we construct the braid
   \newdimen\braid@width
 488 \newdimen\braid@height
 489 \newdimen\braid@tx
 490 \newdimen\braid@ty
 491 \newdimen\braid@nx
 492 \newdimen\braid@ny
 493 \newdimen\braid@cy
 494 \newdimen\braid@dy
   \newdimen\braid@eh
```

An if to decide whether or not to step to the next level or not

496 \newif\ifbraid@increase@level

```
An if to decide whether label indices should be absolute or not
 497 \newif\ifbraid@strand@labels@origin
    Some initial values
 498 \let\braid@style\pgfutil@empty
 499 \let\braid@floors@style\pgfutil@empty
 500 \def\braid@over@cross{1}
    Counters to track the strands and the levels.
 501 \newcounter{braid@level}
 502 \newcounter{braid@strands}
    All the keys we'll use.
 503 \pgfkeys{
Handle unknown keys by passing them to pgf and tikz.
        /tikz/braid/.search also={/pgf},
 504
        /pgf/braid/.search also={/pgf,/tikz},
 505
Our "namespace" is /pgf/braid.
        /pgf/braid/.cd,
        number of strands/.initial=0,
 507
        height/.initial=1cm,
 508
        width/.initial=1cm,
 509
        gap/.initial=.1,
 510
        border height/.initial=.25cm,
 511
        control factor/.initial=.5,
 512
        nudge factor/.initial=.05,
        name/.code={%
          \def\braid@name{#1}%
 515
 516
        },
        at/.code={%
 517
          \braid@relocate{#1}%
 518
 519
        floor command/.code={%
 520
          \def\braid@render@floor{#1}%
 521
 522
        style strands/.code 2 args={%
 523
          \def\braid@temp{#2}%
          \braidset{style each strand/.list={#1}}%
 526
        style each strand/.code={%
 527
           \expandafter\edef%
 528
          \csname braid@options@strand@#1\endcsname{\braid@temp}%
 529
 530
        style floors/.code 2 args={%
 531
          \def\braid@temp{#2}%
 532
          \braidset{style each floor/.list={#1}}%
 533
        style each floor/.code={%
          \expandafter\edef%
          \csname braid@options@floor@#1\endcsname{\braid@temp}%
 537
 538
        style all floors/.code={%
 539
          \def\braid@floors@style{#1}
 540
        },
 541
```

```
strand label/.style={},
                  strand label by origin/.is if=braid@strand@labels@origin,
            543
            544 }
\braidset Shorthand for setting braid-specific keys.
            545 \def\braidset#1{%
                \pgfkeys{/pgf/braid/.cd,#1}}
           (End definition for \braidset. This function is documented on page ??.)
            547 (*library)
            548 (@@=braid)
                Reimplementation as a TikZ Library
          Life is so much easier with LATEX3.
            549 \ProvidesFile{tikzlibrarybraids.code.tex}[%
                2022/10/26 v2.2 Tikz/PGF library for drawing braid diagrams%
            551
            552 \RequirePackage{expl3}
            553 \ExplSyntaxOn
           Define all the variables we'll be using.
            554 \tl_new:N \l__braid_tmpa_tl
            555 \tl_new:N \l__braid_tmpb_tl
            556 \tl_new:N \l__braid_tmpc_tl
            557 \tl_new:N \l__braid_tmpd_tl
            558 \tl_new:N \l__braid_anchor_strand_tl
            \verb| 559 $$ $$ $$ l_new: N $$ l_braid_anchor_level_tl $$
            560 \fp_new:N \l__braid_height_fp
            561 \fp_new:N \l__braid_width_fp
            563 \fp_new:N \l__braid_control_fp
            564 \fp_new:N \l__braid_ctrlax_fp
            565 \fp_new:N \l__braid_ctrlay_fp
            566 \fp_new:N \l__braid_ctrlbx_fp
            567 \fp_new:N \l__braid_ctrlby_fp
            568 \fp_new:N \l__braid_endx_fp
            569 \fp_new:N \l__braid_endy_fp
            fp_new:N \l_braid_anchor_x_fp
            571 \fp_new:N \l__braid_anchor_y_fp
            ^{573} \int_new:N \l__braid_tmpb_int
            574 \int_new:N \l__braid_length_int
```

576 \int_new:N \l__braid_crossing_int
577 \int_new:N \l__braid_crossing_start_int
578 \int_new:N \l__braid_crossing_end_int
579 \int_new:N \l__braid_crossing_width_int
580 \int_new:N \l__braid_crossing_long_int

581 \int_new:N \l__braid_crossing_start_factor_int
582 \int_new:N \l__braid_crossing_end_factor_int
583 \int_new:N \l__braid_anchor_level_int
584 \int_new:N \l__braid_floor_int

```
585 \seq_new:N \l__braid_tmpa_seq
 586 \seq_new:N \l__braid_word_seq
 587 \seq_new:N \l__braid_crossing_seq
 588 \seq_new:N \l__braid_anchor_seq
 589 \seq_new:N \l__braid_floors_seq
 590 \str_new:N \l__braid_tmpa_str
 591 \str_new:N \l__braid_sup_str
 592 \str_set:Nn \l__braid_sup_str {^}
 593 \str_new:N \l__braid_sub_str
 594 \str_set:Nn \l__braid_sub_str {_}
 595 \str_new:N \l__braid_hyphen_str
 596 \str_set:Nn \l__braid_hyphen_str {-}
 597 \str_new:N \l__braid_bar_str
 598 \str_set:Nn \l__braid_bar_str {|}
 599 \str_new:N \l__braid_one_str
 600 \str_set:Nn \l__braid_one_str {1}
 601 \bool_new:N \l__braid_step_level_bool
 602 \bool_new:N \l__braid_swap_crossing_bool
 603 \bool_new:N \l__braid_floor_bool
 604 \prop_new:N \l__braid_strands_prop
 605 \prop_new:N \l__braid_permutation_prop
 606 \prop_new:N \l__braid_crossing_permutation_prop
 607 \prop_new:N \l__braid_inverse_prop
 608 \prop_new:N \l__braid_anchor_prop
 609 \cs_generate_variant:Nn \seq_set_split:Nnn {NVn}
Our interface is through a TikZ pic.
   \tikzset{
 610
       braid/.pic={
 611
         \__braid_parse_word:n {#1}
 612
         \__braid_count:
 613
         \__braid_render:
 614
       },
 615
       floor/.pic={
 616
         \path[pic~ actions, draw=none] (0,0) rectangle (1,1);
 617
         \path[pic~ actions, fill=none] (0,0) -- (1,0) (0,1) -- (1,1);
 618
 619
       /tikz/braid/.search~ also={/tikz},
 620
       braid/.cd,
 621
```

The various TikZ parameters for the braid.

The anchor determines which part of the braid is located at the position specified by the pic. It can be of the form n-m where n is a strand number and +m+ is a crossing level. The strand number can be either a number or rev-n to use the ending numbering of the strands. The crossing level can also be s or e which means the actual start or end of the strand (including the border).

```
anchor/.initial=1-s,
```

number of strands sets a minimum for the number of strands in the braid (otherwise, it is set by the strands used in the specified crossings).

```
number~ of~ strands/.initial=0,
```

height is the distance between crossings (can be negative).

```
height/.initial=-1cm,
```

```
width is the distance between strands (can be negative).
```

```
width/.initial=1cm,
```

gap is for determining the gap in the under-strand of a crossing.

```
gap/.initial=.05,
```

border height is a length added at the start and end of each strand.

```
border~ height/.initial=.25cm,
```

floor border is added to the width of any floors

```
floor~ border/.initial=.25cm,
```

floors is a list of floors to draw, specified as a cslist of coordinates as (x,y,w,h,a) in which the units are numbers of strands and crossing levels. The parameters are: coordinates of lower left corner, width, height, (optional) name for styling.

```
add~ floor/.code={
629
630
        \seq_push: Nn \l__braid_floors_seq {#1}
631
      },
```

control factor determines the proportion of the height used for the control points.

```
control~ factor/.initial=.5,
```

nudge factor is used to compress each crossing slightly within its rectangle.

```
nudge~ factor/.initial=.05
634 }
```

__braid_parse_word: Nn Parse the braid word as a token list and convert it into a sequence.

```
635 \cs_new_nopar:Npn \__braid_parse_word:n #1
636 {
     \seq_clear:N \l__braid_word_seq
637
     \tl_clear:N \l__braid_tmpa_tl
638
639
     \tl_set:Nn \l__braid_tmpb_tl {#1}
640
     \bool_until_do:nn { \tl_if_empty_p:N \l_braid_tmpb_tl }
641
     {
642
```

We step through the braid specification, looking for special characters. To avoid catcode issues, the comparison is as strings. Some actions may involve consuming more tokens from the list so we can't do a simple map_inline but have to keep stripping off the head token.

The idea is to store information about the current crossing in a token list (noting that it may be specified in a variety of orders) and then when we're sure we have all the information we add it to our sequence of crossings.

```
\str_set:Nx \l__braid_tmpa_str {\tl_head:N \l__braid_tmpb_tl}
       \tl_set:Nx \l__braid_tmpb_tl {\tl_tail:N \l__braid_tmpb_tl}
644
       \str_case_e:nnTF {\l__braid_tmpa_str}
645
646
```

Underscore introduces the crossing numbers

```
{_}
        {
648
          \tl_put_right:Nx \l__braid_tmpa_tl
650
            \exp_not:N \__braid_parse_index:n {\tl_head:N \l__braid_tmpb_tl}
651
652
          \tl_set:Nx \l__braid_tmpb_tl {\tl_tail:N \l__braid_tmpb_tl}
653
654
```

```
Power is used to indicate inverse.
          {^}
 655
 656
            \tl_put_left:Nx \l__braid_tmpa_tl
 657
            {
 658
              \exp_not:N \__braid_parse_exponent:n {\tl_head:N \l__braid_tmpb_tl}
 659
            \tl_set:Nx \l__braid_tmpb_tl {\tl_tail:N \l__braid_tmpb_tl}
 661
         }
Bar is for floors.
          {|}
 663
 664
           \tl_if_empty:NF \l__braid_tmpa_tl
 665
 666
             \seq_put_right:NV \l__braid_word_seq \l__braid_tmpa_tl
 667
             \tl_clear:N \l__braid_tmpa_tl
 668
 669
 670
           \tl_set:Nn \l__braid_tmpa_tl {
 671
             \bool_set_false:N \l__braid_step_level_bool
 672
             \bool_set_true:N \l__braid_floor_bool
 673
 674
           \seq_put_right:NV \l__braid_word_seq \l__braid_tmpa_tl
 675
           \tl_clear:N \l__braid_tmpa_tl
 676
 677
Hyphen says the next crossing is on the same level as the current one.
          {-}
 678
 679
            \tl_put_right:Nn \l__braid_tmpa_tl
 680
              \bool_set_false:N \l__braid_step_level_bool
           }
 683
 684
1 is for the identity (i.e., no crossing but still have a level). We put a nop token on the
list so that it is no longer empty.
          {1}
 686
           \tl_if_empty:NF \l__braid_tmpa_tl
 687
           {
 688
             \seq_put_right:NV \l__braid_word_seq \l__braid_tmpa_tl
 689
             \tl_clear:N \l__braid_tmpa_tl
 690
 691
            \tl_put_right:Nn \l__braid_tmpa_tl {\__braid_do_identity:}
 692
         }
 693
Ignore spaces.
         {~}
          {
         }
        }
 697
        {
 698
        }
 699
```

{

If we get an unrecognised token, it's our trigger to start accumulating information for the next crossing.

At the end, we also put our current token list on the word sequence.

(End definition for __braid_parse_word:Nn.)

__braid_parse_index:n

Parse an index, saving it in a sequence with the two indices such that the first goes over the second.

```
714 \cs_new_nopar:Npn \__braid_parse_index:n #1
715 {
     \seq_clear:N \l__braid_crossing_seq
716
     \clist_map_inline:nn {#1}
717
718
       \tl_if_in:nnTF {##1} {-}
719
          \seq_set_split:Nnn \l__braid_tmpa_seq {-} {##1}
721
          \int_compare:nTF {\seq_item:Nn \l__braid_tmpa_seq {1} < \seq_item:Nn \l__braid_tmpa_se
723
            \int_set:Nn \l__braid_tmpa_int {1}
724
725
726
            \int_set:Nn \l__braid_tmpa_int {-1}
728
          \int_step_inline:nnnn {\seq_item:Nn \l__braid_tmpa_seq {1}} {\l__braid_tmpa_int} {\sec_item:Nn \l__braid_tmpa_seq {1}}
            \seq_put_right: Nn \l__braid_crossing_seq {####1}
731
         }
732
734
          \seq_put_right:Nn \l__braid_crossing_seq {##1}
735
       }
736
737
     \int_compare:nT {\seq_count:N \l__braid_crossing_seq == 1}
738
739
       \seq_put_right:Nx \l__braid_crossing_seq {\int_eval:n {#1 + 1} }
740
741
     \bool_if:NF \l__braid_swap_crossing_bool
742
743
       \seq_reverse:N \l__braid_crossing_seq
744
     }
745
746 }
```

```
Parse an exponent, basically testing to see if it is -1 in which case our crossing numbers
\__braid_parse_exponent:n
                             should be reversed..
                              747 \cs_new_nopar:Npn \__braid_parse_exponent:n #1
                              748 {
                              749
                                   \int \int d^2 r dr dr
                              750
                                      \bool_set_true:N \l__braid_swap_crossing_bool
                              751
                              752
                              753
                                      \bool_set_false:N \l__braid_swap_crossing_bool
                              754
                                   }
                              755
                              756 }
                             (End definition for \__braid_parse_exponent:n.)
    \__braid_do_identity:
                              757 \cs_new_nopar:Npn \__braid_do_identity:
                              758 {
                              759 }
                             (End definition for \__braid_do_identity:.)
                            Work out how big the braid is by counting strands and levels. We also figure out the
       \__braid_count:NNN
                             permutation from the start to end of the strands. This is useful for labelling various parts
                             of the braid.
                              760 \cs_new_nopar:Npn \__braid_count:
                              761 {
                                   \int_zero:N \l__braid_length_int
                              762
                                   \int_set:Nn \l__braid_strands_int {\__braid_value:n {number~of~strands}}
                              763
                                   \prop_clear:N \l__braid_permutation_prop
                              764
                                   \prop_clear:N \l__braid_crossing_permutation_prop
                              765
                                   \prop_clear:N \l__braid_anchor_prop
                              766
                                   \prop_clear:N \l__braid_inverse_prop
                              767
                              768
                                   \seq_map_inline: Nn \l__braid_word_seq
                              770
                                   {
                             Clear the crossing sequence and assume we're going to step the level.
                                      \seq_clear:N \l__braid_crossing_seq
                                      \bool_set_true:N \l__braid_step_level_bool
                                      \bool_set_false:N \l__braid_swap_crossing_bool
                              773
                             Run the details of this crossing.
                             If we're increasing the level (no hyphen), do so.
                                      \bool_if:NT \l__braid_step_level_bool
                              775
                              776
                                        \int_incr:N \l__braid_length_int
                              777
```

 $(End\ definition\ for\ _braid_parse_index:n.)$

If we have a crossing, check we have enough strands to cover it.

Now that we know how many strands we have, we can initialise our permutation props. One will hold the overall permutation, the other will keep track of our current permutation.

Now we step through the braid word again and record the permutations so that we can calculate the overall permutation defined by the braid.

We will also figure out our shift from the anchor, so first we need to get some information about the anchor.

If the anchor specification has a hyphen then it is of the form strand-level, otherwise it is an anchor as if the whole braid were contained in a rectangular node.

```
\tl_set:Nx \l__braid_tmpa_tl {\__braid_value:n {anchor}}
     \tl_if_in:NnTF \l__braid_tmpa_tl {-}
797
     {
798
       \seq_set_split:NnV \l__braid_anchor_seq {-} \l__braid_tmpa_tl
799
800
       \tl_set:Nx \l__braid_tmpa_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
801
       \tl_if_eq:VnTF \l__braid_tmpa_tl {rev}
802
         \tl_set:Nx \l__braid_anchor_strand_tl {\seq_item:Nn \l__braid_anchor_seq {2}}
         \tl_set:Nx \l__braid_anchor_level_tl {\seq_item:Nn \l__braid_anchor_seq {3}}
805
      }
806
807
         \tl_set:Nx \l__braid_anchor_strand_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
808
         \tl_set:Nx \l__braid_anchor_level_tl {\seq_item:Nn \l__braid_anchor_seq {2}}
809
810
```

The important information is as to the level at which the requested anchor resides. If it is at the end or start of a strand, we set the level to -1 so that it never matches a level number.

```
817
          {
            \int_set:Nn \l__braid_anchor_level_int {-1}
818
          }
819
          {
820
            \int_set:Nn \l__braid_anchor_level_int
821
            {\tl_use:N \l__braid_anchor_level_tl}
822
823
       }
824
     }
825
     {
826
```

There wasn't a hyphen in the anchor specification, so assume it's an anchor on a node surrounding the entire braid. For now, set the anchor strand and level to -1.

```
\int_set:Nn \l__braid_anchor_level_int {-1}
827
       \tl_set:Nn \l__braid_anchor_strand_tl {-1}
828
     }
829
830
     \int_zero:N \l__braid_crossing_int
831
     \int_incr:N \l__braid_crossing_int
832
     \seq_map_inline:Nn \l__braid_word_seq
833
834
       \bool_set_true: N \l__braid_step_level_bool
835
       \seq_clear:N \l__braid_crossing_seq
836
       \bool_set_false:N \l__braid_swap_crossing_bool
837
838
       \seq_if_empty:NF \l__braid_crossing_seq
          \int_step_inline:nnn {2} {\seq_count:N \l__braid_crossing_seq}
842
            \int_set:Nn \l__braid_tmpa_int {###1}
843
            \label{local_set} $$ \left( \sum_{k=0}^{\infty} 1_k \right) = \left( \sum_{k=0}^{\infty} 1_k \right) $$
844
845
            \prop_get:NxN \l__braid_permutation_prop
846
847
              \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
848
            } \l__braid_tmpa_tl
849
            \prop_get:NxN \l__braid_permutation_prop
              \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
852
            } \l__braid_tmpb_tl
853
854
            \prop_put:NxV \l__braid_permutation_prop
855
856
              \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
857
            } \l__braid_tmpa_tl
858
            \prop_put:NxV \l__braid_permutation_prop
859
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
            } \l__braid_tmpb_tl
         }
863
       }
864
```

See if the current level is what was requested by the anchor.

```
% \int_compare:nT {\l__braid_crossing_int = \l__braid_anchor_level_int}
```

```
866
           \prop_set_eq:NN \l__braid_anchor_prop \l__braid_permutation_prop
 867
 868
        \bool_if:NT \l__braid_step_level_bool
 869
 870
           \int_incr:N \l__braid_crossing_int
 871
 872
 873
This inverts the anchor permutation.
      \int_step_inline:nnnn {1} {1} {\l_braid_strands_int}
 874
 875
        \prop_get:NnN \l__braid_anchor_prop {##1} \l__braid_tmpa_tl
 876
        \prop_put:NVn \l__braid_inverse_prop \l__braid_tmpa_tl {##1}
 877
 878
      \prop_set_eq:NN \l__braid_anchor_prop \l__braid_inverse_prop
 879
This inverts the full permutation.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
 880
 881
        \prop_get:NnN \l__braid_permutation_prop {##1} \l__braid_tmpa_tl
        \prop_put:NVn \l__braid_inverse_prop \l__braid_tmpa_tl {##1}
 883
 884
Now that we have the inverse, we can figure out our anchor. If the strand was recorded
as -1, then we want to figure out the position from the braid as a whole so we don't
bother with processing.
      \tl_if_eq:VnF \l__braid_anchor_strand_tl {-1}
 886
      {
Now, see if we requested a strand by its position at the end of the braid.
        \tl_set:Nx \l__braid_tmpa_tl {\seq_item:Nn \l__braid_anchor_seq {1}}
        \tl_if_eq:VnT \l__braid_tmpa_tl {rev}
 889
          \prop_get:NVN \l__braid_permutation_prop
 890
          \l_braid_anchor_strand_tl \l_braid_anchor_strand_tl
 891
 892
        \tl_if_eq:VnF \l__braid_anchor_level_tl {s}
 893
 894
          \tl_if_eq:VnTF \l__braid_anchor_level_tl {e}
            \prop_get:NVN \l__braid_inverse_prop
            \l_braid_anchor_strand_tl \l_braid_anchor_strand_tl
 898
 899
 900
             \prop_get:NVN \l__braid_anchor_prop
 901
            \l_braid_anchor_strand_tl \l_braid_anchor_strand_tl
 902
 903
 904
      }
 905
 906 }
```

(End definition for __braid_count:NNN.)

```
\_braid_dim_value:n Extract a length or a value from a PGF key.
    \__braid_value:n
                        907 \cs_new_nopar:Npn \__braid_dim_value:n #1
                         908 {
                              \dim_to_fp:n {\pgfkeysvalueof{/tikz/braid/#1}}
                         909
                         910 }
                         911 \cs_new_nopar:Npn \__braid_value:n #1
                         912 {
                         913
                              \pgfkeysvalueof{/tikz/braid/#1}
                         914 }
                       (End\ definition\ for\ \\_braid\_dim\_value:n\ and\ \\_braid\_value:n.)
                       This is the macro that converts the braid word into TikZ paths.
    \__braid_render:
                         915 \cs_generate_variant:Nn \prop_get:NnN {NxN}
                         916 \cs_generate_variant:Nn \prop_put:Nnn {NxV}
                         917 \cs_generate_variant:Nn \tl_if_eq:nnTF {VnTF}
                         918 \cs_generate_variant:Nn \tl_if_eq:nnF {VnF}
                         919 \cs_generate_variant:Nn \tl_if_eq:nnT {VnT}
                         920
                         921 \cs_new_nopar:Npn \__braid_render:
                         922 {
                       Start by figuring out our anchor.
                              \tl_if_eq:VnTF \l__braid_anchor_strand_tl {-1}
                         923
                         924
                       The strand is -1 then we're working with the braid as if a node. We'll redefine this node
                       later anyway.
                         925
                                \tl_set:cn {pgf@sh@ns@temporary braid node}{rectangle}
                         926
                                \tl_set:cx {pgf@sh@np@temporary braid node}{%
                                  \exp_not:N\def
                         927
                                  \exp_not:N\southwest
                         928
                                  {
                         929
                                     \exp_not:N\pgfqpoint
                         930
                                     {0pt}
                         931
                                     {Opt}
                         932
                         933
                                  \exp_not:N\def
                                  \exp_not:N\northeast
                         936
                                     \exp_not:N\pgfqpoint
                         937
                         938
                                       \fp_to_dim:n
                         939
                                       {
                         940
                                         (\l_braid_strands_int - 1)
                         941
                         942
                                         abs(\__braid_dim_value:n {width})
                         943
                                       }
                                     }
                                     {
                         947
                                       \fp_to_dim:n
                         948
                                         \l__braid_length_int * abs(\__braid_dim_value:n {height})
                         949
                                         + 2 * \__braid_dim_value:n {border~ height}
                         950
```

```
}
 952
          }
 953
        }%
 954
        \pgfgettransform\l__braid_tmpa_tl
 955
        \tl_set:cV {pgf@sh@nt@temporary braid node} \l__braid_tmpa_tl
 956
        \tl_set:cV {pgf@sh@pi@temporary braid node} \pgfpictureid
 957
        \pgfpointanchor{temporary braid node} {\__braid_value:n {anchor}}
 958
Adjustments due to the possibility of negative widths/heights
        \fp_set:Nn \l__braid_anchor_x_fp {
 959
          - \dim_use:c {pgf@x}
 960
          - (1 - sign(\__braid_dim_value:n {width})) / 2
 961
          * (\l__braid_strands_int - 1)
          * \__braid_dim_value:n {width}
 965
        \fp_set:Nn \l__braid_anchor_y_fp {
          - \dim_use:c {pgf@y}
 966
          - (1 - sign(\__braid_dim_value:n {height})) / 2
 967
 968
          \l__braid_length_int * abs(\__braid_dim_value:n {height})
 969
          + 2 * \_braid_dim_value:n {border~ height}
 970
          ) * sign(\_braid_dim_value:n {height})
 971
 972
      }
 973
      {
 974
The strand is not -1 so we're setting the anchor via strand and level numbers.
        \fp_set:Nn \l__braid_anchor_x_fp { - 1 * (\tl_use:N \l__braid_anchor_strand_tl - 1) * \_
 975
 976
        \tl_if_eq:VnTF \l__braid_anchor_level_tl {s}
 977
          fp_set:Nn l_braid_anchor_y_fp {0}
        }
 980
 981
          \tl_if_eq:VnTF \l__braid_anchor_level_tl {e}
 982
 983
            \fp_set:Nn \l__braid_anchor_y_fp {
 984
              -1 * \l_braid_length_int * \_braid_dim_value:n {height}
 985
              - sign(\__braid_dim_value:n {height})
 986
              * 2 * \__braid_dim_value:n {border~ height}
 987
            }
          }
            \fp_set:Nn \l__braid_anchor_y_fp {
 991
              -1 * \l__braid_anchor_level_tl * \__braid_dim_value:n {height}
 992
              - sign(\__braid_dim_value:n {height})
 993
               * \__braid_dim_value:n {border~ height}
 994
 995
 996
        }
 997
      }
 998
      \begin{scope}[
        shift={
1001
```

(\fp_to_decimal:N \l__braid_anchor_x_fp pt,

```
\fp_to_decimal:N \l__braid_anchor_y_fp pt
1004
        }
1005
      ]
1006
Initialise a prop for the individual strands.
      \prop_clear:N \l__braid_strands_prop
Initialise some lengths.
      \fp_zero:N \l__braid_height_fp
      \fp_zero:N \l__braid_nudge_fp
1009
      \fp_zero:N \l__braid_control_fp
1010
This holds our current height of our strands.
      \fp_set:Nn \l__braid_height_fp
1011
        sign(\__braid_dim_value:n {height})
1013
          \__braid_dim_value:n {border~ height}
1014
1015
This holds the total width of our strands.
      \fp_set:Nn \l__braid_width_fp
1017
        (\l_braid_strands_int - 1) * \_braid_dim_value:n {width}
1018
        + 2 * sign(\__braid_dim_value:n{width})
1019
         * \__braid_dim_value:n {floor~ border}
1020
1021
Each crossing actually starts a little bit into the crossing space, as defined by the
nudge factor.
      \fp_set:Nn \l__braid_nudge_fp
1023
        \__braid_value:n {nudge~ factor} * \__braid_dim_value:n {height}
1024
1025
This sets where the control points for the crossing curves will be.
      \fp_set:Nn \l__braid_control_fp
           _braid_value:n {control~ factor} * \__braid_dim_value:n {height}
1028
1029
      \fp_sub:\n \l__braid_control_fp {\l__braid_nudge_fp}
1030
Initialise our strand paths with a \draw.
      \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1031
1032
        \prop_get:NnN \l__braid_inverse_prop {##1} \l__braid_tmpa_tl
1033
        \prop_put:Nnx \l__braid_strands_prop {##1}
1034
1035
          \exp_not:N \draw[
1036
            braid/every~ strand/.try,
1037
            braid/strand~ ##1/.try
1038
          \exp_not:N \__braid_moveto:nn {
1040
            \fp_eval:n {(##1 - 1) * \__braid_dim_value:n {width} }
1041
          } {0}
1042
          \exp_not:N \__braid_lineto:nn {
1043
            \fp_eval:n {(##1 - 1) * \__braid_dim_value:n {width} }
1044
```

```
Add a load of coordinates at the start of each strand, indexed by both forward and
backward strand numbers.
        \__braid_coordinate:xxxx {-##1-s} {-rev-\l__braid_tmpa_tl-s}
        {fp_eval:n {(\#1 - 1) * \_braid_dim_value:n {width} }} {0}
1048
        \__braid_coordinate:xxxx {-##1-0} {-rev-\l__braid_tmpa_tl-0}
1050
        {\phi_{m} = {(\#1 - 1) * \_braid\_dim\_value:n {width} }}
1051
        { \fp_to_decimal:N \l__braid_height_fp}
1052
1053
    Run through any extra floors requested.
      \seq_map_inline: Nn \l__braid_floors_seq
1054
1055
        \tl_set:Nx \l__braid_tmpa_tl {\clist_item:nn {##1} {5}}
1056
        \__braid_do_floor: Vxxxx \l__braid_tmpa_tl
1057
        {\fp_eval:n
1058
            -1*sign(\__braid_dim_value:n{width})
             * \__braid_dim_value:n {floor~ border}
1062
             + (\_braid_dim_value:n {width}) * (\clist_item:nn {##1} {1} - 1)
          }
1063
1064
          pt
        }
1065
        {\fp_eval:n
1066
          {
1067
             l_{\text{braid\_height\_fp}} + ( l_{\text{braid\_dim\_value:n}} \{height\} ) * (list_item:nn {##1} {2})
1068
          }
1069
          pt
        }
        {\fp_eval:n {
1072
             ( (\clist_item:nn {##1} {3}) * \__braid_dim_value:n {width}
1073
            + 2 * sign(\__braid_dim_value:n{width})
1074
             * \__braid_dim_value:n {floor~ border} ) / \dim_to_fp:n {1cm}
1075
          }
1076
1077
        {\fp_eval:n {
1078
             (\clist_item:nn {##1} {4}) * ( \__braid_dim_value:n {height} ) / \dim_to_fp:n {1cm}
1079
          }
        }
1081
      }
1082
    Keep track of the crossing level for the floor.
      \int_zero:N \l__braid_crossing_int
1083
      \int_incr:N \l__braid_crossing_int
1085
1086
      \seq_map_inline:Nn \l__braid_word_seq
      {
1087
Clear the flags for this segment of the braid word
        \seq_clear:N \l__braid_crossing_seq
1088
        \bool_set_true: N \l__braid_step_level_bool
1089
        \bool_set_false:N \l__braid_floor_bool
1090
        \bool_set_false:N \l__braid_swap_crossing_bool
1091
```

{ \fp_to_decimal:N \l__braid_height_fp}

```
##1
1092
If we're drawing a floor, do so straightaway.
        \bool_if:NT \l__braid_floor_bool
1094
          \__braid_do_floor:Vxxxx \l__braid_crossing_int
          {\fp_eval:n
            {
1097
              -1*sign(\__braid_dim_value:n{width})
1098
                \__braid_dim_value:n {floor~ border}
1099
            }
1100
            pt
          }
1102
          {\fp_to_decimal:N \l__braid_height_fp pt}
1103
          {\fp_eval:n { \l__braid_width_fp / \dim_to_fp:n {1cm} }}
1104
          1105
1106
If we have a crossing, process it.
        \seq_if_empty:NF \l__braid_crossing_seq
          \int_set:Nn \l__braid_crossing_long_int
1110
          {
                     \label{lem:nnl} $$ \simeq_{\mathrm{Nn} \ell_{\mathrm{n}}} \simeq {\count:N \ell_{\mathrm{n}}} \
            \seq_item: Nn \l__braid_crossing_seq {1}
1113
          \int_set:Nn \l__braid_crossing_start_int
            \int_min:nn
1116
1117
              \seq_item: Nn \l__braid_crossing_seq {1}
1118
            }
            {
1120
              \seq_item:\n \l__braid_crossing_seq {\seq_count:\n \l__braid_crossing_seq}
            }
1123
          \int_set:Nn \l__braid_crossing_end_int
1124
1125
            \int_max:nn
1126
1127
              \seq_item: Nn \l__braid_crossing_seq {1}
            }
              \seq_item:\n \l__braid_crossing_seq {\seq_count:\nabla \l__braid_crossing_seq}
            }
1134
          \int_set:Nn \l__braid_crossing_width_int
1135
1136
            \l__braid_crossing_end_int
1137
1138
            \l__braid_crossing_start_int
```

Step through the crossing

```
\int_step_inline:nnn {2} {\seq_count:N \l__braid_crossing_seq}
1141
          {
1142
             \int_set:Nn \l__braid_tmpa_int {###1}
1143
            \int_set:Nn \l__braid_tmpb_int {####1 - 1}
1144
Keep track of the current permutation.
          \prop_get:NxN \l__braid_crossing_permutation_prop
1145
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpa_tl
1146
          \prop_get:NxN \l__braid_crossing_permutation_prop
1147
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpb_tl
1148
1149
          \prop_put:NxV \l__braid_crossing_permutation_prop
1150
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpa_tl
1151
          \prop_put:NxV \l__braid_crossing_permutation_prop
1152
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpb_tl
Now get the strands corresponding to the ones involved in the crossing.
          \prop_get:NxN \l__braid_strands_prop
1154
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpa_tl
1155
          \prop_get:NxN \l__braid_strands_prop
1156
          {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpb_tl
The over-strand is easy as that's a single curve.
1158 %
           \int_set:Nn \l__braid_crossing_start_factor_int {1}
          \int_set:Nn \l__braid_crossing_end_factor_int {1}
1159
    %
            \int_compare:nT {
1160
1161
    %
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1162 %
1163 %
              \l__braid_crossing_long_int
           }
1164 %
1165 %
           {
            \int_set:Nn \l__braid_crossing_start_factor_int {0}
1166
            \int_set:Nn \l__braid_crossing_end_factor_int {0}
1167
1168
            \int_compare:nT {
1169
               ####1 = \seq_count:N \l__braid_crossing_seq
1170
            }
             {
               \int_set:Nn \l__braid_crossing_end_factor_int {1}
            }
             \int_compare:nT {
1175
               ####1 = 2
1176
1177
            {
1178
               \int_set:Nn \l__braid_crossing_start_factor_int {1}
1179
            }
1180
1181
1182
          \tl_put_right:Nx \l__braid_tmpa_tl
1183
1184
            \exp_not:N \__braid_lineto:nn
1185
1186
1187
            {\sigma: (fp_eval:n)}
1188
               ₹
                 (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int} - 1)
1189
```

```
1190
                   \__braid_dim_value:n {width}
               }
1191
            }
1192
             {\fp_eval:n { \l__braid_height_fp + \l__braid_nudge_fp * \l__braid_crossing_start_fa
1193
                 + \_braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l__braid_crossing_s
1194
     } }
1195
1196
             \exp_not:N \__braid_curveto:nnnnn
1197
1198
             {0}
1199
             {\bf \{\fp\_eval:n\ \{\ \l_\_braid\_control\_fp\ \ \ \}}
1200
                  * \l__braid_crossing_start_factor_int
1201 %
                 * 1/(\seq_count:N \l__braid_crossing_seq - 1)}}
1202
1203
1204
             {\sigma = -1_braid_control_fp}
1205
1206 %
                  * \l__braid_crossing_end_factor_int
                 * 1/(\seq_count:N \l__braid_crossing_seq - 1)}}
1207
             {\sigma: n}
               {
                 (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1211
                   \__braid_dim_value:n {width}
               }
            }
1214
             {\fp_eval:n
1216
               {
1217
                 \l__braid_height_fp
                 + \__braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \1__braid_crossing_s
1218
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
               }
1220
            }
1221
          }
1222
The under-strand is a bit more complicated as we need to break it in the middle.
1223 %
            \int_set:Nn \l__braid_crossing_start_factor_int {1}
1224 %
            \int_set:Nn \l__braid_crossing_end_factor_int {1}
1225 %
            \int_compare:nT {
1226 %
              \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
1227 %
1228 %
              \l__braid_crossing_long_int
           }
1229 %
            {
1230 %
             \int_set:Nn \l__braid_crossing_start_factor_int {0}
             \int_set:Nn \l__braid_crossing_end_factor_int {0}
1233
             \int_compare:nT {
1234
               ####1 = \seq_count:N \l__braid_crossing_seq
1235
             }
1236
               \int_set:Nn \l__braid_crossing_end_factor_int {1}
1238
             }
1239
             \int_compare:nT {
1240
               ####1 = 2
1241
             }
1242
```

```
1243
                                   \int_set:Nn \l__braid_crossing_start_factor_int {1}
1244
                             }
1245
                          }
1246
1247
                        \tl_put_right:Nx \l__braid_tmpb_tl
1248
1249
                              \exp_not:N \__braid_lineto:nn
1250
                             {\sigma: (fp_eval:n)}
                                  {
                                         (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1254
                                             \__braid_dim_value:n {width}
1255
                                   }
1256
1257
                             {\fp_eval:n { \l__braid_height_fp + \l__braid_nudge_fp * \l__braid_crossing_start_fa
1258
                                        + \_braid_dim_value:n {height} * (###1 - 2)/(\seq_count:N \l_braid_crossing_s
1259
1260
                             } }
                             \exp_not:N \__braid_curveto:nnnnn
                             {0}
1265
                              ₹
1266
                                   \fp_eval:n {
1267
                                         \l_{\rm braid\_control\_fp} * (.5 - \__braid\_value:n {gap} * (\seq_count:N \l__braid_control_fp + (.5 - \__braid_control_fp + (.5 - \__braid_con
1268
1269 %
                                           * \l__braid_crossing_start_factor_int
                                  }
1270
                             }
1271
1272
                             {
                                   \fp_eval:n {
                                         - (.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) ) / 3
1275
                                        \__braid_bezier_tangent:nnnnn
1276
                                        {.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
1277
                                        {0}
1278
                                        {0}
1279
1280
                                              (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1281
                                                  \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                                                  \__braid_dim_value:n {width}
                                       }
                                        {
                                              (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                                              - \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                                                  \__braid_dim_value:n {width}
1288
1289
                                  }
1290
                             }
1291
1292
                                   \fp_eval:n {
                                        -(.5 - \__braid_value:n \{gap\} * (\seq_count:N \l__braid_crossing_seq - 1) ) / 3
1295
                                        \__braid_bezier_tangent:nnnnn
```

{.5 - __braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }

```
{0}
                {
1298
                     _braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                  \1_
1299
                   * \l__braid_crossing_start_factor_int
1300
1301
                {
1302
                  \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1303
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1304
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
                  - \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                   * \l__braid_crossing_end_factor_int
1307
                }
1308
                {
1309
                    _braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                    \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                    \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
              }
1314
           }
              \fp_eval:n {
1318
                (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1319
                * \__braid_dim_value:n {width} +
                \__braid_bezier_point:nnnnn
1321
                \{.5 - \_ braid\_value:n \{gap\} * (\seq\_count:N \l__braid\_crossing\_seq - 1) \}
1322
                {0}
1323
                {0}
1324
                {
1325
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                  * \__braid_dim_value:n {width}
                }
1329
                {
1330
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
                    \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                  * \__braid_dim_value:n {width}
1334
1335
              }
           }
            {
              \fp_eval:n {
                \l__braid_height_fp
                + \l_braid_nudge_fp * \l_braid_crossing_start_factor_int
1340
                + \_braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l_braid_crossing_s
1341
1342
                \__braid_bezier_point:nnnnn
1343
                {.5 - \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
1344
                {0}
1345
1346
                  \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1348 %
                   * \l__braid_crossing_start_factor_int
1349
                {
```

```
\__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1351
                  - \l_braid_nudge_fp * \l_braid_crossing_start_factor_int
1352
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1353
                  - \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1354
                   * \l__braid_crossing_end_factor_int
1355
                }
1356
                {\_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1357
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1358
                  - \l_braid_nudge_fp * \l_braid_crossing_end_factor_int
             }
           }
1362
1363
            \exp_not:N \__braid_moveto:nn
1364
1365
            {
              \fp_eval:n {
1366
                (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int} - 1)
1367
                * \__braid_dim_value:n {width} +
1368
                \__braid_bezier_point:nnnnn
                {.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
                {0}
                {0}
1372
1373
                ₹
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1374
                  - \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                    \__braid_dim_value:n {width}
1376
                }
1377
                {
1378
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1379
                    \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1381
                  * \__braid_dim_value:n {width}
              }
1383
           }
1384
            {
1385
              \fp_eval:n {
1386
                \l__braid_height_fp
1387
                + \l_braid_nudge_fp * \l_braid_crossing_start_factor_int
1388
                + \_braid_dim_value:n {height} * (###1 - 2)/(\seq_count:N \l_braid_crossing_s
1389
                \__braid_bezier_point:nnnnn
                \{.5 + \_ braid\_value:n \{gap\} * (\seq\_count:N \l\_braid\_crossing\_seq - 1) \}
1393
                {0}
1394
                ₹
                  \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1395
                   * \l__braid_crossing_start_factor_int
1396
1397
1398
                  \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1399
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1400
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
                    \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1403 %
                   * \l__braid_crossing_end_factor_int
```

```
- \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
                  - \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1408
             }
1409
           }
1410
1411
           \exp_not:N \__braid_curveto:nnnnn
1412
           {
1414
             \fp_eval:n {
                (.5 - \__braid_value:n \{gap\} * (\ensuremath{\mbox{ (Neq_count:} N \l__braid_crossing_seq - 1) ) / 3 *}
1416
                \__braid_bezier_tangent:nnnnn
1417
               {.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
1418
                {0}
1419
                {0}
1420
1421
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1422
                   \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
                   \__braid_dim_value:n {width}
               }
               {
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
1427
                  - \seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int})
1428
                   \__braid_dim_value:n {width}
1429
1430
             }
1431
           }
1432
           {
1433
             \fp_eval:n {
                (.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_crossing_seq - 1) ) / 3 *
                \__braid_bezier_tangent:nnnnn
1437
               {.5 + \__braid_value:n {gap} * (\seq_count:N \l__braid_crossing_seq - 1) }
               {0}
1438
                {
1439
                  \l__braid_control_fp * 1/(\seq_count:N \l__braid_crossing_seq - 1)
1440
                   * \l_braid_crossing_start_factor_int
1441
               }
1442
1443
                  \__braid_dim_value:n {height} * 1/(\seq_count:N \l__braid_crossing_seq - 1)
                   \l_braid_nudge_fp * \l_braid_crossing_start_factor_int
                   \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
                  - \l_braid_control_fp * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1447
                  * \l__braid_crossing_end_factor_int
1448
1449
               {\_braid_dim_value:n {height} * 1/(\seq_count:N \l_braid_crossing_seq - 1)
1450
                  - \l__braid_nudge_fp * \l__braid_crossing_start_factor_int
1451
                  - \l_braid_nudge_fp * \l_braid_crossing_end_factor_int
1452
1453
             }
           }
           {0}
1457
           {\neq \cdot fp_eval:n }
1458
```

```
- \l_braid_control_fp * (.5 - \_braid_value:n {gap} * (\seq_count:N \l_braid_
1459
                  * \l__braid_crossing_end_factor_int
1460 %
                 * 1/(\seq_count:N \l__braid_crossing_seq - 1)}
1461
             }
1462
1463
             {\fp_eval:n
1464
                  (\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int} - 1)
                   \__braid_dim_value:n {width}
               }
             }
             {\fp_eval:n
1470
               {
1471
                  \label{locality} $$ l__braid_height_fp $$
1472
                 + \_braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \l__braid_crossing_s
1473
                   \l__braid_nudge_fp * \l__braid_crossing_end_factor_int
1474
1475
             }
          }
Now put those new strands back in the prop.
           \prop_put:NxV \l__braid_strands_prop
1479
1480
           {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpb_int}} \l__braid_tmpa_tl
           \prop_put:NxV \l__braid_strands_prop
           {\seq_item:Nn \l__braid_crossing_seq {\l__braid_tmpa_int}} \l__braid_tmpb_tl
If the strands are more than one apart, the intermediate strands need to be broken as
well.
           \int_compare:nT
1483
           {
1484
             \int_max:nn
1485
             {
1486
               \seq_item:Nn \l__braid_crossing_seq {####1 - 1}
               \seq_item: Nn \l__braid_crossing_seq {####1}
             }
1491
             \int_min:nn
1493
             {
1494
               \seq_item: Nn \l__braid_crossing_seq {####1 - 1}
1495
1496
1497
               \seq_item: Nn \l__braid_crossing_seq {####1}
             }
             > 1
1500
          }
1501
1502
             \int_step_inline:nnnn
1503
             {
1504
               \int min:nn
1505
1506
                 \seq_item: Nn \l__braid_crossing_seq {####1 - 1}
1507
```

```
{
                 \seq_item:Nn \l__braid_crossing_seq {###1}
1510
              }
1511
              + 1}
1512
            {1}
1513
            {
1514
               \int_max:nn
1515
               {
1516
                 \seq_item:Nn \l__braid_crossing_seq {####1 - 1}
               }
               {
                 \seq_item: Nn \l__braid_crossing_seq {####1}
1520
              }
1521
1522
            }
1523
            {
1524
1525
               \prop_get:NnN \l__braid_strands_prop {#######1} \l__braid_tmpa_tl
1526
               \tl_put_right:Nx \l__braid_tmpa_tl
                 {
                   \exp_not:N \__braid_lineto:nn
                   {\phi_0} {\phi_0} = {\phi_0} 
1531
                   {\phi_{\text{p_eval:n}}}
                     {
1532
                       \l__braid_height_fp + \l__braid_nudge_fp
1533
                       + .5 * \l_braid_control_fp / (\seq_count:N \l_braid_crossing_seq - 1)
1534
                       + \_braid_dim_value:n {height} * (####1 - 2)/(\seq_count:N \l__braid_cros
1535
                     }
1536
                   }
1537
                   \exp_not:N \__braid_moveto:nn
                   {\fp_eval:n {(#######1 - 1) * \_braid_dim_value:n {width} }}
                   {\p_eval:n}
1541
1542
                       \l__braid_height_fp
                       - \l__braid_nudge_fp - .5 * \l__braid_control_fp / (\seq_count:N \l__braid
1543
                       + \_braid_dim_value:n {height} * (####1 - 1)/(\seq_count:N \l_braid_cros
1544
1545
                   }
1546
                }
1547
                 \prop_put:NnV \l__braid_strands_prop {#######1} \l__braid_tmpa_tl
               }
          }
1551
Reset the current long
          \int_compare:nTF
1552
1553
             \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpa_int}
             \l__braid_crossing_long_int
          }
1557
          {
1558
            \int_set:Nn \l__braid_crossing_long_int {\seq_item:Nn \l__braid_crossing_seq {\l__br
1559
          }
1560
          {
1561
```

```
1562
          \int_compare:nT
          {
1563
            \seq_item: Nn \l__braid_crossing_seq {\l__braid_tmpb_int}
1564
1565
            \l__braid_crossing_long_int
1566
1567
1568
            \int_set:Nn \l__braid_crossing_long_int {\seq_item:Nn \l__braid_crossing_seq {\l__br
1571
1572
          }
          }
1573
1574
If we're to step the level, increase the height and add a load of coordinates.
        \bool_if:NT \l__braid_step_level_bool
1575
1576
          \fp_add:Nn \l__braid_height_fp { \__braid_dim_value:n {height} }
1577
          \int_step_inline:nnnn {1} {1} {\l__braid_strands_int}
1581
            \prop_get:NnN \l__braid_crossing_permutation_prop
            1582
            \prop_get:NVN \l__braid_inverse_prop
1583
            \l__braid_tmpb_tl \l__braid_tmpa_tl
1584
1585
            \__braid_coordinate:xxxx
1586
            {-\l_braid_tmpb_tl-\int_use:N \l_braid_crossing_int}
1587
            {-rev-\l_braid_tmpa_tl-\int_use:N \l_braid_crossing_int }
1588
            {\phi_0 * \phi_1 * \_ eval:n { (####1 - 1) * \_ braid_dim_value:n {width} }}
            {\fp_to_decimal:N \l__braid_height_fp}
1591
1592
          \int_incr:N \l__braid_crossing_int
1593
        }
1594
      }
1595
1596
      \fp_add:Nn \l__braid_height_fp
1597
1598
        sign(\__braid_dim_value:n {height})
          \__braid_dim_value:n {border~ height}
1600
      }
1601
Add a little bit to the end of each strand, together with some coordinates.
      \int_step_inline:nnnn {1} {1} {\l_braid_strands_int}
1602
1603
        \prop_get:NxN \l__braid_strands_prop {##1} \l__braid_tmpa_tl
        \prop_get:NxN \l__braid_permutation_prop {##1} \l__braid_tmpb_tl
1607
        \tl_put_right:Nx \l__braid_tmpa_tl {
          \exp_not:N \__braid_lineto:nn
1608
          {\phi_{width} } 
1609
          {\fp_to_decimal:N \l__braid_height_fp}
1610
          coordinate (-rev-##1-e)
1611
```

```
coordinate (-\l__braid_tmpb_tl-e)
1612
1613
1614
1615
         \prop_put:NnV \l__braid_strands_prop {##1} \l__braid_tmpa_tl
1616
1617
This is where we actually carry out the drawing commands.
      \int_step_inline:nnnn {1} {1} {\l_braid_strands_int}
1618
1619
         \prop_get:NnN \l__braid_strands_prop {##1} \l__braid_tmpa_tl
1620
         \tl_use:N \l__braid_tmpa_tl
1621
      }
1622
Finally, put a node around the whole braid if it's been named
      \tl_if_empty:cF {tikz@fig@name}
1623
      {
1624
         \tl_gset:cn {pgf@sh@ns@ \tl_use:c{tikz@fig@name} }{rectangle}
1625
         \tl_gset:cx {pgf@sh@np@ \tl_use:c{tikz@fig@name} }{%
1626
           \exp_not:N\def
           \exp_not:N\southwest
             \exp_not:N\pgfqpoint
1630
             {
1631
               \fp_to_dim:n
1632
               {
1633
                 min(0,
1634
                  (\l__braid_strands_int - 1)
1635
1636
                  (\__braid_dim_value:n {width})
1637
               }
             }
1640
             {
1641
               \fp_to_dim:n
1642
               {
1643
                 min(0,
1644
                 \l__braid_length_int * (\__braid_dim_value:n {height})
1645
                 + 2 * sign(\_braid_dim_value:n {height}) *
1646
                  \__braid_dim_value:n {border~ height}
1647
                 )
               }
             }
           }
1651
           \exp_not:N\def
1652
           \exp_not:N\northeast
1653
1654
             \exp_not:N\pgfqpoint
1655
1656
               \fp_to_dim:n
1657
1658
                 max(0,
                  (\l_braid_strands_int - 1)
1661
                  (\__braid_dim_value:n {width})
1662
```

```
}
                                1664
                                            }
                                1665
                                            {
                                1666
                                               \fp_to_dim:n
                                1667
                                               {
                                1668
                                1669
                                                 \l__braid_length_int * (\__braid_dim_value:n {height})
                                1670
                                                 + 2 * sign(\__braid_dim_value:n {height}) *
                                                 \__braid_dim_value:n {border~ height}
                                              }
                                1674
                                            }
                                1675
                                          }
                                1676
                                1677
                                        \pgfgettransform\l__braid_tmpa_tl
                                1678
                                        \tl_gset:cV {pgf@sh@nt@ \tl_use:c{tikz@fig@name} } \l__braid_tmpa_tl
                                1679
                                        \tl_gset:cV {pgf@sh@pi@ \tl_use:c{tikz@fig@name} } \pgfpictureid
                                      \end{scope}
                                1683 }
                               (End definition for \__braid_render:.)
                               These are our interfaces to the TikZ code.
          \__braid_moveto:nn
          \__braid_lineto:nn
                                1684 \cs_new_nopar:Npn \__braid_moveto:nn #1#2
      _braid_curveto:nnnnnn
   \__braid_coordinate:nnnn
                                1686
                                      (#1 pt, #2 pt)
                                1687 }
                                   \cs_new_nopar:Npn \__braid_lineto:nn #1#2
                                      -- (#1 pt, #2 pt)
                                1690
                                1691
                                    \cs_new_nopar:Npn \__braid_curveto:nnnnnn #1#2#3#4#5#6
                                1692
                                1693
                                1694 %
                                       -- + (5 pt, 0) -- + (0 pt, 0pt)
                                      -- +(#1 pt, #2 pt) -- (#5 pt + #3 pt, #6 pt + #4 pt) -- (#5 pt, #6 pt)
                                1695 %
                                      .. controls +(#1 pt, #2 pt) and +(#3 pt, #4 pt)
                                      .. (#5 pt, #6 pt)
                                    \cs_new_nopar:Npn \__braid_coordinate:nnnn #1#2#3#4
                                1700
                                      \coordinate[alias=#2] (#1) at (#3 pt,#4 pt);
                                1702 }
                                1703 \cs_generate_variant:Nn \__braid_coordinate:nnnn {xxxx}
                               (End\ definition\ for\ \_\_braid\_moveto:nn\ and\ others.)
                               Used to calculate intermediate points and tangents on a bezier curve.
\__braid_bezier_point:nnnnn
        \ braid bezier tangent:nnnnn
                                1704 \cs_new_nopar:Npn \__braid_bezier_point:nnnnn #1#2#3#4#5
                                1705 {
                                      \fp_eval:n
                                1706
                                      {
                                1707
                                        (1 - (#1)) * (1 - (#1)) * (1 - (#1)) * (#2)
                                1708
                                1709
```

)

```
3 * (1 - (#1)) * (1 - (#1)) * (#1) * (#3)
        3 * (1 - (#1)) * (#1) * (#1) * (#4)
1713
         (#1) * (#1) * (#1) * (#5)
1715
1716 }
     \cs_new_nopar:Npn \__braid_bezier_tangent:nnnnn #1#2#3#4#5
1717
       \fp_eval:n
1719
1720
         3 * (1 - (#1)) * (1 - (#1)) * (#3 - (#2))
1721
         6 * (1 - (#1)) * (#1) * (#4 - (#3))
1723
1724
        3 * (#1) * (#1) * (#5 - (#4))
1725
1726
1727 }
    \cs_new_nopar:Npn \__braid_do_floor:nnnnn #1#2#3#4#5
1728
1729 {
      \pic[pic~ type=floor,
1730
        xscale=#4,
1731
         yscale=#5,
         at={(#2,#3)},
         braid/every~ floor/.try,
1734
         braid/floor~#1/.try,
1735
1736
1737 }
1738 \cs_generate_variant:Nn \__braid_do_floor:nnnnn {Vxxxx}
(\mathit{End \ definition \ for \ \_braid\_bezier\_point:nnnnn} \ \mathit{and \ \setminus\_braid\_bezier\_tangent:nnnnn})
1739 \ExplSyntaxOff
```