The spath3 package: code

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1 Introduction

The spath3 package is intended as a library for manipulating PGF's soft paths. In between defining a path and using it, PGF stores a path as a soft path where all the defining structure has been resolved into the basic operations but these have not yet been written to the output file. They can therefore still be manipulated by TEX, and as they have a very rigid form (and limited vocabulary), they are relatively easy to modify. This package provides some methods for working with these paths. It was originally not really intended for use by end users but as a foundation on which other packages can be built. However, over the years I've found myself using it at ever higher levels and so a set of interfaces has been designed using TikZ keys.

It also provides the engine that drives a few other packages, such as the calligraphy, knot, and penrose packages. The first two of these are subpackages of this one. The calligraphy package simulates a calligraphic pen stroking a path. The knots package can be used to draw knot (and similar) diagrams.

For usage, see the documentation of the following packages (texdoc <package>):

- · calligraphy
- knots
- penrose
- spath3 (this document is the code, there's another which focuses on usage)

2 Technical Details

The format of a soft path is a sequence of triples of the form \macro {dimension}{dimension}. The macro is one of a short list, the dimensions are coordinates in points. There are certain further restrictions, particularly that every path must begin with a move to, and Bézier curves consist of three triples.

In the original implementation, I wrapped this token list in a **prop** to store useful information along with the path. Over time, this additional structure has proved a little unwieldy and I've pared it back to working primarily with the original soft path as a token list.

A frequent use of this package is to break a path into pieces and do something with each of those pieces. To that end, there are various words that I use to describe the levels of the structure of a path.

At the top level is the path itself. At the bottom level are the triples of the form $\mbox{\mbox{\tt macro{dim}{dim}}}$, as described above. In between these are the segments and components.

A *segment* is a minimal drawing piece. Thus it might be a straight line or a Bézier curve. When a path is broken into segments then each segment is a complete path so it isn't simply a selection of triples from the original path.

A component is a minimal connected section of the path. So every component starts with a move command and continues until the next move command. For ease of implementation (and to enable a copperplate pen in the calligraphy package!), an isolated move is considered as a component. Thus the following path consists of three components:

```
\path (0,0) -- (1,0) (2,0) (3,0) to[out=0,in=90] (4,0);
```

3 Implementation

3.1 Initialisation

```
1 (@@=spath)
    Load the LATEX3 foundation and register us as a LATEX3 package.
  2 \NeedsTeXFormat{LaTeX2e}
  3 \RequirePackage{expl3}
  4 \RequirePackage{pgf}
  5 \ProvidesExplPackage {spath3} {2021/02/21} {2.4} {Functions for
  6 manipulating PGF soft paths}
  7 \RequirePackage{xparse}
    Utilities copied from https://github.com/loopspace/LaTeX3-Utilities for adding
something in braces to a token list. I find I use this quite a lot in my packages.
  8 \cs_new_protected:Nn \__spath_tl_put_right_braced:Nn
  9 {
      \tl_put_right: Nn #1 { { #2 } }
 10
 11 }
 12 \cs_generate_variant:Nn \__spath_tl_put_right_braced:Nn { NV, cV, cv, Nx, cx }
 14 \cs_new_protected: Nn \__spath_tl_gput_right_braced: Nn
 15 {
      \tl_gput_right:Nn #1 { { #2 } }
 16
 17 }
 18 \cs_generate_variant:Nn \__spath_tl_gput_right_braced:Nn { NV, cV, cv, Nx, cx }
 19 \cs_new_protected:Nn \__spath_tl_put_left_braced:Nn
 20 {
      \tl_put_left:Nn #1 { { #2 } }
 21
 22 }
   \cs_generate_variant:Nn \__spath_tl_put_left_braced:Nn { NV, cV, cv, Nx, cx }
   \cs_new_protected:Nn \__spath_tl_gput_left_braced:Nn
   {
 26
      \tl_gput_left:Nn #1 { { #2 } }
 27
 28 }
 29 \cs_generate_variant:Nn \__spath_tl_gput_left_braced:Nn { NV, cV, cv, Nx, cx }
```

I had to think a bit about how to get TEX to work the way I wanted. I'm really defining functions but TEX doesn't really have that concept, even with all the amazing IATEX3 stuff. The main issue I had was with scoping and return values. By default, TEX functions aren't scoped – they work on the same level as the calling functions. To protect the internals from being overwritten, each core function works inside a group. But then I have to work to get the answer out of it. So each of my core functions finishes by storing its return value in an appropriate output variable. The core functions are then wrapped in a more user friendly interface that will take that output and assign it to a variable. This also means that I can deal with local and global versions without duplicating code.

```
30 \tl_new:N \g__spath_output_tl
31 \int_new:N \g__spath_output_int
32 \seq_new:N \g__spath_output_seq
33 \bool_new:N \g__spath_output_bool
```

To avoid creating vast numbers of variables, we provide ourselves with a few that we reuse frequently. For that reason, most of them don't have very exciting names.

These are general purpose variables.

```
\tl_new:N \l__spath_tmpa_tl
35 \tl_new:N \l__spath_tmpb_tl
36 \tl_new:N \l__spath_tmpc_tl
37 \tl_new:N \l__spath_tmpd_tl
38 \tl_new:N \l__spath_tmpe_tl
39 \tl_new:N \l__spath_tmpf_tl
40 \tl_new:N \l__spath_tmpg_tl
41 \tl_new:N \l__spath_tmph_tl
42 \tl_new:N \l__spath_tmpi_tl
44 \seq_new:N \l__spath_tmpa_seq
45 \seq_new:N \l__spath_tmpb_seq
46 \seq_new:N \l__spath_tmpc_seq
48 \dim_new:N \l__spath_tmpa_dim
49 \dim_new:N \l__spath_tmpb_dim
51 \fp_new:N \l__spath_tmpa_fp
52 \fp_new:N \l__spath_tmpb_fp
53 \fp_new:N \l__spath_tmpc_fp
55 \int_new:N \l__spath_tmpa_int
56 \int_new:N \l__spath_tmpb_int
58 \bool_new:N \l__spath_tmpa_bool
```

Whenever I need more than two dim variables it is because I need to remember the position of a move.

```
59 \dim_new:N \l__spath_move_x_dim
60 \dim_new:N \l__spath_move_y_dim
```

Closed paths often need special handling. When it's needed, this will say whether the path is closed or not.

```
61 \ \bool_new:N \ \l_spath_closed_bool
```

The intersection routine can't happen inside a group so we need two token lists to hold the paths that we'll intersect.

```
62 \tl_new:N \l__spath_intersecta_tl
```

```
63 \tl_new:N \l__spath_intersectb_tl
```

We need to be able to compare against the macros that can occur in a soft path so these token lists contain them. These are global constants so that they can be used in other packages.

```
64 \tl_const:Nn \c_spath_moveto_tl {\pgfsyssoftpath@movetotoken}
65 \tl_const:Nn \c_spath_lineto_tl {\pgfsyssoftpath@linetotoken}
66 \tl_const:Nn \c_spath_curveto_tl {\pgfsyssoftpath@curvetotoken}
67 \tl_const:Nn \c_spath_curvetoa_tl {\pgfsyssoftpath@curvetosupportatoken}
68 \tl_const:Nn \c_spath_curvetob_tl {\pgfsyssoftpath@curvetosupportbtoken}
69 \tl_const:Nn \c_spath_closepath_tl {\pgfsyssoftpath@closepathtoken}
```

We will want to be able to use anonymous spaths internally, so we create a global counter that we can use to refer to them.

```
70 \int_new:N \g__spath_anon_int
71 \int_gzero:N \g__spath_anon_int
And some error messages
72 \msg_new:nnn { spath3 } { unknown path construction }
73 { The~ path~ construction~ element~ #1~ is~ not~ currently~ supported.}
```

3.2 Functional Implementation

In the functional approach, we start with a token list containing a soft path and do something to it (either calculate some information or manipulate it in some fashion). We then store that information, or the manipulated path, in an appropriate macro. The macro to store it in is the first argument. These functions occur in two versions, the one with the $\mathfrak g$ makes the assignment global.

\spath_segments_to_seq:Nn \spath_segments_gto_seq:Nn

Splits a soft path into segments, storing the result in a sequence.

```
74 \cs_new_protected_nopar:Npn \__spath_segments_to_seq:n #1
75 {
    \group_begin:
    \tl_set:Nn \l__spath_tmpa_tl {#1}
77
    \tl_clear:N \l__spath_tmpb_tl
    \seq_clear:N \l__spath_tmpa_seq
79
    \dim_zero:N \l__spath_tmpa_dim
80
    \dim_zero:N \l__spath_tmpb_dim
81
82
    \bool_until_do:nn {
83
      \tl_if_empty_p:N \l__spath_tmpa_tl
84
    }
85
86
      \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
      \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
88
      \tl_case:NnF \l__spath_tmpc_tl
89
90
        \c_spath_moveto_tl
91
92
          \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_moveto_tl
93
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
94
          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
95
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
          \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
```

```
100
          \tl_set:Nx \l__spath_tmpd_tl {\tl_head:N \l__spath_tmpa_tl}
102
          \tl_if_eq:NNF \l__spath_tmpd_tl \c_spath_moveto_tl
103
104
             \tl_clear:N \l__spath_tmpb_tl
105
          }
106
107
        }
109
110
        \c_spath_lineto_tl
        {
           \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_moveto_tl
           \tl_put_right:Nx \l__spath_tmpb_tl
            {\dim_use:N \l__spath_tmpa_dim}
            {\dim_use:N \l__spath_tmpb_dim}
116
117
           \tl_put_right:NV \l__spath_tmpb_tl \c_spath_lineto_tl
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
121
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
123
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
124
          \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
125
126
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
127
        }
128
130
        \c_spath_curvetoa_tl
131
          \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_moveto_tl
          \tl_put_right:Nx \l__spath_tmpb_tl
134
            {\dim_use:N \l__spath_tmpa_dim}
135
            {\dim_use:N \l__spath_tmpb_dim}
136
138
           \tl_put_right:NV \l__spath_tmpb_tl \c_spath_curvetoa_tl
           \prg_replicate:nn {2} {
            \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
142
            \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
143
            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
144
            \tl_put_right:Nx \l__spath_tmpb_tl {\tl_head:N \l__spath_tmpa_tl}
145
            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
146
147
148
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
149
          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
151
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
152
          \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
```

```
\dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
154
                         \label{local_spath_tmpa_tl {\tl_tail:} N \l_spath_tmpa_tl} $$ \t {\tl_tail:} N \l_spath_tmpa_tl} $$
155
156
                    }
158
                     \c_spath_closepath_tl
159
160
                          \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_moveto_tl
161
                          \tl_put_right:Nx \l__spath_tmpb_tl
163
                              {\dim\_use: N \ \lback \ \lba
                              {\dim_use:N \l__spath_tmpb_dim}
165
166
                          \tl_put_right:NV \l__spath_tmpb_tl \c_spath_lineto_tl
167
168
                         \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
169
                          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
170
                          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                         \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
                         \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
                         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
175
176
                    }
178
               }
179
180
181
                     \tl_set_eq:NN \l__spath_tmpb_tl \l__spath_tmpc_tl
182
                     \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
                     \label{lem:local_dim_set:Nn local} $$\dim_{set:Nn \local_spath_tmpa_dim {\local_spath_tmpa_tl}} $$
184
                     \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
185
186
                     \tl_put_right:Nx \l__spath_tmpb_tl {{\tl_head:N \l__spath_tmpa_tl}}
187
                     \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
188
                     \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
189
190
               }
191
192
                \tl_if_empty:NF \l__spath_tmpb_tl
                     \seq_put_right:NV \l__spath_tmpa_seq \l__spath_tmpb_tl
               }
196
                \tl_clear:N \l__spath_tmpb_tl
197
           }
198
199
            200
201
           \seq_gset_eq:NN \g__spath_output_seq \l__spath_tmpa_seq
202
            \group_end:
203 }
      \cs_new_protected_nopar:Npn \spath_segments_to_seq:Nn #1#2
205 {
206
            \__spath_segments_to_seq:n {#2}
           \seq_clear_new:N #1
207
```

```
\seq_set_eq:NN #1 \g__spath_output_seq
      \seq_gclear:N \g_spath_output_seq
 209
 210 }
   \cs_generate_variant:Nn \spath_segments_to_seq:Nn {NV, cn, cV, Nv, cv}
 211
    \cs_new_protected_nopar:Npn \spath_segments_gto_seq:Nn #1#2
 212
 213 {
      \__spath_segments_to_seq:n {#2}
 214
      \seq_clear_new:N #1
 215
      \seq_gset_eq:NN #1 \g__spath_output_seq
      \seq_gclear:N \g__spath_output_seq
 217
 218 }
 (End definition for \spath_segments_to_seq:Nn and \spath_segments_gto_seq:Nn.)
Splits a soft path into components, storing the result in a sequence or a clist.
 220 \cs_new_protected_nopar:Npn \__spath_components_to_seq:n #1
221 {
      \group_begin:
222
      \tl_set:Nn \l__spath_tmpa_tl {#1}
 223
      \seq_clear:N \l__spath_tmpa_seq
      \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_moveto_tl
 226
      \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_moveto_tl
 227
      \bool_do_until:nn {
 228
 229
        \tl_if_empty_p:N \l__spath_tmpa_tl
 230
 231
        \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
 232
        \tl_if_eq:NNT \l__spath_tmpc_tl \c_spath_moveto_tl
 234
          \seq_put_right:NV \l__spath_tmpa_seq \l__spath_tmpb_tl
 235
          \tl_clear:N \l__spath_tmpb_tl
 236
 237
        \tl_if_single:NTF \l__spath_tmpc_tl
          \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpc_tl
       }
 241
        {
 242
          \tl_put_right:Nx \l__spath_tmpb_tl {{\l__spath_tmpc_tl}}
 243
 244
        \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
 245
 246
 247
      \seq_gclear:N \g__spath_output_seq
 248
      \seq_gset_eq:NN \g__spath_output_seq \l__spath_tmpa_seq
      \group_end:
 250
 251
    \cs_new_protected_nopar:Npn \spath_components_to_seq:Nn #1#2
 252
 253 {
      \__spath_components_to_seq:n {#2}
 254
      \seq_clear_new:N #1
 255
```

\spath_components_to_seq:Nn \spath_components_gto_seq:Nn

\spath components to clist:Nn

\spath components gto clist:Nn

\seq_set_eq:NN #1 \g__spath_output_seq

\seq_gclear:N \g__spath_output_seq

256

```
\cs_generate_variant:Nn \spath_components_to_seq:Nn {NV, cn, cV, cv, Nv}
                           \cs_new_protected_nopar:Npn \spath_components_gto_seq:Nn #1#2
                        261
                              \__spath_components_to_seq:n {#2}
                         262
                             \seq_clear_new:N #1
                         263
                             \seq_gset_eq:NN #1 \g__spath_output_seq
                         264
                             \seq_gclear:N \g_spath_output_seq
                         265
                           \cs_generate_variant:Nn \spath_components_gto_seq:Nn {NV, cn, cV, cv, Nv}
                           \cs_new_protected_nopar:Npn \spath_components_to_clist:Nn #1#2
                         269 {
                              \__spath_components_to_seq:n {#2}
                         270
                             \clist_clear_new:N #1
                         271
                              \clist_set_from_seq:NN #1 \g__spath_output_seq
                              \seq_gclear:N \g__spath_output_seq
                         273
                         274 }
                           \cs_generate_variant:Nn \spath_components_to_clist:Nn {NV, cn, cV, cv, Nv}
                         275
                           \cs_new_protected_nopar:Npn \spath_components_gto_clist:Nn #1#2
                         277 {
                              \__spath_components_to_seq:n {#2}
                         278
                             \clist_clear_new:N #1
                         279
                             \clist_gset_from_seq:NN #1 \g__spath_output_seq
                         280
                              \seq_gclear:N \g__spath_output_seq
                         281
                         282 }
                        (End definition for \spath_components_to_seq:Nn and others.)
      \spath_length:n
                       Counts the number of triples in the path.
                         284 \cs_new_protected_nopar:Npn \spath_length:n #1
                        285 {
                              \int \int_{\infty}^{\infty} {tl_count:n {#1} / 3}
                        287 }
                         288 \cs_generate_variant:Nn \spath_length:n {V}
                       (End definition for \spath_length:n.)
\spath_reallength:Nn
                       The real length of a path is the number of triples that actually draw something (that is,
\spath_greallength:Nn
                       the number of lines, curves, and closepaths).
                           \cs_new_protected_nopar:Npn \__spath_reallength:n #1
                        290 {
                              \group_begin:
                         291
                              \int_set:Nn \l__spath_tmpa_int {0}
                         292
                              \tl_map_inline:nn {#1} {
                         293
                                \tl_set:Nn \l__spath_tmpa_tl {##1}
                         294
                                \tl_case:NnT \l__spath_tmpa_tl
                         295
                         296
                                  \c_spath_lineto_tl {}
                         297
                                  \c_spath_curveto_tl {}
                         298
                                  \c_spath_closepath_tl {}
                         299
                         300
                         301
                                  \int_incr:N \l__spath_tmpa_int
```

```
}
 303
      }
 304
      \int_gzero:N \g__spath_output_int
 305
      \int_gset_eq:NN \g__spath_output_int \l__spath_tmpa_int
 306
      \group_end:
 307
 308 }
    \cs_new_protected_nopar:Npn \spath_reallength:Nn #1#2
 309
 310
       \__spath_reallength:n {#2}
 311
      \int_set_eq:NN #1 \g__spath_output_int
 312
      \verb|\int_gzero:N \g_spath_output_int| \\
 313
 314
    \cs_generate_variant:Nn \spath_reallength:Nn {NV, cn, cV, Nv, cv}
 315
    \cs_new_protected_nopar:Npn \spath_greallength:Nn #1#2
 316
 317
      \__spath_reallength:n {#2}
 318
      \int_gset_eq:NN #1 \g__spath_output_int
 319
      \int_gzero:N \g__spath_output_int
 320
 321 }
    \cs_generate_variant:Nn \spath_greallength:Nn {NV, cn, cV}
(End definition for \spath_reallength:Nn and \spath_greallength:Nn.)
```

\spath_numberofcomponents:Nn \spath gnumberofcomponents:Nn

A component is a continuous segment of the path, separated by moves. Successive moves are not collapsed, and zero length moves count.

```
\cs_new_protected_nopar:Npn \__spath_numberofcomponents:n #1
324
     \group_begin:
325
     \int_set:Nn \l__spath_tmpa_int {0}
326
     \tl_map_inline:nn {#1} {
327
       \tl_set:Nn \l__spath_tmpa_tl {##1}
328
       \tl_case:Nn \l__spath_tmpa_tl
329
330
         \c_spath_moveto_tl
331
332
           \int_incr:N \l__spath_tmpa_int
333
334
335
       }
     \int_gzero:N \g__spath_output_int
337
     \int_gset_eq:NN \g__spath_output_int \l__spath_tmpa_int
338
339
     \group_end:
340 }
   \cs_new_protected_nopar:Npn \spath_numberofcomponents:Nn #1#2
341
  {
342
     \__spath_numberofcomponents:n {#2}
343
     \int_set_eq:NN #1 \g_spath_output_int
344
     \int_gzero:N \g__spath_output_int
345
346 }
   \cs_generate_variant:Nn \spath_numberofcomponents:Nn {NV, cn, cV, Nv}
   \cs_new_protected_nopar:Npn \spath_gnumberofcomponents:Nn #1#2
349
     \__spath_numberofcomponents:n {#2}
350
     \int_gset_eq:NN #1 \g__spath_output_int
351
```

```
\verb|\int_gzero:N \ \g__spath_output_int|
                            353 }
                            354 \cs_generate_variant:Nn \spath_gnumberofcomponents:Nn {NV, cn, cV, Nv}
                           (End definition for \spath_numberofcomponents:Nn and \spath_gnumberofcomponents:Nn.)
                          The starting point of the path.
 \spath_initialpoint:Nn
\spath_ginitialpoint:Nn
                            355 \cs_new_protected_nopar:Npn \__spath_initialpoint:n #1
                            356 {
                                 \group_begin:
                            357
                                 \tl_clear:N \l__spath_tmpa_tl
                            358
                                 \tl_set:Nx \l__spath_tmpa_tl
                            350
                            360
                                   { \tl_item:nn {#1} {2} }
                            361
                                    { \tl_item:nn {#1} {3} }
                            362
                            363
                                 \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
                            364
                                 \group_end:
                            366 }
                            367 \cs_new_protected_nopar:Npn \spath_initialpoint:Nn #1#2
                            368 {
                                 \__spath_initial point:n {#2}
                            369
                                 \tl_set_eq:NN #1 \g__spath_output_tl
                            370
                                 \tl_gclear:N \g_spath_output_tl
                            371
                            372 }
                            373 \cs_generate_variant:Nn \spath_initialpoint:Nn {NV, cn, cV, Nv}
                            374 \cs_new_protected_nopar:Npn \spath_ginitialpoint:Nn #1#2
                            375 {
                            376
                                  \__spath_initialpoint:n {#2}
                            377
                                 \tl_gset_eq:NN #1 \g__spath_output_tl
                                 \verb|\tl_gclear:N \g_spath_output_tl|\\
                            379 }
                            380 \cs_generate_variant:Nn \spath_ginitialpoint:Nn {NV, cn, cV, Nv}
                           (End definition for \spath_initialpoint:Nn and \spath_ginitialpoint:Nn.)
   \spath_finalpoint:Nn
                          The final point of the path.
  \spath_gfinalpoint:Nn
                            381 \cs_new_protected_nopar:Npn \__spath_finalpoint:n #1
                            382 {
                            383
                                 \group_begin:
                                 \tl_set:Nn \l__spath_tmpa_tl {#1}
                            384
                                 \tl_reverse:N \l__spath_tmpa_tl
                            385
                                 \tl_clear:N \l__spath_tmpb_tl
                            386
                                 \tl_set:Nx \l__spath_tmpb_tl
                            387
                                 ₹
                            388
                                    { \tl_item:Nn \l__spath_tmpa_tl {2} }
                            389
                                    { \tl_item: Nn \l__spath_tmpa_tl {1} }
                            390
                            391
                                 \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                            392
                            394 }
                            395 \cs_new_protected_nopar:Npn \spath_finalpoint:Nn #1#2
                            396 {
                                 \__spath_finalpoint:n {#2}
                            397
                                 \tl_set_eq:NN #1 \g__spath_output_tl
                            398
```

```
\tl_gclear:N \g_spath_output_tl
 400 }
    \cs_generate_variant:Nn \spath_finalpoint:Nn {NV, cn, cV, Nv}
 401
    \cs_new_protected_nopar:Npn \spath_gfinalpoint:Nn #1#2
    {
 403
      \__spath_finalpoint:n {#2}
      \tl_gset_eq:NN #1 \g__spath_output_tl
 405
      \tl_gclear:N \g_spath_output_tl
 407 }
 408 \cs_generate_variant:Nn \spath_gfinalpoint:Nn {NV, cn, cV, Nv}
(End definition for \spath_finalpoint:Nn and \spath_gfinalpoint:Nn.)
Get the last move on the path.
 409 \cs_new_protected_nopar:Npn \__spath_finalmovepoint:n #1
 410 {
      \group_begin:
 411
      \tl_set:Nn \l__spath_tmpc_tl { {0pt} {0pt} }
 412
      \tl_set:Nn \l__spath_tmpa_tl {#1}
 413
      \bool_do_until:nn
 414
 415
        \tl_if_empty_p:N \l__spath_tmpa_tl
 416
      }
 417
 418
        \tl_set:Nx \l__spath_tmpb_tl {\tl_head:N \l__spath_tmpa_tl}
 419
        \tl_case:Nn \l__spath_tmpb_tl
 420
 421
          \c_spath_moveto_tl
 422
 423
             \tl_set:Nx \l__spath_tmpc_tl
 424
 425
               { \tl_item: Nn \l__spath_tmpa_tl {2} }
 426
               { \tl_item:Nn \l__spath_tmpa_tl {3} }
 427
 428
          }
        }
 430
        \prg_replicate:nn {3}
 431
 432
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
 433
 434
 435
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpc_tl
 436
      \group_end:
 437
 438 }
    \cs_new_protected_nopar:Npn \spath_finalmovepoint:Nn #1#2
 439
 440 {
 441
       \__spath_finalmovepoint:n {#2}
 442
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
 443
 444 }
    \cs_generate_variant:Nn \spath_finalmovepoint:Nn {NV, cn, cV}
 445
    \cs_new_protected_nopar:Npn \spath_gfinalmovepoint:Nn #1#2
 446
 447 {
```

\spath_finalmovepoint:Nn

\spath_gfinalmovepoint:Nn

__spath_finalmovepoint:n {#2}

```
\tl_gset_eq:NN #1 \g__spath_output_tl
                           \tl_gclear:N \g__spath_output_tl
                      450
                      451 }
                      452 \cs_generate_variant:Nn \spath_gfinalmovepoint:Nn {NV, cn, cV}
                     (End definition for \spath_finalmovepoint:Nn and \spath_gfinalmovepoint:Nn.)
                     This computes the reverse of the path.
 \spath_reverse:Nn
\spath_greverse:Nn
                      453 \cs_new_protected_nopar:Npn \__spath_reverse:n #1
                      454 {
                            \group_begin:
                      455
                            \tl_set:Nn \l__spath_tmpa_tl {#1}
                      456
                           \tl_clear:N \l__spath_tmpb_tl
                           \tl_clear:N \l__spath_tmpd_tl
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                           \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
                       461
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                      462
                           \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
                      463
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                      464
                      465
                           \tl_put_left:Nx \l__spath_tmpd_tl
                      466
                       467
                              {\dim_use:N \l__spath_tmpa_dim}
                       468
                              {\dim_use:N \l__spath_tmpb_dim}
                       469
                           }
                      470
                      471
                           \bool_set_false:N \l__spath_closed_bool
                      472
                      473
                           \bool_until_do:nn {
                      474
                              \tl_if_empty_p:N \l__spath_tmpa_tl
                      475
                      476
                      477
                       478
                              \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
                       479
                              \tl_case:NnTF \l__spath_tmpc_tl
                       480
                       481
                                \c_spath_moveto_tl {
                       482
                      483
                                  \bool_if:NT \l__spath_closed_bool
                      484
                      485
                                    \tl_put_right:NV \l__spath_tmpd_tl \c_spath_closepath_tl
                      486
                                    \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpd_tl}
                       487
                                    \tl_put_right:Nx \l__spath_tmpd_tl
                                    {
                                      { \tl_head:N \l__spath_tmpd_tl }
                                      { \tl_head:N \l__spath_tmpe_tl }
                                    }
                      492
                                  }
                      493
                                  \bool_set_false:N \l__spath_closed_bool
                      494
                                  \tl_put_left:NV \l__spath_tmpd_tl \c_spath_moveto_tl
                      495
                                  \tl_put_left:NV \l__spath_tmpb_tl \l__spath_tmpd_tl
                      496
                                  \tl_clear:N \l__spath_tmpd_tl
                      497
```

```
\c_spath_lineto_tl {
499
           \tl_put_left:NV \l__spath_tmpd_tl \c_spath_lineto_tl
500
501
         \c_spath_curveto_tl {
502
           \tl_put_left:NV \l__spath_tmpd_tl \c_spath_curvetoa_tl
503
504
         \c_spath_curvetoa_tl {
505
           \tl_put_left:NV \l__spath_tmpd_tl \c_spath_curveto_tl
506
         \c_spath_curvetob_tl {
508
           \tl_put_left:NV \l__spath_tmpd_tl \c_spath_curvetob_tl
509
510
       }
511
       {
512
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
513
514
         \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
515
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
516
         \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
         \tl_put_left:Nx \l__spath_tmpd_tl
520
521
           {\dim_use:N \l__spath_tmpa_dim}
522
           {\dim_use:N \l__spath_tmpb_dim}
523
524
525
       }
526
527
         \tl_if_eq:NNTF \l__spath_tmpc_tl \c_spath_closepath_tl
529
530
           \bool_set_true: N \l__spath_closed_bool
531
         }
532
           \msg_warning:nnx
533
           { spath3 }
534
           { unknown path construction }
535
           {\l_spath_tmpc_tl }
536
537
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
541
542
      }
543
     }
544
545
     \bool_if:NT \l__spath_closed_bool
546
547
548
       \tl_put_right:NV \l__spath_tmpd_tl \c_spath_closepath_tl
       \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpd_tl}
550
       \tl_put_right:Nx \l__spath_tmpd_tl
551
         { \tl_head:N \l__spath_tmpd_tl }
552
```

```
}
                             554
                                  }
                             555
                             556
                                  \bool_set_false:N \l__spath_closed_bool
                             557
                                  \tl_put_left:NV \l__spath_tmpd_tl \c_spath_moveto_tl
                             558
                                  \tl_put_left:NV \l__spath_tmpb_tl \l__spath_tmpd_tl
                             559
                             560
                                  \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                             561
                                   \group_end:
                             562
                             563 }
                                \cs_new_protected_nopar:Npn \spath_reverse:Nn #1#2
                             564
                             565 {
                                   \__spath_reverse:n {#2}
                             566
                                   \tl_set_eq:NN #1 \g__spath_output_tl
                             567
                                   \tl_gclear:N \g__spath_output_tl
                             568
                             569 }
                                \cs_generate_variant:Nn \spath_reverse:Nn {NV, cn, cV, Nv}
                                \cs_new_protected_nopar:Npn \spath_reverse:N #1
                             572 {
                                  \spath_reverse:NV #1#1
                             573
                             574 }
                                \cs_generate_variant:Nn \spath_reverse:N {c}
                                \verb|\cs_new_protected_nopar:Npn \spath_greverse:Nn #1#2|
                             576
                             577 {
                                   \__spath_reverse:n {#2}
                             578
                                  \tl_gset_eq:NN #1 \g_spath_output_tl
                             579
                                  \tl_gclear:N \g__spath_output_tl
                             580
                             581 }
                             582 \cs_generate_variant:Nn \spath_greverse:Nn {NV, cn, cV, Nv}
                                \cs_new_protected_nopar:Npn \spath_greverse:N #1
                                   \spath_greverse:NV #1#1
                             585
                             586 }
                             587 \cs_generate_variant:Nn \spath_greverse:N {c}
                            (End definition for \spath_reverse:Nn and \spath_greverse:Nn.)
                           This is the first thing that the path does (after the initial move).
 \spath_initialaction:Nn
\spath_ginitialaction:Nn
                                \cs_new_protected_nopar:Npn \__spath_initialaction:n #1
                             588
                             589 {
                                   \group_begin:
                             590
                                  \tl_clear:N \l__spath_tmpa_tl
                             591
                                  \int_compare:nT
                             592
                             593
                                     \t: \{\#1\} > 3
                                  }
                             595
                             596
                                     \tl_set:Nx \l__spath_tmpa_tl
                             597
                             598
                                       \tl_item:Nn {#1} {4}
                             599
                             600
                             601
                                   \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
```

{ \tl_head:N \l__spath_tmpe_tl }

553

```
\group_end:
 604 }
    \cs_new_protected_nopar:Npn \spath_initialaction:Nn #1#2
 605
 606
      \__spath_initialaction:n {#2}
 607
      \tl_set_eq:NN #1 \g__spath_output_tl
 608
      \tl_gclear:N \g__spath_output_tl
 609
 610 }
    \cs_generate_variant:Nn \spath_initialaction:Nn {NV}
    \cs_new_protected_nopar:Npn \spath_ginitialaction:Nn #1#2
 613 {
       \__spath_initialaction:n {#2}
 614
      \tl_gset_eq:NN #1 \g__spath_output_tl
 615
      \tl_gclear:N \g__spath_output_tl
 616
 617 }
 618 \cs_generate_variant:Nn \spath_ginitialaction:Nn {NV}
(\mathit{End \ definition \ for \ \ } \texttt{spath\_initialaction:Nn} \ \mathit{and \ \ } \texttt{spath\_ginitialaction:Nn.})
This is the last thing that the path does.
 619 \cs_new_protected_nopar:Npn \__spath_finalaction:n #1
 620 {
      \group_begin:
 621
      \tl_clear:N \l__spath_tmpb_tl
 622
      \int_compare:nT
 623
 624
         \t: \{#1\} > 3
 625
      }
 626
 627
         \tl_set:Nn \l__spath_tmpa_tl {#1}
 628
         \tl_reverse:N \l__spath_tmpa_tl
 629
         \tl_set:Nx \l__spath_tmpb_tl
 630
 631
 632
           \tl_item:Nn \l__spath_tmpa_tl {3}
        }
 633
         \tl_if_eq:NNT \l__spath_tmpb_tl \c_spath_curvetoa_tl
           \tl_set_eq:NN \l__spath_tmpb_tl \c_spath_curveto_tl
 636
 637
 638
      \tl_gset_eq:NN \g_spath_output_tl \l_spath_tmpb_tl
 639
      \group_end:
 640
 641 }
    \cs_new_protected_nopar:Npn \spath_finalaction:Nn #1#2
 642
 643
       \__spath_finalaction:n {#2}
 645
      \tl_set_eq:NN #1 \g__spath_output_tl
 646
      \tl_gclear:N \g__spath_output_tl
 647
    \cs_generate_variant:Nn \spath_finalaction:Nn {NV}
 648
    \cs_new_protected_nopar:Npn \spath_gfinalaction:Nn #1#2
 649
 650 {
       \_spath_finalaction:n {#2}
 651
```

\spath_finalaction:Nn

\spath_gfinalaction:Nn

\tl_gset_eq:NN #1 \g__spath_output_tl

```
\tl_gclear:N \g_spath_output_tl
                   654 }
                   \mbox{\cs\_generate\_variant:Nn \spath\_gfinalaction:Nn {NV}}
                  (End definition for \spath_finalaction:Nn and \spath_gfinalaction:Nn.)
\spath_minbb:Nn
                  This computes the minimum (bottom left) of the bounding box of the path.
\spath_gminbb:Nn
                      \cs_new_protected_nopar:Npn \__spath_minbb:n #1
                    656
                    657 {
                         \group_begin:
                    658
                         \tl_set:Nn \l__spath_tmpa_tl {#1}
                    659
                         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                    660
                         \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
                    661
                         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                         \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
                         \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                         \bool_until_do:nn {
                    665
                           \tl_if_empty_p:N \l__spath_tmpa_tl
                    666
                        }
                    667
                        {
                    668
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                    669
                           \dim_set:Nn \l__spath_tmpa_dim
                    670
                           {\dim_min:nn {\tl_head:N \l__spath_tmpa_tl} {\l__spath_tmpa_dim}}
                    671
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                    672
                           \dim_set:Nn \l__spath_tmpb_dim
                    673
                           674
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                    675
                    676
                         \tl_clear:N \l__spath_tmpb_tl
                    677
                         \tl_put_right:Nx \l__spath_tmpb_tl
                    678
                    679
                           {\dim_use:N \l__spath_tmpa_dim}
                    680
                           {\dim_use:N \l__spath_tmpb_dim}
                    681
                    682
                         \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                    684
                         \group_end:
                   685 }
                      \cs_new_protected_nopar:Npn \spath_minbb:Nn #1#2
                   686
                      {
                   687
                         \__spath_minbb:n {#2}
                    688
                        \tl_set_eq:NN #1 \g__spath_output_tl
                    689
                        \tl_gclear:N \g__spath_output_tl
                    690
                    691 }
                       \cs_generate_variant:Nn \spath_minbb:Nn {NV, cn, cV}
                    692
                       \cs_new_protected_nopar:Npn \spath_gminbb:Nn #1#2
                    693
                    694 {
                         \__spath_minbb:n {#2}
                    695
                    696
                        \tl_gset_eq:NN #1 \g__spath_output_tl
                    697
                        \tl_gclear:N \g__spath_output_tl
                   698
                    699 \cs_generate_variant:Nn \spath_gminbb:Nn {NV, cn, cV}
                  (End definition for \spath_minbb:Nn and \spath_gminbb:Nn.)
```

```
This computes the maximum (top right) of the bounding box of the path.
     \spath_maxbb:Nn
    \spath_gmaxbb:Nn
                        700 \cs_new_protected_nopar:Npn \__spath_maxbb:n #1
                        701 {
                            \group_begin:
                        702
                            \tl_set:Nn \l__spath_tmpa_tl {#1}
                        703
                            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                        704
                            \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
                        705
                            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                        706
                            \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
                            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                            \bool_until_do:nn {
                        710
                              \tl_if_empty_p:N \l__spath_tmpa_tl
                        711
                            {
                              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                        713
                              \dim_set:Nn \l__spath_tmpa_dim
                        714
                              715
                              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                        716
                              \dim_set:Nn \l__spath_tmpb_dim
                              718
                              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                        719
                        720
                            }
                            \tl_clear:N \l__spath_tmpb_tl
                        721
                            \tl_put_right:Nx \l__spath_tmpb_tl
                            {
                              {\dim_use:N \l__spath_tmpa_dim}
                        724
                              {\dim_use:N \l__spath_tmpb_dim}
                        725
                        726
                            \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                        727
                            \group_end:
                        729 }
                        730 \cs_new_protected_nopar:Npn \spath_maxbb:Nn #1#2
                        731 {
                            \__spath_maxbb:n {#2}
                            \tl_set_eq:NN #1 \g__spath_output_tl
                        733
                            \tl_gclear:N \g_spath_output_tl
                        734
                       735 }
                        736 \cs_generate_variant:Nn \spath_maxbb:Nn {NV, cn, cV}
                        737 \cs_new_protected_nopar:Npn \spath_gmaxbb:Nn #1#2
                        738 {
                            \__spath_maxbb:n {#2}
                        739
                            \tl_gset_eq:NN #1 \g__spath_output_tl
                            \tl_gclear:N \g_spath_output_tl
                        741
                        742 }
                        743 \cs_generate_variant:Nn \spath_gmaxbb:Nn {NV, cn, cV}
                      (End definition for \spath_maxbb:Nn and \spath_gmaxbb:Nn.)
                      This saves a soft path to the auxile. The first argument is the macro that will be assigned
\spath_save_to_aux:Nn
                      to the soft path when the aux file is read back in.
\spath_save_to_aux:N
                        744 \int_set:Nn \l__spath_tmpa_int {\char_value_catcode:n {'@}}
                        745 \char_set_catcode_letter:N @
                        746 \cs_new_protected_nopar:Npn \spath_save_to_aux:Nn #1#2 {
```

\tl_if_empty:nF {#2}

```
748
       \tl_clear:N \l__spath_tmpa_tl
749
       \tl_put_right:Nn \l__spath_tmpa_tl {
750
         \ExplSyntax0n
751
         \tl_clear:N #1
752
         \tl_set:Nn #1 {#2}
753
         \ExplSyntaxOff
754
755
       \protected@write\@auxout{}{
757
         \tl_to_str:N \l__spath_tmpa_tl
758
     }
759
760 }
   \char_set_catcode:nn {'@} {\l__spath_tmpa_int}
   \cs_generate_variant:Nn \spath_save_to_aux:Nn {cn, cV, NV}
   \cs_new_protected_nopar:Npn \spath_save_to_aux:N #1
763
764 {
     \tl_if_exist:NT #1
765
       \spath_save_to_aux:NV #1#1
768
769 }
```

(End definition for \spath_save_to_aux:Nn and \spath_save_to_aux:N.)

3.3 Path Manipulation

These functions all manipulate a soft path. They come with a variety of different argument specifications. As a general rule, the first argument is the macro in which to store the modified path, the second is the path to manipulate, and the rest are the information about what to do. There is always a variant in which the path is specified by a macro and restored back in that same macro.

\spath_translate:Nnnn \spath_translate:Nnn \spath_gtranslate:Nnnn \spath_gtranslate:Nnn

Translates a path by an amount.

```
770 \cs_new_protected_nopar:Npn \__spath_translate:nnn #1#2#3
771 {
     \group_begin:
     \tl_set:Nn \l__spath_tmpa_tl {#1}
773
     \tl_clear:N \l__spath_tmpb_tl
774
     \bool_until_do:nn {
775
       \tl_if_empty_p:N \l__spath_tmpa_tl
776
    }
    {
778
       \tl_put_right:Nx \l__spath_tmpb_tl {\tl_head:N \l__spath_tmpa_tl}
779
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
780
781
       \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl + #2}
782
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
783
       \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_t1 + #3}
785
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
786
787
       \tl_put_right:Nx \l__spath_tmpb_tl
788
789
```

```
{\dim_use:N \l__spath_tmpb_dim}
                              791
                              792
                              793
                                   \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                              794
                                   \group_end:
                              795
                              796 }
                                 \cs_generate_variant:Nn \__spath_translate:nnn {nVV}
                                 \cs_new_protected_nopar:Npn \spath_translate:Nnnn #1#2#3#4
                              799
                                   \__spath_translate:nnn {#2}{#3}{#4}
                              800
                                   \tl_set_eq:NN #1 \g__spath_output_tl
                              801
                                   \t_gclean: N \g_spath_output_tl
                              802
                              803
                                 \cs_generate_variant:Nn \spath_translate:Nnnn {NVxx, NVVV, NVnn}
                              804
                                 \cs_new_protected_nopar:Npn \spath_translate:Nnn #1#2#3
                              805
                                {
                              806
                                   \spath_translate:NVnn #1#1{#2}{#3}
                              807
                              808 }
                                 \cs_generate_variant:Nn \spath_translate:Nnn {NVV, cnn, cVV}
                                 \cs_new_protected_nopar:Npn \spath_gtranslate:Nnnn #1#2#3#4
                              811 {
                                   \_spath_translate:nnn {#2}{#3}{#4}
                              812
                                   \tl_gset_eq:NN #1 \g__spath_output_tl
                              813
                                   \tl_gclear:N \g__spath_output_tl
                              814
                              815 }
                                 \cs_generate_variant:Nn \spath_gtranslate:Nnnn {NVxx, NVVV, NVnn}
                              816
                                 \cs_new_protected_nopar:Npn \spath_gtranslate:Nnn #1#2#3
                              817
                                   \spath_gtranslate:NVnn #1#1{#2}{#3}
                              819
                              820 }
                              821 \cs_generate_variant:Nn \spath_gtranslate:Nnn {NVV, cnn, cVV}
                                 This variant allows for passing the coordinates as a single braced group as it strips
                            off the outer braces of the second argument.
                                 \cs_new_protected_nopar:Npn \spath_translate:Nn #1#2
                                   \spath_translate:Nnn #1 #2
                              825 }
                                \cs_generate_variant:Nn \spath_translate:Nn {NV}
                                \cs_new_protected_nopar:Npn \spath_gtranslate:Nn #1#2
                              828 {
                                   \spath_gtranslate:Nnn #1 #2
                              829
                              830 }
                              831 \cs_generate_variant:Nn \spath_gtranslate:Nn {NV}
                             (End\ definition\ for\ \verb|\spath_translate:Nnnn|\ and\ others.)
                            Translates a path so that it starts at a point.
\spath_translate_to:Nnnn
  \spath_translate_to:Nnn
                              832 \cs_new_protected_nopar:Npn \__spath_translate_to:nnn #1#2#3
\spath_gtranslate_to:Nnnn
                              833 {
\spath_gtranslate_to:Nnn
                                   \group_begin:
                              834
                                   \spath_initialpoint:Nn \l__spath_tmpa_tl {#1}
                              835
                              836
                                   \dim_set:Nn \l__spath_tmpa_dim
                              837
```

{\dim_use:N \l__spath_tmpa_dim}

790

```
{
 838
        #2
 839
 840
        \tl_item:Nn \l__spath_tmpa_tl {1}
 841
 842
      \dim_set:Nn \l__spath_tmpb_dim
 843
      {
 844
        #3
 845
 847
        \tl_item:Nn \l__spath_tmpa_tl {2}
 848
 849
      \__spath_translate:nVV {#1} \l__spath_tmpa_dim \l__spath_tmpb_dim
 850
      \group_end:
 851
 852 }
    \cs_new_protected_nopar:Npn \spath_translate_to:Nnnn #1#2#3#4
 853
    {
 854
      \__spath_translate_to:nnn {#2}{#3}{#4}
 855
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
 858 }
    \cs_generate_variant:Nn \spath_translate_to:Nnnn {NVxx, NVVV, NVnn}
    \cs_new_protected_nopar:Npn \spath_translate_to:Nnn #1#2#3
 860
    {
 861
      \spath_translate_to:NVnn #1#1{#2}{#3}
 862
 863 }
    \cs_generate_variant:Nn \spath_translate_to:Nnn {NVV, cnn, cVV}
 864
    \cs_new_protected_nopar:Npn \spath_gtranslate_to:Nnnn #1#2#3#4
 865
 866
      \__spath_translate_to:nnn {#2}{#3}{#4}
 868
      \tl_gset_eq:NN #1 \g__spath_output_tl
 869
      \tl_gclear:N \g__spath_output_tl
 870 }
    \cs_generate_variant:Nn \spath_gtranslate_to:Nnnn {NVxx, NVVV, NVnn}
    \cs_new_protected_nopar:Npn \spath_gtranslate_to:Nnn #1#2#3
 872
 873
      \spath_gtranslate_to:NVnn #1#1{#2}{#3}
 874
 875 }
    \cs_generate_variant:Nn \spath_gtranslate_to:Nnn {NVV, cnn, cVV}
    This variant allows for passing the coordinates as a single braced group as it strips
off the outer braces of the second argument.
    \cs_new_protected_nopar:Npn \spath_translate_to:Nn #1#2
 878 {
      \spath_translate_to:Nnn #1 #2
 879
 880 }
    \cs_generate_variant:Nn \spath_translate_to:Nn {NV}
    \cs_new_protected_nopar:Npn \spath_gtranslate_to:Nn #1#2
 883
      \spath_gtranslate_to:Nnn #1 #2
 885 }
 886 \cs_generate_variant:Nn \spath_gtranslate_to:Nn {NV}
(End definition for \spath translate to:Nnnn and others.)
```

```
Scale a path.
\spath_scale:Nnnn
 \spath_scale:Nnn
                      887 \cs_new_protected_nopar:Npn \__spath_scale:nnn #1#2#3
\spath_gscale:Nnnn
                     888 {
\spath_gscale:Nnn
                           \group_begin:
                     889
                           \tl_set:Nn \l__spath_tmpa_tl {#1}
                      890
                           \tl_clear:N \l__spath_tmpb_tl
                      891
                           \bool_until_do:nn {
                      892
                             \tl_if_empty_p:N \l__spath_tmpa_tl
                      893
                             \tl_put_right:Nx \l__spath_tmpb_tl {\tl_head:N \l__spath_tmpa_tl}
                             \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                      897
                      898
                             \fp_set:\n \l__spath_tmpa_fp {\tl_head:\n \l__spath_tmpa_tl * #2}
                      899
                             \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                      900
                      901
                             \fp_set:\n \l__spath_tmpb_fp {\tl_head:\nabla \l__spath_tmpa_tl * #3}
                      902
                             \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                      903
                             \tl_put_right:Nx \l__spath_tmpb_tl
                               {\fp_to_dim:N \l__spath_tmpa_fp}
                      907
                               {\fp_to_dim:N \l__spath_tmpb_fp}
                      908
                      909
                      910
                           \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                      911
                           \group_end:
                      912
                      913 }
                         \cs_new_protected_nopar:Npn \spath_scale:Nnnn #1#2#3#4
                      914
                      915 {
                           \_spath_scale:nnn {#2}{#3}{#4}
                      916
                           \tl_set_eq:NN #1 \g__spath_output_tl
                      917
                           \tl_gclear:N \g__spath_output_tl
                      918
                      919 }
                      920 \cs_generate_variant:Nn \spath_scale:Nnnn {NVnn, Nnxx}
                         \cs_new_protected_nopar:Npn \spath_scale:Nnn #1#2#3
                      921
                      922 {
                           \spath_scale:NVnn #1#1{#2}{#3}
                      923
                      924 }
                      925 \cs_generate_variant:Nn \spath_scale:Nnn {cnn, cVV, NVV}
                      926 \cs_new_protected_nopar:Npn \spath_gscale:Nnnn #1#2#3#4
                      927 {
                           \_spath_scale:nnn {#2}{#3}{#4}
                      928
                           \tl_gset_eq:NN #1 \g__spath_output_tl
                      929
                           \tl_gclear:N \g__spath_output_tl
                      930
                      931 }
                      932 \cs_generate_variant:Nn \spath_gscale:Nnnn {NVnn, Nnxx}
                      933 \cs_new_protected_nopar:Npn \spath_gscale:Nnn #1#2#3
                      934 {
                           \spath_gscale:NVnn #1#1{#2}{#3}
                      935
                      936 }
                      937 \cs_generate_variant:Nn \spath_gscale:Nnn {cnn, cVV, NVV}
```

This variant allows for passing the coordinates as a single braced group as it strips

off the outer braces of the second argument.

```
938 \cs_new_protected_nopar:Npn \spath_scale:Nn #1#2
939 {
940   \spath_scale:Nnn #1 #2
941 }
942
943 \cs_generate_variant:Nn \spath_scale:Nn {NV}
944 \cs_new_protected_nopar:Npn \spath_gscale:Nn #1#2
945 {
946   \spath_gscale:Nnn #1 #2
947 }
948
949 \cs_generate_variant:Nn \spath_gscale:Nn {NV}
```

(End definition for \spath_scale:Nnnn and others.)

\spath_transform:Nnnnnnn \spath_transform:Nnnnnnn \spath_gtransform:Nnnnnnnn \spath_gtransform:Nnnnnnn Applies an affine (matrix and vector) transformation to path. The matrix is specified in rows first.

```
950 \cs_new_protected_nopar:Npn \__spath_transform:nnnnnnn #1#2#3#4#5#6#7
951 {
952
     \group_begin:
     \tl_set:Nn \l__spath_tmpa_tl {#1}
953
     \tl_clear:N \l__spath_tmpb_tl
954
     \bool_until_do:nn {
955
       \tl_if_empty_p:N \l__spath_tmpa_tl
956
957
958
       \tl_put_right:Nx \l__spath_tmpb_tl {\tl_head:N \l__spath_tmpa_tl}
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
       \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
       \tl_set:Nx \l__spath_tmpd_tl {\tl_head:N \l__spath_tmpa_tl}
       \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
964
965
       \fp_set:Nn \l__spath_tmpa_fp
966
       {\l_spath_tmpc_tl * #2 + \l_spath_tmpd_tl * #4 + #6}
967
       \fp_set:Nn \l__spath_tmpb_fp
968
       {\l_spath_tmpc_tl * #3 + \l_spath_tmpd_tl * #5 + #7}
969
       \tl_put_right:Nx \l__spath_tmpb_tl
971
         {\fp_to_dim:N \l__spath_tmpa_fp}
972
         {\fp_to_dim:N \l__spath_tmpb_fp}
973
974
     }
975
976
     \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
977
978
     \group_end:
979 }
980 \cs_new_protected_nopar:Npn \spath_transform:Nnnnnnn #1#2#3#4#5#6#7#8
981 {
     \__spath_transform:nnnnnn {#2}{#3}{#4}{#5}{#6}{#7}{#8}
     \tl_set_eq:NN #1 \g__spath_output_tl
     \tl_gclear:N \g_spath_output_tl
985
```

```
\cs_generate_variant:Nn \spath_transform:Nnnnnnn
                           {NVnnnnn, Nnxxxxx, cnnnnnnn}
                           \cs_new_protected_nopar:Npn \spath_transform:Nnnnnn #1#2#3#4#5#6#7
                        988
                           {
                        989
                             \spath_transform:NVnnnnnn #1#1{#2}{#3}{#4}{#5}{#6}{#7}
                        990
                        991 }
                           \cs_generate_variant:Nn \spath_transform:Nnnnnnn {cnnnnnn}
                           \cs_new_protected_nopar:Npn \spath_transform:Nnn #1#2#3
                             \spath_transform:Nnnnnnn #1{#2}#3
                        995
                        996 }
                           \cs_generate_variant:Nn \spath_transform:Nnn {cnn, cVn, NVn, NnV}
                           \cs_new_protected_nopar:Npn \spath_transform:Nn #1#2
                        998
                        999
                             \spath_transform:NVnnnnnn #1#1#2
                       1000
                       1001
                           \cs_generate_variant:Nn \spath_transform:Nn {cn, cV, NV}
                       1002
                       1003
                           \cs_new_protected_nopar:Npn \spath_gtransform:Nnnnnnn #1#2#3#4#5#6#7#8
                        1005
                             \__spath_transform:nnnnnn {#2}{#3}{#4}{#5}{#6}{#7}{#8}
                        1006
                             \tl_gset_eq:NN #1 \g__spath_output_tl
                        1007
                             \tl_gclear:N \g__spath_output_tl
                       1008
                       1009
                           \cs_generate_variant:Nn \spath_gtransform:Nnnnnnnn {NVnnnnnn, Nnxxxxxx, cnnnnnnn}
                       1010
                           \cs_new_protected_nopar:Npn \spath_gtransform:Nnnnnnn #1#2#3#4#5#6#7
                       1011
                       1012
                             \spath_gtransform:NVnnnnnn #1#1{#2}{#3}{#4}{#5}{#6}{#7}
                       1013
                       1014 }
                           \cs_generate_variant:Nn \spath_gtransform:Nnnnnnn {cnnnnnn}
                           \cs_new_protected_nopar:Npn \spath_gtransform:Nnn #1#2#3
                       1017
                             \spath_gtransform:Nnnnnnn #1{#2}#3
                       1018
                       1019
                           \cs_generate_variant:Nn \spath_gtransform:Nnn {cnn, cVn, NVn, NnV}
                       1020
                           \cs_new_protected_nopar:Npn \spath_gtransform:Nn #1#2
                       1021
                       1022
                       1023
                             \spath_gtransform:NVnnnnnn #1#1#2
                           \cs_generate_variant:Nn \spath_gtransform:Nn {cn, cV, NV}
                       (End definition for \spath_transform: Nnnnnnn and others.)
    \spath_span:Nnnn
                       The span functions transform a path to start and end at specified points. The normalise
     \spath_span:Nnn
                       functions transform it to start at the origin and end at (1pt, 0pt).
                           If the path starts and ends at the same point then it is translated to the specified
   \spath_gspan:Nnnn
                       point (or origin) but not otherwise changed.
    \spath_gspan:Nnn
 \spath_normalise:Nn
                           \cs_new_protected_nopar:Npn \__spath_span:nnn #1#2#3
                       1026
  \spath_normalise:N
                       1027 {
\spath_gnormalise:Nn
                             \group_begin:
                       1028
                             \spath_initialpoint:Nn \l__spath_tmpa_tl {#1}
 \spath_gnormalise:N
                       1029
                             \spath_finalpoint:Nn \l__spath_tmpb_tl {#1}
                       1030
```

1031 1032

\fp_set:Nn \l__spath_tmpa_fp

```
1033
        (\tl_item:Nn \l__spath_tmpb_tl {1}) -
1034
        (\tl_item: \n \l_spath_tmpa_tl \ \{1\})
1035
1036
      \fp_set:Nn \l__spath_tmpb_fp
1037
1038
        (\tl_item:Nn \l__spath_tmpb_tl {2}) -
1039
        (\tl_item:Nn \l__spath_tmpa_tl {2})
1040
1041
      \fp_set:Nn \l__spath_tmpc_fp
1042
1043
        (\label{local_spath_tmpa_fp}) * (\label{local_spath_tmpa_fp})
1044
1045
        (\l_spath_tmpb_fp * \l_spath_tmpb_fp)
1046
1047
1048
      \fp_compare:nTF
1049
1050
        \l_spath_tmpc_fp < 0.001
      }
        \spath_translate_to:Nnnn \l__spath_tmpd_tl {#1} #2
1054
      }
1055
1056
        \fp_set:Nn \l__spath_tmpa_fp
1057
1058
1059
          ((\tl_item:nn {#3} {1})
1060
1061
           (\tl_item:nn {#2} {1}))
          ((\tl_item:Nn \l__spath_tmpb_tl {1})
1065
          (\tl_item:Nn \l__spath_tmpa_tl {1}))
1066
1067
          ((\tl_item:nn {#3} {2})
1068
1069
          (\tl_item:nn {#2} {2}))
1070
1071
          ((\tl_item:Nn \l__spath_tmpb_tl {2})
          (\tl_item:Nn \l__spath_tmpa_tl {2}))
1075
1076
          \l_spath_tmpc_fp
1077
1078
        \fp_set:Nn \l__spath_tmpb_fp
1079
1080
1081
1082
           ((\t1_item:nn {#3} {2})
          (\tl_item:nn {#2} {2}))
1085
          ((\tl_item:Nn \l__spath_tmpb_tl {1})
1086
```

```
1087
          (\tl_item:Nn \l__spath_tmpa_tl {1}))
1088
1089
          ((\tl_item:nn {#3} {1})
1090
1091
          (\tl_item:nn {#2} {1}))
1092
1093
          ((\tl_item:Nn \l__spath_tmpb_tl {2})
1094
          (\tl_item:Nn \l__spath_tmpa_tl {2}))
1098
          \label{local_spath_tmpc_fp} $$ l_spath_tmpc_fp $$
1099
1100
        \tl_set:Nx \l__spath_tmpc_tl
1104
             \fp_to_decimal:N \l__spath_tmpa_fp
          }
            \fp_to_decimal:N \l__spath_tmpb_fp
1108
          }
1109
1110
             \fp_eval:n { - \l__spath_tmpb_fp }
1111
1113
            \fp_to_decimal:N \l__spath_tmpa_fp
1114
1115
            \fp_to_dim:n
1117
               \tl_item:nn {#2} {1}
1119
1120
               \l_spath_tmpa_fp * (\tl_item:Nn \l_spath_tmpa_tl {1})
1121
               \l_spath_tmpb_fp * (\tl_item:Nn \l_spath_tmpa_t1 {2})
1124
1125
          }
1126
             \fp_to_dim:n
               \tl_item:nn {#2} {2}
1129
1130
               \l__spath_tmpb_fp * (\tl_item:Nn \l__spath_tmpa_tl {1})
1131
1132
               \l_spath_tmpa_fp * (\tl_item:Nn \l_spath_tmpa_tl {2})
1134
          }
1135
1136
1137
        \spath_transform: NnV \l__spath_tmpd_tl {#1} \l__spath_tmpc_tl
1138
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpd_tl
1139
      \group_end:
```

```
\cs_new_protected_nopar:Npn \spath_span:Nnnn #1#2#3#4
1142
1143
      \__spath_span:nnn {#2}{#3}{#4}
1144
      \tl_set_eq:NN #1 \g__spath_output_tl
1145
      \tl_gclear:N \g_spath_output_tl
1146
1147
    \cs_generate_variant:Nn \spath_span:Nnnn {NVnn, NVVV, NnVV}
1148
    \cs_new_protected_nopar:Npn \spath_span:Nnn #1#2#3
1150
      \spath_span:NVnn #1#1{#2}{#3}
1151
1152
    \cs_generate_variant:Nn \spath_span:Nnn {NVV, cnn, cvv, cVV}
    cs_new_protected_nopar:Npn \spath_gspan:Nnnn #1#2#3#4
1154
1155
      \__spath_span:nnn {#2}{#3}{#4}
1156
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
1158
    \cs_generate_variant:Nn \spath_gspan:Nnnn {NVnn, NVVV}
    \cs_new_protected_nopar:Npn \spath_gspan:Nnn #1#2#3
1162
      \spath_gspan:NVnn #1#1{#2}{#3}
1163
1164 }
    \cs_generate_variant:Nn \spath_gspan:Nnn {NVV, cnn, cvv, cVV}
1165
    \cs_new_protected_nopar:Npn \__spath_normalise:n #1
1166
1167
      \__spath_span:nnn {#1}{{0pt}{0pt}}{{1pt}{0pt}}
1168
1169
    \cs_new_protected_nopar:Npn \spath_normalise:Nn #1#2
1171
      \_\_spath_normalise:n {#2}
1173
      \tl_set_eq:NN #1 \g__spath_output_tl
      \t_gclean: N \g_spath_output_tl
1174
1175
    \cs_generate_variant:Nn \spath_normalise:Nn {cn,NV, cV, cv}
    \cs_new_protected_nopar:Npn \spath_normalise:N #1
1177
1178
1179
      \spath_normalise:NV #1#1
    \cs_generate_variant:Nn \spath_normalise:N {c}
    \cs_new_protected_nopar:Npn \spath_gnormalise:Nn #1#2
1183
      \__spath_normalise:n {#2}
1184
      \tl_gset_eq:NN #1 \g__spath_output_tl
1185
      \tl_gclear:N \g__spath_output_tl
1186
1187 }
    \cs_generate_variant:Nn \spath_gnormalise:Nn {cn,NV, cV, cv}
    \cs_new_protected_nopar:Npn \spath_gnormalise:N #1
1190
      \spath_gnormalise:NV #1#1
1192 }
1193 \cs_generate_variant:Nn \spath_gnormalise:N {c}
(End definition for \spath_span:Nnnn and others.)
```

\spath_splice_between:Nnnn \spath_splice_between:Nnnn \spath_gsplice_between:Nnnn \spath_gsplice_between:Nnn

\spath_close_with:Nn \spath_gclose_with:Nn

This takes three paths and returns a single path in which the middle one is adjusted (and welded) so that it joins the first path to the third.

```
\cs_new_protected_nopar:Npn \__spath_splice_between:nnn #1#2#3
1196
      \group_begin:
      \spath_finalpoint:NV \l__spath_tmpd_tl {#1}
1197
      \spath_initialpoint:NV \l__spath_tmpe_tl {#3}
1198
      \spath_span:NnVV \1__spath_tmpb_tl {#2} \1__spath_tmpd_tl \1__spath_tmpe_tl
1199
      \spath_append_no_move: NnV \l__spath_tmpa_tl {#1} \l__spath_tmpb_tl
1200
      \spath_append_no_move: Nn \l__spath_tmpa_tl {#3}
1201
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
      \group_end:
    \cs_new_protected_nopar:Npn \spath_splice_between:Nnnn #1#2#3#4
1205
1206
    {
      \__spath_splice_between:nnn {#2}{#3}{#4}
1207
      \tl_set_eq:NN #1 \g__spath_output_tl
1208
      \tl_gclear:N \g__spath_output_tl
1209
1210 }
    \cs_generate_variant:Nn \spath_splice_between:Nnnn {NVnn, NVVV}
1211
    \cs_new_protected_nopar:Npn \spath_splice_between:Nnn #1#2#3
1212
      \spath_splice_between:NVnn #1#1{#2}{#3}
1215
    \cs_generate_variant:Nn \spath_splice_between:Nnn {NVV, cnn, cvv, Nvn, NVn}
    \cs_new_protected_nopar:Npn \spath_gsplice_between:Nnnn #1#2#3#4
1218 {
      \_spath_splice_between:nnn {#2}{#3}{#4}
1219
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g_spath_output_tl
1222 }
    \cs_generate_variant:Nn \spath_gsplice_between:Nnnn {NVnn, NVVV}
    \cs_new_protected_nopar:Npn \spath_gsplice_between:Nnn #1#2#3
      \spath_gsplice_between:NVnn #1#1{#2}{#3}
1227
\cs_generate_variant:Nn \spath_gsplice_between:Nnn {NVV, cnn, cvv, Nvn, NVn}
(End definition for \spath_splice_between: Nnnn and others.)
Closes the first path by splicing in the second.
1229 \cs_new_protected_nopar:Npn \__spath_close_with:nn #1#2
1230
      \group_begin:
1231
      \spath_finalmovepoint:Nn \l__spath_tmpa_tl {#1}
      \spath_finalpoint:Nn \l__spath_tmpb_tl {#1}
1234
      \dim_compare:nTF
1235
        \dim_abs:n
1237
          \tl_item:Nn \l__spath_tmpa_tl {1}
1239
          \tl_item:Nn \l__spath_tmpb_tl {1}
1240
1241
```

```
1242
         \dim_abs:n
1243
1244
           \tl_item:Nn \l__spath_tmpa_tl {2}
1245
1246
           \tl_item:Nn \l__spath_tmpb_tl {2}
1247
        }
1248
          0.01pt
1249
      }
      {
1251
         \__spath_close:n {#1}
1252
      }
1253
1254
         \spath_span:\nvv \l__spath_tmpc_tl {#2} \l__spath_tmpb_tl \l__spath_tmpa_tl
1255
         \spath_append_no_move:\nv \l__spath_tmpd_tl {#1} \l__spath_tmpc_tl
1256
         \__spath_close:V \l__spath_tmpd_tl
1257
1258
       \group_end:
1259
1260 }
    cs_new_protected_nopar:Npn \spath_close_with:Nnn #1#2#3
1262
      \_{\rm spath\_close\_with:nn} \  \{#2\}\{#3\}
1263
      \tl_set_eq:NN #1 \g__spath_output_tl
1264
      \tl_gclear:N \g__spath_output_tl
1265
1266 }
    \cs_generate_variant:Nn \spath_close_with:Nnn {cnn, cVV, cvv, NVn}
1267
    \cs_new_protected_nopar:Npn \spath_close_with:Nn #1#2
1268
1269
      \spath_close_with:NVn #1#1{#2}
1270
1271 }
    \cs_generate_variant:Nn \spath_close_with:Nn {cn, cV, cv, NV}
    \cs_new_protected_nopar:Npn \spath_gclose_with:Nnn #1#2#3
1274
      \__spath_close_with:nn {#2}{#3}
1275
      \tl_gset_eq:NN #1 \g__spath_output_tl
1276
      \tl_gclear:N \g__spath_output_tl
1278 }
    \cs_generate_variant:Nn \spath_gclose_with:Nnn {cnn, cVV, cvv, NVn}
1280
    \cs_new_protected_nopar:Npn \spath_gclose_with:Nn #1#2
      \spath_gclose_with:NVn #1#1{#2}
1283 }
1284 \cs_generate_variant:Nn \spath_gclose_with:Nn {cn, cV, cv, NV}
(End definition for \spath_close_with:Nn and \spath_gclose_with:Nn.)
This welds one path to another, moving the second so that its initial point coincides with
the first's final point. It is called a weld because the initial move of the second path is
removed.
1285
    \cs_new_protected_nopar:Npn \__spath_weld:nn #1#2
1286
```

\spath_weld:Nnn \spath_weld:Nn

\spath_gweld:Nnn

\spath_gweld:Nn

1287

\group_begin:

\tl_set:Nn \l__spath_tmpa_tl {#1}
\tl_set:Nn \l__spath_tmpb_tl {#2}

```
\spath_finalpoint:Nn \l__spath_tmpc_tl {#1}
1290
      \spath_translate_to:NV \l__spath_tmpb_tl \l__spath_tmpc_tl
1291
1292
      \__spath_append_no_move:VV \l__spath_tmpa_tl \l__spath_tmpb_tl
1293
      \group_end:
1294
1295
    \cs_new_protected_nopar:Npn \spath_weld:Nnn #1#2#3
1296
1297
       \__spath_weld:nn {#2}{#3}
1298
      \tl_set_eq:NN #1 \g__spath_output_tl
1299
      \tl_gclear:N \g__spath_output_tl
1300
1301
    \cs_generate_variant:Nn \spath_weld:Nnn {NVV,NVn}
1302
    \cs_new_protected_nopar:Npn \spath_weld:Nn #1#2
1303
1304
      \spath_weld:NVn #1#1{#2}
1305
1306
    \cs_generate_variant:Nn \spath_weld:Nn {NV, Nv, cV, cv}
1307
    \cs_new_protected_nopar:Npn \spath_gweld:Nnn #1#2#3
1309
      \_spath_weld:nn {#2}{#3}
1310
      \tl_gset_eq:NN #1 \g__spath_output_tl
1311
      \tl_gclear:N \g__spath_output_tl
1312
1313 }
    \cs_generate_variant:Nn \spath_gweld:Nnn {NVV, NVn}
1314
    \cs_new_protected_nopar:Npn \spath_gweld:Nn #1#2
1315
1316
      \spath_gweld:NVn #1#1{#2}
1317
1318 }
1319 \cs_generate_variant:Nn \spath_gweld:Nn {NV, Nv, cV, cv}
(End definition for \spath_weld:Nnn and others.)
Append the path from the second spath to the first, removing the adjoining move.
1320 \cs_new_protected_nopar:Npn \__spath_append_no_move:nn #1#2
1321 {
1322
      \group_begin:
      \tl_set:Nn \l__spath_tmpa_tl {#1}
1323
      \tl_set:Nn \l__spath_tmpb_tl {#2}
1324
      \tl_set:Nx \l__spath_tmpb_tl {\tl_tail:N \l__spath_tmpb_tl}
      \tl_set:Nx \l__spath_tmpb_tl {\tl_tail:N \l__spath_tmpb_tl}
1326
      \tl_set:Nx \l__spath_tmpb_tl {\tl_tail:N \l__spath_tmpb_tl}
1327
1328
      \tl_put_right:NV \l__spath_tmpa_tl \l__spath_tmpb_tl
1329
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
1330
      \group_end:
1332 }
    \cs_generate_variant:Nn \__spath_append_no_move:nn {VV}
    \cs_new_protected_nopar:Npn \spath_append_no_move:Nnn #1#2#3
1334
1335
       \__spath_append_no_move:nn {#2}{#3}
1336
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
1338
```

\spath_append_no_move:Nnn \spath_append_no_move:Nn

\spath gappend no move:Nnn

\spath_gappend_no_move:Nn

1339 }

```
\cs_new_protected_nopar:Npn \spath_append_no_move:Nn #1#2
                               1342
                                     \spath_append_no_move:NVn #1#1{#2}
                               1343
                               1344
                                   \cs_generate_variant:Nn \spath_append_no_move:Nn {NV, cv, Nv, cV}
                               1345
                                   \cs_new_protected_nopar:Npn \spath_gappend_no_move:Nnn #1#2#3
                               1346
                               1347
                                     \__spath_append_no_move:nn {#2}{#3}
                                     \tl_gset_eq:NN #1 \g__spath_output_tl
                                     \tl_gclear:N \g__spath_output_tl
                               1351
                                   \cs_generate_variant:Nn \spath_gappend_no_move:Nnn {NVV, NVn}
                               1352
                                   \cs_new_protected_nopar:Npn \spath_gappend_no_move:Nn #1#2
                               1353
                               1354
                                     \spath_gappend_no_move:NVn #1#1{#2}
                               1355
                               1356
                                  \cs_generate_variant:Nn \spath_gappend_no_move:Nn {NV, cv, Nv, cV}
                              (End definition for \spath_append_no_move:Nnn and others.)
                              Prepend the path from the second spath to the first.
          \spath_append:Nnn
           \spath_append:Nn
                               1358 \cs_new_protected_nopar:Npn \spath_append:Nnn #1#2#3
         \spath_gappend:Nnn
                               1359
          \spath_gappend:Nn
                                     \tl_set:Nn #1 {#2}
                               1360
                                     \tl_put_right:Nn #1 {#3}
                               1361
                               1362
                                  \cs_generate_variant:Nn \spath_append:Nnn {NVV, NVn}
                                   \cs_new_protected_nopar:Npn \spath_append:Nn #1#2
                               1365
                                     \spath_append:NVn #1#1{#2}
                               1366
                                  \cs_generate_variant:Nn \spath_append:Nn {NV, Nv, cv, cV}
                                   \cs_new_protected_nopar:Npn \spath_gappend:Nnn #1#2#3
                               1369
                               1370
                                     \tl_gset:Nn #1 {#2}
                               1371
                                     \tl_gput_right:Nn #1 {#3}
                               1372
                               1373
                                   \cs_generate_variant:Nn \spath_gappend:Nnn {NVV, NVn}
                                   \cs_new_protected_nopar:Npn \spath_gappend:Nn #1#2
                                     \spath_gappend:NVn #1#1{#2}
                               1378
                                  \cs_generate_variant:Nn \spath_gappend:Nn {NV, Nv, cv, cV}
                              (End definition for \spath_append:Nnn and others.)
                              Prepend the path from the second spath to the first, removing the adjoining move.
 \spath_prepend_no_move:Nnn
  \spath_prepend_no_move:Nn
                               1380 \cs_new_protected_nopar:Npn \spath_prepend_no_move:Nnn #1#2#3
\spath_gprepend_no_move:Nnn
                                     \spath_append_no_move:Nnn #1{#3}{#2}
\spath_gprepend_no_move:Nn
                               1382
                               1384 \cs_generate_variant:Nn \spath_prepend_no_move:Nnn {NVV, NVn}
                               \cs_new_protected_nopar:Npn \spath_prepend_no_move:Nn #1#2
                               1386
```

\cs_generate_variant:Nn \spath_append_no_move:Nnn {NVV, NVn, NnV}

```
\spath_prepend_no_move:NVn #1#1{#2}
                         1387
                         1388 }
                             \cs_generate_variant:Nn \spath_prepend_no_move:Nn {NV, cv}
                         1389
                             \cs_new_protected_nopar:Npn \spath_gprepend_no_move:Nnn #1#2#3
                             {
                         1391
                               \spath_gappend_no_move:Nnn #1{#3}{#2}
                         1392
                         1393
                             \cs_generate_variant:Nn \spath_gprepend_no_move:Nnn {NVV, NVn}
                             \cs_new_protected_nopar:Npn \spath_gprepend_no_move:Nn #1#2
                               \spath_gprepend_no_move:NVn #1#1{#2}
                         1398
                             \cs_generate_variant:Nn \spath_gprepend_no_move:Nn {NV, cv}
                        (End definition for \spath_prepend_no_move:Nnn and others.)
   \spath_prepend:Nnn
                        Prepend the path from the second spath to the first.
    \spath_prepend:Nn
                         1400 \cs_new_protected_nopar:Npn \spath_prepend:Nnn #1#2#3
  \spath_gprepend:Nnn
                         1401 {
   \spath_gprepend:Nn
                               \spath_append: Nnn #1{#3}{#2}
                         1402
                         1403 }
                             \cs_generate_variant:Nn \spath_prepend:Nnn {NVV, NVn}
                             \cs_new_protected_nopar:Npn \spath_prepend:Nn #1#2
                               \spath_prepend:NVn #1#1{#2}
                         1408 }
                             \cs_generate_variant:Nn \spath_prepend:Nn {NV}
                         1409
                             \cs_new_protected_nopar:Npn \spath_gprepend:Nnn #1#2#3
                         1410
                         1411
                               \spath_gappend:Nnn #1{#3}{#2}
                         1412
                         1413 }
                             \cs_generate_variant:Nn \spath_gprepend:Nnn {NVV, NVn}
                         1414
                             \cs_new_protected_nopar:Npn \spath_gprepend:Nn #1#2
                         1415
                         1416
                               \spath_gprepend:NVn #1#1{#2}
                         1417
                         1418 }
                            \cs_generate_variant:Nn \spath_gprepend:Nn {NV}
                        (End definition for \spath prepend:Nnn and others.)
                        The corner rounding routine is applied quite late in the process of building a soft path
 \spath_bake_round:Nn
  \spath_bake_round:N
                        so this ensures that it is done.
\spath_gbake_round:Nn
                             \cs_new_protected_nopar:Npn \__spath_bake_round:n #1
 \spath_gbake_round:N
                         1421 {
                               \group_begin:
                         1422
                               \tl_set:Nn \l__spath_tmpa_tl {#1}
                         1423
                               \pgf@@processround \l__spath_tmpa_tl\l__spath_tmpb_tl
                         1424
                               \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                         1425
                               \group_end:
                         1426
                         1427
                             \cs_new_protected_nopar:Npn \spath_bake_round:Nn #1#2
                         1429
                         1430
                               \__spath_bake_round:n {#2}
                               \tl_set_eq:NN #1 \g__spath_output_tl
                         1431
```

```
\tl_gclear:N \g_spath_output_tl
                   1433
                       \cs_generate_variant:Nn \spath_bake_round:Nn {NV}
                   1434
                       \cs_new_protected_nopar:Npn \spath_bake_round:N #1
                   1436
                         \spath_bake_round:NV #1#1
                   1437
                   1438
                       \cs_generate_variant:Nn \spath_bake_round:N {c}
                       \cs_new_protected_nopar:Npn \spath_gbake_round:Nn #1#2
                   1441
                         \__spath_bake_round:n {#2}
                         \tl_gset_eq:NN #1 \g__spath_output_tl
                   1443
                         \tl_gclear:N \g__spath_output_tl
                   1444
                   1445
                       \cs_generate_variant:Nn \spath_gbake_round:Nn {NV}
                   1446
                       \cs_new_protected_nopar:Npn \spath_gbake_round:N #1
                   1448
                         \spath_gbake_round:NV #1#1
                   1449
                   1450 }
                       \cs_generate_variant:Nn \spath_gbake_round:N {c}
                   (End definition for \spath_bake_round:Nn and others.)
                  Appends a close path to the end of the path.
\spath_close:Nn
 \spath_close:N
                   1452 \cs_new_protected_nopar:Npn \__spath_close:n #1
\spath_gclose:Nn
                   1453 {
\spath_gclose:N
                         \group_begin:
                   1454
                         \tl_set:Nn \l__spath_tmpa_tl {#1}
                   1455
                         \spath_finalmovepoint:NV \l__spath_tmpb_tl \l__spath_tmpa_tl
                   1456
                         \tl_put_right:NV \l__spath_tmpa_tl \c_spath_closepath_tl
                   1457
                         \tl_put_right:NV \l__spath_tmpa_tl \l__spath_tmpb_tl
                   1458
                         \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
                   1459
                         \group_end:
                   1460
                       \cs_generate_variant:Nn \__spath_close:n {V}
                       \cs_new_protected_nopar:Npn \spath_close:Nn #1#2
                   1464
                         \__spath_close:n {#2}
                   1465
                         \tl_set_eq:NN #1 \g__spath_output_tl
                   1466
                         \tl_gclear:N \g__spath_output_tl
                   1467
                   1468
                       \cs_generate_variant:Nn \spath_close:Nn {NV}
                       \cs_new_protected_nopar:Npn \spath_close:N #1
                   1471
                         \spath_close:NV #1#1
                       \cs_generate_variant:Nn \spath_close:N {c}
                   1475
                       \cs_new_protected_nopar:Npn \spath_gclose:Nn #1#2
                   1476
                         \__spath_close:n {#2}
                   1477
                         \tl_gset_eq:NN #1 \g__spath_output_tl
                   1478
                         \tl_gclear:N \g__spath_output_tl
                   1479
                   1480 }
                   1481 \cs_generate_variant:Nn \spath_gclose:Nn {NV}
```

```
\cs_new_protected_nopar:Npn \spath_gclose:N #1
                   1483
                         \spath_gclose:NV #1#1
                   1484
                   1485 }
                   1486 \cs_generate_variant:Nn \spath_gclose:N {c}
                  (End definition for \spath_close:Nn and others.)
\spath_open:Nn
                  Removes all close paths from the path, replacing them by lineto if they move any
 \spath_open:N
                  distance.
\spath_gopen:Nn
                   1487 \cs_new_protected_nopar:Npn \__spath_open:n #1
\spath_gopen:N
                   1488 {
                         \group_begin:
                   1489
                         \tl_set:Nn \l__spath_tmpa_tl {#1}
                   1490
                         \tl_clear:N \l__spath_tmpb_tl
                   1491
                         \bool_until_do:nn {
                           \tl_if_empty_p:N \l__spath_tmpa_tl
                   1493
                        }
                        {
                           \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
                   1496
                           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                   1497
                   1498
                           \tl_case:NnF \l__spath_tmpc_tl
                   1499
                   1500
                             \c_spath_closepath_tl {
                   1501
                   1502
                               \bool_if:nF
                   1503
                                 \dim_compare_p:n
                   1505
                                 {
                                   \l_spath_move_x_dim == \l_spath_tmpa_dim
                   1507
                                 }
                   1508
                                 &&
                   1509
                                 \dim_compare_p:n
                   1510
                                 {
                   1511
                                   \l_spath_move_y_dim == \l_spath_tmpb_dim
                   1512
                                 }
                   1513
                               }
                   1514
                               {
                                 \tl_put_right:NV \l__spath_tmpb_tl \c_spath_lineto_tl
                   1517
                                 \tl_put_right:Nx \l__spath_tmpb_tl {
                   1518
                                   { \dim_use:N \l__spath_move_x_dim }
                   1519
                                   { \dim_use:N \l__spath_move_y_dim }
                   1520
                                 }
                   1521
                               }
                   1522
                   1523
                               \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
                   1524
                               \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                   1526
                               \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
                   1527
                               \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
                   1528
                   1529
                             \c_spath_moveto_tl {
                   1530
```

```
\tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpc_tl
1531
1532
            \dim_set:Nn \l__spath_move_x_dim {\tl_head:N \l__spath_tmpa_tl}
1533
            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
1534
            \dim_set:Nn \l__spath_move_y_dim {\tl_head:N \l__spath_tmpa_tl}
1535
            \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
1536
1537
            \tl_put_right:Nx \l__spath_tmpb_tl {
1538
              { \dim_use:N \l__spath_move_x_dim }
              { \dim_use: N \l_spath_move_y_dim }
1542
            \dim_set_eq:NN \l__spath_tmpa_dim \l__spath_move_x_dim
1543
            \dim_set_eq:NN \l__spath_tmpb_dim \l__spath_move_y_dim
1544
1545
       }
1546
1547
          \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpc_tl
1548
          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpa_tl}
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
          \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpa_tl}
1552
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
1553
1554
          \tl_put_right:Nx \l__spath_tmpb_tl {
1555
            { \dim_use:N \l__spath_tmpa_dim }
1556
            { \dim_use:N \l__spath_tmpb_dim }
1557
         }
1558
       }
1559
1560
     \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
1561
1562
      \group_end:
1563
   \cs_new_protected_nopar:Npn \spath_open:Nn #1#2
1564
1565
      \__spath_open:n {#2}
1566
     \tl_set_eq:NN #1 \g_spath_output_tl
1567
      \tl_gclear:N \g__spath_output_tl
1568
1569 }
   \cs_generate_variant:Nn \spath_open:Nn {NV}
   \cs_new_protected_nopar:Npn \spath_open:N #1
1572
   {
      \spath_open:NV #1#1
1573
1574
   \verb|\cs_new_protected_nopar:Npn \spath_gopen:Nn #1#2|
1575
1576
      \__spath_open:n {#2}
1577
     \tl_gset_eq:NN #1 \g__spath_output_tl
1578
     \tl_gclear:N \g_spath_output_tl
1579
1580 }
   \cs_generate_variant:Nn \spath_gopen:Nn {NV}
   \cs_new_protected_nopar:Npn \spath_gopen:N #1
1583 {
     \spath_gopen:NV #1#1
```

```
1585 }
```

(End definition for \spath_open:Nn and others.)

```
\spath_replace_lines:Nn
\spath_replace_lines:Nn
\spath_replace_lines:Nn
\spath_replace_lines:Nn
```

```
Replace any line segments by Bézier curves.
1586 \cs_new_protected_nopar:Npn \__spath_replace_lines:n #1
1587 {
      \group_begin:
1588
      \tl_set:Nn \l__spath_tmpa_tl {#1}
1589
      \tl_clear:N \l__spath_tmpb_tl
1590
      \dim_set:Nn \l__spath_tmpa_dim {0pt}
1591
      \dim_set:Nn \l__spath_tmpb_dim {Opt}
1592
      \bool_do_until:nn
         \tl_if_empty_p:N \l__spath_tmpa_tl
 1596
      }
1597
      {
1598
         \tl_set:Nx \l__spath_tmpc_tl {\tl_item:Nn \l__spath_tmpa_tl {1}}
1599
         \tl_set:Nx \l__spath_tmpd_tl {\tl_item:Nn \l__spath_tmpa_tl {2}}
1600
         \tl_set:Nx \l__spath_tmpe_tl {\tl_item:Nn \l__spath_tmpa_tl {3}}
1601
1602
         \tl_if_eq:NNTF \l__spath_tmpc_tl \c_spath_lineto_tl
1603
1604
           \tl_put_right:NV \l__spath_tmpb_tl \c_spath_curvetoa_tl
1605
           \tl_put_right:Nx \l__spath_tmpb_tl
1606
1607
1608
               \fp_to_dim:n
1609
1610
                 2/3 * (\1_spath_tmpa_dim)
1611
1612
                  1/3 * (\l_spath_tmpd_tl)
1613
1614
             }
           }
1616
           \tl_put_right:Nx \l__spath_tmpb_tl
1617
1618
             {
1619
               \fp_to_dim:n
1620
               {
1621
                 2/3 * (\1__spath_tmpb_dim)
1622
1623
                 1/3 * (\l_spath_tmpe_tl)
1624
               }
1625
             }
           }
1627
           \tl_put_right:NV \l__spath_tmpb_tl \c_spath_curvetob_tl
1628
           \tl_put_right:Nx \l__spath_tmpb_tl
1629
1630
           ₹
1631
                \fp_to_dim:n
1632
1633
                 1/3 * (\l_spath_tmpa_dim)
1634
```

```
1635
                2/3 * (\l_spath_tmpd_tl)
1636
1637
            }
1638
1639
          \tl_put_right:Nx \l__spath_tmpb_tl
1640
1641
1642
              \fp_to_dim:n
              {
                1/3 * (\l_spath_tmpb_dim)
1646
                2/3 * (\l_spath_tmpe_tl)
1647
              }
1648
            }
1649
1650
          \tl_put_right:NV \l__spath_tmpb_tl \c_spath_curveto_tl
1651
          \__spath_tl_put_right_braced:NV \l__spath_tmpb_tl \l__spath_tmpd_tl
1652
          \__spath_tl_put_right_braced:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
       }
        {
          \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpc_tl
1656
          \__spath_tl_put_right_braced:NV \l__spath_tmpb_tl \l__spath_tmpd_tl
1657
          \__spath_tl_put_right_braced:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
1658
1659
1660
        \dim_set:Nn \l__spath_tmpa_dim {\l__spath_tmpd_tl}
1661
        \dim_set:Nn \l__spath_tmpb_dim {\l__spath_tmpe_tl}
1662
1663
        \prg_replicate:nn {3}
1665
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
1666
1667
1668
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
1669
      \group_end:
1670
1671 }
1672
   \cs_generate_variant:Nn \__spath_replace_lines:n {V}
1673
   \cs_new_protected_nopar:Npn \spath_replace_lines:Nn #1#2
1674
1675
      \__spath_replace_lines:n {#2}
      \tl_set_eq:NN #1 \g__spath_output_tl
      \t \g_spath_output_tl
1677
1678 }
   \cs_generate_variant:Nn \spath_replace_lines:Nn {NV, cV, cv, Nv}
1679
   \cs_new_protected_nopar:Npn \spath_replace_lines:N #1
1680
1681
      \spath_replace_lines:NV #1#1
1682
1683
    \cs_generate_variant:Nn \spath_replace_lines:N {c}
   \cs_new_protected_nopar:Npn \spath_greplace_lines:Nn #1#2
1686
      \__spath_replace_lines:n {#2}
1687
      \tl_gset_eq:NN #1 \g__spath_output_tl
1688
```

```
\tl_gclear:N \g_spath_output_tl
1690 }
    \cs_generate_variant:Nn \spath_greplace_lines:Nn {NV, cV, cv, Nv}
    \cs_new_protected_nopar:Npn \spath_greplace_lines:N #1
1693
      \spath_greplace_lines:NV #1#1
1694
1695
    \cs_generate_variant:Nn \spath_greplace_lines:N {c}
(End\ definition\ for\ \verb|\spath_replace_lines:Nn.|)
Remove any component that is simply a moveto.
```

\spath remove empty components:Nn \spath remove empty components:N \spath_gremove_empty_components:Nn \spath_gremove_empty_components:N

```
1697 \cs_new_protected_nopar:Npn \__spath_remove_empty_components:n #1
1698 {
     \group_begin:
     \spath_components_to_seq: Nn \l__spath_tmpa_seq {#1}
     \tl_clear:N \l__spath_tmpa_tl
     \seq_map_inline: Nn \l__spath_tmpa_seq
1702
       \int_compare:nF
1704
          \t: \{\#1\} == 3
1706
1708
          \tl_put_right:Nn \l__spath_tmpa_tl {##1}
       }
1710
     }
1711
     \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
1712
1713
     \group_end:
1714 }
   \cs_new_protected_nopar:Npn \spath_remove_empty_components:Nn #1#2
1715
1716
1717
      \__spath_remove_empty_components:n {#2}
1718
     \tl_set_eq:NN #1 \g_spath_output_tl
     \tl_gclear:N \g_spath_output_tl
   \cs_generate_variant:Nn \spath_remove_empty_components:Nn {NV}
   \cs_new_protected_nopar:Npn \spath_remove_empty_components:N #1
     \spath_remove_empty_components:NV #1#1
1724
   }
1725
   \cs_generate_variant:Nn \spath_remove_empty_components:N {c}
1726
   \cs_new_protected_nopar:Npn \spath_gremove_empty_components:Nn #1#2
1727
1728
      \__spath_remove_empty_components:n {#2}
1729
     \tl_gset_eq:NN #1 \g__spath_output_tl
1730
     \tl_gclear:N \g__spath_output_tl
1731
1732
   \cs_generate_variant:Nn \spath_gremove_empty_components:Nn {NV}
   \cs_new_protected_nopar:Npn \spath_gremove_empty_components:N #1
1734
1735
     \spath_gremove_empty_components:NV #1#1
1736
1737 }
1738 \cs_generate_variant:Nn \spath_gremove_empty_components:N {c}
```

\spath_if_eq:nn Test if two soft paths are equal, we allow a little tolerance on the calculations.

```
\prg_new_protected_conditional:Npnn \spath_if_eq:nn #1#2 { T, F, TF }
1740 {
1741
                     \group_begin:
1742
                    \tl_set:Nn \l__spath_tmpa_tl {#1}
                    \tl_set:Nn \l__spath_tmpb_tl {#2}
1743
                    \bool_gset_true:N \g__spath_tmpa_bool
1744
                    \int_compare:nNnTF
1745
                    {\tl_count:N \l_spath_tmpa_tl}
1746
1747
                   {\tl_count:N \l_spath_tmpb_tl}
1748
1749
                           \int_step_inline:nnnn {1} {3} {\tl_count:N \l__spath_tmpa_tl}
1750
1751
                                  \tl_set:Nx \l__spath_tmpc_tl {\tl_item:Nn \l__spath_tmpa_tl {##1}}
1752
                                  \tl_set:Nx \l__spath_tmpd_tl {\tl_item:Nn \l__spath_tmpb_tl {##1}}
1753
1754
                                  \tl_if_eq:NNF \l__spath_tmpc_tl \l__spath_tmpd_tl
                                  {
                                          \bool_gset_false:N \g__spath_tmpa_bool
1756
1757
                                  \label{lem:nn ll_spath_tmpa_dim {ll_item:Nn ll_spath_tmpa_tl {##1+1}}} $$ \dim_set:Nn \label{ll_spath_tmpa_dim} $$ \left( \int_set^n \left( \int_se
1758
                                  \dim_set:Nn \l__spath_tmpb_dim {\tl_item:Nn \l__spath_tmpb_tl {##1+1}}
1759
                                   \dim_compare:nF
1760
                                          \dim_abs:n
                                                 \l_spath_tmpa_dim - \l_spath_tmpb_dim
1764
1765
                                          < 0.001pt
1766
                                  }
1767
                                  {
1768
                                          \bool_gset_false:N \g__spath_tmpa_bool
1769
1770
                                  \dim_set:Nn \l__spath_tmpa_dim {\tl_item:Nn \l__spath_tmpa_tl {##1+2}}
1771
                                  \dim_set:Nn \l__spath_tmpb_dim {\tl_item:Nn \l__spath_tmpb_tl {##1+2}}
                                  \dim_compare:nF
1773
1774
                                          \dim_abs:n
1775
1776
                                                 \l_spath_tmpa_dim - \l_spath_tmpb_dim
1777
                                         }
1778
                                          < 0.001pt
1779
1780
1781
                                           \bool_gset_false:N \g_spath_tmpa_bool
                          }
                   }
1785
1786
                           \bool_gset_false:N \g__spath_tmpa_bool
1787
1788
                    \group_end:
1789
```

```
1790 \bool_if:NTF \g_spath_tmpa_bool
1791 {
1792  \prg_return_true:
1793  }
1794  {
1795  \prg_return_false:
1796  }
1797 }
1798 \prg_generate_conditional_variant:Nnn \spath_if_eq:nn {VV, Vn, nV, vv} {TF, T, F}
(End definition for \spath_if_eq:nn.)
```

3.4 Splitting Commands

\spath_split_curve:NNnn \spath_gsplit_curve:NNnn Splits a Bezier cubic into pieces, storing the pieces in the first two arguments.

```
\cs_new_protected_nopar:Npn \__spath_split_curve:nn #1#2
1800 {
1801
      \group_begin:
1802
      \tl_set_eq:NN \l__spath_tmpa_tl \c_spath_moveto_tl
      \tl_put_right:Nx \l__spath_tmpa_tl {
1803
        {\tl_item:nn {#1} {2}}
1804
        {\tl_item:nn {#1} {3}}
1805
1806
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curvetoa_tl
1807
      \tl_put_right:Nx \l__spath_tmpa_tl
1808
        {\fp_to_dim:n
1811
          (1 - #2) * \tl_item:nn {#1} {2} + (#2) * \tl_item:nn {#1} {5}
1812
       }}
1813
        {\fp_to_dim:n
1814
1815
          (1 - #2) * \tl_item:nn {#1} {3} + (#2) * \tl_item:nn {#1} {6}
1816
       }}
1817
     }
1818
1819
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curvetob_tl
1820
1821
      \tl_put_right:Nx \l__spath_tmpa_tl
1822
        {\phi_t}
1823
1824
          (1 - #2)^2 * \tilde{1}_{item:nn} {#1} {2}
1825
          + 2 * (1 - #2) * (#2) * \tl_item:nn {#1} {5}
1826
          + (#2)^2 * \tl_item:nn {#1} {8}
1827
       }}
1828
        {\fp_to_dim:n
1829
          (1 - #2)^2 * \tilde{41}_{item:nn}  {3}
          + 2 * (1 - #2) * (#2) * \tl_item:nn {#1} {6}
          + (#2)^2 * \tl_item:nn {#1} {9}
1833
       }}
1834
     }
1835
1836
     \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curveto_tl
1837
```

```
\tl_put_right:Nx \l__spath_tmpa_tl
1838
1839
        {\fp_to_dim:n
1840
          {
1841
            (1 - #2)^3 * \text{tl_item:nn } {#1} {2}
1842
            + 3 * (1 - #2)^2 * (#2) * \tl_item:nn {#1} {5}
1843
            + 3 * (1 - #2) * (#2)^2 * \tl_item:nn {#1} {8}
1844
            + (#2)^3 * \tl_item:nn {#1} {11}
1845
        }}
        {\fp_to_dim:n
1847
1848
          (1 - #2)^3 * \tilde{41}_{item:nn} {#1} {3}
1849
          + 3 * (1 - #2)^2 * (#2) * \text{litem:nn } {#1} {6}
1850
          + 3 * (1 - #2) * (#2)^2 * \tl_item:nn {#1} {9}
1851
          + (#2)^3 * \tl_item:nn {#1} {12}
1852
        }}
1853
1854
1855
      \tl_gclear:N \g_spath_output_tl
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpa_tl
1857
      \tl_clear:N \l__spath_tmpa_tl
1859
      \tl_set_eq:NN \l__spath_tmpa_tl \c_spath_moveto_tl
1860
      \tl_put_right:Nx \l__spath_tmpa_tl
1861
      {
1862
1863
        {\fp_to_dim:n
1864
          {
            (1 - #2)^3 * \text{tl_item:nn } {#1} {2}
1865
            + 3 * (1 - #2)^2 * (#2) * \tl_item:nn {#1} {5}
1866
            + 3 * (1 - #2) * (#2)^2 * \tl_item:nn {#1} {8}
            + (#2)^3 * \tl_item:nn {#1} {11}
1868
        }}
1869
1870
        {\fp_to_dim:n
1871
          (1 - #2)^3 * \text{tl_item:nn } {#1} {3}
1872
          + 3 * (1 - #2)^2 * (#2) * \\tl_item:nn {#1} {6}
1873
          + 3 * (1 - #2) * (#2)^2 * \tl_item:nn {#1} {9}
1874
1875
          + (#2)^3 * \tl_item:nn {#1} {12}
1876
        }}
     }
1877
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curvetoa_tl
1880
      \tl_put_right:Nx \l__spath_tmpa_tl
1881
     {
        {\fp_to_dim:n
1882
        {
1883
          (1 - #2)^2 * \tilde{41}_{item:nn}  {5}
1884
          + 2 * (1 - #2) * (#2) * \tl_item:nn {#1} {8}
1885
          + (#2)^2 * \tl_item:nn {#1} {11}
1886
1887
        }}
        {\fp_to_dim:n
1889
          (1 - #2)^2 * \tilde{41}_{item:nn}  {6}
1890
          + 2 * (1 - #2) * (#2) * \tl_item:nn {#1} {9}
1891
```

```
+ (#2)^2 * \tl_item:nn {#1} {12}
1892
        }}
1893
      7
1894
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curvetob_tl
1895
      \tl_put_right:Nx \l__spath_tmpa_tl
1896
1897
        {\fp_to_dim:n
1898
1899
          (1 - #2) * \tl_item:nn {#1} {8} + (#2) * \tl_item:nn {#1} {11}
        }}
1901
1902
        {\fp_to_dim:n
1903
          (1 - #2) * \tl_item:nn {#1} {9} + (#2) * \tl_item:nn {#1} {12}
1904
        }}
1905
1906
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_curveto_tl
1907
      \tl_put_right:Nx \l__spath_tmpa_tl {
1908
        {\tl_item:nn {#1} {11}}
1909
        {\tl_item:nn {#1} {12}}
1911
1912
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpa_tl
1913
1914
      \group end:
1915 }
    \cs_generate_variant:Nn \__spath_split_curve:nn {nv, nV}
1916
    \cs_new_protected_nopar:Npn \spath_split_curve:NNnn #1#2#3#4
1917
1918
      \__spath_split_curve:nn {#3}{#4}
1919
      \tl_set:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
1920
      \tl_set:Nx #2 {\tl_item:Nn \g_spath_output_tl {2}}
      \tl_gclear:N \g_spath_output_tl
1922
1923 }
    \cs_generate_variant:Nn \spath_split_curve:NNnn {NNnV, NNVn, NNVV}
1924
    \cs_new_protected_nopar:Npn \spath_gsplit_curve:NNnn #1#2#3#4
1925
1926
      \__spath_split_curve:nn {#3}{#4}
1927
      \tl_gset:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
1928
      \tl_gset:Nx #2 {\tl_item:Nn \g_spath_output_tl {2}}
1929
1930
      \tl_gclear:N \g_spath_output_tl
1931 }
   \cs_generate_variant:Nn \spath_gsplit_curve:NNnn {NNnV, NNVn, NNVV}
(End definition for \spath_split_curve:NNnn and \spath_gsplit_curve:NNnn.)
```

\spath_maybe_split_curve:Nn \spath_maybe_gsplit_curve:Nn Possibly splits a bezier curve to ensure that the pieces don't self-intersect. Figuring out whether a Bezier cubic self intersects is apparently a difficult problem so we don't bother. We compute a point such that if there is an intersection then it lies on either side of the point. I don't recall where the formula came from!

```
\tl_item:nn {#1} {3}
1939
        - 3 * \tl_item:nn {#1} {6}
1940
        + 3 * \tl_item:nn {#1} {9}
1941
        - \tl_item:nn {#1} {12}
1942
1943
1944
        (3 * \tl_item:nn {#1} {8} - 3 * \tl_item:nn {#1} {11})
1945
1946
        \tl_item:nn {#1} {2}
1948
        - 3 * tl_item:nn {#1} {5}
        + 3 * \tl_item:nn {#1} {8}
1950
        - \tl_item:nn {#1} {11}
1951
1952
1953
        (3 * \text{tl_item:nn } \{\#1\} \{9\} - 3 * \text{tl_item:nn } \{\#1\} \{12\})
1954
1955
      \fp_set:Nn \l__spath_tmpb_fp
1956
1957
        \tl_item:nn {#1} {2}
1959
        - 3 * \tl_item:nn {#1} {5}
1960
        + 3 * \tl_item:nn {#1} {8}
1961
        - \tl_item:nn {#1} {11}
1962
1963
1964
1965
        3 * \tl_item:nn {#1} {6}
1966
        - 6 * \tl_item:nn {#1} {9}
1967
        + 3 * \tl_item:nn {#1} {12}
1969
1970
1971
        \tl_item:nn {#1} {3}
1972
        - 3 * \tl_item:nn {#1} {6}
1973
        + 3 * \tl_item:nn {#1} {9}
1974
        - \tl_item:nn {#1} {12}
1975
1976
1977
        3 * \til_item:nn {#1} {5}
        - 6 * \tl_item:nn {#1} {8}
        + 3 * \tl_item:nn {#1} {11}
1981
1982
1983
      \fp_compare:nTF
1984
1985
        \l__spath_tmpb_fp != 0
1986
1987
1988
        \fp_set:Nn \l__spath_tmpa_fp {.5 * \l__spath_tmpa_fp / \l__spath_tmpb_fp}
1990
        \fp_compare:nTF
1991
          0 < \l_spath_tmpa_fp && \l_spath_tmpa_fp < 1</pre>
1992
```

```
{
                            1994
                                        __spath_split_curve:nV {#1} \l__spath_tmpa_fp
                            1995
                                   }
                            1996
                                    {
                            1997
                                      \t_gset:Nn \g_spath_output_tl { $$\#1$ {} $}
                            1998
                            1999
                                 }
                            2000
                                    \tl_gset:Nn \g__spath_output_tl { {#1} {} }
                            2002
                                 }
                            2003
                                  \group_end:
                            2004
                               }
                            2005
                                \cs_new_protected_nopar:Npn \spath_maybe_split_curve:NNn #1#2#3
                            2006
                            2007
                                  \__spath_maybe_split_curve:n {#3}
                            2008
                                  \tl_set:Nx #1 {\tl_item:Nn \g__spath_output_tl {1}}
                            2009
                                  \tl_set:Nx #2 {\tl_item:Nn \g__spath_output_tl {2}}
                            2010
                                  \tl_gclear:N \g__spath_output_tl
                            2012 }
                                \cs_generate_variant:Nn \spath_maybe_split_curve:NNn {NNn, NNV }
                               \cs_new_protected_nopar:Npn \spath_maybe_gsplit_curve:NNn #1#2#3
                            2014
                            2015
                                  \__spath_maybe_split_curve:n {#3}
                            2016
                                  \tl_gset:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
                            2017
                                  \tl_gset:Nx #2 {\tl_item:Nn \g_spath_output_tl {2}}
                            2018
                            2019
                                  \tl_gclear:N \g__spath_output_tl
                            2020 }
                               \cs_generate_variant:Nn \spath_maybe_gsplit_curve:NNn {NNn, NNV}
                           (End definition for \spath_maybe_split_curve:Nn and \spath_maybe_gsplit_curve:Nn.)
 \spath_split_curves:Nn
                           Slurp through the path ensuring that beziers don't self-intersect.
\spath_gsplit_curves:Nn
                               \cs_new_protected_nopar:Npn \__spath_split_curves:n #1
                            2023 {
                            2024
                                  \group_begin:
                                  \tl_set:Nn \l__spath_tmpa_tl {#1}
                            2025
                                  \tl_clear:N \l__spath_tmpb_tl
                            2026
                                  \tl_clear:N \l__spath_tmpc_tl
                            2027
                                  \bool_do_until:nn
                            2028
                                  {
                            2029
                                    \tl_if_empty_p:N \l__spath_tmpa_tl
                            2030
                            2031
                            2032
                                    \tl_set:Nx \l__spath_tmpc_tl {\tl_head:N \l__spath_tmpa_tl}
                            2033
                                    \tl_case:NnF \l__spath_tmpc_tl
                            2034
                            2035
                                      \c_spath_curvetoa_tl
                            2036
                            2037
                                      {
                                        \tl_clear:N \l__spath_tmpd_tl
                            2038
                                        \tl_set_eq:NN \l__spath_tmpd_tl \c_spath_moveto_tl
                            2039
                                        \tl_put_right:Nx \l__spath_tmpd_tl
                            2040
                            2041
                                          { \dim_use:N \l__spath_tmpa_dim }
```

}

1993

```
{ \dim_use:N \l__spath_tmpb_dim }
           }
2044
            \dim_set:Nn \l__spath_tmpa_dim
2045
            {
2046
              \tl_item:Nn \l__spath_tmpa_tl {8}
2047
            }
2048
            \dim_set:Nn \l__spath_tmpb_dim
2049
2050
              \tl_item:Nn \l__spath_tmpa_tl {9}
           }
            \prg_replicate:nn {3}
            {
2054
              \tl_put_right:Nx \l__spath_tmpd_tl
2055
              {
2056
                \tl_item:Nn \l__spath_tmpa_tl {1}
2057
                2058
                {\tl_item:Nn \l__spath_tmpa_tl {3}}
2059
2060
              \prg_replicate:nn {3}
              {
                \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
              }
           }
2065
2066
            \spath_maybe_split_curve:NNV
2067
            \l_spath_tmpd_tl
2068
            \l__spath_tmpe_tl
2069
            \l_spath_tmpd_tl
2070
            \prg_replicate:nn {3}
2071
              \tl_set:Nx \l__spath_tmpd_tl {\tl_tail:N \l__spath_tmpd_tl}
              \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl}
2075
            \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpd_tl
2076
            \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
2077
2078
       }
2079
2080
2081
          \dim_set:Nn \l__spath_tmpa_dim
            \tl_item:Nn \l__spath_tmpa_tl {2}
         }
2085
          \dim_set:Nn \l__spath_tmpb_dim
2086
          ₹
            \tl_item:Nn \l__spath_tmpa_tl {3}
2087
2088
          \tl_put_right:Nx \l__spath_tmpb_tl
2089
2090
            \tl_item:Nn \l__spath_tmpa_tl {1}
2091
            {\tl_item:Nn \l_spath_tmpa_tl {2}}
2092
            {\tl_item:Nn \l_spath_tmpa_tl {3}}
2095
          \prg_replicate:nn {3}
2096
```

```
}
                           2099
                                 }
                           2100
                                 \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
                                 \group_end:
                           2103
                               \cs_new_protected_nopar:Npn \spath_split_curves:Nn #1#2
                           2104
                           2105
                                  \__spath_split_curves:n {#2}
                           2106
                                 \tl_set_eq:NN #1 \g__spath_output_tl
                           2107
                                 \tl_gclear:N \g_spath_output_tl
                           2108
                           2109 }
                               \cs_generate_variant:Nn \spath_split_curves:Nn {NV, cV, cn, cv }
                           2110
                               \cs_new_protected_nopar:Npn \spath_split_curves:N #1
                           2111
                           2112
                                 \spath_split_curves:NV #1#1
                           2113
                           2114 }
                               \cs_generate_variant:Nn \spath_split_curves:N {c}
                               \cs_new_protected_nopar:Npn \spath_gsplit_curves:Nn #1#2
                           2117
                                 \__spath_split_curves:n {#2}
                           2118
                                 \tl_gset_eq:NN #1 \g__spath_output_tl
                           2119
                                 \t_gclean: N \g_spath_output_tl
                           2120
                           2121 }
                               \cs_generate_variant:Nn \spath_gsplit_curves:Nn {NV, cV, cn, cv }
                               \cs_new_protected_nopar:Npn \spath_gsplit_curves:N #1
                           2123
                           2124 {
                                 \spath_gsplit_curves:NV #1#1
                           2125
                           2126 }
                           2127 \cs_generate_variant:Nn \spath_gsplit_curves:N {c}
                           (End definition for \spath_split_curves:Nn and \spath_gsplit_curves:Nn.)
                          Splits a line segment.
 \spath_split_line:NNnn
\spath_gsplit_line:NNnn
                               \cs_new_protected_nopar:Npn \__spath_split_line:nn #1#2
                           2128
                           2129 {
                                 \group_begin:
                           2130
                                 \tl_set_eq:NN \l__spath_tmpa_tl \c_spath_moveto_tl
                                 \tl_put_right:Nx \l__spath_tmpa_tl {
                                   {\tl_item:nn {#1} {2}}
                                   {\tl_item:nn {#1} {3}}
                           2134
                           2135
                                 \tl_put_right:NV \l__spath_tmpa_tl \c_spath_lineto_tl
                           2136
                                 \tl_put_right:Nx \l__spath_tmpa_tl
                           2137
                           2138
                           2139
                                   {\fp_to_dim:n
                           2140
                                      (1 - #2) * \tl_item:nn {#1} {2} + (#2) * \tl_item:nn {#1} {5}
                           2141
                                   }}
                           2142
                                   {\fp_to_dim:n
                           2143
                           2144
                                      (1 - #2) * \tl_item:nn {#1} {3} + (#2) * \tl_item:nn {#1} {6}
                           2145
```

}

2098

\tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}

```
2147
      \tl_gclear:N \g_spath_output_tl
2148
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpa_tl
2149
2150
      \tl_clear:N \l__spath_tmpa_tl
      \tl_set_eq:NN \l__spath_tmpa_tl \c_spath_moveto_tl
      \tl_put_right:Nx \l__spath_tmpa_tl
2153
2154
        {\fp_to_dim:n
2155
2156
          (1 - #2) * \tl_item:nn {#1} {2} + (#2) * \tl_item:nn {#1} {5}
2157
        }}
2158
        {\fp_to_dim:n
2159
2160
          (1 - #2) * \tl_item:nn {#1} {3} + (#2) * \tl_item:nn {#1} {6}
        }}
2162
2163
      \tl_put_right:NV \l__spath_tmpa_tl \c_spath_lineto_tl
2164
      \tl_put_right:Nx \l__spath_tmpa_tl {
        {\tl_item:nn {#1} {5}}
        {\tl_item:nn {#1} {6}}
2167
2168
2169
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpa_tl
2170
2171
      \group_end:
2172 }
    \cs_new_protected_nopar:Npn \spath_split_line:NNnn #1#2#3#4
2173
2174
    {
      \__spath_split_line:nn {#3}{#4}
2175
2176
      \tl_set:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
2177
      \tl_set:Nx #2 {\tl_item:Nn \g__spath_output_tl {2}}
      \tl_gclear:N \g__spath_output_tl
2178
2179 }
    \cs_generate_variant:Nn \spath_split_line:NNnn {NNnV, NNVN, NNVV}
2180
    \cs_new_protected_nopar:Npn \spath_gsplit_line:NNnn #1#2#3#4
2181
2182
      \__spath_split_line:nn {#3}{#4}
      \tl_gset:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
2184
2185
      \tl_gset:Nx #2 {\tl_item:Nn \g_spath_output_tl {2}}
      \tl_gclear:N \g_spath_output_tl
2187 }
    \cs_generate_variant:Nn \spath_gsplit_line:NNnn {NNnV, NNVN, NNVV}
(End definition for \spath_split_line:NNnn and \spath_gsplit_line:NNnn.)
Split a path according to the parameter generated by the intersection routine. The
versions with two N arguments stores the two parts in two macros, the version with a
single N joins them back into a single path (as separate components).
    \cs_new_protected_nopar:Npn \__spath_split_at:nn #1#2
2189
2190 {
2191
      \group_begin:
2192
      \int_set:Nn \l__spath_tmpa_int {\fp_to_int:n {floor(#2) + 1}}
2193
      \fp_set:\n \l__spath_tmpa_fp {#2 - floor(#2)}
```

\spath_split_at:NNnn

\spath gsplit at:NNnn_\spath gsplit at:Nnn

\spath_split_at:Nnn

\spath_split_at:Nn

\spath_gsplit_at:Nn

2194

```
% Is split point near one end or other of a component?
2195
     \fp_compare:nT
2196
2197
        \l_spath_tmpa_fp < 0.01
2198
2199
     {
2200
        % Near the start, so we'll place it at the start
2201
        \fp_set:Nn \l__spath_tmpa_fp {0}
2202
     \fp_compare:nT
2204
2205
     {
        \l_spath_tmpa_fp > 0.99
2206
2207
     {
2208
        % Near the end, so we'll place it at the end
2209
        \fp_set:Nn \l__spath_tmpa_fp {0}
        \int_incr:N \l__spath_tmpa_int
2212
     \int_zero:N \l__spath_tmpb_int
     \bool_set_true:N \l__spath_tmpa_bool
2215
2216
     \tl_set:Nn \l__spath_tmpe_tl {#1}
2217
     \tl_clear:N \l__spath_tmpc_tl
2218
2219
     \dim_zero:N \l__spath_tmpa_dim
     \dim_zero:N \l__spath_tmpb_dim
     \bool_until_do:nn {
2223
2224
        \tl_if_empty_p:N \l__spath_tmpe_tl
2225
        11
        \int_compare_p:n { \l__spath_tmpa_int == \l__spath_tmpb_int }
2226
     }
2227
2228
        \tl_set:Nx \l__spath_tmpf_tl {\tl_head:N \l__spath_tmpe_tl}
2229
        \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2230
        \tl_case:Nn \l__spath_tmpf_tl
2232
2233
          \c_spath_lineto_tl
2234
            \int_incr:N \l__spath_tmpb_int
          }
          \c_spath_curvetoa_tl
          {
2238
            \int_incr:N \l__spath_tmpb_int
2239
2240
       }
2241
        \int_compare:nT { \l__spath_tmpb_int < \l__spath_tmpa_int }</pre>
2242
2243
2244
          \tl_put_right:NV \l__spath_tmpc_tl \l__spath_tmpf_tl
2246
          \tl_put_right:Nx \l__spath_tmpc_tl
          {{ \tl_head:N \l__spath_tmpe_tl }}
2247
          \dim_set:Nn \l__spath_tmpa_dim {\tl_head:N \l__spath_tmpe_tl}
2248
```

```
\tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2249
2250
          \tl_put_right:Nx \l__spath_tmpc_tl
2251
          {{ \tl_head:N \l__spath_tmpe_tl }}
          \dim_set:Nn \l__spath_tmpb_dim {\tl_head:N \l__spath_tmpe_tl}
2253
          \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2254
2255
2256
     }
2257
2258
     \tl_clear:N \l__spath_tmpd_tl
2259
     \tl_put_right:NV \l__spath_tmpd_tl \c_spath_moveto_tl
2260
     \tl_put_right:Nx \l__spath_tmpd_tl
2261
2262
     {
        {\dim_use:N \l__spath_tmpa_dim}
2263
        {\dim_use:N \l__spath_tmpb_dim}
2264
2265
2266
      \fp_compare:nTF
        \l_spath_tmpa_fp == 0
     }
     {
2271
        \tl_set_eq:NN \l__spath_tmpb_tl \l__spath_tmpd_tl
2272
        \tl_if_empty:NF \l__spath_tmpe_tl
2273
2274
          \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpf_tl
2275
          \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
2276
       }
2277
     }
2278
     {
2279
2280
2281
        \tl_case:Nn \l__spath_tmpf_tl
2282
          \c_spath_lineto_tl
2283
2284
            \tl_put_right:NV \l__spath_tmpd_tl \l__spath_tmpf_tl
2285
            \tl_put_right:Nx \l__spath_tmpd_tl
2286
2287
            {{ \tl_head:N \l_spath_tmpe_tl }}
            \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
            \tl_put_right:Nx \l__spath_tmpd_tl
            {{ \tl_head:N \l__spath_tmpe_tl }}
2291
            \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2292
2293
            \spath_split_line:NNVV
2294
            \l_spath_tmpa_tl
2295
            \l_spath_tmpb_tl
2296
            \l_spath_tmpd_tl
2297
2298
            \l_spath_tmpa_fp
            \prg_replicate:nn {3} {
2301
              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2302
```

```
2303
            \tl_put_right:NV \l__spath_tmpc_tl \l__spath_tmpa_tl
2304
            \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
2305
2306
          \c_spath_curvetoa_tl
2307
2308
            \tl_put_right:NV \l__spath_tmpd_tl \l__spath_tmpf_tl
2309
            \tl_put_right:Nx \l__spath_tmpd_tl
2310
            {{ \tl_head:N \l_spath_tmpe_tl }}
            \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2312
2313
            \tl_put_right:Nx \l__spath_tmpd_tl
2314
            {{ \tl_head:N \l__spath_tmpe_tl }}
            \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2316
2317
            \prg_replicate:nn {2} {
2318
2319
              \tl_put_right:Nx \l__spath_tmpd_tl
              { \tl_head:N \l__spath_tmpe_tl }
              \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
              \tl_put_right:Nx \l__spath_tmpd_tl
2324
              {{ \tl_head:N \l__spath_tmpe_tl }}
2325
              \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2326
2327
              \tl_put_right:Nx \l__spath_tmpd_tl
2328
              {{ \tl_head:N \l__spath_tmpe_tl }}
2329
              \tl_set:Nx \l__spath_tmpe_tl {\tl_tail:N \l__spath_tmpe_tl }
2330
2331
            \spath_split_curve:NNVV
2333
2334
            \l_spath_tmpa_tl
2335
            \l_spath_tmpb_tl
            \l__spath_tmpd_tl \l__spath_tmpa_fp
2336
            \prg_replicate:nn {3} {
2338
              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2339
2340
2341
            \tl_put_right:NV \l__spath_tmpc_tl \l__spath_tmpa_tl
            \tl_put_right:NV \l__spath_tmpb_tl \l__spath_tmpe_tl
          7
       }
2345
     }
2346
2347
      \tl_gclear:N \g__spath_output_tl
2348
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpc_tl
2349
      \__spath_tl_gput_right_braced:NV \g__spath_output_tl \l__spath_tmpb_tl
2350
2351
      \group_end:
2352
   \cs_new_protected_nopar:Npn \spath_split_at:NNnn #1#2#3#4
2354
2355
      \c spath_split_at:nn {#3}{#4}
      \tl_set:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
2356
```

```
\tl_set:Nx #2 {\tl_item:Nn \g_spath_output_tl {2}}
     \tl_gclear:N \g_spath_output_tl
2358
2359 }
   \cs_generate_variant:Nn \spath_split_at:NNnn {NNVn, NNVV, NNnV}
2360
   \cs_new_protected_nopar:Npn \spath_gsplit_at:NNnn #1#2#3#4
2361
2362
      \_ spath_ split_at:nn {#3}{#4}
2363
     \tl_gset:Nx #1 {\tl_item:Nn \g_spath_output_tl {1}}
2364
     \t \ #2 {\tl_item:Nn \g_spath_output_t1 {2}}
     \tl_gclear:N \g__spath_output_tl
2367 }
   \cs_generate_variant:Nn \spath_gsplit_at:NNnn {NNVn, NNVV, NNnV}
   \cs_new_protected_nopar:Npn \spath_split_at:Nnn #1#2#3
2369
2370
      \_spath_split_at:nn {#2}{#3}
2371
2372
     \tl_set:Nx #1
        \tl_item: Nn \g__spath_output_tl {1}
2374
        \tl_item: Nn \g__spath_output_tl {2}
2376
     \tl_gclear:N \g__spath_output_tl
2377
2378 }
   \cs_generate_variant:Nn \spath_split_at:Nnn {NVn, NVV}
2379
   \cs_new_protected_nopar:Npn \spath_split_at:Nn #1#2
2380
   {
2381
     \spath_split_at:NVn #1#1{#2}
2383
   \cs_new_protected_nopar:Npn \spath_gsplit_at:Nnn #1#2#3
2385
2386
      \_spath_split_at:nn {#2}{#3}
     \tl_gset:Nx #1
2387
2388
     {
        \tl_item:Nn \g__spath_output_tl {1}
2389
        \tl_item: Nn \g__spath_output_tl {2}
2390
2391
     \tl_gclear:N \g__spath_output_tl
2392
   \cs_generate_variant:Nn \spath_gsplit_at:Nnn {NVn, NVV}
   \cs_new_protected_nopar:Npn \spath_gsplit_at:Nn #1#2
2396
     \spath_gsplit_at:NVn #1#1{#2}
2397
2398 }
```

(End definition for \spath_split_at:NNnn and others.)

3.5 Shortening Paths

This code relates to shortening paths. For curved paths, the routine uses the derivative at the end to figure out how far back to shorten. This means that the actual length that it shortens by is approximate, but it is guaranteed to be along its length.

As in the previous section, there are various versions. In particular, there are versions where the path can be specified by a macro and is saved back into that macro.

\spath_shorten_at_end: Nnn This macro shortens a path from the end by a dimension.

```
2399 \cs_new_protected_nopar:Npn \__spath_shorten_at_end:nn #1#2
2400 {
     \int_compare:nTF
2401
        }
2405
        \group_begin:
2406
        \tl_set:Nn \l__spath_tmpa_tl {#1}
2407
        \tl_reverse:N \l__spath_tmpa_tl
2408
2409
       \tl_set:Nx \l__spath_tmpb_tl {\tl_item:Nn \l__spath_tmpa_tl {3}}
2410
2411
        \tl_clear:N \l__spath_tmpe_tl
2412
        \tl_if_eq:NNTF \l__spath_tmpb_tl \c_spath_curveto_tl
          \int_set:Nn \l__spath_tmpa_int {3}
2415
       }
2416
       {
2417
          \int_set:Nn \l__spath_tmpa_int {1}
2418
2419
2420
        \prg_replicate:nn { \l__spath_tmpa_int }
2421
2422
          \tl_put_right:Nx \l__spath_tmpe_tl
            {\tl_head:N \l__spath_tmpa_tl}
2426
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2427
2428
          \tl_put_right:Nx \l__spath_tmpe_tl
2429
            {\tl_head:N \l__spath_tmpa_tl}
2430
2431
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2432
          \tl_put_right:Nx \l__spath_tmpe_tl
2433
            \tl_head:N \l__spath_tmpa_tl
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2437
2438
2439
        \tl_put_right:Nx \l__spath_tmpe_tl
2440
2441
          {\tl_item:Nn \l__spath_tmpa_tl {1}}
2442
          {\tl_item:Nn \l__spath_tmpa_t1 {2}}
2443
        \tl_put_right:NV \l__spath_tmpe_tl \c_spath_moveto_tl
       \tl_reverse:N \l__spath_tmpa_tl
2447
2448
       \fp_set:Nn \l__spath_tmpa_fp
2449
2450
          \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {4}}
2451
```

```
2452
          \label{lem:nn ll_spath_tmpe_tl {1}} $$ \dim_to_fp:n {\tilde l_item:Nn ll_spath_tmpe_tl {1}} $$
2453
2454
2455
        \fp_set:Nn \l__spath_tmpb_fp
2456
2457
          \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {5}}
2458
          \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {2}}
2461
        \fp_set:Nn \l__spath_tmpc_fp
2463
2464
          sqrt(
2465
          \l__spath_tmpa_fp * \l__spath_tmpa_fp
2466
2467
          \l_spath_tmpb_fp * \l_spath_tmpb_fp
2468
          ) * \l__spath_tmpa_int
2469
        \fp_compare:nTF
2472
2473
          \l_spath_tmpc_fp > #2
2474
        }
2475
        {
2476
2477
          \fp_set:Nn \l__spath_tmpc_fp
2478
2479
             (\l_spath_tmpc_fp - #2)/ \l_spath_tmpc_fp
2480
          \tl_reverse:N \l__spath_tmpe_tl
2483
2484
          \tl_if_eq:NNTF \l__spath_tmpb_tl \c_spath_curveto_tl
2485
2486
             \spath_split_curve:NNVV
2487
             \l__spath_tmpc_tl
2488
             \l_spath_tmpd_tl
2489
2490
             \l_spath_tmpe_tl
             \l_spath_tmpc_fp
          }
             \spath_split_line:NNVV
             \l_spath_tmpc_tl
2495
             \l_spath_tmpd_tl
2496
             \l_spath_tmpe_tl
2497
             \l_spath_tmpc_fp
2498
2499
2500
2501
          \prg_replicate:nn {3}
             \tl_set:Nx \l__spath_tmpc_tl {\tl_tail:N \l__spath_tmpc_tl}
2504
2505
```

```
2512
                                            \tl_count:N \l__spath_tmpa_t1 > 3
                                2513
                                2515
                                            \dim_set:Nn \l__spath_tmpa_dim {\fp_to_dim:n {#2 - \l__spath_tmpc_fp } }
                                2516
                                            \spath_shorten_at_end:NV \l__spath_tmpa_tl \l__spath_tmpa_dim
                                2517
                                2518
                                2519
                                2520
                                        \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
                                2521
                                        \group_end:
                                2522
                                      }
                                2523
                                        \tl_gset:Nn \g__spath_output_tl {#1}
                                2526
                                2527 }
                                    \cs_new_protected_nopar:Npn \spath_shorten_at_end:Nnn #1#2#3
                                2528
                                2529
                                    {
                                      \__spath_shorten_at_end:nn {#2}{#3}
                                2530
                                      \tl_set_eq:NN #1 \g__spath_output_tl
                                2531
                                      \tl_gclear:N \g__spath_output_tl
                                2532
                                2533 }
                                    \cs_generate_variant:Nn \spath_shorten_at_end:Nnn {NVV, cnn, cVV, NVn}
                                    \cs_new_protected_nopar:Npn \spath_shorten_at_end:Nn #1#2
                                      \spath_shorten_at_end:NVn #1#1{#2}
                                2537
                                2538 }
                                    \cs_generate_variant:Nn \spath_shorten_at_end:Nn {cn, cV, NV}
                                    \cs_new_protected_nopar:Npn \spath_gshorten_at_end:Nnn #1#2#3
                                2540
                                2541
                                      \_spath_shorten_at_end:nn {#2}{#3}
                                2542
                                2543
                                      \tl_gset_eq:NN #1 \g__spath_output_tl
                                2544
                                      \tl_gclear:N \g_spath_output_tl
                                    \cs_generate_variant:Nn \spath_gshorten_at_end:Nnn {NVV, cnn, cVV, NVn}
                                    \cs_new_protected_nopar:Npn \spath_gshorten_at_end:Nn #1#2
                                2548
                                      \spath_gshorten_at_end:NVn #1#1{#2}
                                2549
                                2550 }
                                2551 \cs_generate_variant:Nn \spath_gshorten_at_end:Nn {cn, cV, NV}
                                (End definition for \spath_shorten_at_end:Nnn.)
                               This macro shortens a path from the start by a dimension.
\spath_shorten_at_start:Nnn
 \spath_shorten_at_start:Nn
                                    \cs_new_protected_nopar:Npn \__spath_shorten_at_start:nn #1#2
\spath_gshorten_at_start:Nnn
\spath_gshorten_at_start:Nn
                                      \int_compare:nTF
                                2555
                                      {
```

\tl_put_right:NV \l__spath_tmpa_tl \l__spath_tmpc_tl

2507

2508

2509 2510

2511

}

{

\int_compare:nT

```
\t1_count:n {#1} > 3
2556
     }
2557
     {
2558
      \group_begin:
2559
     \tl_set:Nn \l__spath_tmpa_tl {#1}
2560
2561
     \tl_set:Nx \l__spath_tmpb_tl {\tl_item:Nn \l__spath_tmpa_tl {4}}
2562
2563
        \tl_clear:N \l__spath_tmpe_tl
2565
     \tl_if_eq:NNTF \l__spath_tmpb_tl \c_spath_curvetoa_tl
2567
        \int_set:Nn \l__spath_tmpa_int {3}
2568
     }
2569
2570
        \int_set:Nn \l__spath_tmpa_int {1}
2571
2572
2573
     \tl_set_eq:NN \l__spath_tmpe_tl \c_spath_moveto_tl
2574
     \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl }
     \prg_replicate:nn { \l__spath_tmpa_int }
2577
2578
        \__spath_tl_put_right_braced:Nx
2579
        \l_spath_tmpe_tl
2580
        {\tl_item:Nn \l__spath_tmpa_tl {1}}
2581
        \__spath_tl_put_right_braced:Nx
2582
        \l_spath_tmpe_tl
2583
        {\tl_item:Nn \l__spath_tmpa_tl {2}}
2584
        \tl_put_right:Nx \l__spath_tmpe_tl {\tl_item:Nn \l__spath_tmpa_tl {3}}
2586
2587
        \prg_replicate:nn {3}
2588
          \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl }
2589
       }
2590
2591
      \__spath_tl_put_right_braced:Nx
2592
     \l_spath_tmpe_tl
2593
     {\tl_item:Nn \l_spath_tmpa_tl {1}}
      \__spath_tl_put_right_braced:Nx
     \l_spath_tmpe_tl
     {\tilde n} = {\tilde n} - {\tilde n} 
     \fp_set:Nn \l__spath_tmpa_fp
2599
2600
        \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {5}}
2601
2602
        \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {2}}
2603
2604
2605
     \fp_set:Nn \l__spath_tmpb_fp
2607
        \dim_to_fp:n {\tl_item:Nn \l__spath_tmpe_tl {6}}
2608
2609
```

```
\label{lem:nn loss} $$\dim_to_fp:n {\tilde \mathbb N}  \label{loss} $$1_spath_tmpe_tl {3}}
2610
2611
2612
      \footnotemark \ensuremath{\texttt{Nn } l\_spath\_tmpc\_fp}
2613
2614
2615
        \l_spath_tmpa_fp * \l_spath_tmpa_fp
2616
2617
        \l_spath_tmpb_fp * \l_spath_tmpb_fp
2619
         \l__spath_tmpa_int
2621
2622
2623
      \fp_compare:nTF
2624
2625
         \l_spath_tmpc_fp > #2
2626
      }
2627
         \fp_set:Nn \l__spath_tmpc_fp
2631
           #2/ \l__spath_tmpc_fp
2632
2633
2634
        \tl_if_eq:NNTF \l__spath_tmpb_tl \c_spath_curvetoa_tl
2635
2636
           \spath_split_curve:NNVV
2637
           \l_spath_tmpc_tl
2638
           \l_spath_tmpd_tl
           \l_spath_tmpe_tl
           \l_spath_tmpc_fp
        }
2642
2643
           \spath_split_line:NNVV
2644
           \l_spath_tmpc_tl
2645
           \l__spath_tmpd_tl
2646
2647
           \l_spath_tmpe_tl
2648
           \l_spath_tmpc_fp
         \prg_replicate:nn {2}
2652
           \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
2653
2654
2655
         \tl_put_left:NV \l__spath_tmpa_tl \l__spath_tmpd_tl
2656
2657
      }
2658
2659
      {
        \tl_put_left:NV \l__spath_tmpa_tl \c_spath_moveto_tl
2662
        \int_compare:nT
2663
```

```
\tl_count:N \l__spath_tmpa_t1 > 3
2665
        }
2666
        {
2667
           \dim_set:Nn \l__spath_tmpa_dim {\fp_to_dim:n {#2 - \l__spath_tmpc_fp } }
2668
          \spath_shorten_at_start:NV \l__spath_tmpa_tl \l__spath_tmpa_dim
2669
2670
      }
2671
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
2673
2674
      \group_end:
      }
2675
      {
2676
        \tl_gset:Nn \g__spath_output_tl {#1}
2677
2678
2679
    cs_new_protected_nopar:Npn \spath_shorten_at_start:Nnn #1#2#3
2680
2681
      \__spath_shorten_at_start:nn {#2}{#3}
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
2685
    \cs_generate_variant:Nn \spath_shorten_at_start:Nnn {NVV, cnn, cVV, NVn}
2686
    \cs_new_protected_nopar:Npn \spath_shorten_at_start:Nn #1#2
2687
   {
2688
      \spath_shorten_at_start:NVn #1#1{#2}
2689
2690 }
    \cs_generate_variant:Nn \spath_shorten_at_start:Nn {cn, cV, NV}
    \cs_new_protected_nopar:Npn \spath_gshorten_at_start:Nnn #1#2#3
2692
      \__spath_shorten_at_start:nn {#2}{#3}
2694
      \tl_gset_eq:NN #1 \g__spath_output_tl
2696
      \tl_gclear:N \g__spath_output_tl
2697
    \cs_generate_variant:Nn \spath_gshorten_at_start:Nnn {NVV, cnn, cVV, NVn}
2698
    \cs_new_protected_nopar:Npn \spath_gshorten_at_start:Nn #1#2
2699
2700
2701
      \spath_gshorten_at_start:NVn #1#1{#2}
2702 }
   \cs_generate_variant:Nn \spath_gshorten_at_start:Nn {cn, cV, NV}
(End definition for \spath_shorten_at_start:Nnn and others.)
```

3.6 Points on a Path

\spath_point_at:Nnn \spath_gpoint_at:Nnn Get the location of a point on a path, using the same location specification as the intersection library.

```
2704 \cs_new_protected_nopar:Npn \__spath_point_at:nn #1#2
2705 {
2706   \group_begin:
2707   \int_set:Nn \l__spath_tmpa_int {\fp_to_int:n {floor(#2) + 1}}
2708   \fp_set:Nn \l__spath_tmpa_fp {#2 - floor(#2)}
2709
2710   \spath_segments_to_seq:Nn \l__spath_tmpa_seq {#1}
```

```
\int_compare:nTF
2712
2713
        \l__spath_tmpa_int < 1</pre>
2714
      {
2716
        \spath_initialpoint:Nn \l__spath_tmpc_tl {#1}
2717
2718
2719
        \int_compare:nTF
2720
2721
           \l_spath_tmpa_int > \seq_count:N \l_spath_tmpa_seq
        }
        {
2724
           \spath_finalpoint: Nn \l__spath_tmpc_tl {#1}
2725
2726
2728
          \t: Nx
           \l_spath_tmpa_tl
           {\seq_item:Nn \l__spath_tmpa_seq { \l__spath_tmpa_int} }
          \int_compare:nTF
2733
2734
             \t: N \l_spath_tmpa_tl > 3
2735
2736
             \tl_set:Nx \l__spath_tmpb_tl {\tl_item:Nn \l__spath_tmpa_tl {4}}
2738
2739
             \label{lem:Nn ll_spath_tmpb_tl {\line:Nn ll_spath_tmpa_tl {1}}} $$ $$ \tilde{\mathbb{N}} \leq \tilde{\mathbb{N}} . $$
          }
2742
2743
          \tl_clear:N \l__spath_tmpc_tl
2744
2745
           \tl_case:Nn \l__spath_tmpb_tl
2746
2747
2748
             \c_spath_moveto_tl
2749
               \tl_set:Nx \l__spath_tmpc_tl
               {
                    \tl_item:Nn \l__spath_tmpa_tl {2}
2754
2755
                    \tl_item:Nn \l__spath_tmpa_tl {3}
2756
2757
               }
2758
             }
2759
2760
             \c_spath_lineto_tl
               \tl_set:Nx \l__spath_tmpc_tl
2763
               {
2764
```

```
{\fp_to_dim:n
2766
                  ₹
                    (1 - l_spath_tmpa_fp) * ( l_item:Nn l_spath_tmpa_tl {2} )
2767
2768
                    \l_spath_tmpa_fp * ( \tl_item:Nn \l_spath_tmpa_tl {5} )
2769
                  }
                }
2771
                {\fp_to_dim:n
2772
                    (1 - \l_spath_tmpa_fp) * ( \tl_item:\n \l_spath_tmpa_tl {3} )
                    \l_spath_tmpa_fp * ( \tl_item:Nn \l_spath_tmpa_tl {6} )
2776
2777
                }
2778
              }
2779
            }
2780
2781
            \c_spath_closepath_tl
2782
              \tl_set:Nx \l__spath_tmpc_tl
              {
                {\tt \{\fp\_to\_dim:n}
2787
                    (1 - \l_spath_tmpa_fp) * ( \tl_item: Nn \l_spath_tmpa_tl {2} )
2789
                    \l_spath_tmpa_fp * ( \tl_item:Nn \l_spath_tmpa_tl {5} )
2790
                  }
2791
                }
2792
                {\fp_to_dim:n
2793
                    (1 - \l_spath_tmpa_fp) * ( \tl_item:Nn \l_spath_tmpa_tl {3} )
                    \l_spath_tmpa_fp * ( \tl_item:Nn \l_spath_tmpa_tl {6} )
2797
2798
2799
              }
2800
            }
2801
2802
2803
            \c_spath_curvetoa_tl
              \tl_set:Nx \l__spath_tmpc_tl
              {
                {\tt \{\fp\_to\_dim:n}
                    (1 - \l_spath_tmpa_fp)^3 * \tl_item:Nn \l_spath_tmpa_tl {2}
                    + 3 * (1 - \l_spath_tmpa_fp)^2 * (\l_spath_tmpa_fp)
2810
                    * tl_item:Nn \l_spath_tmpa_tl {5}
2811
                    + 3 * (1 - \l_spath_tmpa_fp) * (\l_spath_tmpa_fp)^2
2812
                    * \tl_item: Nn \l__spath_tmpa_tl {8}
2813
                    + (\l_spath_tmpa_fp)^3 * \tl_item:Nn \l_spath_tmpa_tl {11}
2814
                }}
                {\fp_to_dim:n
2817
                  {
                    (1 - \l_spath_tmpa_fp)^3 * \tl_item:Nn \l_spath_tmpa_tl {3}
2818
```

```
+ 3 * (1 - \l_spath_tmpa_fp)^2 * (\l_spath_tmpa_fp)
2819
                     * \tl_item:Nn \l__spath_tmpa_tl {6}
2820
                     + 3 * (1 - \l_spath_tmpa_fp) * (\l_spath_tmpa_fp)^2
2821
                     * \tl_item:Nn \l__spath_tmpa_tl {9}
2822
                     + (\l_spath_tmpa_fp)^3 * \tl_item:Nn \l_spath_tmpa_tl {12}
2823
                }}
2824
              }
2825
            }
2826
          }
        }
2828
      }
2829
2830
      \t_gclean: N \g_spath_output_tl
2831
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpc_tl
2832
      \group_end:
2833
2834 }
    \cs_new_protected_nopar:Npn \spath_point_at:Nnn #1#2#3
2835
2836
      \__spath_point_at:nn {#2}{#3}
2837
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
2840 }
    \cs_generate_variant:Nn \spath_point_at:Nnn {NVn, NvV, NnV}
2841
    \cs_new_protected_nopar:Npn \spath_gpoint_at:Nnn #1#2#3
2842
   {
2843
2844
      \_ spath_point_at:nn {#2}{#3}
      \tl_gset_eq:NN #1 \g__spath_output_tl
2845
      \tl_gclear:N \g_spath_output_tl
2846
\verb| cs_generate_variant:Nn \spath_gpoint_at:Nnn {NVn, NnV}| \\
(End definition for \spath_point_at:Nnn and \spath_gpoint_at:Nnn.)
```

\spath_tangent_at:Nnn \spath_gtangent_at:Nnn Get the tangent at a point on a path, using the same location specification as the intersection library.

```
2849
   \cs_new_protected_nopar:Npn \__spath_tangent_at:nn #1#2
2850
2851
      \group_begin:
      \int_set:Nn \l__spath_tmpa_int {\fp_to_int:n {floor(#2) + 1}}
     \fp_set:Nn \l__spath_tmpa_fp {#2 - floor(#2)}
2854
     \spath_segments_to_seq:Nn \l__spath_tmpa_seq {#1}
2855
2856
     \int_compare:nTF
2857
2858
        \l_spath_tmpa_int < 1
2859
2860
2861
        \spath_initialpoint:Nn \l__spath_tmpc_tl {#1}
     }
2863
     {
        \int_compare:nTF
2865
2866
          \l__spath_tmpa_int > \seq_count:N \l__spath_tmpa_seq
2867
```

```
}
2868
        {
2869
           \spath_finalpoint:Nn \l__spath_tmpc_tl {#1}
2870
        }
2871
2872
2873
          \tl_set:Nx
2874
           \l_spath_tmpa_tl
2875
           {\seq_item:Nn \l__spath_tmpa_seq { \l__spath_tmpa_int} }
          \int_compare:nTF
          {
2879
             \t! count:N \l_spath_tmpa_tl > 3
2880
2881
          {
2882
             \label{lem:Nn ll_spath_tmpb_tl {\tl_item:Nn ll_spath_tmpa_tl {4}}} $$ \t l_set:Nx \label{ll_spath_tmpb_tl {\tl_item:Nn ll_spath_tmpa_tl {4}}} $$
2883
          }
2884
             \tl_set:Nx \l__spath_tmpb_tl {\tl_item:Nn \l__spath_tmpa_tl {1}}
          \tl_clear:N \l__spath_tmpc_tl
2890
          \tl_case:Nn \l__spath_tmpb_tl
2891
2892
             \c_spath_moveto_tl
2893
2894
               \tl_set:Nx \l__spath_tmpc_tl
2895
2896
                    \tl_item:Nn \l__spath_tmpa_tl {2}
                 }
2900
                    \tl_item:Nn \l__spath_tmpa_t1 {3}
2901
2902
               }
2903
             }
2904
2905
2906
             \c_spath_lineto_tl
               \tl_set:Nx \l__spath_tmpc_tl
               {
                  {\tt \{\fp\_to\_dim:n}
2910
2911
                       ( \t \ \lambda l_spath_tmpa_tl {5} )
2912
2913
                       ( \tl_item:Nn \l__spath_tmpa_tl {2} )
2914
                    }
2915
                 }
2916
2917
                  {\fp_to_dim:n
                      ( \t \ \lambda l_spath_tmpa_tl {6} )
2920
                      2921
```

```
}
2922
                 }
2923
              }
2924
            }
2925
2926
             \c_spath_closepath_tl
2927
2928
               \tl_set:Nx \l__spath_tmpc_tl
2929
               {
                 {\fp_to_dim:n
                      ( \tl_item:Nn \l__spath_tmpa_tl {5} )
2933
2934
                      ( \tl_item: Nn \l__spath_tmpa_tl {2} )
2935
2936
                 }
2937
                 {\fp_to_dim:n
2938
2939
                      ( \tl_item:Nn \l__spath_tmpa_tl {6} )
                      ( \tl_item:Nn \l__spath_tmpa_tl {3} )
                   }
2943
                 }
2944
              }
2945
            }
2946
2947
             \c_spath_curvetoa_tl
2948
2949
               \tl_set:Nx \l__spath_tmpc_tl
2950
               {
                 {\tt \{\fp\_to\_dim:n}
                   {
                     3*(1 - l_spath_tmpa_fp)^2 * (l_item:Nn l_spath_tmpa_tl {5})
2954
                     - \t: Nn \l_spath_tmpa_t1 \{2\})
2955
                     + 6 * (1 - \l__spath_tmpa_fp) * (\l__spath_tmpa_fp) *
2956
                     (\tl_item:Nn \l__spath_tmpa_tl {8}
2957
                      - \tl_item:Nn \l__spath_tmpa_tl {5})
2958
                     + 3*(\l_spath_tmpa_fp)^2 * (\tl_item:Nn \l_spath_tmpa_tl {11}
2959
                     - \tl_item:Nn \l__spath_tmpa_tl {8})
2960
                   }
                 }
                 {\tt \{\fp\_to\_dim:n}
                   {
                     3*(1 - l_spath_tmpa_fp)^2 * (l_item:Nn l_spath_tmpa_tl {6}
2965
                     - \tl_item: Nn \l__spath_tmpa_tl {3})
2966
                     + 6 * (1 - \l__spath_tmpa_fp) * (\l__spath_tmpa_fp) *
2967
                      (\tl_item: Nn \l_spath_tmpa_tl \ \{9\} 
2968
                      - \tl_item: Nn \l__spath_tmpa_tl {6})
2969
                     + 3*(\lambda_{path_tmpa_fp})^2 * (\lambda_{tl_item:Nn \lambda_{path_tmpa_tl} \{12\}
2970
2971
                     - \tl_item:Nn \l__spath_tmpa_tl {9})
                 }}
              }
2973
            }
2974
          }
2975
```

```
}
2976
      }
2977
2978
      \tl_gclear:N \g_spath_output_tl
2979
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpc_tl
2980
      \group_end:
2981
2982
    \cs_new_protected_nopar:Npn \spath_tangent_at:Nnn #1#2#3
2983
      \__spath_tangent_at:nn {#2}{#3}
      \tl_set_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
2987
2988
    \cs_generate_variant:Nn \spath_tangent_at:Nnn {NVn, NvV, NnV}
2989
    \cs_new_protected_nopar:Npn \spath_gtangent_at:Nnn #1#2#3
2990
   {
2991
      \__spath_tangent_at:nn {#2}{#3}
2992
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
2995 }
   \cs_generate_variant:Nn \spath_gtangent_at:Nnn {NVn, NvV, NnV}
(End definition for \spath_tangent_at:Nnn and \spath_gtangent_at:Nnn.)
```

\spath_transformation_at:Nnn \spath gtransformation at:Nnn Gets a transformation that will align to a point on the path with the x-axis along the path.

```
\cs_new_protected_nopar:Npn \__spath_transformation_at:nn #1#2
2998 {
      \group_begin:
2999
     \tl_clear:N \l__spath_tmpa_tl
      \_{spath\_tangent\_at:nn } {#1}{#2}
3001
     \tl_set_eq:NN \l__spath_tmpb_tl \g__spath_output_tl
3002
      \fp_set:Nn \l__spath_tmpa_fp
3003
3004
        sqrt(
3005
        (\tl_item:Nn \l__spath_tmpb_tl {1})^2
3006
        (\tl_item:Nn \l_spath_tmpb_tl {2})^2
     \fp_compare:nTF {\l__spath_tmpa_fp = 0}
3011
3012
        \fp_set:Nn \l__spath_tmpa_fp {1}
3013
        \fp_set:Nn \l__spath_tmpb_fp {0}
3014
3015
3016
        \fp_set:Nn \l__spath_tmpb_fp
3017
        { (\tl_item: Nn \l_spath_tmpb_tl {2}) / \l_spath_tmpa_fp }
3018
        \fp_set:Nn \l__spath_tmpa_fp
3019
3020
        { (\tl_item:\n \l_spath_tmpb_tl {1}) / \l_spath_tmpa_fp }
3021
     \tl_set:Nx \l__spath_tmpa_tl
3022
3023
     {
        { \fp_to_decimal:n { \l__spath_tmpa_fp } }
3024
```

```
{ \fp_to_decimal:n { \l__spath_tmpb_fp } }
       { \fp_to_decimal:n {- \l_spath_tmpb_fp } }
3026
       { \lceil fp\_to\_decimal:n \{ \l\_spath\_tmpa\_fp \} }
3027
3028
      \_ spath_point_at:nn {#1}{#2}
3029
      \tl_put_right:NV \l__spath_tmpa_tl \g__spath_output_tl
3030
     \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
3031
      \group_end:
3032
3033 }
   \cs_new_protected_nopar:Npn \spath_transformation_at:Nnn #1#2#3
3034
3035
      \__spath_transformation_at:nn {#2}{#3}
3036
      \tl_set_eq:NN #1 \g__spath_output_tl
3037
      \tl_gclear:N \g__spath_output_tl
3038
3039 }
   \cs_generate_variant:Nn \spath_transformation_at:Nnn {NVn, NvV, NnV, NvV}
3040
   \cs_new_protected_nopar:Npn \spath_gtransformation_at:Nnn #1#2#3
3041
3042
      \__spath_transformation_at:nn {#2}{#3}
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
3046
3047 \cs_generate_variant:Nn \spath_gtransformation_at:Nnn {NVn, NVV, NnV}
```

3.7 Intersection Routines

Note: I'm not consistent with number schemes. The intersection library is 0-based, but the user interface is 1-based (since if we "count" in a \foreach then it starts at 1). This should be more consistent.

(End definition for \spath_transformation_at:Nnn and \spath_gtransformation_at:Nnn.)

```
\spath_intersect:NN \spath_intersect:nn
```

Pass two spaths to pgf's intersection routine.

```
\cs_new_protected_nopar:Npn \spath_intersect:NN #1#2
3048
3049 {
      \pgfintersectionofpaths%
3050
3051
        \pgfsetpath #1
3052
        \pgfsetpath #2
     }
3055
3056
   \cs_new_protected_nopar:Npn \spath_intersect:nn #1#2
3057
3058 {
     \tl_set:Nn \l__spath_intersecta_tl {#1}
3059
     \tl_set:Nn \l__spath_intersectb_tl {#2}
3060
      \spath_intersect:NN \l__spath_intersecta_tl \l__spath_intersectb_tl
3061
3062 }
```

(End definition for \spath_intersect:NN and \spath_intersect:nn.)

\spath_split_component_at_intersections:Nnn

Split a component where it intersects a path. Key assumption is that the first path is a single component, so if it is closed then the end joins up to the beginning. The component is modified but the path is not.

```
\cs_new_protected_nopar:Npn \__spath_split_component_at_intersections:nn #1#2
3064
      \group_begin:
3065
     \tl_clear:N \l__spath_tmpe_tl
3066
      \seq_clear:N \l__spath_tmpb_seq
3067
3068
     % Find the intersections of these segments
3069
     \tl_set:Nn \l__spath_tmpb_tl {#1}
3070
     \tl_set:Nn \l__spath_tmpc_tl {#2}
3071
3072
     \spath_reallength: Nn \l__spath_tmpa_int {#1}
3073
3074
     % Remember if the component is closed
3075
      \spath_finalaction:NV \l__spath_tmpa_tl \l__spath_tmpb_tl
3076
3077
      \bool_set:Nn \l__spath_closed_bool
3078
3079
        \tl_if_eq_p:NN \l__spath_tmpa_tl \c_spath_closepath_tl
3080
     % Open it
3083
      \spath_open:N \l__spath_tmpb_tl
3084
3085
     % Sort intersections along the component
3086
      \pgfintersectionsortbyfirstpath
3087
      \spath_intersect:NN \l__spath_tmpb_tl \l__spath_tmpc_tl
3088
3089
     % If we get intersections
3090
     \int_compare:nT {\pgfintersectionsolutions > 0}
3091
       \% Find the times of the intersections on the component
3093
        \int_step_inline:nnnn {1} {1} {\pgfintersectionsolutions}
3094
3095
          \pgfintersectiongetsolutiontimes{##1}{\l__spath_tmph_tl}{\l__spath_tmpi_tl}
3096
          \seq_put_left:NV \l__spath_tmpb_seq \l__spath_tmph_tl
3097
3098
3099
        \seq_get_left:NN \l__spath_tmpb_seq \l__spath_tmpa_tl
3100
3101
        \fp_compare:nT
          \l_spath_tmpa_tl > \l_spath_tmpa_int - .01
       }
3104
        {
3105
          \bool_set_false:N \l__spath_closed_bool
3106
3107
        \seq_get_right:NN \l__spath_tmpb_seq \l__spath_tmpa_tl
3108
        \fp_compare:nT
3109
3110
          \l_spath_tmpa_tl < .01
3111
3112
       }
3113
        {
3114
          \bool_set_false:N \l__spath_closed_bool
3115
3116
```

```
3117
        \tl_set:Nn \l__spath_tmpg_tl {-1}
3118
3119
        \seq_map_inline: Nn \l__spath_tmpb_seq
3120
3121
          \tl_set:Nn \l__spath_tmph_tl {##1}
3122
3123
          \tl_set_eq:NN \l__spath_tmpa_tl \l__spath_tmph_tl
3124
3125
          \int_compare:nT
3126
          {
            \fp_to_int:n {floor( \l__spath_tmph_tl) }
3127
3128
             \fp_to_int:n {floor( \l__spath_tmpg_tl) }
3129
          }
3130
3131
             \tl_set:Nx \l__spath_tmph_tl
3132
            {
3133
               \fp_eval:n {
3134
                 {\tt floor(\ \ \ \ \ } {\tt l\_spath\_tmph\_tl\ )}
                 ( \l_spath_tmph_tl - floor( \l_spath_tmph_tl) )
3138
                 ( \l_spath_tmpg_tl - floor( \l_spath_tmpg_tl) )
3139
              }
3140
            }
3141
3142
          \tl_set_eq:NN \l__spath_tmpg_tl \l__spath_tmpa_tl
3143
3144
          \spath_split_at:NNVV
3145
          \l_spath_tmpd_tl
          \l_spath_tmpf_tl
3147
          \l_spath_tmpb_tl
3148
3149
          \l_spath_tmph_tl
3150
          \tl_put_left:NV \l__spath_tmpe_tl \l__spath_tmpf_tl
3151
          \tl_set_eq:NN \l__spath_tmpb_tl \l__spath_tmpd_tl
3152
3153
3154
        }
3155
        \tl_put_left:NV \l__spath_tmpe_tl \l__spath_tmpb_tl
        \spath_remove_empty_components:N \l__spath_tmpe_tl
3159
3160
        \tl_set_eq:NN \l__spath_tmpb_tl \l__spath_tmpe_tl
3161
     }
3162
3163
      \bool_if:NT \l__spath_closed_bool
3164
3165
     {
3166
        \spath_join_component:Nn \l__spath_tmpb_tl {1}
3167
     }
3168
      \tl_gclear:N \g__spath_output_tl
3169
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpb_tl
3170
```

```
3171
      \group_end:
3172
3173
    \cs_new_protected_nopar:Npn \spath_split_component_at_intersections:Nnn #1#2#3
3174
3175
      \__spath_split_component_at_intersections:nn {#2}{#3}
3176
      \tl_set_eq:NN #1 \g__spath_output_tl
3177
      \tl_gclear:N \g__spath_output_tl
3178
3179 }
    \cs_generate_variant:Nn \spath_split_component_at_intersections:Nnn {NVn, NVV}
    cs_new_protected_nopar:Npn \spath_split_component_at_intersections:Nn #1#2
3181
3182
      \spath_split_component_at_intersections:NVn #1#1{#2}
3183
3184
    \cs_generate_variant:Nn \spath_split_component_at_intersections:Nn {cn, cv}
3185
    cs_new_protected_nopar:Npn \spath_gsplit_component_at_intersections:Nnn #1#2#3
3186
3187
      \__spath_split_component_at_intersections:nn {#2}{#3}
3188
      \tl_gset_eq:NN #1 \g__spath_output_tl
 3189
      \tl_gclear:N \g__spath_output_tl
3191 }
    \cs_generate_variant:Nn \spath_gsplit_component_at_intersections:Nnn {NVn, NVV}
    \cs_new_protected_nopar:Npn \spath_gsplit_component_at_intersections:Nn #1#2
3193
3194
    {
      \spath_gsplit_component_at_intersections:NVn #1#1{#2}
3195
3196 }
3197 \cs_generate_variant:Nn \spath_gsplit_component_at_intersections:Nn {cn, cv}
(End definition for \spath_split_component_at_intersections:Nnn.)
Split paths at their intersections. The path versions only split the first path. The others
3198 \cs_new_protected_nopar:Npn \__spath_split_path_at_intersections:nn #1#2
```

\spath split path at intersections:Nnn \spath split path at intersections:Nn \spath gsplit path at intersections:Nnn \spath gsplit path at intersections:Nn \spath split at intersections:NNnn \spath split at intersections:NN \spath_gsplit_at_intersections:NNnn \spath_gsplit_at_intersections:NN

split both paths.

```
3199 {
      \group_begin:
3200
3201
      \seq_clear:N \l__spath_tmpa_seq
3202
3203
      \seq_clear:N \l__spath_tmpb_seq
      \spath_components_to_seq: Nn \l__spath_tmpa_seq {#1}
     \seq_map_inline: Nn \l__spath_tmpa_seq
3206
3207
        \spath_split_component_at_intersections: Nnn \l__spath_tmpa_tl {##1} {#2}
3208
        \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
3209
3210
3211
      \tl_gclear:N \g__spath_output_tl
3212
      \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpb_seq {} }
3213
      \group_end:
3214
3215 }
3216
   \cs_new_protected_nopar:Npn \spath_split_path_at_intersections:Nnn #1#2#3
3217
      \__spath_split_path_at_intersections:nn {#2}{#3}
3218
     \tl_set_eq:NN #1 \g__spath_output_tl
3219
```

```
\tl_gclear:N \g_spath_output_tl
3221 }
   \cs_generate_variant:\n \spath_split_path_at_intersections:\nn
3223 {NVn, NVV, cVn, cVV, cvn, cvv}
    \cs_new_protected_nopar:Npn \spath_split_path_at_intersections:Nn #1#2
3225
      \spath_split_path_at_intersections:NVn #1#1{#2}
3226
3227
    \cs_generate_variant:Nn \spath_split_path_at_intersections:Nn {cv, NV}
    \cs_new_protected_nopar:Npn \spath_gsplit_path_at_intersections:Nnn #1#2#3
3230
      \__spath_split_path_at_intersections:nn {#2}{#3}
3231
      \tl_gset_eq:NN #1 \g__spath_output_tl
3232
      \tl_gclear:N \g__spath_output_tl
3233
3234 }
    \cs_generate_variant:\n \spath_gsplit_path_at_intersections:\nn
3235
    {NVn, NVV, cVn, cVV, cvn, cvv}
3236
    \cs_new_protected_nopar:Npn \spath_gsplit_path_at_intersections:Nn #1#2
      \spath_gsplit_path_at_intersections:NVn #1#1{#2}
3239
3240 }
    \cs_generate_variant:Nn \spath_gsplit_path_at_intersections:Nn {cv, NV}
    \cs_new_protected_nopar:Npn \spath_split_at_intersections:NNnn #1#2#3#4
3242
3243
      \__spath_split_path_at_intersections:nn {#3}{#4}
3244
      \tl_set_eq:NN #1 \g__spath_output_tl
3245
3246
      \__spath_split_path_at_intersections:nn {#4}{#3}
      \tl_set_eq:NN #2 \g_spath_output_tl
3247
      \tl_gclear:N \g_spath_output_tl
3248
    \cs_generate_variant:Nn \spath_split_at_intersections:NNnn
    {NNVn, NNVV, ccVn, ccVV, ccvn, ccvv}
3252
    \cs_new_protected_nopar:Npn \spath_split_at_intersections:NN #1#2
3253
      \spath_split_at_intersections:NNVV #1#2#1#2
3254
3255 }
    \cs_generate_variant:Nn \spath_split_at_intersections:NN {cc}
3256
3257
    cs_new_protected_nopar:Npn \spath_gsplit_at_intersections:NNnn #1#2#3#4
3258
      \_spath_split_path_at_intersections:nn {#3}{#4}
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \__spath_split_path_at_intersections:nn {#4}{#3}
      \tl_gset_eq:NN #2 \g__spath_output_tl
3262
      \tl_gclear:N \g__spath_output_tl
3263
3264 }
    \cs_generate_variant:\n \spath_gsplit_at_intersections:\nn
    {NNVn, NNVV, ccVn, ccVV, ccvn, ccvv}
    \cs_new_protected_nopar:Npn \spath_gsplit_at_intersections:NN #1#2
3268
   {
3269
      \spath_gsplit_at_intersections:NNVV #1#2#1#2
3270 }
   \cs_generate_variant:Nn \spath_gsplit_at_intersections:NN {cc}
(End definition for \spath_split_path_at_intersections:Nnn and others.)
```

th_split_component_at_self_intersections:Nn
ath_split_component_at_self_intersections:N
h_gsplit_component_at_self_intersections:Nn
th gsplit component at self intersections:N

```
Given a component of a path, split it at points where it self-intersects.
3272 \cs_new_protected_nopar:Npn \__spath_split_component_at_self_intersections:n #1
      \group_begin:
3274
      \tl_set:Nn \l__spath_tmpe_tl {#1}
3275
3276
      % Remember if the component is closed
3277
3278
      \spath_finalaction:NV \l__spath_tmpa_tl \l__spath_tmpe_tl
      \bool_set:Nn \l__spath_closed_bool
        \tl_if_eq_p:NN \l__spath_tmpa_tl \c_spath_closepath_tl
3282
3283
3284
      % Copy the path
3285
      \tl_set:Nn \l__spath_tmpe_tl {#1}
3286
3287
      % Open the path
3288
      \spath_open:N \l__spath_tmpe_tl
      % Ensure beziers don't self-intersect
      \spath_split_curves:N \l__spath_tmpe_tl
3292
      % Make a copy for later
3293
      \tl_set_eq:NN \l__spath_tmpg_tl \l__spath_tmpe_tl
3294
3295
      % Clear some token lists and sequences
3296
      \tl_clear:N \l__spath_tmpd_tl
3297
      \seq_clear:N \l__spath_tmpb_seq
3298
      \int_zero:N \l__spath_tmpa_int
3299
      \pgfintersectionsortbyfirstpath
3302
      % Split the path into a sequence of segments
3303
      \spath_segments_to_seq:NV \l__spath_tmpa_seq \l__spath_tmpe_tl
3304
3305
      \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
3306
3307
        \seq_map_indexed_inline:Nn \l__spath_tmpa_seq
3308
3309
          \% Don't intersect a segment with itself
           \int_compare:nF
3312
             ##1 == ####1
3313
          }
3314
3315
             \spath_intersect:nn {##2} {####2}
3316
3317
             \int_compare:nT {\pgfintersectionsolutions > 0}
3318
3319
               % Find the times of the intersections on each path
3320
               \int_step_inline:nnnn {1} {1} {\pgfintersectionsolutions}
               {
                 \verb|\pgfintersectiongetsolution times|
3323
```

{#######1}{\l__spath_tmpb_tl}{\l__spath_tmpc_tl}

3324

```
3325
                                                                                   \bool_if:nT
3326
                                                                                   {
3327
                                                                                               !(
3328
                                                                                               fp_compare_p:n { l_spath_tmpb_tl > .99 }
3329
3330
                                                                                              \int_compare_p:n {##1 + 1 == ####1}
3331
                                                                                              )
3332
                                                                                              &&
                                                                                               ! (
                                                                                               \fp_compare_p:n { \l__spath_tmpb_tl < .01 }
                                                                                              &&
3336
                                                                                               \int \int \int d^2 r d^2 
3337
                                                                                              )
3338
                                                                                              &&
3339
                                                                                               !(
3340
                                                                                               \l_spath_closed_bool
3341
                                                                                              &&
3342
                                                                                               \fp_compare_p:n { \l__spath_tmpb_tl < .01 }
                                                                                              &&
                                                                                               \int \int d^2 p 
                                                                                              &&
                                                                                               \int_compare_p:n {\seq_count:N \l__spath_tmpa_seq == ####1}
3347
                                                                                              )
3348
                                                                                              &&
3349
                                                                                               !(
3350
                                                                                               \l_spath_closed_bool
3351
3352
                                                                                               fp_compare_p:n { l__spath_tmpb_tl > .99 }
3353
                                                                                               \int_compare_p:n {####1 == 1}
                                                                                              &&
                                                                                               \int_compare_p:n {\seq_count:N \l__spath_tmpa_seq == ##1}
3357
                                                                                              )
3358
                                                                                 }
3359
3360
                                                                                               \tl_set:Nx \l__spath_tmpa_tl
3361
                                                                                              {fp_to_decimal:n {\l_spath_tmpb_tl + ##1 - 1}}
3362
3363
                                                                                               \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
                                                 }
3367
                                       }
3368
                            }
3369
3370
                            \% Sort the sequence by reverse order along the path
3371
                             \seq_sort:Nn \l__spath_tmpb_seq
3372
3373
3374
                                        \fp_compare:nNnTF { ##1 } < { ##2 }
3375
                                        { \sort_return_swapped: }
3376
                                        { \sort_return_same: }
                            }
3377
3378
```

```
\seq_get_left:NN \l__spath_tmpb_seq \l__spath_tmpa_tl
3370
      \fp_compare:nT
3380
3381
        \l_spath_tmpa_tl > \seq_count:N \l_spath_tmpa_seq - .01
3382
3383
     {
3384
        \bool_set_false:N \l__spath_closed_bool
3385
3386
      \seq_get_right:NN \l__spath_tmpb_seq \l__spath_tmpa_tl
3387
      \fp_compare:nT
3388
3389
      {
        \l_spath_tmpa_tl < .01
3390
3391
3392
      {
        \bool_set_false:N \l__spath_closed_bool
3393
3394
3395
      % Restore the original copy of the path
3396
      \tl_set_eq:NN \l__spath_tmpe_tl \l__spath_tmpg_tl
     % Clear the token lists
      \tl_clear:N \l__spath_tmpf_tl
3400
      \tl_clear:N \l__spath_tmph_tl
3401
      \tl_clear:N \l__spath_tmpg_tl
3402
3403
      \tl_set:Nn \l__spath_tmpi_tl {-1}
3404
3405
      \seq_map_inline: Nn \l__spath_tmpb_seq
3406
3407
        \tl_set:Nn \l__spath_tmpb_tl {##1}
        \tl_set_eq:NN \l__spath_tmpa_tl \l__spath_tmpb_tl
3409
        \int_compare:nT
3410
3411
          \fp_to_int:n {floor( \l_spath_tmpb_tl ) }
3412
3413
          \fp_to_int:n {floor( \l__spath_tmpi_tl) }
3414
       }
3415
3416
3417
          \tl_set:Nx \l__spath_tmpb_tl
            \fp_eval:n {
              floor( \l__spath_tmpb_tl )
3421
              ( \l_spath_tmpb_tl - floor( \l_spath_tmpb_tl) )
3422
3423
              ( \l_spath_tmpi_tl - floor( \l_spath_tmpi_tl) )
3424
3425
          }
3426
       }
3427
3428
        \tl_set_eq:NN \l__spath_tmpi_tl \l__spath_tmpa_tl
3430
        \spath_split_at:NNVV
        \l_spath_tmpf_tl
3431
        \l_spath_tmph_tl
3432
```

```
\l_spath_tmpe_tl
3433
        \l_spath_tmpb_tl
3434
3435
        \tl_put_left:NV \l__spath_tmpg_tl \l__spath_tmph_tl
3436
        \tl_set_eq:NN \l__spath_tmpe_tl \l__spath_tmpf_tl
3437
3438
      }
3439
3440
      \tl_put_left:NV \l__spath_tmpg_tl \l__spath_tmpe_tl
3441
3442
      \tl_if_empty:NT \l__spath_tmpg_tl
3443
3444
        \tl_set_eq:NN \l__spath_tmpg_tl \l__spath_tmpe_tl
3445
3446
3447
      \spath_remove_empty_components:N \l__spath_tmpg_tl
3448
3449
      % Do something with closed
3450
      \bool_if:NT \l__spath_closed_bool
        \spath_join_component:Nn \l__spath_tmpg_tl {1}
3453
      }
3454
3455
      \tl_gclear:N \g_spath_output_tl
3456
      \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpg_tl
3457
      \group_end:
3458
3459 }
    \cs_new_protected_nopar:Npn \spath_split_component_at_self_intersections:Nn #1#2
3460
3461
      \__spath_split_component_at_self_intersections:n {#2}
3463
      \tl_set_eq:NN #1 \g__spath_output_tl
3464
      \tl_gclear:N \g__spath_output_tl
3465
    \cs_generate_variant:Nn \spath_split_component_at_self_intersections:Nn {NV}
3466
    \cs_new_protected_nopar:Npn \spath_split_component_at_self_intersections:N #1
3467
3468
   {
      \spath_split_component_at_self_intersections:NV #1#1
3469
3470 }
    \cs_generate_variant:Nn \spath_split_component_at_self_intersections:N {c}
    \cs_new_protected_nopar:Npn \spath_gsplit_component_at_self_intersections:Nn #1#2
3473
      \__spath_split_component_at_self_intersections:n {#2}
3475
      \tl_gset_eq:NN #1 \g__spath_output_tl
      \tl_gclear:N \g__spath_output_tl
3476
3477
    \cs_generate_variant:Nn \spath_gsplit_component_at_self_intersections:Nn {NV}
    \cs_new_protected_nopar:Npn \spath_gsplit_component_at_self_intersections:N #1
3480
   {
      \spath_gsplit_component_at_self_intersections:NV #1#1
3481
3482 }
   \cs_generate_variant:Nn \spath_gsplit_component_at_self_intersections:N {c}
(End definition for \spath_split_component_at_self_intersections:Nn and others.)
```

Split a path at its self intersections. We iterate over the components, splitting each

where it meets all the others and itself. To make this more efficient, we split against the components of the original path rather than updating each time.

```
\cs new_protected nopar:Npn \__spath_split_at_self_intersections:n #1
3485
     \group_begin:
     \spath_components_to_seq: Nn \l__spath_tmpa_seq {#1}
     \seq_clear:N \l__spath_tmpb_seq
     \seq_clear:N \l__spath_tmpc_seq
3489
3490
     % Iterate over the components of the original path.
3491
     \bool_do_until:nn
3492
     {
3493
        \seq_if_empty_p:N \l__spath_tmpa_seq
3494
3495
3496
       % Get the next component
        \seq_pop_left:NN \l__spath_tmpa_seq \l__spath_tmpa_tl
       % Copy for later
        \tl_set_eq:NN \l__spath_tmpc_tl \l__spath_tmpa_tl
        \int_compare:nT
3501
3502
          \tl_count:N \l__spath_tmpa_t1 > 3
3503
       }
3504
        {
3505
3506
         % Split against itself
          \spath_split_component_at_self_intersections:N \l__spath_tmpa_tl
         % Grab the rest of the path
3510
          \tl_set:Nx \l__spath_tmpb_tl
3511
3512
            \seq_use:Nn \l__spath_tmpb_seq {}
            \seq_use:Nn \l__spath_tmpa_seq {}
3513
3514
         % Split against the rest of the path
3515
          \spath_split_path_at_intersections:NV \l__spath_tmpa_tl \l__spath_tmpb_tl
3516
3517
       % Save the split path
        \seq_put_right:NV \l__spath_tmpc_seq \l__spath_tmpa_tl
       % Add the original copy to the sequence of processed components
3520
        \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpc_tl
3521
3522
3523
     \tl_gclear:N \g__spath_output_tl
3524
     \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpc_seq {} }
3525
     \group_end:
3526
3527 }
   \cs_generate_variant:Nn \__spath_split_at_self_intersections:n {V, v}
   \cs_new_protected_nopar:Npn \spath_split_at_self_intersections:Nn #1#2
     \__spath_split_at_self_intersections:n {#2}
3531
     \tl_set_eq:NN #1 \g__spath_output_tl
3532
     \tl_gclear:N \g_spath_output_tl
3533
3534 }
3535 \cs_generate_variant:Nn \spath_split_at_self_intersections:Nn {NV, cn, cV, cv}
```

```
\cs_new_protected_nopar:Npn \spath_split_at_self_intersections:N #1
 3537
               \spath_split_at_self_intersections:NV #1#1
 3538
         }
 3539
          \cs_generate_variant:Nn \spath_split_at_self_intersections:N {c}
 3540
          \cs_new_protected_nopar:Npn \spath_gsplit_at_self_intersections:Nn #1#2
 3542
                \__spath_split_at_self_intersections:n {#2}
 3543
              \tl_gset_eq:NN #1 \g__spath_output_tl
               \tl_gclear:N \g__spath_output_tl
  3545
 3546 }
          \cs_generate_variant:Nn \spath_gsplit_at_self_intersections:Nn {NV, cn, cV, cv}
          \cs_new_protected_nopar:Npn \spath_gsplit_at_self_intersections:N #1
 3548
 3549
               \spath_gsplit_at_self_intersections:NV #1#1
 3550
 3551 }
         \cs_generate_variant:Nn \spath_gsplit_at_self_intersections:N {c}
(End definition for \spath_split_at_self_intersections:Nn and others.)
Join the specified component of the spath to its predecessor.
          \cs_new_protected_nopar:Npn \__spath_join_component:nn #1#2
               \group_begin:
 3555
              \spath_numberofcomponents: Nn \l__spath_tmpa_int {#1}
 3556
 3557
              \bool_if:nTF
 3558
  3550
              {
                    \int \int d^2 p 
  3560
  3561
                    \int_compare_p:n { #2 <= \l__spath_tmpa_int }
  3564
                    \int_compare:nTF
                    {
                        #2 == 1
                   }
  3569
                         \int_compare:nTF
 3570
                        {
 3571
                             \l__spath_tmpa_int == 1
 3572
 3573
 3574
                             \tl_set:Nn \l__spath_tmpa_tl {#1}
 3575
                             \spath_initialpoint:Nn \l__spath_tmpb_tl {#1}
 3576
                             \tl_put_right:NV \l__spath_tmpa_tl \c_spath_closepath_tl
  3577
                             \tl_put_right:NV \l__spath_tmpa_tl \l__spath_tmpb_tl
  3578
 3579
                             \tl_gclear:N \g_spath_output_tl
                             \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
  3580
  3581
 3582
                              \spath_components_to_seq: Nn \l__spath_tmpa_seq {#1}
 3583
                             \seq_pop_left:NN \l__spath_tmpa_seq \l__spath_tmpa_tl
  3584
```

\spath_join_component:Nnn

\spath_join_component:Nn

\spath_gjoin_component:Nnn \spath_gjoin_component:Nn

```
\prg_replicate:nn {3}
3587
              \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
3588
3589
3590
            \seq_put_right:NV \l__spath_tmpa_seq \l__spath_tmpa_tl
3591
            \tl_gclear:N \g_spath_output_tl
            \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpa_seq {}}
       }
        {
3597
          \spath_components_to_seq:Nn \l__spath_tmpa_seq {#1}
3598
3599
          \seq_clear:N \l__spath_tmpb_seq
3600
          \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
3601
3602
            \tl_set:Nn \l__spath_tmpa_tl {##2}
3603
            \int \int d^2 t dt
              \prg_replicate:nn {3}
                \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
              }
3610
            \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
3611
3612
3613
          \tl_gclear:N \g_spath_output_tl
3614
          \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpb_seq {}}
       }
3616
     }
3617
3618
     {
        \tl_gclear:N \g__spath_output_tl
3619
        \tl_gset:Nn \g__spath_output_tl {#1}
3620
3621
3622
3623
      \group_end:
3624 }
3625
   \cs_new_protected_nopar:Npn \spath_join_component:Nnn #1#2#3
      \__spath_join_component:nn {#2}{#3}
3628
     \tl_set_eq:NN #1 \g__spath_output_tl
     \tl_gclear:N \g__spath_output_tl
3629
3630 }
   \cs_generate_variant:Nn \spath_join_component:Nnn {NVn, NVV}
3631
   \cs_new_protected_nopar:Npn \spath_join_component:Nn #1#2
3632
3633
   {
      \spath_join_component:NVn #1#1{#2}
3634
3635
   \cs_generate_variant:Nn \spath_join_component:Nn {cn, NV, cV}
   \cs_new_protected_nopar:Npn \spath_gjoin_component:Nnn #1#2#3
3638
      \__spath_join_component:nn {#2}{#3}
3639
```

```
3640  \tl_gset_eq:NN #1 \g__spath_output_tl
3641  \tl_gclear:N \g__spath_output_tl
3642 }
3643  \cs_generate_variant:Nn \spath_gjoin_component:Nnn {NVn, NVV}
3644  \cs_new_protected_nopar:Npn \spath_gjoin_component:Nn #1#2
3645 {
3646  \spath_gjoin_component:NVn #1#1{#2}
3647 }
3648  \cs_generate_variant:Nn \spath_gjoin_component:Nn {cn, NV, cV}
```

(End definition for \spath_join_component:Nnn and others.)

\spath_spot_weld_components:Nn \spath_spot_weld_components:Nn \spath_spot_gweld_components:Nn \spath_spot_gweld_components:N Weld together any components where the last point of one is at the start point of the next (within a tolerance).

```
\cs_new_protected_nopar:Npn \__spath_spot_weld_components:n #1
3650 {
      \group_begin:
3651
      \dim_zero:N \l__spath_move_x_dim
3652
      \dim_zero:N \l__spath_move_y_dim
3653
3654
      \spath_components_to_seq: Nn \l__spath_tmpa_seq {#1}
3655
      \seq_clear:N \l__spath_tmpb_seq
3656
      \label{lem:nn {#1} {2} + 10 pt} $$ \dim_{\text{set:Nn } l_spath_{\text{move}} x_{\dim} {\tl_{item:nn {#1} {2}} + 10 pt} $$
3657
      \dim_set:Nn \l__spath_move_y_dim {\tl_item:nn {#1} {3} + 10 pt}
3658
3659
      \int_set:Nn \l__spath_tmpa_int {\seq_count:N \l__spath_tmpa_seq}
3660
3661
      \sc q_map_inline:Nn \l_spath_tmpa_seq
3662
3663
        \tl_set:Nn \l__spath_tmpa_tl {##1}
3664
        \bool_if:nT
3665
3666
           \dim_compare_p:n
3667
           {
3668
             \dim_abs:n
3669
             {\l_spath_move_x_dim - \tl_item:Nn \l_spath_tmpa_tl {2} }
3670
3671
3672
          }
          &&
           \dim_compare_p:n
           {
3675
3676
             \dim_abs:n
             {\l_spath_move_y_dim - \tl_item:Nn \l_spath_tmpa_tl {3} }
3677
             < 0.01pt
3678
3679
        }
3680
3681
           \prg_replicate:nn {3}
3682
             \tl_set:Nx \l__spath_tmpa_tl {\tl_tail:N \l__spath_tmpa_tl}
3686
           \int_decr:N \l__spath_tmpa_int
3687
        \tl_reverse:N \l__spath_tmpa_tl
3688
```

```
\dim_set:Nn \l__spath_move_x_dim {\tl_item:Nn \l__spath_tmpa_tl {2}}
3689
        \dim_set:Nn \l__spath_move_y_dim {\tl_item:Nn \l__spath_tmpa_tl {1}}
3690
        \tl_reverse:N \l__spath_tmpa_tl
3691
        \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
3692
3693
3694
      \tl_set:Nx \l__spath_tmpa_tl {\seq_use:Nn \l__spath_tmpb_seq {} }
3695
      \spath_components_to_seq:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
3696
3698
      \spath_initialpoint:Nn \l__spath_tmpa_tl {#1}
3699
      \spath_finalpoint: Nn \l__spath_tmpb_tl {#1}
3700
3701
      \bool_if:nT
3702
3703
        \dim_compare_p:n
3704
3705
          \dim_abs:n
3706
            \tl_item:Nn \l__spath_tmpa_tl {1} - \tl_item:Nn \l__spath_tmpb_tl {1}
          }
          <
3710
          0.01pt
3711
        }
3712
        &&
3713
3714
        \dim_compare_p:n
3715
          \dim_abs:n
3716
3717
            \label{lem:Nn l_spath_tmpa_tl {2} - lem:Nn l_spath_tmpb_tl {2}} $$ \t l_item:Nn l_spath_tmpb_tl {2} $$
          }
3719
3720
          0.01pt
3721
        }
3722
      }
3723
3724
        \int_compare:nTF
3725
3726
3727
          \seq_count:N \l__spath_tmpb_seq > 1
        }
        {
3730
          \seq_pop_left:NN \l__spath_tmpb_seq \l__spath_tmpb_tl
3731
          \prg_replicate:nn {3}
3732
3733
             \tl_set:Nx \l__spath_tmpb_tl {\tl_tail:N \l__spath_tmpb_tl}
3734
3735
          \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpb_tl
3736
        }
3737
3738
3739
          \tl_set:NV \l__spath_tmpb_tl \c_spath_closepath_tl
3740
          \tl_put_right:Nx \l__spath_tmpb_tl
3741
            { \tl_item: Nn \l__spath_tmpa_tl {1} }
3742
```

```
{ \tilde{1}_{spath_tmpa_t1 } }
3743
3744
          \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpb_tl
3745
3746
3747
3748
      \tl_gset:Nx \g_spath_output_tl {\seq_use:Nn \l_spath_tmpb_seq {}}
3749
      \group_end:
3750
3751
   \cs_new_protected_nopar:Npn \spath_spot_weld_components:Nn #1#2
3752
3753
      \__spath_spot_weld_components:n {#2}
3754
      \tl_set_eq:NN #1 \g__spath_output_tl
3755
      \tl_gclear:N \g__spath_output_tl
3756
3757
   \cs_generate_variant:Nn \spath_spot_weld_components:Nn {NV, cV, cn}
3758
    \cs_new_protected_nopar:Npn \spath_spot_weld_components:N #1
3759
3760
      \spath_spot_weld_components:NV #1#1
3761
3762 }
   \cs_generate_variant:Nn \spath_spot_weld_components:N {c}
   \cs_new_protected_nopar:Npn \spath_spot_gweld_components:Nn #1#2
3764
3765
      \__spath_spot_weld_components:n {#2}
3766
     \tl_gset_eq:NN #1 \g__spath_output_tl
3767
      \tl_gclear:N \g__spath_output_tl
3768
3769 }
    \cs_generate_variant:Nn \spath_spot_gweld_components:Nn {NV, cV, cn}
   \cs_new_protected_nopar:Npn \spath_spot_gweld_components:N #1
3771
      \spath_spot_gweld_components:NV #1#1
3773
3774 }
3775 \cs_generate_variant:Nn \spath_spot_gweld_components:N {c}
```

 $(End\ definition\ for\ \verb|\spath_spot_weld_components:Nn|\ and\ others.)$

3.8 Exporting Commands

```
\spath_convert_to_svg:Nn
\spath_gconvert_to_svg:Nn
```

Convert the soft path to an SVG document.

```
3776 \cs_new_protected_nopar:Npn \__spath_convert_to_svg:n #1
3777
      \group_begin:
3778
      \tl_clear:N \l__spath_tmpa_tl
3779
      \tl_put_right:Nn \l__spath_tmpa_tl
3780
3781
        <?xml~ version="1.0"~ standalone="no"?>
3782
        \iow_newline:
        <!DOCTYPE~ svg~ PUBLIC~ "-//W3C//DTD SVG 1.1//EN"~
        "http://www.w3.org/Graphics/SVG/1.1/DTD/svg11.dtd">
3786
        \iow_newline:
        <svg~ xmlns="http://www.w3.org/2000/svg"~ version="1.1"~viewBox="</pre>
3787
3788
3789
     \spath_minbb:Nn \l__spath_tmpb_tl {#1}
3790
```

```
\spath_maxbb:Nn \l__spath_tmpc_tl {#1}
3791
      \tl_put_right:Nx \l__spath_tmpa_tl
3792
3793
        \dim_to_decimal:n
3794
3795
          \tl_item:Nn \l__spath_tmpb_tl {1} - 10pt
3796
        }
3797
        \exp_not:n {~}
        \dim_to_decimal:n
          \tl_item:Nn \l__spath_tmpb_tl {2} - 10pt
        }
3802
        \exp_not:n {~}
3803
        \dim_to_decimal:n
3804
3805
          \tl_item:Nn \l__spath_tmpc_tl {1}
3806
3807
          \tl_item:Nn \l__spath_tmpb_tl {1}
          + 20pt
        \exp_not:n {~}
3811
        \dim_to_decimal:n
3812
3813
          \tl_item:Nn \l__spath_tmpc_tl {2}
3814
3815
          \tl_item:Nn \l__spath_tmpb_tl {2}
3816
          + 20pt
3817
        }
3818
     }
3819
      \tl_put_right:Nn \l__spath_tmpa_tl
3821
3822
     {
3823
        \iow_newline:
3824
        <path~ d="
3825
3826
      \tl_set:Nn \l__spath_tmpc_tl {use:n}
3827
3828
      \tl_map_inline:nn {#1}
3829
        \tl_set:Nn \l__spath_tmpb_tl {##1}
        \tl_case:NnF \l__spath_tmpb_tl
3832
          \c_spath_moveto_tl
3833
          {
3834
             \tl_put_right:Nn \l__spath_tmpa_tl {M~}
3835
            \tl_set:Nn \l__spath_tmpc_tl {use:n}
3836
3837
          \c_spath_lineto_tl
3838
3839
3840
             \tl_put_right:Nn \l__spath_tmpa_tl {L~}
            \tl_set:Nn \l__spath_tmpc_tl {use:n}
3842
          }
3843
          \c_spath_closepath_tl
          {
3844
```

```
\tl_set:Nn \l__spath_tmpc_tl {use_none:n}
                            3846
                            3847
                                      \c_spath_curvetoa_tl
                            3848
                            3849
                                        \tl_put_right:Nn \l__spath_tmpa_tl {C~}
                            3850
                                        \tl_set:Nn \l__spath_tmpc_tl {use:n}
                            3851
                            3852
                                      \c_spath_curvetob_tl {
                                        \tl_set:Nn \l__spath_tmpc_tl {use:n}
                            3854
                                      \c_spath_curveto_tl {
                            3856
                                        \tl_set:Nn \l__spath_tmpc_tl {use:n}
                            3857
                            3858
                            3859
                            3860
                                      \tl_put_right:Nx
                            3861
                                      \l_spath_tmpa_tl
                                      {\use:c { \l_spath_tmpc_tl } {\dim_to_decimal:n {##1}} ~}
                                  \tl_put_right:Nn \l__spath_tmpa_tl
                            3866
                            3867
                                    "~ fill="none"~ stroke="black"~ />
                            3868
                                    \iow_newline:
                            3869
                                    </svg>
                            3870
                            3871
                                    \iow_newline:
                            3872
                                  \tl_gset_eq:NN \g__spath_output_tl \l__spath_tmpa_tl
                            3873
                            3874
                                  \group_end:
                            3875 }
                               \cs_new_protected_nopar:Npn \spath_convert_to_svg:Nn #1#2
                            3876
                            3877 {
                                  \__spath_convert_to_svg:n {#2}
                            3878
                                  \tl_set_eq:NN #1 \g__spath_output_tl
                            3879
                                  \tl_gclear:N \g_spath_output_tl
                            3880
                            3881 }
                            3882
                               \cs_new_protected_nopar:Npn \spath_gconvert_to_svg:Nn #1#2
                            3883
                                  \__spath_convert_to_svg:n {#2}
                                  \tl_gset_eq:NN #1 \g__spath_output_tl
                                  \tl_gclear:N \g__spath_output_tl
                            3887 }
                           (End definition for \spath_convert_to_svg:Nn and \spath_gconvert_to_svg:Nn.)
                           Save a soft path to an SVG file.
\spath_export_to_svg:nn
                            3888 \iow_new:N \g__spath_stream
                               \cs_new_protected_nopar:Npn \spath_export_to_svg:nn #1#2
                            3890 {
                                  \group_begin:
                            3891
                                  \spath_convert_to_svg:Nn \l__spath_tmpa_tl {#2}
                            3892
                                  \iow_open:Nn \g__spath_stream {#1 .svg}
                            3893
                                  \iow_now:Nx \g__spath_stream
```

\tl_put_right:Nn \l__spath_tmpa_tl {Z~}

3845

```
\tl_use:N \l__spath_tmpa_tl
                 3896
                 3897
                       \iow_close:N \g_spath_stream
                 3898
                       \group_end:
                 3899
                 3900 }
                     \cs_generate_variant:Nn \spath_export_to_svg:nn {nv, nV}
                 (End definition for \spath_export_to_svg:nn.)
\spath_show:n Displays the soft path on the terminal.
                     \cs_new_protected_nopar:Npn \spath_show:n #1
                 3903
                       \int_step_inline:nnnn {1} {3} {\tl_count:n {#1}}
                 3904
                 3905
                         \iow_term:x {
                 3906
                           \tl_item:nn {#1} {##1}
                 3907
                            {\tl_item:nn {#1} {##1+1}}
                 3908
                            {\tl_item:nn {#1} {##1+2}}
                 3909
                 3910
                 3911
                       }
                     \cs_generate_variant:Nn \spath_show:n {V, v}
                 (End definition for \spath_show:n.)
```

3.9 PGF and TikZ Interface Functions

Spaths come from PGF so we need some functions that get and set spaths from the pgf system.

```
Grab the current soft path from PGF.
\spath_get_current_path:N
\spath_gget_current_path:N
                                  \cs_new_protected_nopar:Npn \spath_get_current_path:N #1
                              3915 {
                                     \pgfsyssoftpath@getcurrentpath #1
                              3916
                              3917 }
                                  \cs_new_protected_nopar:Npn \spath_gget_current_path:N #1
                              3918
                              3919 {
                                     \pgfsyssoftpath@getcurrentpath #1
                              3920
                                     \t=0tl_gset_eq:NN #1 #1
                              3921
                              (End definition for \spath_get_current_path:N and \spath_gget_current_path:N.)
    \spath_protocol_path:n
                              This feeds the bounding box of the soft path to PGF to ensure that its current bounding
                              box contains the soft path.
                                  \cs_new_protected_nopar:Npn \spath_protocol_path:n #1
                              3923
                                     \spath_minbb: Nn \l__spath_tmpa_tl {#1}
                               3925
                                    \exp_last_unbraced:NV \pgf@protocolsizes\l__spath_tmpa_tl
                               3927
                                    \spath_maxbb:Nn \l__spath_tmpa_tl {#1}
                               3928
                                     \exp_last_unbraced:NV \pgf@protocolsizes\l__spath_tmpa_tl
                               3929
```

3931 \cs_generate_variant:Nn \spath_protocol_path:n {V}

3930 }

```
(End definition for \spath_protocol_path:n.)
                             Sets the current path to the specified soft path.
\spath_set_current_path:n
\spath_set_current_path:N
                                 \cs_new_protected_nopar:Npn \spath_set_current_path:n #1
                              3933 {
                                    \spath_protocol_path:n {#1}
                              3934
                                    \tl_set:Nn \l__spath_tmpa_tl {#1}
                              3935
                                    \pgfsyssoftpath@setcurrentpath\l__spath_tmpa_tl
                              3936
                              3937 }
                                  \cs_new_protected_nopar:Npn \spath_set_current_path:N #1
                              3938
                                 {
                              3939
                                    \spath_protocol_path:V #1
                              3940
                              3941
                                    \pgfsyssoftpath@setcurrentpath #1
                              3942 }
                                 \cs_generate_variant:Nn \spath_set_current_path:N {c}
                             (End definition for \spath_set_current_path:n and \spath_set_current_path:N.)
       \spath_use_path:nn
                             Uses the given soft path at the PGF level.
                                 \cs_new_protected_nopar:Npn \spath_use_path:nn #1#2
                              3945 {
                                    \spath_set_current_path:n {#1}
                              3946
                                    \pgfusepath{#2}
                              3947
                              3948 }
                             (End definition for \spath_use_path:nn.)
                             Uses the given soft path at the TikZ level.
      \spath_tikz_path:nn
                                 \cs_new_protected_nopar:Npn \spath_tikz_path:nn #1#2
                              3950 {
                                    \path[#1] \pgfextra{
                              3951
                                      \spath_set_current_path:n {#2}
                              3952
                                      \tl_put_right:Nn \tikz@preactions {\def\tikz@actions@path{#2}}
                              3953
                                    };
                              3954
                              3955 }
                                  \cs_generate_variant:Nn \spath_tikz_path:nn {Vn, VV, nv, Vv, nV}
                             (End definition for \spath_tikz_path:nn.)
                             Sets the \tikz@lastx and other coordinates from the soft path.
   \spath_set_tikz_data:n
                                 \cs_new_protected_nopar:Npn \spath_set_tikz_data:n #1
                              3958 {
                                    \spath_finalpoint: Nn \l__spath_tmpa_tl {#1}
                              3959
                                    \tl_set:Nx \l__spath_tmpa_tl
                              3960
                                    ₹
                              3961
                                      \exp_not:c {pgf@x}=\tl_item:Nn \l__spath_tmpa_tl {1}
                              3962
                                      \exp_not:c {pgf@y}=\tl_item:Nn \l__spath_tmpa_tl {2}
                              3963
                              3964
                                    \use:c {pgf@process}{%
                              3965
                                      \tl_use:N \l__spath_tmpa_tl
                              3967
                                      \pgftransforminvert
                                      \use:c {pgf@pos@transform@glob}
                              3968
                              3969
                                    \tl_set:Nx \l__spath_tmpa_tl
                              3970
                                    {
                              3971
```

```
\exp_not:c {tikz@lastx}=\exp_not:c {pgf@x}
3972
        \exp_not:c {tikz@lasty}=\exp_not:c {pgf@y}
3973
        \exp_not:c {tikz@lastxsaved}=\exp_not:c {pgf@x}
3974
        \exp_not:c {tikz@lastysaved}=\exp_not:c {pgf@y}
3975
3976
      \tl_use:N \l__spath_tmpa_tl
3977
      \spath_finalmovepoint: Nn \l__spath_tmpa_tl {#1}
3978
      \ifpgfsyssoftpathmovetorelevant%
3979
      \tl_gset_eq:cN {pgfsyssoftpath@lastmoveto} \l__spath_tmpa_tl
3981
      \tl_set:Nx \l__spath_tmpa_tl
3982
      {
3083
        \exp_not:c {pgf@x}=\tl_item:Nn \l__spath_tmpa_tl {1}
3984
        \exp_not:c {pgf@y}=\tl_item:Nn \l__spath_tmpa_tl {2}
3985
3986
      \use:c {pgf@process}{%
3987
        \tl_use:N \l__spath_tmpa_tl
3988
        \pgftransforminvert
3989
        \use:c {pgf@pos@transform@glob}
      \tl_set:Nx \l__spath_tmpa_tl
      {
3003
        \exp_not:c {tikz@lastmovetox}=\exp_not:c {pgf@x}
3994
        \exp_not:c {tikz@lastmovetoy}=\exp_not:c {pgf@y}
3995
3996
      \tl_use:N \l__spath_tmpa_tl
3997
      \tl_clear_new:c {tikz@timer}
3998
      \tl_set:cn {tikz@timer}
3999
4000
        \pgftransformreset
4001
        \spath_reallength:Nn \l__spath_tmpa_int {#1}
4002
        \tl_set_eq:Nc \l__spath_tmpb_tl {tikz@time}
4003
        \tl_set:Nx \l__spath_tmpb_tl
4004
         \{ \fp_to_decimal: n \ \{(\l_spath_tmpb_tl) \ * \ (\l_spath_tmpa_int) \} \} 
4005
        \spath_transformation_at: NnV \l__spath_tmpc_tl {#1} \l__spath_tmpb_tl
4006
4007
        \tl_set:Nx \l__spath_tmpa_tl
4008
4009
4010
          \exp_not:N \pgfpoint
          { \tl_item: Nn \l__spath_tmpc_tl {5} }
          { \tl_item: Nn \l__spath_tmpc_tl {6} }
4013
        \exp_args:NV \pgftransformshift \l__spath_tmpa_tl
4014
4015
        \ifpgfresetnontranslationattime
4016
        \pgftransformresetnontranslations
4017
4018
4019
        \ifpgfslopedattime
4020
4021
        \tl_set:Nx \l__spath_tmpa_tl
4022
4023
          { \tl_item: Nn \l__spath_tmpc_tl {1} }
4024
          { \tl_item: Nn \l__spath_tmpc_tl {2} }
4025
```

```
{ \tilde{3} } 
4026
         { \tl_item: Nn \l__spath_tmpc_tl {4} }
4027
4028
       \ifpgfallowupsidedownattime
4029
4030
       \fp_compare:nT { \tl_item:Nn \l__spath_tmpc_tl {4} < 0}
4031
4032
         \tl_set:Nx \l__spath_tmpa_tl
4033
4034
           { \lceil fp_{eval:n} \  \  } 
4035
           { \lceil fp_{eval:n} \  \  } 
4036
           { fp_eval:n { - (\tl_item:Nn \l_spath_tmpc_tl {3})} }
4037
           { fp_eval:n { - (\tl_item:Nn \l_spath_tmpc_tl {4})} }
4038
4039
       }
4040
       \fi
4041
       \tl_put_right:Nn \l__spath_tmpa_tl {{\pgfpointorigin}}
4042
       \exp_last_unbraced:NV \pgftransformcm \l__spath_tmpa_tl
     }
4045
4046 }
   \cs_generate_variant:Nn \spath_set_tikz_data:n {V, v}
(End definition for \spath_set_tikz_data:n.)
```

4 The TikZ interface

This provides an interface to the soft path manipulation routines via a series of TikZ keys. They all live in the spath family.

```
4048 \RequirePackage{spath3}
4049 \RequirePackage{expl3}
4050 \ExplSyntaxOn
4051
4052 \tl_new:N \l__spath_current_tl
4053 \tl_new:N \l__spath_reverse_tl
4054 \tl_new:N \l__spath_prefix_tl
4055 \tl_new:N \l__spath_suffix_tl
4056 \tl_new:N \g__spath_smuggle_tl
4057 \seq_new:N \g__spath_tmpa_seq
4058 \seq_new:N \l__spath_draft_bool
```

We surround all the keys with checks to ensure that the soft path under consideration does actually exist, but if it doesn't we should warn the user.

```
4060 \msg_new:nnn { spath3 } { missing soft path } { Soft~ path~ #1~ doesn't~ exist }
4061 \msg_new:nnnn { spath3 } { empty soft path } { Soft~ path~ #1~ is~ empty}
4062 {If~ it~ was~ defined~ inside~ a~ group,~ try~ using~ "save~ global". }
4063 \msg_new:nnn { spath3 } { load intersections }
4064 { You~ need~ to~ load~ the~ "intersections"~ library~ to~ work~ with~ intersections }
```

When saving a soft path, by default we use a naming convention that is compatible with the intersections library so that paths saved here and paths saved by the name path facility of the intersections library are mutually exchangeable.

```
4065 \tl_set:Nn \l__spath_prefix_tl {tikz@intersect@path@name@}
4066 \tl_set:Nn \l__spath_suffix_tl {}
```

When a soft path is grabbed from TikZ we're usually deep in a group so I've adapted the code from the intersections library to dig the definition out of the group without making everything global.

```
\t_new:N \g_spath_tikzfinish_tl
                            \cs_new_protected_nopar:Npn \spath_at_end_of_path:
                        4069
                               \tl_use:N \g__spath_tikzfinish_tl
                        4070
                              \t_gclear:N \g_spath_tikzfinish_tl
                        4071
                        4072 }
                            \tl_put_right:Nn \tikz@finish {\spath_at_end_of_path:}
                        4073
                        4074
                            \cs_new_protected_nopar:Npn \spath_save_path:Nn #1#2
                        4075
                        4077
                               \tl_gput_right:Nn \g__spath_tikzfinish_tl
                        4078
                        4079
                                 \tl_clear_new:N #1
                                 \tl_set:Nn #1 {#2}
                        4080
                        4081
                        4082
                            \cs_generate_variant:Nn \spath_save_path:Nn {cn, NV, cV}
                        4083
                        4084
                            \cs_new_protected_nopar:Npn \spath_gsave_path:Nn #1#2
                        4085
                         4086
                               \tl_gput_right:Nn \g__spath_tikzfinish_tl
                         4087
                                 \tl_gclear_new:N #1
                        4089
                                 \tl_gset:Nn #1 {#2}
                        4090
                        4091
                        4092 }
                            \cs_generate_variant:Nn \spath_gsave_path:Nn {cn, NV, cV}
                       Process a point via TikZ and store the resulting dimensions.
\_spath_process_tikz_point:Nn
                            \cs_new_protected_nopar:Npn \__spath_process_tikz_point:Nn #1#2
                        4095 {
                               \group_begin:
                        4096
                              \use:c {tikz@scan@one@point} \use:n #2 \scan_stop:
                        4097
                              \tl_gset:Nx \g__spath_output_tl
                        4098
                        4099
                                 { \dim_use:c {pgf@x} }
                        4100
                                 { \dim_use:c {pgf@y} }
                        4101
                        4102
                               \group_end:
                        4103
                              \tl_set_eq:NN #1 \g__spath_output_tl
                        4104
                              \tl_gclear:N \g_spath_output_tl
                        4105
                        4106
                        (End definition for \__spath_process_tikz_point:Nn.)
                       Wrapper around \tikzset for expansion.
  \__spath_tikzset:n
                        4107 \cs_set_eq:NN \__spath_tikzset:n \tikzset
                        4108 \cs_generate_variant:Nn \__spath_tikzset:n {V, v}
```

 $(\mathit{End \ definition \ for \ } \verb|_spath_tikzset:n.)$

When joining two paths we provide a set of options for how to process the second path.

```
4109 \bool_new:N \l__spath_reverse_bool
4110 \bool_new:N \l__spath_weld_bool
4111 \bool_new:N \l__spath_move_bool
4112 \bool_new:N \l__spath_global_bool
4113 tl_new:N l_spath_joinpath_tl
   \tl_new:N \l__spath_transformation_tl
4115
   \cs_new_protected_nopar:Npn \__spath_set_bool:Nn #1#2
4116
4117
      \tl_if_eq:nnTF {#2}{false}
4118
     {
4119
        \bool_set_false:N #1
4120
4121
4122
        \bool_set_true:N #1
4123
     }
4124
4125 }
   <text>
4126
     spath/join/.is~ family,
4127
     spath/join/.cd,
4128
     reverse/.code = {
4129
        \__spath_set_bool:Nn \l__spath_reverse_bool {#1}
4130
4131
     reverse/.default = true,
4132
4133
     weld/.code = {
4134
        \__spath_set_bool: Nn \l__spath_weld_bool {#1}
4135
     },
4136
     weld/.default = true,
     no~ weld/.code = {
4137
        \__spath_set_bool:Nn \l__spath_weld_bool {#1}
4138
        \bool_set:Nn \l__spath_weld_bool {! \l__spath_weld_bool}
4139
     },
4140
     no~ weld/.default = true,
4141
     move/.code = {
        \__spath_set_bool:Nn \l__spath_move_bool {#1}
4143
     },
4144
     move/.default = true,
4145
     no~ move/.code = {
4146
        \__spath_set_bool: Nn \l__spath_move_bool {#1}
4147
        \bool_set:Nn \l__spath_move_bool {! \l__spath_move_bool}
4148
     },
4149
     no~ move/.default = true,
4150
     global/.code = {
4151
        \__spath_set_bool:Nn \l__spath_global_bool {#1}
4152
4153
      global/.default = true,
4154
      transform/.store~in=\l__spath_transformation_tl,
4155
      .unknown/.code = {
4156
        \tl_set_eq:NN \l__spath_joinpath_tl \pgfkeyscurrentname
4157
4158
4159 }
```

When we split a soft path into components, we make it a comma separated list so that it can be fed into a \foreach loop. This can also make it possible to extract a single component, but to do this we need a wrapper around \clist_item:Nn (there doesn't appear to be a PGF way of getting an item of a CS list).

```
4160 \cs_set_eq:NN \getComponentOf \clist_item:Nn
    Now we define all of our keys.
4161 \tikzset{
    We're in the spath key family.
      spath/.is~family,
4162
      spath/.cd,
4163
    We provide for saving soft paths with a specific prefix and suffix in the name. The
default is to make it compatible with the intersections library.
      set~ prefix/.store~ in=\l__spath_prefix_tl,
4164
      prefix/.is~choice,
4165
      prefix/default/.style={
4166
        /tikz/spath/set~ prefix=tikz@intersect@path@name@
4167
4168
      set~ suffix/.store~ in=\l__spath_suffix_tl,
4169
      suffix/.is~choice,
4170
      suffix/default/.style={
4171
         /tikz/spath/set~ suffix={}
4172
      },
4173
      set~ name/.style={
4174
        /tikz/spath/prefix=#1,
4175
         /tikz/spath/suffix=#1
4176
4177
    Keys for saving and cloning a soft path.
      save/.code={
4178
         \tikz@addmode{
           \spath_get_current_path:N \l__spath_tmpa_tl
4180
           \spath_bake_round:NV \l__spath_tmpa_tl \l__spath_tmpa_tl
4181
           \spath_save_path:cV
4182
           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4183
           \l_spath_tmpa_tl
4184
        }
4185
      },
4186
      save~ global/.code={
4187
         \tikz@addmode{
4188
           \spath_get_current_path:N \l__spath_tmpa_tl
4189
4190
           \spath_bake_round:NV \l__spath_tmpa_tl \l__spath_tmpa_tl
           \spath_gsave_path:cV
4191
           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4192
           \l__spath_tmpa_tl
4193
4194
      },
4195
      clone/.code~ 2~ args={
4196
```

{\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}

\tl_if_exist:cTF

4197

4198 4199

```
4200
         \tl_clear_new:c
         4201
         \tl_set_eq:cc
4202
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4203
         {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
4204
       }
4205
4206
         \msg_warning:nnn { spath3 } { missing soft path } { #2 }
       }
     },
4209
     clone~ global/.code~ 2~ args={
4210
       \tl_if_exist:cTF
4211
       {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
4212
4213
         \tl_gclear_new:c
4214
         4215
         \tl_gset_eq:cc
4216
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4217
         {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
       }
         \msg_warning:nnn { spath3 } { missing soft path } { #2 }
4221
       }
4222
     },
4223
   Saves a soft path to the aux file.
     save~ to~ aux/.code={
4224
       \tl_if_exist:cTF
4225
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4226
4228
         \spath_save_to_aux:c
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4229
4230
       }
4231
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4232
       }
4233
     },
4234
   Exports the path as an SVG file.
     export~ to~ svg/.code={
       \tl_if_exist:cTF
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4238
         \spath_export_to_svg:nv {#1}
4239
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4240
       }
4241
       {
4242
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4243
4244
4245
     },
```

Inserts the named path at the current point in the path, with options for how this is accomplished. The inserted path can be transformed, reversed, moved to the current

point, and welded to the current path. If this is used before the path has been started then it becomes the start of the path (and the "current point" is taken as the origin).

```
use/.code={
4246
        \bool_set_false:N \l__spath_reverse_bool
4247
        \bool_set_false: N \l__spath_weld_bool
        \bool_set_false:N \l__spath_move_bool
        \tl_clear:N \l__spath_joinpath_tl
        \tl_clear:N \l__spath_transformation_tl
4251
        \tikzset{
4252
          spath/join/.cd,
4253
4254
4255
4256
        \tl_if_exist:cTF
4257
4258
          \tl_use:N \l__spath_prefix_tl
          \tl_use:N \l__spath_joinpath_tl
          \verb|\tl_use:N \ll_spath_suffix_tl|
4261
       }
4262
        {
4263
          \tl_if_empty:cT
4264
          {
4265
            \tl_use:N \l__spath_prefix_tl
4266
            \tl_use:N \l__spath_joinpath_tl
4267
            \tl_use:N \l__spath_suffix_tl
4268
            \msg_warning:nnn { spath3 } { empty soft path } { #1 }
4271
          }
4272
4273
          \tl_set_eq:Nc \l__spath_joinpath_tl
4274
            \tl_use:N \l__spath_prefix_tl
4275
            \tl_use:N \l__spath_joinpath_tl
4276
            \tl_use:N \l__spath_suffix_tl
4277
4278
          \spath_get_current_path:N \l__spath_current_tl
4279
          \bool_if:NT \l__spath_reverse_bool
4282
            \spath_reverse:N \l__spath_joinpath_tl
4283
4284
4285
          \tl_if_empty:NF \l__spath_transformation_tl
4286
4287
            \group_begin:
4288
            \pgftransformreset
4289
            \__spath_tikzset:V \l__spath_transformation_tl
            \pgfgettransform \l_spath_tmpa_tl
            \tl_gset:Nn \g__spath_smuggle_tl
4293
            {
               \spath_transform:Nnnnnn
4294
               \l_spath_joinpath_tl
4295
4296
            \tl_gput_right:NV \g__spath_smuggle_tl \l__spath_tmpa_tl
4297
```

```
4298
            \group_end:
            \t \ \g_spath_smuggle_tl
4299
4300
4301
          \bool_if:NT \l__spath_move_bool
4302
4303
            \tl_if_empty:NTF \l__spath_current_tl
4304
4305
               \tl_set:Nn \l__spath_tmpc_tl { {0pt} {0pt} }
            }
               \spath_finalpoint:NV
4309
               \l_spath_tmpc_tl
4310
               \l__spath_current_tl
4311
4312
             \spath_translate_to:NV \l__spath_joinpath_tl \l__spath_tmpc_tl
4313
          }
4314
4315
          \tl_if_empty:NTF \l__spath_current_tl
            \verb|\tl_if_empty:NTF \ | l_spath_joinpath_tl|
4319
               \tl_set_eq:NN \l__spath_current_tl \c_spath_moveto_tl
4320
               \tl_put_right:Nn \l__spath_current_tl {{0pt}{0pt}}
4321
4322
4323
               \tl_set_eq:NN \l__spath_current_tl \l__spath_joinpath_tl
4324
            }
4325
          }
4326
          {
            \t! Clear: N \l_spath_tmpa_tl
4330
            \tl_set:Nn \l__spath_tmpa_tl {spath_}
4331
            \tl_put_right:Nn \l__spath_tmpa_tl {append}
4332
4333
            \verb|\bool_if:NT \ll_spath_weld_bool|
4334
4335
4336
               \tl_put_right:Nn \l__spath_tmpa_tl {_no_move}
            }
            \tl_put_right:Nn \l__spath_tmpa_tl {:NV}
            \use:c {\tl_use:N \l__spath_tmpa_tl }
4340
4341
            \l_spath_current_tl
            \l_spath_joinpath_tl
4342
4343
4344
          \spath_set_current_path: N \l__spath_current_tl
4345
          \spath_set_tikz_data: V \l__spath_joinpath_tl
4346
4347
        }
        {
4349
          \msg_warning:nnx
4350
          { spath3 }
          { missing soft path }
4351
```

```
4352
          {\tl_use:N \l__spath_joinpath_tl }
4353
     },
4354
    Some aliases for the above.
     restore/.style={/tikz/spath/use={#1}},
4355
     restore~ reverse/.style={/tikz/spath/use={reverse, #1}},
4356
     append/.style={/tikz/spath/use={move, weld, #1}},
4357
     append~ no~ move/.style={/tikz/spath/use={weld, #1}},
     append~ reverse/.style={/tikz/spath/use={move, weld, reverse, #1}},
     append~ reverse~ no~ move/.style={/tikz/spath/use={weld, reverse, #1}},
     insert/.style={/tikz/spath/use={#1}},
4361
     insert~ reverse/.style={/tikz/spath/use={reverse, #1}},
4362
    Diagnostic, show the current path in the terminal and log.
     show~current~path/.code={
4363
        \tikz@addmode{
4364
          \pgfsyssoftpath@getcurrentpath\l__spath_tmpa_tl
          \iow_term:n {---~ current~ soft~ path~ ---}
          \spath_show:V \l__spath_tmpa_tl
       }
     },
4369
   Diagnostic, show the named soft path in the terminal and log.
     show/.code={
4370
        \tl_if_exist:cTF
4371
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4372
4373
          \tl_if_empty:cTF
4374
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4376
            \msg_warning:nnn { spath3 } { empty soft path } { #1 }
4377
4378
         }
4379
            \iow_term:n {---~ soft~ path~ #1~ ---}
4380
            \spath_show:v
4381
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4382
4383
       }
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
        }
     },
4388
```

This joins a path on to an existing path, possibly modifying it first. The possible options are the same as those for use. It is possible to specify the same path both for the initial and the joining path as a copy is made internally first.

```
join~ with/.code~ 2~ args={

injury args = {

injury
```

```
\bool_set_false: N \l__spath_global_bool
4396
          \tl_clear:N \l__spath_joinpath_tl
4397
          \tl_clear:N \l__spath_transformation_tl
4398
          \tikzset{
4399
            spath/join/.cd,
4400
            #2
4401
          }
4402
4403
          \tl_if_exist:cTF
          {
            \tl_use:N \l__spath_prefix_tl
            4407
            \tl_use:N \l__spath_suffix_tl
4408
4409
4410
            \tl_set_eq:Nc \l__spath_joinpath_tl
4411
4412
              \tl_use:N \l__spath_prefix_tl
4413
              \tl_use:N \l__spath_joinpath_tl
              \tl_use:N \l__spath_suffix_tl
4417
            \verb|\bool_if:NT \ll_spath_reverse_bool|
4418
4419
              \spath_reverse:N \l__spath_joinpath_tl
4420
4421
4422
            \tl_if_empty:NF \l__spath_transformation_tl
4423
4424
              \group_begin:
              \pgftransformreset
4426
              \__spath_tikzset:V \l__spath_transformation_tl
4427
              \verb|\pgfgettransform \l_spath_tmpa_tl|
4428
              \tl_gset:Nn \g__spath_smuggle_tl
4429
              {
4430
                \spath_transform: Nnnnnnn
4431
                \l__spath_joinpath_tl
4432
              }
4433
              \tl_gput_right:NV \g__spath_smuggle_tl \l__spath_tmpa_tl
              \group_end:
              \tl_use:N \g__spath_smuggle_tl
            }
4438
            \bool_if:NT \l__spath_move_bool
4439
4440
              \spath_finalpoint:Nv
4441
              \l_spath_tmpc_tl
4442
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4443
              \spath_translate_to:NV \l__spath_joinpath_tl \l__spath_tmpc_tl
            }
4447
            \tl_clear:N \l__spath_tmpa_tl
            \tl_set:Nn \l__spath_tmpa_tl {spath_}
4448
4449
```

```
\bool_if:NT \l__spath_global_bool
4450
4451
               \tl_put_right:Nn \l__spath_tmpa_tl {g}
4452
4453
4454
             \tl_put_right:Nn \l__spath_tmpa_tl {append}
4455
4456
             \bool_if:NT \l__spath_weld_bool
               \tl_put_right:Nn \l__spath_tmpa_tl {_no_move}
             }
             \tl_put_right:Nn \l__spath_tmpa_tl {:cV}
4461
4462
             \cs_if_exist:cF {\tl_use:N \l__spath_tmpa_tl}
4463
4464
               \tl_show:N \l__spath_tmpa_tl
4465
4466
             \use:c {\tl_use:N \l__spath_tmpa_tl }
             {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
             \label{local_spath_joinpath_tl} $$ 1__spath_joinpath_tl $$
          }
4471
           {
4472
             \msg_warning:nnx
4473
             { spath3 }
4474
             { missing soft path }
4475
             {\tl_use:N \l__spath_joinpath_tl }
4476
4477
        }
4478
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4480
        }
4481
      },
4482
```

Does a "spot weld" on a soft path, which means that any components that start where the previous component ends are welded together.

```
spot~ weld/.code={
4483
       \tl_if_exist:cTF
4484
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4485
4486
         \spath_spot_weld_components:c
4487
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4488
4489
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
      }
4492
     },
4493
     spot~ weld~ globally/.code={
4494
       \tl_if_exist:cTF
4495
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4496
4497
         \spath_spot_gweld_components:c
4498
4499
```

```
4501
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4502
       }
4503
     },
4504
    Reverses the named path.
     reverse/.code={
4505
       \tl_if_exist:cTF
4506
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4508
          \spath_reverse:c
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4510
4511
4512
       {
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4513
4514
     },
4515
     reverse~ globally/.code={
4516
       \tl_if_exist:cTF
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4519
         \spath_reverse:c
4520
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4521
       }
4522
       {
4523
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4524
       }
4525
     },
4526
    Adjust a path to span between two points.
     span/.code ~n~ args={3}{
4527
       \tl_if_exist:cTF
4528
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4529
4530
          \__spath_process_tikz_point:Nn \l__spath_tmpa_tl {#2}
4531
         \__spath_process_tikz_point:Nn \l__spath_tmpb_tl {#3}
4532
         \spath_span:cVV
4533
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4534
4535
         \l_spath_tmpa_tl \l_spath_tmpb_tl
       }
       {
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
       }
4530
     },
4540
     span~ global/.code ~n~ args={3}{
4541
       \tl_if_exist:cTF
4542
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4543
4544
          \__spath_process_tikz_point:Nn \l__spath_tmpa_tl {#2}
4545
4546
         \__spath_process_tikz_point:Nn \l__spath_tmpb_tl {#3}
         \spath_gspan:cVV
         4548
4549
          \l__spath_tmpa_tl \l__spath_tmpb_tl
4550
```

```
4551
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4552
        }
4553
     },
4554
    Defines a to path
      to/.style={
4555
        to~path={
4556
             spath/span={#1}{(\tikztostart)){(\tikztotarget)},
4558
             spath/append~no~move={#1},
4560
           \tikztonodes
4561
4562
4563
```

Splice three paths together, transforming the middle one so that it exactly fits between the first and third.

```
splice/.code ~n~ args={3}{
4564
       \tl_if_exist:cTF
4565
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4566
4567
         \tl_if_exist:cTF
         {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
           \tl_if_exist:cTF
4571
           {\tl_use:N \l__spath_prefix_tl #3 \tl_use:N \l__spath_suffix_tl}
4572
4573
             \spath_splice_between:cvv
4574
             {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4575
             {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
4576
4577
             {\tl_use:N \l__spath_prefix_tl #3 \tl_use:N \l__spath_suffix_tl}
           }
             \msg_warning:nnn { spath3 } { missing soft path } { #3 }
4581
         }
4582
4583
           \msg_warning:nnn { spath3 } { missing soft path } { #2 }
4584
         }
4585
       }
4586
4587
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4588
       }
     },
     splice~ global/.code ~n~ args={3}{
4591
       \tl_if_exist:cTF
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4593
4594
         \tl_if_exist:cTF
4595
         4596
4597
4598
           \tl_if_exist:cTF
           {\tl_use:N \l__spath_prefix_tl #3 \tl_use:N \l__spath_suffix_tl}
```

```
{
4600
           \spath_gsplice_between:cvv
4601
           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4602
           {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
4603
           4604
4605
4606
           \msg_warning:nnn { spath3 } { missing soft path } { #3 }
       }
4609
4610
       {
         \msg_warning:nnn { spath3 } { missing soft path } { #2 }
4611
4612
      }
4613
      {
4614
        4615
4616
    }
```

Join the components of a path by splicing in the second path whenever the components are sufficiently far apart. The third argument is a list of components to splice after, if it is empty then all components are used and a spot weld is done first so that the splicing only happens if there is an actual gap.

The upright versions will join with the reflection of the splice path if it detects that the gap is "upside-down".

```
join~ components~ with/.code~2~args={
        \tl_if_exist:cTF
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4621
          \tl_if_head_is_group:nTF {#2}
4622
4623
            \tl_set:Nx \l__spath_tmpc_tl { \tl_item:nn {#2} {1} }
4624
            \tl_set:Nx \l__spath_tmpd_tl { \tl_item:nn {#2} {2} }
4625
4626
4627
            \tl_set:Nn \l__spath_tmpc_tl {#2}
4628
            \tl_clear:N \l__spath_tmpd_tl
          }
          \tl_if_exist:cTF
4631
4632
            \tl_use:N \l__spath_prefix_tl
4633
            \tl_use:N \l__spath_tmpc_tl
4634
            \tl_use:N \l__spath_suffix_tl
4635
4636
4637
            \tl_if_empty:NT \l__spath_tmpd_tl
4638
4639
              \spath_spot_weld_components:c
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4642
4643
            \spath_components_to_seq:Nv
4644
            \l_spath_tmpa_seq
4645
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4646
```

```
4647
           \verb|\seq_gclear:N \g_spath_tmpa_seq| \\
4648
4649
           \tl_if_empty:NTF \l__spath_tmpd_tl
4650
4651
             \int_step_inline:nnnn {1}{1} {\seq_count:N \l__spath_tmpa_seq}
4652
             {
4653
               \seq_gput_right:Nn \g__spath_tmpa_seq {##1}
             }
           }
4657
             \foreach \l_spath_tmpa_tl in \l_spath_tmpd_tl
4658
             {
4659
               \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
4660
             }
4661
             \seq_gsort:Nn \g__spath_tmpa_seq
4662
4663
               \int \int \int d^2 t dt
               { \sort_return_same: }
               { \sort_return_swapped: }
             }
           }
4669
           4670
           4671
4672
           \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
4673
4674
             \int_compare:nTF
4675
             {
               ##1 == \l_spath_tmpb_tl
4677
             }
             {
4679
               \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpb_tl
4680
4681
                 \tl_set:Nn \l__spath_tmpb_tl {-1}
4682
4683
               \spath_splice_between:Nvn \l__spath_tmpa_tl
4684
                 \tl_use:N \l__spath_prefix_tl
                 \tl_use:N \l__spath_tmpc_tl
                 \tl_use:N \l__spath_suffix_tl
               }
               {##2}
4690
             }
4691
             {
4692
               \tl_put_right:Nn \l__spath_tmpa_tl {##2}
4693
             }
4694
           }
4695
           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
           \l_spath_tmpa_tl
4699
         {
4700
```

```
4701
            \msg_warning:nnx
            { spath3 }
4702
            { missing soft path }
4703
            { \tl_use:N \l__spath_tmpc_tl }
4704
4705
        }
4706
        {
4707
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4708
4709
        }
4710
     },
      join~ components~ globally~ with/.code~2~args={
4711
        \tl_if_exist:cTF
4712
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4713
4714
          \tl_if_head_is_group:nTF {#2}
4715
4716
            \tl_set:Nx \l__spath_tmpc_tl { \tl_item:nn {#2} {1} }
4717
            \tl_set:Nx \l__spath_tmpd_tl { \tl_item:nn {#2} {2} }
4718
          }
            \tl_set:Nn \l__spath_tmpc_tl {#2}
            \tl_clear:N \l__spath_tmpd_tl
4722
          }
4723
          \tl_if_exist:cTF
4724
4725
            \t_use:N \l_spath_prefix_tl
4726
            \tl_use:N \l__spath_tmpc_tl
4727
            \tl_use:N \l__spath_suffix_tl
4728
4729
            \tl_if_empty:NT \l__spath_tmpd_tl
4733
               \spath_spot_weld_components:c
               4734
4735
4736
            \spath_components_to_seq:Nv
4737
            \l_spath_tmpa_seq
4738
4739
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
            \seq_gclear:N \g__spath_tmpa_seq
            \tl_if_empty:NTF \l__spath_tmpd_tl
4743
4744
            {
               \label{lem:nnnn} $$ \inf_{s \in \mathbb{N} \leq nnnn} \{1\}_{1} {\seq_count:} \mathbb{N} = \sup_{s \in \mathbb{N}} \{n_s \in \mathbb{N} \in \mathbb{N} \} $$
4745
               {
4746
                 \seq_gput_right:Nn \g__spath_tmpa_seq {##1}
4747
               }
4748
            }
4749
4750
               \foreach \l__spath_tmpa_tl in \l__spath_tmpd_tl
               {
4753
                 \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
               }
4754
```

```
\verb|\seq_gsort:Nn \g_spath_tmpa_seq| \\
4755
              {
4756
                 \int_compare:nNnTF {##1} < {##2}
4757
                 { \sort_return_same: }
4758
                 { \sort_return_swapped: }
4759
              }
4760
            }
4761
            \seq_pop_left:NN \l__spath_tmpa_seq \l__spath_tmpa_tl
            \seq_gpop_left:NN \g__spath_tmpa_seq \l__spath_tmpb_tl
            \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
4766
            {
4767
               \int_compare:nTF
4768
              {
4769
                 ##1 == \l__spath_tmpb_tl
4770
              }
4771
              {
4772
                 \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpb_tl
                   \tl_set:Nn \l__spath_tmpb_tl {-1}
                }
                 \spath_splice_between:Nvn \l__spath_tmpa_tl
4777
                   \tl_use:N \l__spath_prefix_tl
4779
                   \tl_use:N \l__spath_tmpc_tl
4780
                   \tl_use:N \l__spath_suffix_tl
4781
                }
4782
                 {##2}
4783
              }
              {
                 \tl_put_right:Nn \l__spath_tmpa_tl {##2}
              }
4787
4788
            \tl_gset_eq:cN
4789
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4790
            \l_spath_tmpa_tl
4791
          }
4792
4793
            \msg_warning:nnx
            { spath3 }
            { missing soft path }
4797
            { \tl_use:N \l__spath_tmpc_tl }
          }
4798
        }
4799
        {
4800
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
4801
        }
4802
     },
4803
4804
      join~ components~ upright~ with/.code~2~args={
        \tl_if_exist:cTF
4806
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4807
          \tl_if_head_is_group:nTF {#2}
4808
```

```
{
4809
            \tl_set:Nx \l__spath_tmpc_tl { \tl_item:nn {#2} {1} }
4810
            \tl_set:Nx \l__spath_tmpd_tl { \tl_item:nn {#2} {2} }
4811
4812
4813
            \tl_set:Nn \l__spath_tmpc_tl {#2}
4814
           \tl_clear:N \l__spath_tmpd_tl
4815
4816
         \tl_if_exist:cTF
4817
         {
4818
           \tl_use:N \l__spath_prefix_tl
4819
           \t_use:N \l_spath_tmpc_tl
4820
            \tl_use:N \l__spath_suffix_tl
4821
4822
4823
            \tl_if_empty:NT \l__spath_tmpd_tl
4824
4825
              \spath_spot_weld_components:c
4826
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
           \spath_components_to_seq:Nv
4830
           \l_spath_tmpa_seq
4831
           4832
4833
           \verb|\seq_gclear:N \g_spath_tmpa_seq| \\
4834
4835
           \tl_if_empty:NTF \l__spath_tmpd_tl
4836
4837
              \int_step_inline:nnnn {1}{1} {\seq_count:N \l__spath_tmpa_seq}
4839
                \seq_gput_right: Nn \g__spath_tmpa_seq {##1}
4840
             }
4841
           }
4842
           {
4843
              \foreach \l_spath_tmpa_tl in \l_spath_tmpd_tl
4844
              {
4845
                \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
4846
              }
              \seq_gsort:Nn \g__spath_tmpa_seq
              {
                \int_compare:nNnTF {##1} < {##2}
                { \sort_return_same: }
4851
                { \sort_return_swapped: }
4852
             }
4853
           }
4854
4855
           \seq_pop_left:NN \l__spath_tmpa_seq \l__spath_tmpa_tl
4856
           \seq_gpop_left:NN \g__spath_tmpa_seq \l__spath_tmpb_tl
4857
4858
           \tl_set_eq:Nc \l__spath_tmpc_tl
              \tl_use:N \l__spath_prefix_tl
4861
              \tl_use:N \l__spath_tmpc_tl
4862
```

```
\tl_use:N \l__spath_suffix_tl
4863
            }
4864
            \label{lem:nvnnnnn} $$ \sup_{t=0}^{t} \lim_{t\to\infty} 1_{spath_tmpd_tl} = \int_{t}^{t} \{1\}\{0\}\{0\}\{0\}\{0\}\{0\}\{0\}\} 
4865
   1}{0pt}{0pt}
4866
            \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
4867
            {
4868
              \int_compare:nTF
              {
                ##1 == \l__spath_tmpb_tl
              }
              {
4873
                 \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpb_tl
4874
                 {
4875
                   \tl_set:Nn \l__spath_tmpb_tl {-1}
4876
4877
                 \spath_finalpoint:NV \l__spath_tmpe_tl \l__spath_tmpa_tl
4878
                 \spath_initialpoint:Nn \l__spath_tmpf_tl {##2}
                 \dim_compare:nTF
                   \tl_item:Nn \l__spath_tmpe_tl {1}
4884
                   \tl_item:Nn \l__spath_tmpf_tl {1}
                }
4886
4887
                   \spath_splice_between:NVn
4888
                   \l_spath_tmpa_tl
4889
                   \l_spath_tmpd_tl
4890
                   {##2}
                }
                   \spath_splice_between:NVn
4894
                   \l__spath_tmpa_tl
4895
                   \l__spath_tmpc_tl
4896
                   {##2}
4897
                }
4898
              }
4899
4900
              {
                 \tl_put_right:Nn \l__spath_tmpa_tl {##2}
              }
            }
4904
            \tl_set_eq:cN
            4905
            \l_spath_tmpa_tl
4906
          }
4907
          {
4908
            \msg_warning:nnx
4909
            { spath3 }
4910
4911
            { missing soft path }
            { \tl_use:N \l__spath_tmpc_tl }
4913
          }
       }
4914
        {
4915
```

```
\msg_warning:nnn { spath3 } { missing soft path } { #1 }
4916
       }
4917
     },
4918
      join~ components~ globally~ upright~ with/.code~2~args={
4919
        \tl_if_exist:cTF
4920
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4921
4922
          \tl_if_head_is_group:nTF {#2}
4923
            \label{locality} $$ \tilde{N}  = \frac{1}{2} {1} $
4925
            \t! \tl_set:Nx \l_spath_tmpd_tl { \tl_item:nn {#2} {2} }
4926
4927
4928
            \tl_set:Nn \l__spath_tmpc_tl {#2}
4929
            \tl_clear:N \l__spath_tmpd_tl
4930
4931
          \tl_if_exist:cTF
4932
4933
            \tl_use:N \l__spath_prefix_tl
            \tl_use:N \l__spath_tmpc_tl
            \tl_use:N \l__spath_suffix_tl
          }
4937
          ₹
4938
            \tl_if_empty:NT \l__spath_tmpd_tl
4939
4940
              \spath_spot_weld_components:c
4941
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4942
4943
4944
            \verb|\spath_components_to_seq:Nv| \\
            \l_spath_tmpa_seq
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
4947
4948
            \seq_gclear:N \g__spath_tmpa_seq
4949
4950
            \tl_if_empty:NTF \l__spath_tmpd_tl
4951
4952
4953
              \int_step_inline:nnnn {1}{1} {\seq_count:N \l__spath_tmpa_seq}
4954
                 \seq_gput_right:Nn \g__spath_tmpa_seq {##1}
              }
            }
            {
4958
              \foreach \l__spath_tmpa_tl in \l__spath_tmpd_tl
4959
              {
4960
                 \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
4961
              }
4962
              \seq_gsort:Nn \g__spath_tmpa_seq
4963
              {
4964
                 \int_compare:nNnTF {##1} < {##2}
                 { \sort_return_same: }
                 { \sort_return_swapped: }
              }
4968
            }
4969
```

```
4970
           \ensuremath{\verb| l_spath_tmpa_seq | l_spath_tmpa_tl|}
4971
           \seq_gpop_left:NN \g__spath_tmpa_seq \l__spath_tmpb_tl
4972
4973
           \tl_set_eq:Nc \l__spath_tmpc_tl
4974
           {
4975
             \tl_use:N \l__spath_prefix_tl
4976
             \tl_use:N \l__spath_tmpc_tl
4977
             \tl_use:N \l__spath_suffix_tl
4979
           1}{0pt}{0pt}
4981
           \seq_map_indexed_inline:Nn \l__spath_tmpa_seq
4982
           {
4983
              \int_compare:nTF
4984
             {
4985
               ##1 == \l__spath_tmpb_tl
             }
             {
                \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpb_tl
                 \tl_set:Nn \l__spath_tmpb_tl {-1}
                \spath_finalpoint:NV \l__spath_tmpe_tl \l__spath_tmpa_tl
4993
               \spath_initialpoint: Nn \l__spath_tmpf_tl {##2}
4994
4995
               \dim_compare:nTF
4996
4997
                 \tl_item:Nn \l__spath_tmpe_tl {1}
                 \tl_item:Nn \l__spath_tmpf_tl {1}
               }
5001
5002
                  \spath_splice_between:NVn
5003
                 \l_spath_tmpa_tl
5004
                 \l_spath_tmpd_tl
5005
                  {##2}
5006
5007
               }
                  \spath_splice_between:NVn
                  \l_spath_tmpa_tl
5011
                  \l__spath_tmpc_tl
                 {##2}
5012
               }
5013
             }
5014
             {
5015
                \tl_put_right:Nn \l__spath_tmpa_tl {##2}
5016
             }
5017
5018
           \tl_gset_eq:cN
5020
           {\tl_use:N \l_spath_prefix_tl #1 \tl_use:N \l_spath_suffix_tl}
5021
           \l__spath_tmpa_tl
5022
```

```
{
5023
            \msg_warning:nnx
5024
           { spath3 }
5025
           { missing soft path }
5026
            { \tl_use:N \l__spath_tmpc_tl }
5027
5028
       }
5029
       {
5030
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5031
5032
     },
5033
    Close a path.
     close/.code={
5034
       \tl_if_exist:cTF
5035
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5036
5037
          \spath_close:c
5038
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
       }
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5042
       }
5043
     },
5044
     close~ globally/.code={
5045
       \tl_if_exist:cTF
5046
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5047
5048
          \spath_gclose:c
5049
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
       }
5051
5052
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5053
       }
5054
     },
5055
    Close a path with another path.
     close~ with/.code~ 2~ args={
5056
5057
       \tl_if_exist:cTF
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
         \tl_if_exist:cTF
         {\tl_use:N \l_spath_prefix_tl #2 \tl_use:N \l_spath_suffix_tl}
5061
5062
           \spath_close_with:cv
5063
           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5064
           5065
5066
5067
5068
            \msg_warning:nnn { spath3 } { missing soft path } { #2 }
         }
5070
       }
5071
       {
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5072
```

```
}
5073
     },
5074
     close~ globally~ with/.code~ 2~ args={
5075
       \tl_if_exist:cTF
5076
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5077
5078
        \tl_if_exist:cTF
5079
        {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5080
          \spath_gclose_with:cv
5082
          5083
          {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5084
5085
5086
           \msg_warning:nnn { spath3 } { missing soft path } { #2 }
5087
5088
5089
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
     },
   These keys shorten the path.
     shorten~ at~ end/.code~ 2~ args={
5094
       \tl_if_exist:cTF
5095
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5096
5097
5098
        \spath_shorten_at_end:cn
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl} {#2}
5099
      }
5101
      {
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5102
      }
5103
5104
     },
     shorten~ at~ start/.code~ 2~ args ={
5105
       \tl_if_exist:cTF
5106
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5107
5108
5109
         \spath_shorten_at_start:cn
        5112
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5113
      }
5114
     ٦.
5115
     shorten~ at~ both~ ends/.code~ 2~ args={
5116
       \tl_if_exist:cTF
5117
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5118
5119
5120
         \spath_shorten_at_end:cn
5121
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl} {#2}
5122
        \spath_shorten_at_start:cn
        5123
5124
```

```
5125
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5126
      }
5127
    },
5128
    shorten~ globally~ at~ end/.code~ 2~ args={
5129
      \tl_if_exist:cTF
5130
      {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5131
5132
        \spath_gshorten_at_end:cn
5133
        5134
5135
      }
      {
5136
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5137
5138
    },
5139
    shorten~ globally~ at~ start/.code~ 2~ args ={
5140
      \tl_if_exist:cTF
5141
      {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5142
        \spath_gshorten_at_start:cn
        5145
      }
5146
      {
5147
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5148
5149
    },
5150
    shorten~ globally~ at~ both~ ends/.code~ 2~ args={
5151
      \tl_if_exist:cTF
5152
      {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5153
5154
5155
        \spath_shorten_at_end:cn
        5156
5157
        \spath_shorten_at_start:cn
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl} {#2}
5158
      }
5159
5160
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5161
5162
5163
   This translates the named path.
    translate/.code~ n~ args={3}{
5164
      \tl_if_exist:cTF
5165
      {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5166
5167
        \spath_translate:cnn
5168
        5169
      }
5170
5171
      {
5172
        \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5173
      }
5174
    },
    translate~ globally/.code~ n~ args={3}{
5175
      \tl_if_exist:cTF
5176
```

```
{\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5177
5178
         \spath_gtranslate:cnn
5179
         5180
5181
5182
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5183
5184
     },
5185
   This normalises the named path.
     normalise/.code={
5186
       \tl_if_exist:cTF
5187
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5188
5189
         \spath_normalise:c
5190
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5191
5192
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
       }
     },
5196
     normalise~ globally/.code={
5197
       \tl_if_exist:cTF
5198
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5199
5200
5201
         \spath_gnormalise:c
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5202
5203
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5205
       }
5206
5207
     },
   Transforms the named path using TikZ transformation specifications.
     transform/.code~ 2~ args={
5208
       \tl_if_exist:cTF
5209
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5210
5211
5212
         \group_begin:
         \pgftransformreset
         \tikzset{#2}
5215
         \pgfgettransform \l__spath_tmpa_tl
         \tl_gset:Nn \g__spath_smuggle_tl
5216
5217
           \spath_transform:cnnnnn
5218
           {\tl_use:N \l_spath_prefix_tl #1 \tl_use:N \l_spath_suffix_tl}
5219
5220
         \tl_gput_right:NV \g__spath_smuggle_tl \l__spath_tmpa_tl
5221
5222
         \group_end:
         \tl_use:N \g__spath_smuggle_tl
5224
       }
5225
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5226
```

```
}
5227
     },
5228
     transform~globally/.code~ 2~ args={
5229
        \tl_if_exist:cTF
5230
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5231
5232
          \group_begin:
5233
          \pgftransformreset
5234
          \tikzset{#2}
          \pgfgettransform \l__spath_tmpa_tl
5237
          \tl_gset:Nn \g__spath_smuggle_tl
5238
            \spath_gtransform:cnnnnn
5239
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5240
5241
          \tl_gput_right:NV \g__spath_smuggle_tl \l__spath_tmpa_tl
5242
          \group_end:
5243
          \tl_use:N \g__spath_smuggle_tl
5244
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
       }
5248
     },
5249
    Splits first path where it intersects with the second.
     split~ at~ intersections~ with/.code~ n~ args={2}{
5250
        \tl_if_exist:cTF
5251
5252
          tikz@library@intersections@loaded
5253
5254
       }
5255
          \tl_if_exist:cTF
5256
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5257
5258
            \tl_if_exist:cTF
5259
            {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5260
5261
              \spath_split_path_at_intersections:cv
5262
5263
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
              {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
            }
              \msg_warning:nnn { spath3 } { missing soft path } { #2 }
5267
5268
          }
5269
          {
5270
            \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5271
          }
5272
       }
5273
5274
          \msg_warning:nn { spath3 } { load intersections }
5276
       }
5277
     },
     split~ globally~ at~ intersections~ with/.code~ n~ args={2}{
5278
```

```
\tl_if_exist:cTF
5279
       ₹
5280
        tikz@library@intersections@loaded
5281
      }
5282
5283
       \tl_if_exist:cTF
5284
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5285
5286
          \tl_if_exist:cTF
          {\tl_use:N \l_spath_prefix_tl #2 \tl_use:N \l_spath_suffix_tl}
            \spath_gsplit_path_at_intersections:cv
5290
            5291
            {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5292
5293
          {
5294
            \msg_warning:nnn { spath3 } { missing soft path } { #2 }
5295
5296
        }
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
        }
5300
      }
5301
5302
         \msg_warning:nn { spath3 } { load intersections }
5303
      }
5304
    },
5305
   Splits two paths at their mutual intersections.
     split~ at~ intersections/.code~ n~ args={2}{
       \tl_if_exist:cTF
5307
5308
        tikz@library@intersections@loaded
5300
      }
5310
5311
        \tl_if_exist:cTF
5312
        5313
5314
5315
          \tl_if_exist:cTF
          {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
            \spath_split_at_intersections:cc
            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5319
            5320
          }
5321
5322
            \msg_warning:nnn { spath3 } { missing soft path } { #2 }
5323
          }
5324
        }
5325
5326
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5328
        }
      }
5320
       {
5330
```

```
\msg_warning:nn { spath3 } { load intersections }
5331
       }
5332
     },
5333
     split~ globally~ at~ intersections/.code~ n~ args={2}{
5334
       \tl_if_exist:cTF
5335
5336
         tikz@library@intersections@loaded
5337
       }
5338
         \tl_if_exist:cTF
5340
         {\tl_use:N \l_spath_prefix_tl #1 \tl_use:N \l_spath_suffix_tl}
5341
5342
           \tl_if_exist:cTF
5343
           {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5344
5345
              \spath_gsplit_at_intersections:cc
5346
              {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5347
              {\tl_use:N \l__spath_prefix_tl #2 \tl_use:N \l__spath_suffix_tl}
5348
              \msg_warning:nnn { spath3 } { missing soft path } { #2 }
5352
         }
5353
5354
            \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5355
         }
5356
       }
5357
5358
          \msg_warning:nn { spath3 } { load intersections }
5359
       }
5360
     },
5361
   Splits a path at its self-intersections.
     split~ at~ self~ intersections/.code={
5362
       \tl_if_exist:cTF
5363
5364
         tikz@library@intersections@loaded
5365
5366
5367
         \tl_if_exist:cTF
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
           \spath_split_at_self_intersections:c
5371
           5372
5373
5374
            \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5375
         }
5376
       }
5377
5378
          \msg_warning:nn { spath3 } { load intersections }
5380
       }
5381
     },
     split~ globally~ at~ self~ intersections/.code={
5382
```

```
\tl_if_exist:cTF
5383
       ₹
5384
         \verb|tikz@library@intersections@loaded|\\
5385
       }
5386
5387
         \tl_if_exist:cTF
5388
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5389
5390
           \spath_gsplit_at_self_intersections:c
           }
5393
         {
5394
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5395
         }
5396
5397
       {
5398
         \msg_warning:nn { spath3 } { load intersections }
5399
5400
     },
```

Extract the components of a path into a comma separated list (suitable for using in a \foreach loop).

```
get~ components~ of/.code~ 2~ args={
        \tl_if_exist:cTF
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5405
          \clist_clear_new:N #2
5406
          \spath_components_to_seq:Nv
5407
          \l_spath_tmpa_seq
5408
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5409
          \seq_map_inline: Nn \l__spath_tmpa_seq
5410
5411
            \tl_new:c
            {
              \tl_use:N \l__spath_prefix_tl
5414
              anonymous\_\int\_use: \c \g\_spath\_anon\_int
5415
              \tl_use:N \l__spath_suffix_tl
5416
            }
5417
            \tl_set:cn
5418
            {
5419
              \tl_use:N \l__spath_prefix_tl
5420
              \verb"anonymous_\int_use:N \ \g_spath_anon_int"
5421
              \tl_use:N \l__spath_suffix_tl
5422
            } {##1}
            \clist_put_right:Nx #2 {anonymous_\int_use:N \g__spath_anon_int}
            \int_gincr:N \g__spath_anon_int
5425
          }
5426
       }
5427
        {
5428
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5429
       }
5430
     },
5431
5432
     get~ components~ of~ globally/.code~ 2~ args={
        \tl_if_exist:cTF
```

```
{\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5434
        ₹
5435
          \clist_gclear_new:N #2
5436
          \spath_components_to_seq:Nv
5437
          \l_spath_tmpa_seq
5438
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5439
          \seq_map_inline: Nn \l__spath_tmpa_seq
5440
            \tl_new:c
5443
            {
              \tl_use:N \l__spath_prefix_tl
5444
              anonymous_\int_use:N \g__spath_anon_int
5445
              \tl_use:N \l__spath_suffix_tl
5446
            }
5447
            \tl_gset:cn
5448
            {
5449
              \tl_use:N \l__spath_prefix_tl
5450
              anonymous_\int_use:N \g__spath_anon_int
5451
              \tl_use:N \l__spath_suffix_tl
            } {##1}
            \clist_gput_right:Nx #2 {anonymous_\int_use:N \g__spath_anon_int}
            \int_gincr:N \g__spath_anon_int
5455
          }
5456
       }
5457
        {
5458
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5459
        }
5460
     },
5461
```

Loop through the components of a soft path and render each as a separate ${\rm Tik}{\rm Z}$ path so that they can be individually styled.

```
render~ components/.code={
5463
        \tl_if_exist:cTF
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5465
          \group_begin:
5466
          \spath_components_to_seq:Nv
5467
          \l_spath_tmpa_seq
5468
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5469
          \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
5470
5471
            \spath_tikz_path:nn
5472
5473
              every~ spath~ component/.try,
              spath ~component~ ##1/.try,
              spath ~component/.try={##1},
5476
              every~ #1~ component/.try,
5477
              #1 ~component~ ##1/.try,
5478
              #1 ~component/.try={##1},
5479
5480
            {
5481
              ##2
5482
5483
            }
          }
```

```
5485 \group_end:
5486 }
5487 {
5488 \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5489 }
5490 },
```

This puts gaps between components of a soft path. The list of components is passed through a \foreach loop so can use the shortcut syntax from those loops.

```
insert~ gaps~ after~ components/.code~ 2~ args={
5492
       \tl_if_exist:cTF
       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5493
          \group_begin:
5496
         \tl_if_head_is_group:nTF {#2}
5497
5498
            \tl_set:Nx \l__spath_tmpc_tl { \tl_item:nn {#2} {1} }
            \tl_set:Nx \l__spath_tmpd_tl { \tl_item:nn {#2} {2} }
5499
5500
5501
            \tl_set:Nn \l__spath_tmpc_tl {#2}
5502
            \tl_clear:N \l__spath_tmpd_tl
5503
         \seq_gclear:N \g__spath_tmpa_seq
         \verb|\seq_gclear:N \g_spath_tmpb_seq| \\
         \spath_numberofcomponents:Nv \l__spath_tmpa_int
5507
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5508
5509
         \spath_components_to_seq:Nv
5510
         \l__spath_tmpa_seq
5511
         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5512
5513
         \tl_if_empty:NTF \l__spath_tmpd_tl
5514
5515
           \int_step_inline:nnnn {1}{1} { \l__spath_tmpa_int - 1 }
5516
           {
5517
              \seq_gput_right:Nn \g_spath_tmpa_seq {##1}
5518
              \seq_gput_right:Nx
5519
              \g_spath_tmpb_seq
5520
              {\int_eval:n {##1 + 1}}
5521
5522
           }
         }
5523
5524
            \foreach \l_spath_tmpa_tl in \l_spath_tmpd_tl
              5527
              \seq_gput_right:Nx
5528
              \g_spath_tmpb_seq
5529
              {\int_eval:n
5530
5531
                  \int_mod:nn { \l__spath_tmpa_tl }{ \l__spath_tmpa_int } + 1
5532
               }
5533
5534
             }
           }
5535
```

```
}
5536
5537
                           \seq_clear:N \l__spath_tmpb_seq
5538
                           \seq_map_indexed_inline:Nn \l__spath_tmpa_seq
5539
5540
                                 \tl_set:Nn \l__spath_tmpa_tl {##2}
5541
                                \seq_if_in:NnT \g__spath_tmpa_seq {##1}
5542
                                      \spath_shorten_at_end: Nn \l__spath_tmpa_tl {\l__spath_tmpc_tl/2}
                                }
                                 \seq_if_in:NnT \g__spath_tmpb_seq {##1}
5547
                                {
                                      \spath_shorten_at_start: Nn \l__spath_tmpa_tl {\l__spath_tmpc_tl/2}
5548
5549
                                 \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
5550
5551
                           \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpb_seq {} }
5552
                           \group_end:
5553
                           \tl_set_eq:cN
                           \g__spath_output_tl
                           \tl_gclear:N \g_spath_output_tl
5557
                    }
5558
5559
                           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5560
                    }
5561
               },
5562
               insert~ gaps~ globally~ after~ components/.code~ 2~ args={
5563
5564
                     5566
5567
                           \group_begin:
5568
                           \tl_if_head_is_group:nTF {#2}
5569
                                 \tl_set:Nx \l__spath_tmpc_tl { \tl_item:nn {#2} {1} }
5570
                                 \t: Nx \leq t:Nx 
5571
5572
5573
5574
                                 \tl_set:Nn \l__spath_tmpc_tl {#2}
                                 \tl_clear:N \l__spath_tmpd_tl
                           \seq_gclear:N \g__spath_tmpa_seq
                           \seq_gclear:N \g__spath_tmpb_seq
5578
                           \spath_numberofcomponents:Nv \l__spath_tmpa_int
5579
                           5580
5581
                           \spath_components_to_seq:Nv
5582
5583
                           \l_spath_tmpa_seq
                           {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5584
5585
                          \tl_if_empty:NTF \l__spath_tmpd_tl
                                \int_step_inline:nnnn {1}{1} { \l__spath_tmpa_int - 1 }
5588
                                {
5589
```

```
\seq_gput_right: Nn \g_spath_tmpa_seq {##1}
5590
                                   \seq_gput_right:Nx
5591
                                   \g_spath_tmpb_seq
5592
                                   {\int_eval:n {##1 + 1}}
5593
                              }
5594
                        }
5595
5596
                               \foreach \l__spath_tmpa_tl in \l__spath_tmpd_tl
5597
                                   \seq_gput_right:Nx
                                   \g_spath_tmpb_seq
5601
                                   {\int_eval:n
5602
5603
                                        {
                                               \int_mod:nn { \l__spath_tmpa_tl }{ \l__spath_tmpa_int } + 1
5604
5605
                                   }
5606
                             }
5607
                        }
                         \seq_clear:N \l__spath_tmpb_seq
                         \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
5611
5612
                              \tl_set:Nn \l__spath_tmpa_tl {##2}
5613
                              \ensuremath{$\scriptstyle -$} seq_if_in: \ensuremath{$\scriptstyle -$} \ensuremath{$\scriptstyle -$} spath_tmpa\_seq \ensuremath{$\scriptstyle -$} \{\#1\}
5614
                              {
5615
                                   \spath_shorten_at_end: Nn \l__spath_tmpa_tl {\l__spath_tmpc_t1/2}
5616
                              }
5617
                              \seq_if_in:NnT \g__spath_tmpb_seq {##1}
5618
                                   \label{lem:local_spath_tmpa_tl {\l_spath_tmpa_tl {\l_spath_tmpc_tl/2}}} $$ \end{substitute} $$ \sum_{x \in \mathbb{N}^n \leq x} \lim_{x \in \mathbb{N}^n \leq x} \| x \|_{x} $$ $$ \end{substitute} $$ \end{substitute} $$ \sum_{x \in \mathbb{N}^n \leq x} \| x \|_{x} $$ $$ \end{substitute} $$ 
5621
                              }
                              \seq_put_right:NV \l__spath_tmpb_seq \l__spath_tmpa_tl
5622
                        }
5623
                         \tl_gset:Nx \g__spath_output_tl {\seq_use:Nn \l__spath_tmpb_seq {} }
5624
                         \group_end:
5625
                         \tl_gset_eq:cN
5626
5627
                         {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5628
                         \g_spath_output_tl
                         \tl_gclear:N \g_spath_output_tl
                   }
                         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5632
                   }
5633
              },
5634
          Join the specified components together, joining each to its previous one.
              join~ components/.code~ 2~ args={
5635
                    \tl_if_exist:cTF
5636
5637
                    {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
                         \verb|\seq_gclear:N \g_spath_tmpa_seq| \\
5639
5640
                         \foreach \l__spath_tmpa_tl in {#2}
                        {
5641
```

```
\seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
5642
                            }
5643
5644
                            \seq_gsort:Nn \g__spath_tmpa_seq
                            {
5645
                                   \int_compare:nNnTF {##1} > {##2}
5646
                                  { \sort_return_same: }
5647
                                  { \sort_return_swapped: }
5648
                            \seq_map_inline: Nn \g_spath_tmpa_seq
                            {
5651
5652
                                   \spath_join_component:cn
                                  5653
5654
                      }
5655
                       {
5656
                             \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5657
5658
5659
                join~ components~ globally/.code~ 2~ args={
                       \tl_if_exist:cTF
                       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5663
                            \label{lem:normalised} $$  \sq_gclear: N $$  \g_spath_tmpa_seq $$
5664
                            \foreach \l__spath_tmpa_tl in {#2}
5665
5666
                                   \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
5667
                            }
5668
5669
                            \seq_gsort:Nn \g__spath_tmpa_seq
5670
                                  \int \int d^2 \pi 
                                  { \sort_return_same: }
5673
                                  { \sort_return_swapped: }
                            }
5674
5675
                            \seq_map_inline: Nn \g_spath_tmpa_seq
5676
                                   \spath_gjoin_component:cn
5677
                                   {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}{##1}
5678
5679
5680
                      }
                             \mbox{msg\_warning:nnn } \{ \mbox{spath3} \} \{ \mbox{missing soft path } \{ \mbox{#1} \}
                      }
                },
5684
           Remove all components of the path that don't actually draw anything.
                remove~ empty~ components/.code={
5685
                       \tl_if_exist:cTF
5686
                       {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5687
5688
                             \spath_remove_empty_components:c
5689
                            {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5691
                      }
5692
                       {
                            \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5693
```

```
}
5694
     },
5695
     remove~ empty~ components~ globally/.code={
5696
        \tl_if_exist:cTF
5697
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5698
5699
          \spath_gremove_empty_components:c
5700
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5701
        }
        {
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5705
     },
5706
    Replace all line segments by Bézier curves.
     replace~ lines/.code={
5707
        \tl_if_exist:cTF
5708
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5709
          \spath_replace_lines:c
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5712
        }
5713
        {
5714
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5715
5716
     },
5717
     replace~ lines~ globally/.code={
5718
        \tl_if_exist:cTF
5719
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5720
5722
          \spath_greplace_lines:c
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5723
5724
        }
5725
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5726
        }
5727
     },
5728
    Join the specified components together, joining each to its previous one.
      remove~ components/.code~ 2~ args={
        \tl_if_exist:cTF
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5731
5732
          \scalebox{$\scalebox{$\sim$} seq_gclear:N $\scalebox{$\sim$} spath_tmpa_seq}
5733
          \foreach \l__spath_tmpa_tl in {#2}
5734
          {
5735
            \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
5736
          }
5737
5738
          \seq_gsort:Nn \g__spath_tmpa_seq
5739
            \int_compare:nNnTF {##1} < {##2}
            { \sort_return_same: }
5742
            { \sort_return_swapped: }
5743
```

```
5744
          \spath_components_to_seq:Nv
          \l_spath_tmpa_seq
5745
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5746
          \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpa_tl
5747
5748
             \tl_clear:N \l__spath_tmpa_tl
5749
          }
5750
          \seq_clear:N \l__spath_tmpb_seq
5751
          \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
5753
            \tl_set:Nn \l__spath_tmpb_tl {##1}
            \tl_if_eq:NNTF \l__spath_tmpb_tl \l__spath_tmpa_tl
5755
5756
               \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpa_tl
5757
5758
                 \tl_clear:N \l__spath_tmpa_tl
5759
               }
5760
            }
5761
               \seq_put_right:Nn \l__spath_tmpb_seq {##2}
          }
5765
          \tl_set:cx {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5766
          {\seq_use: Nn \l__spath_tmpb_seq {} }
5767
5768
5769
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5770
        }
5771
     },
5772
      remove~ components~ globally/.code~ 2~ args={
5774
        \tl_if_exist:cTF
        {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5775
5776
          \scalebox{$\scalebox{$\sim$} seq_gclear:N $\scalebox{$\sim$} spath_tmpa_seq}
5777
          \foreach \l__spath_tmpa_tl in {#2}
5778
5779
             \seq_gput_right:NV \g__spath_tmpa_seq \l__spath_tmpa_tl
5780
5781
5782
          \seq_gsort:Nn \g__spath_tmpa_seq
             \int_compare:nNnTF {##1} < {##2}
            { \sort_return_same: }
5786
            { \sort_return_swapped: }
5787
          \spath_components_to_seq:Nv
5788
          \l__spath_tmpa_seq
5789
          {\tl_use:N \l__spath_prefix_tl #1 \tl_use:N \l__spath_suffix_tl}
5790
          \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpa_tl
5791
5792
5793
             \tl_clear:N \l__spath_tmpa_tl
          }
          \verb|\seq_clear:N| \verb|\l_spath_tmpb_seq||
5796
          \seq_map_indexed_inline: Nn \l__spath_tmpa_seq
          {
5797
```

```
\tl_set:Nn \l__spath_tmpb_tl {##1}
5798
             \tl_if_eq:NNTF \l__spath_tmpb_tl \l__spath_tmpa_tl
5799
5800
               \seq_gpop_left:NNF \g__spath_tmpa_seq \l__spath_tmpa_tl
5801
               {
5802
                  \tl_clear:N \l__spath_tmpa_tl
5803
               }
             }
             {
                \seq_put_right:Nn \l__spath_tmpb_seq {##2}
             }
          }
5809
           \label{local_spath_prefix_tl #1 \tl_use:N \l_spath_suffix_tl} $$ $$ \tilde{\tl}_use:N \l_spath_suffix_tl} $$
5810
           {\seq_use: Nn \l__spath_tmpb_seq {} }
5811
5812
        {
5813
           \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5814
5815
      },
```

This puts a conditional around the **spot weld** key because when figuring out a knot drawing then we will initially want to render it without the spot weld to keep the number of components constant.

```
draft~ mode/.is~ choice,
5817
    draft~ mode/true/.code={
5818
      \bool_set_true:N \l__spath_draft_bool
    },
    draft~ mode/false/.code={
      \bool_set_false:N \l__spath_draft_bool
5822
    },
5823
    maybe~ spot~ weld/.code={
5824
      \bool_if:NF \l__spath_draft_bool
5825
5826
       \tl_if_exist:cTF
5827
       {\tl_use:N \l_spath_prefix_tl #1 \tl_use:N \l_spath_suffix_tl}
5828
5829
         \spath_spot_weld_components:c
         5831
5832
5833
         \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5834
       }
5835
     }
5836
    },
5837
    maybe~ spot~ weld~ globally/.code={
5838
      \bool_if:NF \l__spath_draft_bool
5839
       \tl_if_exist:cTF
       5843
         \spath_spot_gweld_components:c
5844
         5845
5846
       {
5847
```

```
\msg_warning:nnn { spath3 } { missing soft path } { #1 }
5848
         }
5849
       }
5850
     },
5851
    Set the transformation to lie along a path.
     transform~ to/.code~ 2~ args={
5852
        \group_begin:
5853
        \tl_if_exist:cTF
5854
5855
          \tl_use:N \l__spath_prefix_tl
          #1
5857
          \tl_use:N \l__spath_suffix_tl
5858
       }
5859
5860
          \spath_reallength:Nv
5861
          \l__spath_tmpa_int
5862
            \tl_use:N \l__spath_prefix_tl
            #1
            \tl_use:N \l__spath_suffix_tl
5867
5868
          \tl_set:Nx \l__spath_tmpb_tl
5869
          {\phi: \{(\#2) * (\l_spath_tmpa_int)\}}
5870
          \spath_transformation_at:NvV \l__spath_tmpc_tl
5871
5872
            \tl_use:N \l__spath_prefix_tl
5873
            #1
5874
5875
            \tl_use:N \l__spath_suffix_tl
          }
5876
5877
          \l_spath_tmpb_tl
          \tl_gset_eq:NN \g__spath_smuggle_tl \l__spath_tmpc_tl
5878
       }
5879
5880
          \msg_warning:nnn { spath3 } { missing soft path } { #1 }
5881
          \tl_gset_eq:NN \g__spath_smuggle_tl { {1}{0}{0}{1}{0pt}{0pt} }
5882
5883
        \group_end:
        \exp_last_unbraced:NV \pgfsettransformentries \g__spath_smuggle_tl
        \tl_gclear:N \g__spath_smuggle_tl
     },
```

As above, but with a possible extra 180° rotation if needed to ensure that the new y-axis points vaguely upwards.

```
\spath_reallength:Nv
5897
                                \l_spath_tmpa_int
5898
5899
                                {
                                       \tl_use:N \l__spath_prefix_tl
5900
                                      #1
5901
                                       \tl_use:N \l__spath_suffix_tl
5902
5903
                                \tl_set:Nx \l__spath_tmpb_tl
                                {\fp_to_decimal:n {(#2) * (\l_spath_tmpa_int)}}
                                \spath_transformation_at:NvV \l__spath_tmpc_tl
5908
                                       \tl_use:N \l__spath_prefix_tl
5909
                                      #1
5910
                                       \tl_use:N \l__spath_suffix_tl
5911
5912
                                \l__spath_tmpb_tl
5913
                                \tl_gset_eq:NN \g__spath_smuggle_tl \l__spath_tmpc_tl
5914
                         {
                                \msg_warning:nnn { spath3 } { missing soft path } { #1 }
                                \tl_gset_eq:NN \g__spath_smuggle_tl { {1}{0}{0}{1}{0pt}{0pt} }
5918
5919
                         \label{lem:nt_g_spath_smuggle_tl {4} < 0} $$ \int_{\mathbb{R}^{n}} \int_{\mathbb{R}^{n}} \left\{ \int_
5920
5921
                                \tl_gset:Nx \g__spath_smuggle_tl
5922
5923
                                      { \lceil fp_{eval:n} \ - (\tl_item:Nn \g_spath_smuggle_tl \{1})} }
5924
                                       { \fp_eval:n { - (\tl_item:Nn \g_spath_smuggle_tl {2})} }
5925
                                      { \fp_eval:n { - (\tl_item:\Nn \g_spath_smuggle_tl {3})} }
                                      { fp_eval:n { - (\tl_item:Nn \g_spath_smuggle_tl {4})} }
                                       { \tl_item: Nn \g__spath_smuggle_tl {5} }
5929
                                       { \tl_item: Nn \g_spath_smuggle_tl {6} }
                               }
5930
                        }
5931
                         \group_end:
5932
                         \exp_last_unbraced:NV \pgfsettransformentries \g_spath_smuggle_tl
5933
                         \tl_gclear:N \g__spath_smuggle_tl
5934
5935
             This is a useful set of styles for drawing a knot diagram.
                  knot/.style~ n~ args={3}{
                         spath/split~ at~ self~ intersections=#1,
5937
                         spath/remove~ empty~ components=#1,
5938
                         spath/insert~ gaps~ after~ components={#1}{#2}{#3},
5939
                        spath/maybe~ spot~ weld=#1,
5940
                        spath/render~ components=#1
5941
5942
                 global~ knot/.style~ n~ args={3}{
5943
                         spath/split~ globally~ at~ self~ intersections=#1,
5944
                         spath/remove~ empty~ components~ globally=#1,
                         spath/insert~ gaps~ globally ~after~ components={#1}{#2}{#3},
5947
                        spath/maybe~ spot~ weld~ globally=#1,
                        spath/render~ components=#1
5948
```

```
5950 }
    This defines a coordinate system that finds a position on a soft path.
   \tikzdeclarecoordinatesystem{spath}{%
5951
      \group_begin:
5952
     \tl_set:Nn \l__spath_tmpa_tl {#1}
5953
     \tl_trim_spaces:N \l__spath_tmpa_tl
5954
     \seq_set_split:\nv \l__spath_tmpa_seq {~} \l__spath_tmpa_tl
5956
     \seq_pop_right:NN \l__spath_tmpa_seq \l__spath_tmpb_tl
5957
5958
      \tl_set:Nx \l__spath_tmpa_tl { \seq_use:Nn \l__spath_tmpa_seq {~} }
5959
      \tl_if_exist:cTF
5960
     {
5961
        \tl_use:N \l__spath_prefix_tl
5962
        \tl_use:N \l__spath_tmpa_tl
5963
        \tl_use:N \l__spath_suffix_tl
5964
     }
     {
        \tl_set_eq:Nc
5968
        \l_spath_tmpa_tl
5969
5970
          \tl_use:N \l__spath_prefix_tl
5971
          \tl_use:N \l__spath_tmpa_tl
5972
          \tl_use:N \l__spath_suffix_tl
5973
5974
5975
        \tl_if_empty:NTF \l__spath_tmpa_tl
5977
          \tl_gset_eq:NN \g__spath_smuggle_tl \pgfpointorigin
5978
       }
5979
5980
          \spath_reallength:NV \l__spath_tmpa_int \l__spath_tmpa_tl
5981
          \tl_set:Nx \l__spath_tmpb_tl
5982
          {\fp_to_decimal:n {(\l__spath_tmpb_tl) * (\l__spath_tmpa_int)}}
5983
          \spath_point_at:NVV \l__spath_tmpc_tl \l__spath_tmpa_tl \l__spath_tmpb_tl
5984
          \tl_clear:N \l__spath_tmpd_tl
          \tl_put_right:Nn \l__spath_tmpd_tl {\pgf@x=}
          \tl_put_right:Nx \l__spath_tmpd_tl {\tl_item:Nn \l__spath_tmpc_tl {1}}
          \tl_put_right:Nn \l__spath_tmpd_tl {\relax}
5989
          \tl_put_right:Nn \l__spath_tmpd_tl {\pgf@y=}
5990
          \tl_put_right:Nx \l__spath_tmpd_tl {\tl_item:Nn \l__spath_tmpc_tl {2}}
5991
          \tl_put_right:Nn \l__spath_tmpd_tl {\relax}
5992
          \tl_gset_eq:NN \g__spath_smuggle_tl \l__spath_tmpd_tl
5993
5994
     }
5995
5996
        \msg_warning:nnx
5998
       { spath3 }
        { missing soft path }
5999
        { \tl_use:N \l__spath_tmpa_tl }
6000
```

5949

},

```
6001
6002
    \group_end:
6003
    \use:c {pgf@process}{%
6004
      \tl_use:N \g__spath_smuggle_tl
6005
      \pgftransforminvert
6006
      \use:c {pgf@pos@transform@glob}
6007
6008
6009 }
6010
   \ExplSyntaxOff
```

5 The Calligraphy Package

6012 (@@=cal)

5.1 Initialisation

```
6013 \RequirePackage{spath3}
   \ExplSyntaxOn
6015
6016 \tl_new:N \l__cal_tmpa_tl
_{6017} \tl_new:N \l__cal_tmpb_tl
_{6018} \tl_new:N \l__cal_tmp_path_tl
6019 \tl_new:N \l__cal_tmp_rpath_tl
    \tl_new:N \l__cal_tmp_rpathb_tl
    \tl_new:N \l__cal_tmp_patha_tl
6021
    \verb|\seq_new:N \ll_cal_tmpa_seq| \\
6023
6024
6025 \int_new:N \l__cal_tmpa_int
6026 \int_new:N \l__cal_tmpb_int
6027 \int_new:N \g__cal_path_component_int
   \int_new:N \g__cal_label_int
6028
6029
6030 \fp_new:N \l__cal_tmpa_fp
6031 \fp_new:N \l__cal_tmpb_fp
6032 \fp_new:N \l__cal_tmpc_fp
6033 \fp_new:N \l__cal_tmpd_fp
6034 \fp_new:N \l__cal_tmpe_fp
\label{eq:condition} $$ \dim_new:N \l_cal_tmpa_dim $$
\label{loss_continuous_loss} $$\operatorname{\dim_{new}:N \ l\__cal\_tmpb\_dim}$$
6038 \dim_new:N \l__cal_tmpc_dim
\label{eq:collinear} $$\operatorname{\dim_{new}:N \ l\__{cal\_tmpd\_dim}}$$
6040 \dim_new:N \l__cal_tmpe_dim
   \dim_new:N \l__cal_tmpf_dim
    \dim_new:N \l__cal_tmpg_dim
   \dim_new:N \l__cal_tmph_dim
6045 \bool_new:N \l__cal_annotate_bool
6046 \bool_new:N \l__cal_taper_start_bool
6047 \bool_new:N \l__cal_taper_end_bool
6048 \bool_new:N \l__cal_taperable_bool
```

```
6050 \dim_new:N \l__cal_taper_width_dim
6051 \dim_new:N \l__cal_line_width_dim
6052
6053 \bool_set_true:N \l__cal_taper_start_bool
6054 \bool_set_true:N \l__cal_taper_end_bool
6055
6056 \cs_generate_variant:Nn \tl_put_right:Nn {Nv}
6057
6058 \msg_new:nnn { calligraphy } { undefined pen } { The~ pen~ "#1"~ is~ not~ defined. }
```

5.2 TikZ Keys

The public interface to this package is through TikZ keys and styles.

```
\tikzset{
     define~pen/.code={
        \tikzset{pen~name=#1}
        \pgf@relevantforpicturesizefalse
6062
        \tikz@addmode{
6063
          \pgfsyssoftpath@getcurrentpath\l__cal_tmpa_tl
6064
          \spath_components_to_seq:NV \l__cal_tmpa_seq \l__cal_tmpa_tl
6065
          \seq_gclear_new:c {g__cal_pen_\pgfkeysvalueof{/tikz/pen~name}_seq}
6066
          \seq_gset_eq:cN
6067
          {g_cal_pen_\pgfkeysvalueof{/tikz/pen~name}_seq} \l_cal_tmpa_seq
6068
          \pgfusepath{discard}%
       }
6070
     },
     define~pen/.default={default},
6072
     use~pen/.code={
        \tikzset{pen~name=#1}
        \int_gzero:N \g__cal_path_component_int
6075
        \cs_set_eq:NN \pgfpathmoveto \cal_moveto:n
6076
        \tikz@addmode{
6077
          \pgfsyssoftpath@getcurrentpath\l__cal_tmpa_tl
6078
          \spath_components_to_seq:NV \l__cal_tmpa_seq \l__cal_tmpa_tl
6079
          \tl_if_exist:cTF {g__cal_pen_\pgfkeysvalueof{/tikz/pen~name}_seq}
6080
            \cal_path_create:Nc \l__cal_tmpa_seq
            {g_cal_pen_\pgfkeysvalueof{/tikz/pen~name}_seq}
         }
6084
          {
6085
            \msg_warning:nnx { calligraphy } { undefined pen }
6086
            { \pgfkeysvalueof{/tikz/pen~name} }
6087
6088
       }
6089
     use~pen/.default={default},
6091
     pen~name/.initial={default},
     copperplate/.style={pen~name=copperplate},
     pen~colour/.initial={black},
     weight/.is~choice,
     weight/heavy/.style={
6096
       line~width=\pgfkeysvalueof{/tikz/heavy~line~width},
6097
        taper~width=\pgfkeysvalueof{/tikz/light~line~width},
6098
```

```
},
6099
      weight/light/.style={
6100
        line~width=\pgfkeysvalueof{/tikz/light~line~width},
6101
        taper~width=0pt,
6102
6103
      heavy/.style={
6104
        weight=heavy
6105
6106
      light/.style={
6107
        weight=light
6108
6109
      heavy~line~width/.initial=2pt,
6110
      light~line~width/.initial=1pt,
6111
      taper/.is~choice,
6112
      taper/.default=both,
6113
      taper/none/.style={
6114
        taper~start=false,
6115
        taper~end=false,
6116
6117
      taper/both/.style={
        taper~start=true,
6119
        taper~end=true,
6120
      },
6121
      taper/start/.style={
6122
        taper~start=true,
6123
        taper~end=false,
6124
6125
      taper/end/.style={
6126
        taper~start=false,
6127
6128
        taper~end=true,
      },
6129
      taper~start/.code={
6130
        \tl_if_eq:nnTF {#1} {true}
6131
6132
           \bool_set_true:N \l__cal_taper_start_bool
6133
        }
6134
        {
6135
6136
           \bool_set_false:N \l__cal_taper_start_bool
        }
6137
      taper~start/.default={true},
      taper~end/.code={
        \tl_if_eq:nnTF {#1} {true}
6141
6142
           \bool_set_true:N \l__cal_taper_end_bool
6143
        }
6144
        {
6145
           \bool_set_false:N \l__cal_taper_end_bool
6146
        }
6147
6148
      },
6149
      taper~end/.default={true},
      taper~width/.code={\dim_set:Nn \l__cal_taper_width_dim {#1}},
6150
6151
      nib~style/.code~2~args={
        \tl_clear_new:c {l__cal_nib_style_#1}
6152
```

```
\t \int_{\text{cal_nib_style}_{1}} {\#2}
6153
     },
6154
     stroke~style/.code~2~args={
6155
        \tl_clear_new:c {l__cal_stroke_style_#1}
6156
        \tl_set:cn {l__cal_stroke_style_#1} {#2}
6157
6158
      this~stroke~style/.code={
6159
       \tl_clear_new:c
6160
        {l__cal_stroke_inline_style_ \int_use:N \g__cal_path_component_int}
6161
6162
        \tl_set:cn
        {l__cal_stroke_inline_style_ \int_use:N \g__cal_path_component_int} {#1}
6163
     },
6164
      annotate/.style={
6165
        annotate~if,
6166
        annotate~reset,
6167
        annotation~style/.update~value={#1},
6168
6169
      annotate~if/.default={true},
6170
      annotate~if/.code={
        \tl_if_eq:nnTF {#1} {true}
6173
          \bool_set_true:N \l__cal_annotate_bool
6174
       }
6175
6176
          \bool_set_false:N \l__cal_annotate_bool
6177
       }
6178
     },
6179
      annotate~reset/.code={
6180
       \int_gzero:N \g__cal_label_int
6181
6182
     },
      annotation~style/.initial={draw,->},
6183
      annotation~shift/.initial={(0,1ex)},
6184
      every~annotation~node/.initial={anchor=south~west},
6185
      annotation~node~style/.code~2~args={
6186
        \tl_clear_new:c {l__cal_annotation_style_ #1 _tl}
6187
        \tl_set:cn {l__cal_annotation_style_ #1 _tl}{#2}
6188
     },
6189
      tl~use:N/.code={
6190
6191
        \exp_args:NV \pgfkeysalso #1
     tl~use:c/.code={
        \tl_if_exist:cT {#1}
6195
          \exp_args:Nv \pgfkeysalso {#1}
6196
       }
6197
     },
6198
      /handlers/.update~style/.code={
6199
        \tl_if_eq:nnF {#1} {\pgfkeysnovalue}
6200
        {
6201
          \pgfkeys{\pgfkeyscurrentpath/.code=\pgfkeysalso{#1}}
6202
       }
6204
     },
      /handlers/.update~value/.code={
6205
       \tl_if_eq:nnF {#1} {\pgfkeysnovalue}
6206
```

```
\pgfkeyssetvalue{\pgfkeyscurrentpath}{#1}
6208
6209
      },
6210
6211 }
    Some wrappers around the TikZ keys.
   \NewDocumentCommand \pen { O{} }
   {
6213
      \path[define~ pen,every~ calligraphy~ pen/.try,#1]
6214
6215 }
6216
   \NewDocumentCommand \definepen { O{} }
6217
      \tikz \path[define~ pen,every~ calligraphy~ pen/.try,#1]
6220 }
6221
   \NewDocumentCommand \calligraphy { O{} }
6222
6223
      \path[use~ pen,every~ calligraphy/.try,#1]
6224
6225 }
```

5.3 The Path Creation

\cal_path_create:NN

This is the main command for creating the calligraphic paths. First argument is the given path Second argument is the pen path

```
\cs_new_protected_nopar:Npn \cal_path_create:NN #1#2
6227 {
      \int_zero:N \l__cal_tmpa_int
6228
      \seq_map_inline:Nn #1
6229
6230
        \int_compare:nT {\tl_count:n {##1} > 3}
6231
6232
6233
          \int_incr:N \l__cal_tmpa_int
6234
          \int_zero:N \l__cal_tmpb_int
6235
6236
          \tl_set:Nn \l__cal_tmp_path_tl {##1}
          \spath_open:N \l__cal_tmp_path_tl
          \spath_reverse:NV \l__cal_tmp_rpath_tl \l__cal_tmp_path_tl
6239
6240
          \seq_map_inline:Nn #2
6241
6242
            \int_incr:N \l__cal_tmpb_int
6243
            \group_begin:
6244
            \pgfsys@beginscope
6245
            \cal_apply_style:c {l__cal_stroke_style_ \int_use:N \l__cal_tmpa_int}
6246
            \cal_apply_style:c {l__cal_stroke_inline_style_ \int_use:N \l__cal_tmpa_int}
6247
            \cal_apply_style:c {l__cal_nib_style_ \int_use:N \l__cal_tmpb_int}
            \spath_initialpoint:Nn \l__cal_tmpa_tl {###1}
            \tl_set_eq:NN \l__cal_tmp_patha_tl \l__cal_tmp_path_tl
6251
            \spath_translate:NV \l__cal_tmp_patha_tl \l__cal_tmpa_tl
6252
6253
```

```
\int \int \int dt dt dt = 3
           {
6255
             \cal_at_least_three:N \l__cal_tmp_patha_tl
6256
             \spath_protocol_path:V \l__cal_tmp_patha_tl
6257
6258
             \tikz@options
6259
             \dim_set:Nn \l__cal_line_width_dim {\pgflinewidth}
6260
             \cal_maybe_taper:N \l__cal_tmp_patha_tl
           }
             \spath_weld:\n\\l__cal_tmp_patha_tl \{###1\}
             \spath_weld:NV \l__cal_tmp_patha_tl \l__cal_tmp_rpath_tl
6265
             \spath_reverse:Nn \l__cal_tmp_rpathb_tl {###1}
6266
             \spath_weld:NV \l__cal_tmp_patha_tl \l__cal_tmp_rpathb_tl
6267
6268
             \tl_clear:N \l__cal_tmpa_tl
6269
             \tl_set:Nn \l__cal_tmpa_tl
6270
6271
               fill=\pgfkeysvalueof{/tikz/pen~colour},
               draw=none
             }
             \tl_if_exist:cT {l__cal_stroke_style_\int_use:N \l__cal_tmpa_int}
6275
             ł
               \tl_put_right:Nv \l__cal_tmpa_tl
6277
               6278
             }
6279
             \tl_if_exist:cT {l__cal_stroke_inline_style_ \int_use:N \l__cal_tmpa_int}
6280
6281
             {
               \tl_put_right:Nn \l__cal_tmpa_tl {,}
6282
               \tl_put_right:Nv \l__cal_tmpa_tl
               {l__cal_stroke_inline_style_ \int_use:N \l__cal_tmpa_int}
             }
6286
             \tl_if_exist:cT {l__cal_nib_style_ \int_use:N \l__cal_tmpb_int}
             {
6287
               \tl_put_right:Nn \l__cal_tmpa_tl {,}
6288
               \tl_put_right:Nv \l__cal_tmpa_tl
6289
               {l__cal_nib_style_ \int_use:N \l__cal_tmpb_int}
6290
6291
6292
             \spath_tikz_path: VV \l__cal_tmpa_tl \l__cal_tmp_patha_tl
           }
           \pgfsys@endscope
           \group_end:
6296
6297
         \bool_if:NT \l__cal_annotate_bool
         {
6299
           \seq_get_right:NN #2 \l__cal_tmpa_tl
6300
           \spath_finalpoint:NV \l__cal_tmpa_tl \l__cal_tmpa_tl
6301
           \spath_translate:NV \l__cal_tmp_path_tl \l__cal_tmpa_tl
6302
           \tikz@scan@one@point
6303
           \pgfutil@firstofone
           \pgfkeysvalueof{/tikz/annotation~shift}
6306
           \spath_translate:Nnn \l__cal_tmp_path_tl {\pgf@x} {\pgf@y}
6307
```

```
\pgfkeysgetvalue{/tikz/annotation~style}{\l__cal_tmpa_tl}
                           6309
                                       \spath_tikz_path:\VV \l__cal_tmpa_tl \l__cal_tmp_path_tl
                           6310
                           6311
                                       \spath_finalpoint:NV \l__cal_tmpa_tl \l__cal_tmp_path_tl
                           6312
                           6313
                                       \exp_last_unbraced:NV \pgfqpoint \l__cal_tmpa_tl
                           6314
                                       \begin{scope}[reset~ cm]
                           6315
                                       \node[
                                         every~annotation~node/.try,
                           6317
                                         tl~use:c = {l__cal_annotation_style_ \int_use:N \l__cal_tmpa_int _tl}
                           6318
                                       ] at (\pgf@x,\pgf@y) {\int_use:N \l__cal_tmpa_int};
                           6319
                                       \end{scope}
                           6320
                           6321
                           6322
                           6323
                           6324 }
                              \cs_generate_variant:Nn \cal_path_create:NN {Nc}
                          (End definition for \cal_path_create:NN.)
                          When creating the path, we need to keep track of the number of components so that we
         \cal_moveto:n
                          can apply styles accordingly.
                           6326 \cs_new_eq:NN \cal_orig_moveto:n \pgfpathmoveto
                              \cs_new_nopar:Npn \cal_moveto:n #1
                           6328 {
                                 \int_gincr:N \g__cal_path_component_int
                           6329
                                 \cal_orig_moveto:n {#1}
                           6330
                          6331 }
                          (End definition for \cal_moveto:n.)
                         Interface for applying \tikzset to a token list.
    \cal_apply_style:N
                           6332 \cs_new_nopar:Npn \cal_apply_style:N #1
                           6333 {
                           6334
                                 \tl_if_exist:NT #1 {
                                   \exp_args:NV \tikzset #1
                           6335
                           6336
                           6337
                           6338 \cs_generate_variant:Nn \cal_apply_style:N {c}
                          (End\ definition\ for\ \verb|\cal_apply_style:N.|)
\cal_at_least_three:Nn
                          A tapered path has to have at least three components. This figures out if it is necessary
                          and sets up the splitting.
                              \cs_new_protected_nopar:Npn \cal_at_least_three:Nn #1#2
                           6339
                           6340
                                 \spath_reallength:Nn \l__cal_tmpa_int {#2}
                           6341
                                 \tl_clear:N \l__cal_tmpb_tl
                           6342
                                 \tl_set:Nn \l__cal_tmpb_tl {#2}
                                 \int_compare:nTF {\l__cal_tmpa_int = 1}
                           6344
                           6345
                                   \spath_split_at:Nn \l__cal_tmpb_tl {2/3}
                           6346
                                   \spath_split_at:Nn \l__cal_tmpb_tl {1/2}
                           6347
                           6348
```

6308

```
6349
                           \int_compare:nT {\l__cal_tmpa_int = 2}
                    6350
                    6351
                             \spath_split_at:Nn \l__cal_tmpb_tl {1.5}
                    6352
                             \spath_split_at:Nn \l__cal_tmpb_tl {.5}
                    6353
                    6354
                    6355
                         \tl_set_eq:NN #1 \l__cal_tmpb_tl
                    6356
                       \cs_generate_variant:Nn \cal_at_least_three:Nn {NV}
                        \cs_new_protected_nopar:Npn \cal_at_least_three:N #1
                    6360
                         \cal_at_least_three:NV #1#1
                    6361
                    6362 }
                       \cs_generate_variant:Nn \cal_at_least_three:N {c}
                   (End definition for \cal_at_least_three:Nn.)
\cal_maybe_taper:N
                   Possibly tapers the path, depending on the booleans.
                       \cs_new_protected_nopar:Npn \cal_maybe_taper:N #1
                    6364
                    6365
                       {
                         \tl_set_eq:NN \l__cal_tmpa_tl #1
                    6366
                    6367
                         \bool_if:NT \l__cal_taper_start_bool
                    6368
                    6370
                           \dim_set:Nn \l__cal_tmpa_dim {\tl_item:Nn \l__cal_tmpa_t1 {2}}
                    6371
                           \dim_set:Nn \l__cal_tmpb_dim {\tl_item:Nn \l__cal_tmpa_t1 {3}}
                    6372
                           \tl_set:Nx \l__cal_tmpb_tl {\tl_item:Nn \l__cal_tmpa_tl {4}}
                    6373
                    6374
                           \tl_case:NnF \l__cal_tmpb_tl
                    6375
                    6376
                             \c_spath_lineto_tl
                    6377
                    6378
                               \bool_set_true:N \l__cal_taperable_bool
                               \dim_set:Nn \l__cal_tmpg_dim {\tl_item:Nn \l__cal_tmpa_tl {5}}
                               \dim_set:Nn \l__cal_tmph_dim {\tl_item:Nn \l__cal_tmpa_tl {6}}
                    6382
                               6383
                               6384
                               \dim_set:Nn \l__cal_tmpe_dim {(\l__cal_tmpa_dim + 2\l__cal_tmpg_dim)/3}
                    6385
                               \dim_set:Nn \l__cal_tmpf_dim {(\l__cal_tmpb_dim + 2\l__cal_tmph_dim)/3}
                    6386
                               \prg_replicate:nn {4}
                    6387
                    6388
                                 \tl_set:Nx \l__cal_tmpa_tl {\tl_tail:N \l__cal_tmpa_tl}
                    6389
                               }
                               \tl_put_left:NV \l__cal_tmpa_tl \c_spath_moveto_tl
                    6391
                             }
                    6392
                    6393
                             \c_spath_curvetoa_tl
                    6394
                               \bool_set_true:N \l__cal_taperable_bool
                    6395
                               \dim_set:Nn \l__cal_tmpc_dim {\tl_item:Nn \l__cal_tmpa_tl {5}}
                    6396
                               \dim_set:Nn \l__cal_tmpd_dim {\tl_item:Nn \l__cal_tmpa_tl {6}}
                    6397
                               \dim_set:Nn \l__cal_tmpe_dim {\tl_item:Nn \l__cal_tmpa_tl {8}}
```

```
\dim_set:Nn \l__cal_tmpf_dim {\tl_item:Nn \l__cal_tmpa_tl {9}}
           6400
           \dim_set:Nn \l__cal_tmph_dim {\tl_item:Nn \l__cal_tmpa_tl {12}}
6401
           \prg_replicate:nn {10}
6402
6403
             \tl_set:Nx \l__cal_tmpa_tl {\tl_tail:N \l__cal_tmpa_tl}
           }
           \tl_put_left:NV \l__cal_tmpa_tl \c_spath_moveto_tl
         }
       }
       {
         \bool_set_false:N \l__cal_taperable_bool
6410
6411
6412
       \bool_if:NT \l__cal_taperable_bool
6413
6414
          \__cal_taper_aux:
6415
6416
     }
6418
     \bool_if:NT \l__cal_taper_end_bool
6420
6421
6422
       \dim_set:Nn \l__cal_tmpa_dim {\tl_item:Nn \l__cal_tmpa_tl {-2}}
6423
       \dim_set:Nn \l__cal_tmpb_dim {\tl_item:Nn \l__cal_tmpa_tl {-1}}
6424
       \tl_set:Nx \l__cal_tmpb_tl {\tl_item:Nn \l__cal_tmpa_tl {-3}}
6425
6426
       \tl_case:NnF \l__cal_tmpb_tl
6427
6429
         \c_spath_lineto_tl
6430
         {
6431
           \verb|\bool_set_true:N \ll_cal_taperable_bool|
6432
           \dim_set:Nn \l__cal_tmpg_dim {\tl_item:Nn \l__cal_tmpa_tl {-5}}
6433
           \dim_set:Nn \l__cal_tmph_dim {\tl_item:Nn \l__cal_tmpa_tl {-4}}
6434
           \dim_set:Nn \l__cal_tmpc_dim {(2\l__cal_tmpa_dim + \l__cal_tmpg_dim)/3}
6435
           6436
6437
           \dim_set:Nn \l__cal_tmpe_dim {(\l__cal_tmpa_dim + 2\l__cal_tmpg_dim)/3}
           \dim_set:Nn \l__cal_tmpf_dim {(\l__cal_tmpb_dim + 2\l__cal_tmph_dim)/3}
           \tl_reverse:N \l__cal_tmpa_tl
           \prg_replicate:nn {3}
6441
             \tl_set:Nx \l__cal_tmpa_tl {\tl_tail:N \l__cal_tmpa_tl}
6442
6443
           \tl_reverse:N \l__cal_tmpa_tl
6444
6445
         \c_spath_curveto_tl
6446
6447
           \bool_set_true:N \l__cal_taperable_bool
           \label{lem:nn local_tmpc_dim { l_item:Nn l_cal_tmpa_tl {-5}} } $$ \dim_{set:Nn l_cal_tmpa_tl {-5}} $$
           \dim_set:Nn \l__cal_tmpd_dim {\tl_item:Nn \l__cal_tmpa_tl {-4}}
6451
           \dim_set:Nn \l__cal_tmpe_dim {\tl_item:Nn \l__cal_tmpa_tl {-8}}
           \dim_set:Nn \l__cal_tmpf_dim {\tl_item:Nn \l__cal_tmpa_tl {-7}}
6452
```

```
\label{lem:Nn l_cal_tmph_dim { l_cal_tmpa_tl {-10}}} $$ \dim_{\mathbb{N}^n \ l_cal_tmpa_tl {-10}} $$
                       6454
                                    \tl_reverse:N \l__cal_tmpa_tl
                       6455
                                    \prg_replicate:nn {9}
                       6456
                       6457
                                       \tl_set:Nx \l__cal_tmpa_tl {\tl_tail:N \l__cal_tmpa_tl}
                       6458
                                    }
                                    \tl_reverse:N \l__cal_tmpa_tl
                                  }
                               }
                       6462
                               {
                                  \bool_set_false:N \l__cal_taperable_bool
                       6464
                       6465
                       6466
                               \bool_if:NT \l__cal_taperable_bool
                       6467
                       6468
                                  \_\_cal_taper_aux:
                       6469
                       6470
                             }
                       6472
                             \pgfsyssoftpath@setcurrentpath\l__cal_tmpa_tl
                       6474
                             \pgfsetstrokecolor{\pgfkeysvalueof{/tikz/pen~colour}}
                       6475
                             \pgfusepath{stroke}
                       6476
                       6477
                      6478 }
                      (End definition for \cal_maybe_taper:N.)
                      Auxiliary macro to avoid unnecessary code duplication.
\__cal_taper_aux:
                       6479 \cs_new_protected_nopar:Npn \__cal_taper_aux:
                       6480
                       6481
                             \tl_clear:N \l__cal_tmpb_tl
                       6482
                             \tl_put_right:NV \l__cal_tmpb_tl \c_spath_moveto_tl
                             \fp_set:Nn \l__cal_tmpa_fp
                               \label{local_tmpd_dim - l_cal_tmpb_dim} $$ l_cal_tmpb_dim - l_cal_tmpb_dim $$
                       6486
                       6487
                             \fp_set:Nn \l__cal_tmpb_fp
                       6488
                       6489
                               \l__cal_tmpa_dim - \l__cal_tmpc_dim
                       6490
                       6491
                             \fp_set:Nn \l__cal_tmpe_fp
                               (\l_cal_tmpa_fp^2 + \l_cal_tmpb_fp^2)^.5
                       6495
                       6496
                       6497
                             \fp_set:Nn \l__cal_tmpa_fp
                       6498
                               .5*\l_cal_taper_width_dim
                       6499
                       6500
                               \l__cal_tmpa_fp / \l__cal_tmpe_fp
                       6501
                       6502
```

6453

```
6503
    \fp_set:Nn \l__cal_tmpb_fp
6504
      .5*\l_cal_taper_width_dim
6505
6506
      \l__cal_tmpb_fp / \l__cal_tmpe_fp
6507
6508
6509
    \fp_set:Nn \l__cal_tmpc_fp
6510
6511
      \l__cal_tmph_dim - \l__cal_tmpf_dim
6512
6513
    \fp_set:Nn \l__cal_tmpd_fp
6514
6515
      \l__cal_tmpe_dim - \l__cal_tmpg_dim
6516
6517
    \fp_set:Nn \l__cal_tmpe_fp
6518
6519
      (\l_cal_tmpc_fp^2 + \l_cal_tmpd_fp^2)^.5
6520
6521
6523
    \fp_set:Nn \l__cal_tmpc_fp
6524
      .5*\\ \label{line_width_dim} \\
6525
6526
      \l__cal_tmpc_fp / \l__cal_tmpe_fp
6527
6528
    \fp_set:Nn \l__cal_tmpd_fp
6529
6530
      .5*\l__cal_line_width_dim
6531
6532
      \l__cal_tmpd_fp / \l__cal_tmpe_fp
6533
    }
6534
6535
    \tl_put_right:Nx \l__cal_tmpb_tl
6536
6537
      6538
      6539
6540
6541
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetoa_tl
6544
    \tl_put_right:Nx \l__cal_tmpb_tl
6545
      6546
      6547
6548
6549
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetob_tl
6550
6551
6552
    \tl_put_right:Nx \l__cal_tmpb_tl
6553
6554
      {\dim_eval:n { \fp_to_dim:N \l__cal_tmpc_fp + \l__cal_tmpe_dim}}
      6555
    }
6556
```

```
6557
      \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curveto_tl
6558
6559
      \tl_put_right:Nx \l__cal_tmpb_tl
6560
6561
        {\dim_eval:n { \fp_to_dim:N \l__cal_tmpc_fp + \l__cal_tmpg_dim}}
6562
        {\dim_eval:n { \fp_to_dim:N \l__cal_tmpd_fp + \l__cal_tmph_dim}}
6563
6564
      \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetoa_tl
6566
6567
      \tl_put_right:Nx \l__cal_tmpb_tl
6568
      {
6569
        {
6570
           \dim_eval:n
6571
6572
             \fp_to_dim:N \l__cal_tmpc_fp + \l__cal_tmpg_dim
6573
             - \fp_to_dim:n{ 1.32 * \l__cal_tmpd_fp
          }
        }
6577
6578
           \dim_eval:n
6579
6580
             \label{lem:norm} $$ \int_{-\infty}^{\infty}  \| \cdot \|_{-\infty} + \left\| - \right\|_{+\infty} dim . $$
6581
             + \fp_to_dim:n {1.32* \l__cal_tmpc_fp
6582
6583
6584
        }
6585
      }
6587
      \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetob_tl
6588
6589
      \tl_put_right:Nx \l__cal_tmpb_tl
6590
      {
6591
        {
6592
           \dim_eval:n
6593
6594
             -\fp_to_dim:N \l__cal_tmpc_fp + \l__cal_tmpg_dim
6595
             - fp_to_dim:n {1.32 * \l_cal_tmpd_fp}
          }
        }
6599
        {
6600
           \dim_eval:n
6601
6602
             -\fp_to_dim:N \l__cal_tmpd_fp + \l__cal_tmph_dim
6603
             + \fp_to_dim:n {1.32 * \l__cal_tmpc_fp
6604
6605
6606
        }
      }
6608
6609
      \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curveto_tl
```

```
6611
    \tl_put_right:Nx \l__cal_tmpb_tl
6612
6613
      {\dim_eval:n { -\fp_to_dim:N \l__cal_tmpc_fp + \l__cal_tmpg_dim}}
6614
      {\dim_eval:n { -\fp_to_dim:N \l__cal_tmpd_fp + \l__cal_tmph_dim}}
6615
6616
6617
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetoa_tl
6618
6619
    \tl_put_right:Nx \l__cal_tmpb_tl
6620
6621
      6622
      6623
6624
6625
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetob_tl
6626
6627
    \tl_put_right:Nx \l__cal_tmpb_tl
6628
      6631
6632
6633
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curveto_tl
6634
6635
    \tl_put_right:Nx \l__cal_tmpb_tl
6636
6637
      6638
      {\dim_eval:n { -\fp_to_dim:N \l__cal_tmpb_fp + \l__cal_tmpb_dim}}
6639
    }
6640
6641
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetoa_tl
6642
6643
    \tl_put_right:Nx \l__cal_tmpb_tl
6644
    {
6645
      {
6646
        \dim_eval:n
6647
6648
6649
         -\fp_to_dim:N \l__cal_tmpa_fp + \l__cal_tmpa_dim
         + \fp_to_dim:n{ 1.32 * \l__cal_tmpb_fp}
6652
      }
      {
6653
        \dim_eval:n
6654
6655
         -\fp_to_dim:N \l__cal_tmpb_fp + \l__cal_tmpb_dim
6656
          - \fp_to_dim:n {1.32* \l__cal_tmpa_fp}
6657
6658
     }
6659
6660
    }
6662
    \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curvetob_tl
6663
    \tl_put_right:Nx \l__cal_tmpb_tl
6664
```

```
{
                6665
                6666
                         \dim_eval:n
                6667
                        {
                6668
                          \fp_to_dim:N \l__cal_tmpa_fp + \l__cal_tmpa_dim
                6669
                          + \fp_to_dim:n {1.32 * \l__cal_tmpb_fp}
                6670
                6671
                       }
                6672
                       {
                         \dim_eval:n
                6674
                6675
                          \fp_to_dim:N \l__cal_tmpb_fp + \l__cal_tmpb_dim
                6676
                          - \fp_to_dim:n {1.32 * \l__cal_tmpa_fp}
                6677
                6678
                6679
                6680
                6681
                     \tl_put_right:NV \l__cal_tmpb_tl \c_spath_curveto_tl
                6682
                     \tl_put_right:Nx \l__cal_tmpb_tl
                       6686
                       6687
                6688
                6689
                     \pgfsyssoftpath@setcurrentpath\l__cal_tmpb_tl
                6690
                     \pgfsetfillcolor{\pgfkeysvalueof{/tikz/pen~colour}}
                6691
                     \pgfusepath{fill}
                6692
                6693 }
                (End\ definition\ for\ \_\_cal\_taper\_aux:.)
                   Defines a copperplate pen.
                6695 \spath_components_to_seq:NV \l__cal_tmpa_seq \l__cal_tmpa_tl
                6697 \seq_gset_eq:NN \g__cal_pen_copperplate_seq \l__cal_tmpa_seq
               This is used in the decorations section to convert a path to a copperplate path.
\CopperplatePath
                   \DeclareDocumentCommand \CopperplatePath { m }
                6699 {
                     \spath_components_to_seq:NV \l__cal_tmpa_seq #1
                6700
                     \cal_path_create:NN \l__cal_tmpa_seq \g__cal_pen_copperplate_seq
                6701
                6702 }
                (End definition for \CopperplatePath.)
                6703 \ExplSyntaxOff
```

5.4 Decorations

If a decoration library is loaded we define some decorations that use the calligraphy library, specifically the copperplate pen with its tapering.

First, a brace decoration.

 ${\tt 6704 \ \ \ \ } expandafter \verb|\ \ \ | pgfdeclaredecoration \verb|\ \ \ \ | relax$

```
\else
   \pgfdeclaredecoration{calligraphic brace}{brace}%
   {%
      \state{brace}[width=+\pgfdecoratedremainingdistance,next state=final]%
6708
6709
        \pgfsyssoftpath@setcurrentpath{\pgfutil@empty}%
6710
        \pgfpathmoveto{\pgfpointorigin}%
6711
        \pgfpathcurveto%
6712
        {%
          \pgfqpoint%
          {.15\pgfdecorationsegmentamplitude}%
          {.3\pgfdecorationsegmentamplitude}%
6716
        }%
6717
        {%
6718
          \pgfqpoint%
6719
          {.5\pgfdecorationsegmentamplitude}%
6720
          {.5\pgfdecorationsegmentamplitude}%
6721
       }%
6722
        {%
          \pgfqpoint%
          {\pgfdecorationsegmentamplitude}%
          {.5\pgfdecorationsegmentamplitude}%
       }%
6727
        {%
6728
          \pgftransformxshift%
6729
          {+\pgfdecorationsegmentaspect\pgfdecoratedremainingdistance}%
6730
          \pgfpathlineto%
6731
          {%
6732
            \pgfqpoint%
6733
            {-\pgfdecorationsegmentamplitude}%
            {.5\pgfdecorationsegmentamplitude}%
          }%
6737
          \pgfpathcurveto
          {%
6738
            \pgfqpoint%
6739
            {-.5\pgfdecorationsegmentamplitude}%
6740
            {.5\pgfdecorationsegmentamplitude}%
6741
          }%
6742
6743
          {%
            \pgfqpoint%
            {-.15\pgfdecorationsegmentamplitude}%
            {.7\pgfdecorationsegmentamplitude}%
         }%
6747
          {%
6748
            \pgfqpoint%
6749
            {0\pgfdecorationsegmentamplitude}%
6750
            {1\pgfdecorationsegmentamplitude}%
6751
          }%
6752
          \pgfpathmoveto%
6753
          {%
            \pgfqpoint%
            {0\pgfdecorationsegmentamplitude}%
6757
            {1\pgfdecorationsegmentamplitude}%
          }%
6758
```

```
\pgfpathcurveto%
6759
          {%
6760
             \pgfqpoint%
6761
             {.15\pgfdecorationsegmentamplitude}%
6762
             {.7\pgfdecorationsegmentamplitude}%
6763
          }%
6764
          {%
6765
             \pgfqpoint%
             {.5\pgfdecorationsegmentamplitude}%
             {.5\pgfdecorationsegmentamplitude}%
          }%
          {%
6770
             \pgfqpoint%
6771
             {\pgfdecorationsegmentamplitude}%
6772
             {.5\pgfdecorationsegmentamplitude}%
6773
          }%
6774
        }%
6775
        {%
          \pgftransformxshift{+\pgfdecoratedremainingdistance}%
           \pgfpathlineto%
          {%
             \pgfqpoint%
6780
             {-\pgfdecorationsegmentamplitude}%
6781
             {.5\pgfdecorationsegmentamplitude}%
6782
          }%
6783
          \pgfpathcurveto%
6784
          {%
6785
             \pgfqpoint%
6786
             {-.5\pgfdecorationsegmentamplitude}%
6787
             {.5\pgfdecorationsegmentamplitude}%
          }%
          {%
             \pgfqpoint%
6791
             {-.15\pgfdecorationsegmentamplitude}%
6792
             {.3\pgfdecorationsegmentamplitude}%
6793
          }%
6794
          {\bf \{pgfqpoint\{0pt\}\{0pt\}\}\%}
6795
        }%
6796
        \tikzset{%
          taper width=.5\pgflinewidth,%
          taper%
        \pgfsyssoftpath@getcurrentpath\cal@tmp@path%
        \CopperplatePath{\cal@tmp@path}%
      }%
      \state{final}{}%
6804
6805 }%
    The second is a straightened parenthesis (so that when very large it doesn't bow out
too far).
    \pgfdeclaredecoration{calligraphic straight parenthesis}{brace}
    {
6807
      \state{brace}[width=+\pgfdecoratedremainingdistance,next state=final]%
6808
      {%
6809
```

```
\pgfsyssoftpath@setcurrentpath{\pgfutil@empty}%
6810
        \pgfpathmoveto{\pgfpointorigin}%
6811
        \pgfpathcurveto%
6812
        {%
6813
           \pgfqpoint%
6814
          {.76604\pgfdecorationsegmentamplitude}%
6815
          {.64279\pgfdecorationsegmentamplitude}%
6816
        }%
6817
        {%
           \pgfqpoint%
6819
          {2.3333\pgfdecorationsegmentamplitude}%
          {\pgfdecorationsegmentamplitude}%
6821
        }%
6822
        {%
6823
           \pgfqpoint%
6824
          {3.333}pgfdecorationsegmentamplitude}%
6825
          {\pgfdecorationsegmentamplitude}%
6826
        }%
6827
        {%
           \pgftransformxshift{+\pgfdecoratedremainingdistance}%
           \pgfpathlineto%
          {%
6831
             \pgfqpoint%
6832
             {-3.3333\pgfdecorationsegmentamplitude}%
6833
             {\tt \{pgfdecorationsegmentamplitude\}\%}
6834
          }%
6835
           \pgfpathcurveto%
6836
          {%
6837
             \pgfqpoint%
6838
             {-2.3333\pgfdecorationsegmentamplitude}%
             {\pgfdecorationsegmentamplitude}%
6840
          }%
6841
          {%
6842
             \pgfqpoint%
6843
             {-.76604\pgfdecorationsegmentamplitude}%
6844
             {.64279\pgfdecorationsegmentamplitude}%
6845
          }%
6846
          {\pgfqpoint{0pt}{0pt}}%
6847
        }%
        \tikzset{%
          taper width=.5\pgflinewidth,%
          taper%
        }%
6852
        \pgfsyssoftpath@getcurrentpath\cal@tmp@path%
6853
        \CopperplatePath{\cal@tmp@path}%
6854
      }%
6855
      \state{final}{}% \label{final}{}% \label{final}% \label{final}%
6856
6857
    The third is a curved parenthesis.
    \pgfdeclaredecoration{calligraphic curved parenthesis}{brace}
6859
      \state{brace}[width=+\pgfdecoratedremainingdistance,next state=final]%
6860
      {%
6861
        \pgfsyssoftpath@setcurrentpath{\pgfutil@empty}%
6862
```

```
\pgfpathmoveto{\pgfpointorigin}%
        \pgf@xa=\pgfdecoratedremainingdistance\relax%
        \advance\pgf@xa by -1.5890\pgfdecorationsegmentamplitude\relax%
        \edef\cgrphy@xa{\the\pgf@xa}%
6866
        \pgfpathcurveto%
6867
        {%
6868
           \pgfqpoint%
6869
          {1.5890\pgfdecorationsegmentamplitude}%
          {\tt \{1.3333 \backslash pgfdecorationsegmentamplitude\}\%}
6872
        {\pgfqpoint{\cgrphy@xa}{1.3333\pgfdecorationsegmentamplitude}}%
        \pgfqpoint{\pgfdecorated remaining distance}{0pt}}\%
6874
        \tikzset{%
6875
          taper width=.5\pgflinewidth,%
6876
          taper%
6877
6878
        \pgfsyssoftpath@getcurrentpath\cal@tmp@path%
        \CopperplatePath{\cal@tmp@path}%
      \state{final}{}%
6883 }
End the conditional for if pgfdecoration module is loaded
```

6 Drawing Knots

6885 (@@=knot)

6884 \fi

6.1 Initialisation

We load the spath3 library and the intersections TikZ library. Then we get going.

```
\RequirePackage{spath3}
   \usetikzlibrary{intersections,spath3}
6887
6888
   \ExplSyntaxOn
6889
6890
6891 \tl_new:N \l__knot_tmpa_tl
6892 \tl_new:N \l__knot_tmpb_tl
6894 \tl_new:N \l__knot_tmpd_tl
6895 \tl_new:N \l__knot_tmpg_tl
6896 \tl_new:N \l__knot_redraws_tl
6897 \tl_new:N \l__knot_clip_width_tl
6898 \tl_new:N \l__knot_name_tl
6899 \tl_new:N \l__knot_node_tl
6900 \tl_new:N \l__knot_aux_tl
   \tl_new:N \l__knot_auxa_tl
   \tl_new:N \l__knot_prefix_tl
   \seq_new:N \l__knot_segments_seq
6906 \int_new:N \l__knot_tmpa_int
6907 \int_new:N \l__knot_strands_int
```

```
\int_new:N \g__knot_intersections_int
   \int_new:N \g__knot_filaments_int
   \int_new:N \l__knot_component_start_int
6910
6911
   \fp_new:N \l__knot_tmpa_fp
6912
   \fp_new:N \l__knot_tmpb_fp
6913
6914
   \dim_new:N \l__knot_tmpa_dim
   \dim_new:N \l__knot_tmpb_dim
   \dim_new:N \l__knot_tolerance_dim
   \dim_new:N \l__knot_redraw_tolerance_dim
   \dim_new:N \l__knot_clip_bg_radius_dim
   \dim_new:N \l__knot_clip_draw_radius_dim
6920
6921
   \bool_new:N \l__knot_draft_bool
6922
   \bool_new:N \l__knot_ignore_ends_bool
6923
   \bool_new:N \l__knot_self_intersections_bool
   \bool_new:N \l__knot_splits_bool
   \bool_new:N \l__knot_super_draft_bool
   \bool_new:N \l__knot_prepend_prev_bool
   \bool_new:N \l__knot_append_next_bool
   \bool_new:N \l__knot_skip_bool
6930
   \bool_new:N \l__knot_save_bool
6931
6932
6933
   \seq_new:N \g_knot_nodes_seq
6934
   \bool_set_true:N \l__knot_ignore_ends_bool
    Configuration is via TikZ keys and styles.
   \tikzset{
6936
     spath/prefix/knot/.style={
6937
        spath/set~ prefix=knot strand,
6938
6939
     spath/suffix/knot/.style={
6940
       spath/set~ suffix={},
6941
6942
     knot/.code={
        \tl_if_eq:nnTF {#1} {none}
6945
          \tikz@addmode{\tikz@mode@doublefalse}
6946
       }
6947
6948
          \tikz@addmode{\tikz@mode@doubletrue}
6949
          \tl_if_eq:nnTF {\pgfkeysnovalue} {#1}
6950
6951
            \tikz@addoption{\pgfsetinnerstrokecolor{.}}
6952
            \pgfsetinnerstrokecolor{#1}
          }
6956
          \tikz@addoption{
6957
            \pgfsetstrokecolor{knotbg}
6958
6959
          \tl_set:Nn \tikz@double@setup{
6960
```

```
\pgfsetinnerlinewidth{\pgflinewidth}
6961
            \label{linewidth} $$  \pgfsetlinewidth{\dim_eval:n {\tl_use:N \l_knot_gap_tl \pgflinewidth}} $$
6962
6963
       }
6964
     },
6965
     knot~ gap/.store~ in=\l_knot_gap_tl,
6966
     knot~ gap=3,
6967
     knot~ diagram/.is~family,
6968
     knot~ diagram/.unknown/.code={
        \tl_set_eq:NN \l__knot_tmpa_tl \pgfkeyscurrentname
6971
        \pgfkeysalso{
          /tikz/\l_knot_tmpa_tl=#1
6972
6973
     },
6974
      background~ colour/.code={%
6975
        \colorlet{knotbg}{#1}%
6976
6977
      background~ color/.code={%
6978
        \colorlet{knotbg}{#1}%
     },
      background~ colour=white,
     knot~ diagram,
6982
     name/.store~ in=\l__knot_name_tl,
6983
     name={knot},
6984
      save~ intersections/.is~ choice,
6985
      save~ intersections/.default=true,
6986
      save~ intersections/true/.code={
6987
        \bool_set_true: N \l__knot_save_bool
6988
6989
      save~ intersections/false/.code={
6991
       \bool_set_false:N \l__knot_save_bool
6992
     },
6993
      every~ strand/.style={draw},
      ignore~ endpoint~ intersections/.code={
6994
        \tl_if_eq:nnTF {#1} {true}
6995
6996
          \bool_set_true:N \l__knot_ignore_ends_bool
6997
6998
6999
        {
          \bool_set_false:N \l__knot_ignore_ends_bool
       }
7003
      ignore~ endpoint~ intersections/.default=true,
      consider~ self~ intersections/.is~choice,
7004
      consider~ self~ intersections/true/.code={
7005
        \bool_set_true:N \l__knot_self_intersections_bool
7006
        \bool_set_true:N \l__knot_splits_bool
7007
     },
7008
      consider~ self~ intersections/false/.code={
7009
7010
        \bool_set_false:N \l__knot_self_intersections_bool
7011
        \bool_set_false:N \l__knot_splits_bool
7012
     },
      consider~ self~ intersections/no~ splits/.code={
7013
        \bool_set_true: N \l__knot_self_intersections_bool
7014
```

```
\bool_set_false:N \l__knot_splits_bool
7015
     },
7016
     consider~ self~ intersections/.default={true},
7017
     clip~ radius/.code={
7018
        \dim_set:Nn \l__knot_clip_bg_radius_dim {#1}
7019
        \dim_set:Nn \l__knot_clip_draw_radius_dim {#1+2pt}
7020
7021
      clip~ draw~ radius/.code={
7022
       \dim_set:Nn \l__knot_clip_draw_radius_dim {#1}
7023
7024
      clip~ background~ radius/.code={
7025
        \dim_set:Nn \l__knot_clip_bg_radius_dim {#1}
7026
7027
      clip~ radius=10pt,
7028
      end~ tolerance/.code={
7029
        \dim_set:Nn \l__knot_tolerance_dim {#1}
7030
7031
      end~ tolerance=14pt,
7032
      clip/.style={
7033
       clip
7034
      },
7035
      background~ clip/.style={
7036
7037
        clip
     },
7038
      clip~ width/.code={
7039
        \tl_set:Nn \l__knot_clip_width_tl {#1}
7040
7041
      clip~ width=3,
7042
      flip~ crossing/.code={%
7043
        \tl_clear_new:c {l__knot_crossing_#1}
        \tl_set:cn {l__knot_crossing_#1} {x}
7045
     },
7046
      ignore~ crossing/.code={%
7047
        \tl_clear_new:c {l__knot_ignore_crossing_#1}
7048
        \tl_set:cn {l__knot_ignore_crossing_#1} {x}
7049
     },
7050
     draft~ mode/.is~ choice,
7051
7052
      draft~ mode/off/.code={%
7053
        \bool_set_false:N \l__knot_draft_bool
        \bool_set_false:N \l__knot_super_draft_bool
      draft~ mode/crossings/.code={%
        \bool_set_true:N \l__knot_draft_bool
7057
        \bool_set_false:N \l__knot_super_draft_bool
7058
     },
7059
     draft~ mode/strands/.code={%
7060
        \bool_set_true:N \l__knot_draft_bool
7061
        \bool_set_true:N \l__knot_super_draft_bool
7062
7063
7064
      draft/.is~ family,
     draft,
      crossing~ label/.style={
        overlay,
7067
       fill=white,
7068
```

```
text~ opacity=1,
                  7070
                          text=blue,
                  7071
                          pin~ edge={blue,<-}</pre>
                  7072
                  7073
                        strand~ label/.style={
                  7074
                          overlay,
                  7075
                          circle,
                  7076
                          draw=purple,
                  7077
                          fill=white,
                  7078
                          fill~ opacity=.5,
                  7079
                          text~ opacity=1,
                  7080
                          text=purple,
                  7081
                          inner~ sep=0pt
                  7082
                  7083
                  7084 }
                      Wrapper around \tikzset for applying keys from a token list, checking for if the
                 given token list exists.
                  7085 \cs_new_nopar:Npn \knot_apply_style:N #1
                  7086 {
                        \tl_if_exist:NT #1 {
                  7087
                          \exp_args:NV \tikzset #1
                  7088
                  7089
                  7090 }
                      \cs_generate_variant:Nn \knot_apply_style:N {c}
                 The user can specify a comma separated list of crossings to flip.
\flipcrossings
                  7092 \NewDocumentCommand \flipcrossings {m}
                        \tikzset{knot~ diagram/flip~ crossing/.list={#1}}%
                  7094
                  7095 }
                  (End definition for \flipcrossings.)
                 This is how the user specifies a strand of the knot.
       \strand
                      \NewDocumentCommand \strand { O{} }
                  7097 {
                        \int_incr:N \l__knot_strands_int
                  7098
                        \tl_clear_new:c {l__knot_options_strand \int_use:N \l__knot_strands_int}
                  7099
                        \tl_set:cn {l__knot_options_strand \int_use:N \l__knot_strands_int} {#1}
                        \path[#1,spath/set~ name=knot,spath/save=\int_use:N \l__knot_strands_int]
                  7102 }
                  (End definition for \strand.)
                 This is the wrapper environment that calls the knot generation code.
          knot
                  7103 \NewDocumentEnvironment{knot} { O{} }
                  7104 {
                        \knot_initialise:n {#1}
                  7105
                  7106 }
                  7107 {
                        \knot_render:
                  7108
                  7109 }
```

fill~ opacity=.5,

7069

```
(End definition for knot.)
```

\knot_initialise:n Set up some stuff before loading in the strands.

```
7110 \cs_new_protected_nopar:Npn \knot_initialise:n #1
7111 {
7112  \tikzset{knot~ diagram/.cd,every~ knot~ diagram/.try,#1}
7113  \int_zero:N \l__knot_strands_int
7114  \tl_clear:N \l__knot_redraws_tl
7115  \seq_gclear:N \g__knot_nodes_seq
7116 }
```

(End definition for \knot_initialise:n.)

\knot_render:

This is the code that starts the work of rendering the knot.

```
7117 \cs_new_protected_nopar:Npn \knot_render:
7118 {
```

Start a scope and reset the transformation (since all transformations have already been taken into account when defining the strands).

```
7119 \pgfscope
7120 \pgftransformreset
```

Set the dimension for deciding when to include neighbouring strands

Loop through the strands drawing each one for the first time.

7126 \int_step_function:nnnN {1} {1} {\l__knot_strands_int} \knot_draw_strand:n In super draft mode we don't do anything else.

```
7127 \bool_if:NF \l__knot_super_draft_bool
```

In draft mode we draw labels at the ends of the strands; this also handles splitting curves to avoid self-intersections of Bezier curves if that's requested.

\int_step_function:nnnN {1} {1} {\l__knot_strands_int} \knot_draw_labels:n If we're considering self intersections we need to split the strands into filaments.

Initialise the intersection count.

```
7140 \int_gzero:N \g__knot_intersections_int
```

If in draft mode we label the intersections, otherwise we just stick a coordinate at each one.

```
\tl_clear:N \l__knot_node_tl
7141
        \bool_if:NT \l__knot_draft_bool
7142
7143
          \tl_set:Nn \l__knot_node_tl {
7144
            \exp_not:N \node[coordinate,
7145
              pin={[
7146
                  node~ contents={\int_use:N \g__knot_intersections_int},
7147
                  knot~ diagram/draft/crossing~ label,
7148
                  knot~ diagram/draft/crossing~
7149
                   \int_use:N \g__knot_intersections_int \c_space_tl label/.try
                ]
                }]
         }
        }
7154
```

This double loop steps through the pieces (strands or filaments) and computes the intersections and does stuff with those.

If any redraws were requested, do them here.

```
7165 \tl_use:N \l__knot_redraws_tl
```

Draw the crossing nodes

Close the scope

```
7168 \endpgfscope
```

 $(End\ definition\ for\ \verb+\knot_render+:.)$

\knot_draw_strand:n This renders a strand using the options originally specified.

```
7170 \cs_new_protected_nopar:Npn \knot_draw_strand:n #1
7171 {
7172   \pgfscope
7173   \group_begin:
7174   \spath_bake_round:c {knot strand #1}
7175   \tl_set:Nn \l_knot_tmpa_tl {knot~ diagram/every~ strand/.try,}
7176   \tl_put_right:Nv \l_knot_tmpa_tl {l_knot_options_strand #1}
7177   \tl_put_right:Nn \l_knot_tmpa_tl
7178   {
7180     knot~ diagram/only~ when~ rendering/.try,
```

```
7181    only~ when~ rendering/.try
7182    }
7183    \spath_tikz_path:Vv \l__knot_tmpa_tl {knot strand #1}
7184    \group_end:
7185    \endpgfscope
7186 }
7187 \cs_generate_variant:Nn \tl_put_right:Nn {Nv}
(End definition for \knot_draw_strand:n.)
```

\knot_draw_labels:n

Draw a label at each end of each strand, if in draft mode. Also, if requested, split potentially self intersecting Bezier curves.

```
\cs_new_protected_nopar:Npn \knot_draw_labels:n #1
7188
7189 {
     \bool_if:NT \l__knot_draft_bool
7190
7191
       \spath_finalpoint:Nv \l__knot_tmpb_tl {knot strand #1}
7192
       \dim_set:Nn \l__knot_tmpa_dim {\tl_item:Nn \l__knot_tmpb_tl {1}}
       \dim_set:Nn \l__knot_tmpb_dim {\tl_item:Nn \l__knot_tmpb_t1 {2}}
       \node[
7195
         knot~ diagram/draft/strand~label
7196
       ] at (\l_knot_tmpa_dim,\l_knot_tmpb_dim) {#1};
7197
       \spath_initialpoint:Nv \l__knot_tmpb_tl {knot strand #1}
7198
       \dim_set:Nn \l__knot_tmpa_dim {\tl_item:Nn \l__knot_tmpb_tl {1}}
7199
       \dim_set:Nn \l__knot_tmpb_dim {\tl_item:Nn \l__knot_tmpb_tl {2}}
7200
7201
         knot~ diagram/draft/strand~label
7202
       ] at (\l_knot_tmpa_dim,\l_knot_tmpb_dim) {#1};
7204
7205
     \bool_if:nT {
       \l__knot_self_intersections_bool
7206
7207
       \l__knot_splits_bool
7208
     }
7209
       \tl_clear:N \l__knot_tmpa_tl
       \spath_initialpoint:Nv \l__knot_tmpa_tl {knot strand #1}
       \tl_put_left:NV \l__knot_tmpa_tl \c_spath_moveto_tl
       \spath_segments_to_seq:Nv \l__knot_segments_seq {knot strand #1}
       \seq_map_function:NN \l__knot_segments_seq \knot_split_self_intersects:N
       \tl_set_eq:cN {knot strand #1} \l__knot_tmpa_tl
7216
     }
7218 }
```

\knot split self intersects:N

This is the macro that does the split. Figuring out whether a Bezier cubic self intersects is apparently a difficult problem so we don't bother. We compute a point such that if there is an intersection then it lies on either side of the point. I don't recall where the formula came from!

```
7219 \cs_new_protected_nopar:Npn \knot_split_self_intersects:N #1
7220 {
7221 \tl_set:Nx \l_knot_tmpc_tl {\tl_item:nn {#1} {4}}
7222 \tl_case:NnF \l_knot_tmpc_tl
```

(End definition for \knot_draw_labels:n.)

```
\c_spath_curvetoa_tl
7224
7225
          \fp_set:Nn \l__knot_tmpa_fp
7226
            (\tl_item:nn {#1} {3} - 3 * \tl_item:nn {#1} {6}
7228
            + 3 * \tl_item:nn {#1} {9} - \tl_item:nn {#1} {12})
7229
7230
            (3 * \tl_item:nn {#1} {8} - 3 * \tl_item:nn {#1} {11})
            (\tl_item:nn {#1} {2} - 3 * \tl_item:nn {#1} {5}
            + 3 * \tl_item:nn {#1} {8} - \tl_item:nn {#1} {11})
7234
7235
             (3 * \tl_item:nn {#1} {9} - 3 * \tl_item:nn {#1} {12})
7236
          \fp_set:Nn \l__knot_tmpb_fp
7238
7239
            (\tl_item:nn {#1} {2} - 3 * \tl_item:nn {#1} {5}
7240
            + 3 * \tl_item:nn {#1} {8} - \tl_item:nn {#1} {11})
            (3 * \text{tl_item:nn } \{\#1\} \{6\} - 6 * \text{tl_item:nn } \{\#1\} \{9\}
            + 3 * \tl_item:nn {#1} {12})
7244
7245
            \  (\tilde{1}_{item:nn} \ f^{1} \ f^{3} - 3 * \tilde{f}^{item:nn} \ f^{1} \ f^{6}
7246
            + 3 * \tl_item:nn {#1} {9} - \tl_item:nn {#1} {12})
7247
7248
            (3 * \text{tl_item:nn } \{\#1\} \{5\} - 6 * \text{tl_item:nn } \{\#1\} \{8\}
7249
            + 3 * \tl_item:nn {#1} {11})
7250
7251
          \fp_compare:nTF
7253
          {
            \l_knot_tmpb_fp != 0
7255
          }
7256
            \fp_set:\n \l_knot_tmpa_fp \{.5 * \l_knot_tmpa_fp / \l_knot_tmpb_fp\}
7257
            \fp_compare:nTF
7258
            {
7259
              0 < \l_knot_tmpa_fp && \l_knot_tmpa_fp < 1</pre>
7260
7261
               \spath_split_curve:NNnV
               \l__knot_tmpc_tl
               \l__knot_tmpd_tl
               {#1}
               \l_knot_tmpa_fp
               \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
7268
               \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
7269
               \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
               \tl_set:Nx \l__knot_tmpd_tl {\tl_tail:N \l__knot_tmpd_tl}
               \tl_set:Nx \l__knot_tmpd_tl {\tl_tail:N \l__knot_tmpd_tl}
7272
               \tl_set:Nx \l__knot_tmpd_tl {\tl_tail:N \l__knot_tmpd_tl}
               \tl_put_right:NV \l__knot_tmpa_tl \l__knot_tmpc_tl
               \tl_put_right:NV \l__knot_tmpa_tl \l__knot_tmpd_tl
7276
```

```
\tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                          7281
                                         \tl_put_right:NV \l__knot_tmpa_tl \l__knot_tmpc_tl
                          7282
                                       }
                          7283
                                    }
                          7284
                                       \tl_set:Nn \l__knot_tmpc_tl {#1}
                                       \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                                       \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                          7288
                                       \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                          7289
                                       \tl_put_right:NV \l__knot_tmpa_tl \l__knot_tmpc_tl
                          7290
                          7291
                          7292
                                  \c_spath_lineto_tl
                          7293
                          7294
                                    \tl_set:Nn \l__knot_tmpc_tl {#1}
                                    \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                                    \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                                    \tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
                                    \tl_put_right:NV \l__knot_tmpa_tl \l__knot_tmpc_tl
                          7299
                                  }
                          7300
                                }
                          7301
                          7302
                                  \tl_put_right:Nn \l__knot_tmpa_tl {#1}
                          7303
                                }
                          7304
                          7305 }
                          (End\ definition\ for\ \verb+\knot_split_self_intersects:N.)
\knot_intersections:nn
                         This computes the intersections of two pieces and steps through them.
                          7306
                              \cs_new_protected_nopar:Npn \knot_intersections:nn #1#2
                          7307 {
                          7308
                                \group_begin:
                                \tl_set_eq:NN \l__knot_tmpa_tl \l__knot_prefix_tl
                                \tl_put_right:Nn \l__knot_tmpa_tl {#1}
                                \tl_set_eq:NN \l__knot_tmpb_tl \l__knot_prefix_tl
                          7311
                                \tl_put_right:Nn \l__knot_tmpb_tl {#2}
                                \tl_set_eq:Nc \l__knot_tmpc_tl {knot \tl_use:N \l__knot_tmpa_tl}
                                \tl_set_eq:Nc \l__knot_tmpd_tl {knot \tl_use:N \l__knot_tmpb_tl}
                          7314
                          7315
                                \bool_if:nTF {
                          7316
                                  \l__knot_save_bool
                          7317
                                  &&
                          7318
                                  \tl_if_exist_p:c {
                          7319
                          7320
                                    knot~ intersections~
                          7321
                                    \tl_use:N \l__knot_name_tl -
                                    \tl_use:N \l__knot_tmpa_tl -
                          7322
                                     \t_use:N \l_knot_tmpb_tl
                          7323
                                }
                          7325
                                {
                          7326
```

\tl_set:Nn \l__knot_tmpc_tl {#1}

\tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}
\tl_set:Nx \l__knot_tmpc_tl {\tl_tail:N \l__knot_tmpc_tl}

7278

7280

```
\tl_use:c
                                        {
                                7328
                                          knot~ intersections~ \tl_use:N \l__knot_name_tl -
                                7329
                                          \tl_use:N \l__knot_tmpa_tl -
                                7330
                                          \tl_use:N \l__knot_tmpb_tl
                                      }
                                7333
                                      {
                                7334
                                        \pgfintersectionofpaths{\pgfsetpath\l__knot_tmpc_tl}{\pgfsetpath\l__knot_tmpd_tl}
                                7335
                                7336
                                7337
                                7338
                                      \int_compare:nT {\pgfintersectionsolutions > 0}
                                7339
                                7340
                                        \int_step_function:nnnN
                                7341
                                        {1}
                                7342
                                        {1}
                                7343
                                        {\pgfintersectionsolutions}
                                7344
                                        \knot_do_intersection:n
                                      \knot_save_intersections: VV \l__knot_tmpa_tl \l__knot_tmpb_tl
                                7348
                                      \group_end:
                                7349
                                7350 }
                                (End definition for \knot_intersections:nn.)
\knot_save_intersections:nn
                                    \cs_new_protected_nopar:Npn \knot_save_intersections:nn #1#2
                                7351
                                7352
                                      \bool_if:NT \l__knot_save_bool
                                7353
                                7354
                                        \tl_clear:N \l__knot_aux_tl
                                7355
                                        \tl_put_right:Nn \l__knot_aux_tl
                                7356
                                          \def\pgfintersectionsolutions
                                        }
                                        \tl_put_right:Nx \l__knot_aux_tl
                                7360
                                        {
                                7361
                                          {\int_eval:n {\pgfintersectionsolutions}}
                                7362
                                        }
                                7363
                                        \int_compare:nT {\pgfintersectionsolutions > 0}
                                7364
                                7365
                                          \int_step_inline:nnnn {1} {1} {\pgfintersectionsolutions}
                                          {
                                             \pgfpointintersectionsolution{##1}
                                             \dim_set:Nn \l__knot_tmpa_dim {\pgf@x}
                                             \dim_set:Nn \l__knot_tmpb_dim {\pgf@y}
                                             \tl_put_right:Nn \l__knot_aux_tl
                                7371
                                7372
                                             {
                                               \expandafter\def\csname pgfpoint@intersect@solution@##1\endcsname
                                7374
                                             \tl_put_right:Nx \l__knot_aux_tl
                                7375
                                             {
                                7376
```

```
{
                  \exp_not:N \pgf@x
 7378
 7379
                 \dim_use:N \l__knot_tmpa_dim
 7380
                 \exp_not:N \relax
 7381
                 \exp_not:N \pgf@y
 7382
 7383
                 \dim_use:N \l__knot_tmpb_dim
                 \exp_not:N \relax
               }
             }
           }
 7388
           \tl_set:Nn \l__knot_auxa_tl {\expandafter \gdef \csname knot~ intersections~}
 7389
           \tl_put_right:Nx \l__knot_auxa_tl {\tl_use:N \l__knot_name_tl - #1 - #2}
 7390
           \tl_put_right:Nn \l__knot_auxa_tl {\endcsname}
 7391
           \tl_put_right:Nx \l__knot_auxa_tl {{\tl_to_str:N \l__knot_aux_tl}}
 7392
           \protected@write\@auxout{}{\tl_to_str:N \l__knot_auxa_tl}
 7393
 7394
      }
 7395
 7396 }
    \cs_generate_variant:Nn \knot_save_intersections:nn {VV}
(End definition for \knot_save_intersections:nn.)
This handles a specific intersection.
 7398 \cs_new_protected_nopar:Npn \knot_do_intersection:n #1
 7399 {
Get the intersection coordinates.
       \pgfpointintersectionsolution{#1}
      \dim_set:Nn \l__knot_tmpa_dim {\pgf@x}
 7401
      \dim_set:Nn \l__knot_tmpb_dim {\pgf@y}
If we're dealing with filaments, we can get false positives from the end points.
      \bool_set_false:N \l__knot_skip_bool
      \bool_if:NT \l__knot_self_intersections_bool
      {
 7405
If one filament preceded the other, test for the intersection being at the relevant end
point.
         \tl_set:Nn \l__knot_tmpc_tl {knot previous}
 7406
         \tl_put_right:NV \l__knot_tmpc_tl \l__knot_tmpa_tl
 7407
         \tl_set:Nv \l__knot_tmpc_tl \l__knot_tmpc_tl
 7408
         \tl_if_eq:NNT \l__knot_tmpc_tl \l__knot_tmpb_tl
 7409
 7410
           \knot_test_endpoint:NVnT \l__knot_tolerance_dim \l__knot_tmpb_tl {final point}
 7411
           {
             \bool_set_true:N \l__knot_skip_bool
 7413
           }
 7414
        }
 7415
 7416
         \tl_set:Nn \l__knot_tmpc_tl {knot previous}
 7417
         \tl_put_right:NV \l__knot_tmpc_tl \l__knot_tmpb_tl
 7418
         \tl_set:Nv \l__knot_tmpc_tl \l__knot_tmpc_tl
 7419
```

\knot_do_intersection:n

7420

\tl_if_eq:NNT \l__knot_tmpc_tl \l__knot_tmpa_tl

The user can also say that end points of filaments (or strands) should simply be ignored anyway.

```
\bool_if:NT \l__knot_ignore_ends_bool
7428
     {
7429
        \knot_test_endpoint:NVnT \l__knot_tolerance_dim \l__knot_tmpa_tl {initial point}
7430
7431
          \bool_set_true:N \l__knot_skip_bool
7432
7433
        \knot_test_endpoint:NVnT \l__knot_tolerance_dim \l__knot_tmpa_tl {final point}
7434
          \bool_set_true:N \l__knot_skip_bool
       }
7437
        \knot_test_endpoint:NVnT \l__knot_tolerance_dim \l__knot_tmpb_tl {initial point}
7438
7439
          \bool_set_true:N \l__knot_skip_bool
7440
       }
7441
        \knot_test_endpoint:NVnT \l__knot_tolerance_dim \l__knot_tmpb_tl {final point}
7442
7443
          \bool_set_true:N \l__knot_skip_bool
7445
```

Assuming that we passed all the above tests, we render the crossing.

```
7447 \bool_if:NF \l__knot_skip_bool
7448 {
7449
7450 \int_gincr:N \g__knot_intersections_int
```

This is the intersection test. If the intersection finder finds too many, it might be useful to ignore some.

This is the flip test. We only render one of the paths. The "flip" swaps which one we render.

Now we know which one we're rendering, we test to see if we should also render its predecessor or successor to ensure that we render a path through the entire crossing region.

```
\bool_if:NT \l__knot_self_intersections_bool
7474
7475
            \knot_test_endpoint:NVnT
7476
            \l_knot_redraw_tolerance_dim \l_knot_tmpg_tl {initial point}
7477
            {
7478
              \bool_set_true:N \l__knot_prepend_prev_bool
7479
            }
7480
            {
7481
              \bool_set_false: N \l__knot_prepend_prev_bool
            }
            \knot_test_endpoint:NVnT
7484
            \l_knot_redraw_tolerance_dim \l_knot_tmpg_tl {final point}
7485
7486
              \bool_set_true:N \l__knot_append_next_bool
7487
            }
7488
            {
7489
              \bool_set_false:N \l__knot_append_next_bool
7490
7491
```

If either of those tests succeeded, do the appending or prepending.

```
\bool if:nT
7492
            {
7493
              \l_knot_prepend_prev_bool || \l_knot_append_next_bool
7494
7495
              \tl_clear_new:c {knot \tl_use:N \l__knot_prefix_tl -1}
              \tl_set_eq:cc
              {knot \tl_use:N \l__knot_prefix_tl -1}
              {knot \tl_use:N \l__knot_tmpg_tl}
7501
              \tl_clear_new:c {l__knot_options_ \tl_use:N \l_knot_prefix_tl -1}
7502
              \tl_set_eq:cc
7503
              {l_knot_options_ \tl_use:N \l_knot_prefix_tl -1}
7504
              {l_knot_options_ \tl_use:N \l_knot_tmpg_tl}
7505
7506
              \bool_if:nT
7507
              {
                \l__knot_prepend_prev_bool
7510
                \tl_if_exist_p:c {knot previous \tl_use:N \l_knot_tmpg_tl}
7511
7512
                !\tl_if_empty_p:c {knot previous \tl_use:N \l_knot_tmpg_tl}
7513
```

```
}
7514
               {
7515
                 \spath_prepend_no_move:cv
7516
                 {knot \tl_use:N \l__knot_prefix_tl -1}
7517
                 {knot \tl_use:c {knot previous \tl_use:N \l__knot_tmpg_tl}}
7518
If we split potentially self intersecting curves, we test to see if we should prepend yet
another segment.
                 \bool_if:nT
7519
7520
                 {
                   \l__knot_splits_bool
7522
                   \tl_if_exist_p:c {knot previous \tl_use:N \l_knot_tmpg_tl}
7523
7524
                    !\\tl_if_empty_p:c \{knot previous \tl_use:N \tl_knot_tmpg_tl\}
7525
                 }
7526
7527
                   \knot_test_endpoint:NvnT
                   \l__knot_redraw_tolerance_dim
                   {knot previous \tl_use:N \l__knot_tmpg_tl}
                   {initial point}
7531
7532
                     \spath_prepend_no_move:cv
7533
                     {knot \tl_use:N \l_knot_prefix_tl -1}
7534
                     {knot \tl_use:c
                        {knot previous \tl_use:c
7536
                          {knot previous \tl_use:N \l__knot_tmpg_tl}
7537
7538
                     }
                     \tl_set_eq:Nc \l__knot_tmpa_tl {knot \tl_use:N \l__knot_prefix_tl -
    1}
                   }
7541
                 }
7542
7543
Now the same for appending.
               \bool_if:nT
7544
               {
7545
                 \l__knot_append_next_bool
7547
                 \tl_if_exist_p:c {knot next \tl_use:N \l__knot_tmpg_tl}
7548
7549
                 !\tl_if_empty_p:c {knot previous \tl_use:N \l_knot_tmpg_tl}
7550
               }
7551
               {
                 \spath_append_no_move:cv
                 {knot \tl_use:N \l__knot_prefix_tl -1}
7554
                 {knot \tl_use:c {knot next \tl_use:N \l__knot_tmpg_tl}}
7555
                 \bool_if:nT
7556
7557
                   \l__knot_splits_bool
7558
7559
                   \tl_if_exist_p:c {knot previous \tl_use:N
7560
                     \l_knot_tmpg_tl}
7561
```

&&

```
!\tl_if_empty_p:c {knot previous \tl_use:N \l__knot_tmpg_tl}
                }
                 {
                   \knot_test_endpoint:NvnT
7566
                   \l_knot_redraw_tolerance_dim
7567
                   {knot previous \tl_use:N \l_knot_tmpg_tl}
                   {final point}
7569
                   {
                     \spath_append_no_move:cv
                     {knot \tl_use:N \l__knot_prefix_tl -1}
                     {knot \tl_use:c
                        {knot next \tl_use:c
7574
                          {knot next \tl_use:N \l_knot_tmpg_tl}
7575
7576
7577
                   }
7578
                }
7579
               \tl_set:Nn \l__knot_tmpg_tl {\tl_use:N \l__knot_prefix_tl -1}
            }
          }
Now we render the crossing.
          \pgfscope
7584
           \group_begin:
          \tikzset{
            knot~ diagram/every~ intersection/.try,
            every~ intersection/.try,
            knot~ diagram/intersection~ \int_use:N \g_knot_intersections_int/.try
7589
7590
          \knot_draw_crossing:VVV \l__knot_tmpg_tl \l__knot_tmpa_dim \l__knot_tmpb_dim
7591
7592
           (\l_knot_name_tl \c_space_tl \int_use:N \g_knot_intersections_int)
7593
          at (\dim_use:N \l__knot_tmpa_dim, \dim_use:N \l__knot_tmpb_dim);
7594
          \group_end:
7595
          \endpgfscope
This ends the boolean as to whether to consider the intersection at all
7597
And possibly stick a coordinate with a label at the crossing.
        \tl_if_empty:NF \l__knot_node_tl
        {
7599
           \seq_gpush:Nx
7600
           \g__knot_nodes_seq
7601
7602
             \l_knot_node_tl
7603
            at
             (\dim_use:N \l__knot_tmpa_dim, \dim_use:N \l__knot_tmpb_dim) {};
7607
      }
7608
7609 }
7610
7611 \cs_generate_variant:Nn \knot_intersections:nn {VV}
```

```
Test whether the point is near the intersection point.
  \knot_test_endpoint:N
                               \prg_new_conditional:Npnn \knot_test_endpoint:NN #1#2 {p,T,F,TF}
                            7613 {
                            7614
                                  \dim_compare:nTF
                            7615
                                    \dim_abs:n { \l__knot_tmpa_dim - \tl_item:Nn #2 {1}}
                            7616
                            7617
                                    \dim_abs:n { \l__knot_tmpb_dim - \tl_item:Nn #2 {2}}
                            7618
                            7619
                                    #1
                            7620
                                  }
                            7621
                                  {
                            7622
                                    \prg_return_true:
                            7623
                                  }
                            7625
                                    \prg_return_false:
                                  }
                            7627
                            7628
                           (End definition for \knot_test_endpoint:N.)
 \knot_test_endpoint:nn
                           Wrapper around the above.
                            7629 \prg_new_protected_conditional:Npnn \knot_test_endpoint:Nnn #1#2#3 {T,F,TF}
                            7630 {
                                  \use:c {spath_#3:Nv} \l__knot_tmpd_tl {knot #2}
                            7631
                                  \knot_test_endpoint:NNTF #1 \l__knot_tmpd_tl
                            7632
                            7633
                            7634
                                    \prg_return_true:
                            7635
                                  }
                            7637
                                    \prg_return_false:
                                  }
                            7638
                            7639 }
                            7640
                               \cs_generate_variant:Nn \knot_test_endpoint:NnnT {NVnT,NvnT}
                            7641
                               \cs_generate_variant:Nn \knot_test_endpoint:NnnF {NVnF,NvnF}
                               \cs_generate_variant:Nn \knot_test_endpoint:NnnTF {NVnTF,NvnTF}
                           (End definition for \knot_test_endpoint:nn.)
\knot_draw_crossing:nnn
                           This is the code that actually renders a crossing.
                                cs_new_protected_nopar:Npn \knot_draw_crossing:nnn #1#2#3
                            7644
                            7645
                                  \group_begin:
                            7646
                                  \pgfscope
                            7647
                                  \path[knot~ diagram/background~ clip] (#2, #3)
                                  circle[radius=\l__knot_clip_bg_radius_dim];
                            7650
                                  \tl_set:Nn \l__knot_tmpa_tl {knot~ diagram/every~ strand/.try,}
                            7651
                                  \tl_if_exist:cT {l__knot_options_ #1}
                            7652
```

{

7653

7654

(End definition for \knot_do_intersection:n.)

\tl_put_right:Nv \l__knot_tmpa_tl {l__knot_options_ #1}

```
\tl_put_right:Nn \l__knot_tmpa_tl
                          7656
                          7657
                                  , knotbg
                          7658
                                  ,line~ width= \tl_use:N \l__knot_clip_width_tl * \pgflinewidth
                          7659
                          7660
                                \spath_tikz_path: Vv \l__knot_tmpa_tl {knot #1}
                          7661
                          7662
                                \endpgfscope
                          7663
                          7664
                          7665
                                \pgfscope
                                \path[knot~ diagram/clip] (#2, #3)
                          7666
                                circle[radius=\l__knot_clip_draw_radius_dim];
                          7667
                          7668
                                \tl_set:Nn \l__knot_tmpa_tl {knot~ diagram/every~ strand/.try,}
                          7669
                                \tl_if_exist:cT {l__knot_options_ #1}
                          7670
                          7671
                                \tl_put_right:Nv \l__knot_tmpa_tl {l__knot_options_ #1}
                          7672
                               }
                          7673
                                \tl_put_right:Nn \l__knot_tmpa_tl
                          7674
                          7675
                                  ,knot~ diagram/only~ when~ rendering/.try
                          7676
                                  ,only~ when~ rendering/.try
                          7677
                          7678
                                \spath_tikz_path: Vv \l__knot_tmpa_tl {knot #1}
                          7679
                          7680
                                \endpgfscope
                          7681
                                \group_end:
                          7682
                          7683 }
                              \cs_generate_variant:Nn \knot_draw_crossing:nnn {nVV, VVV}
                          7685
                              \cs_new_protected_nopar:Npn \knot_draw_crossing:nn #1#2
                          7687
                          7688
                                \tikz@scan@one@point\pgfutil@firstofone #2 \relax
                          7689
                                \knot_draw_crossing:nVV {#1} \pgf@x \pgf@y
                          7690
                          7691 }
                         (End definition for \knot_draw_crossing:nnn.)
 \knot_split_strands:
                         This, and the following macros, are for splitting strands into filaments.
                              \cs_new_protected_nopar:Npn \knot_split_strands:
                          7693 {
                                \int_gzero:N \g__knot_filaments_int
                                \int_step_function:nnnN {1} {1} {\l__knot_strands_int} \knot_split_strand:n
                                \int_step_function:nnnN {1} {1} {\g_knot_filaments_int} \knot_compute_nexts:n
                          7697 }
                         (End definition for \knot split strands:.)
                         Each filament needs to know its predecessor and successor. We work out the predecessors
\knot_compute_nexts:n
                         as we go along, this fills in the successors.
                          7698 \cs_new_protected_nopar:Npn \knot_compute_nexts:n #1
                          7699 {
```

7655

```
\tl_clear_new:c {knot next \tl_use:c {knot previous filament #1}}
                             \tl_set:cn {knot next \tl_use:c {knot previous filament #1}} {filament #1}
                       7701
                       7702 }
                       (End definition for \knot_compute_nexts:n.)
\knot_split_strand:n Sets up the split for a single strand.
                          \cs_new_protected_nopar:Npn \knot_split_strand:n #1
                       7704 {
                             \int_set_eq:NN \l__knot_component_start_int \g__knot_filaments_int
                       7705
                             \int_incr:N \l__knot_component_start_int
                       7706
                             \tl_set_eq:Nc \l__knot_tmpa_tl {l__knot_options_strand #1}
                             \spath_segments_to_seq:Nv \l__knot_segments_seq {knot strand #1}
                       7708
                             \seq_map_function:NN \l__knot_segments_seq \knot_save_filament:N
                       7709
                       7710 }
                       (End\ definition\ for\ \verb|\knot_split_strand:n.|)
\knot_save_filament: N Saves a filament as a new spath object.
                       7711 \cs_new_protected_nopar:Npn \knot_save_filament:N #1
                       7712 {
                             \t = \t Nx = \t \{t1_{item:nn} \{\#1\} \{4\}\}
                             \tl_case:NnF \l_knot_tmpb_tl
                       7714
                       7715
                               \c_spath_moveto_tl
                       7716
                       7717
                                 \int_compare:nT {\l__knot_component_start_int < \g__knot_filaments_int}
                                   \int_set_eq:NN \l__knot_component_start_int \g__knot_filaments_int
                       7722
                              }
                       7723
                               \c_spath_lineto_tl
                       7724
                                 7725
                                 \tl_clear_new:c {knot filament \int_use:N \g_knot_filaments_int}
                       7726
                                 \tl_set:cn {knot filament \int_use:N \g__knot_filaments_int} {#1}
                       7728
                                 \tl_clear_new:c {l__knot_options_filament \int_use:N \g__knot_filaments_int}
                       7729
                                 \tl_set_eq:cN {l__knot_options_filament \int_use:N \g__knot_filaments_int}
                                 \l__knot_tmpa_tl
                       7731
                                 \tl_clear_new:c {knot previous filament \int_use:N \g__knot_filaments_int}
                                 \int_compare:nF {\l_knot_component_start_int == \g_knot_filaments_int}
                       7734
                       7735
                                   \tl_set:cx {knot previous filament \int_use:N \g__knot_filaments_int}
                       7736
                                   {filament \int_eval:n {\g_knot_filaments_int - 1}}
                       7738
                               }
                       7739
                               \c_spath_curvetoa_tl
                                 \int_gincr:N \g__knot_filaments_int
                       7742
                                 \tl_clear_new:c {knot filament \int_use:N \g_knot_filaments_int}
                       7743
                                 \tl_set:cn {knot filament \int_use:N \g_knot_filaments_int} {#1}
                       7744
                                 7745
                                 \tl_set_eq:cN {l_knot_options_filament \int_use:N \g_knot_filaments_int}
                       7746
```

```
7748
                   \tl_clear_new:c {knot previous filament \int_use:N \g_knot_filaments_int}
          7749
                   \int_compare:nF {\l_knot_component_start_int == \g_knot_filaments_int}
          7750
          7751
                     \tl_set:cx
                     {knot previous filament \int_use:N \g_knot_filaments_int}
                      {filament \int_eval:n {\g_knot_filaments_int - 1}}
                 }
          7756
                 \c_spath_closepath_tl
          7757
          7758
                   \int_gincr:N \g__knot_filaments_int
          7759
                   \tl_clear_new:c {knot filament \int_use:N \g_knot_filaments_int}
          7760
                   \tl_clear:N \l__knot_tmpa_tl
          7761
                   \tl_put_right:Nx
          7762
          7763
                      \tl_item:nn {#1} {1}\tl_item:nn {#1} {2}\tl_item:nn {#1} {3}
          7764
                   \tl_put_right:NV \l__knot_tmpa_tl \c_spath_lineto_tl
                   \tl_put_right:Nx {\tl_item:nn {#1} {5}\tl_item:nn {#1} {6}}
          7768
                   \tl_set:cV {knot filament \int_use:N \g__knot_filaments_int} \l__knot_tmpa_tl
          7769
                   \tl_set_eq:cN {l__knot_options_filament \int_use:N \g__knot_filaments_int}
                   \l knot tmpa tl
          7771
                   \tl_clear_new:c {knot previous filament \int_use:N \g__knot_filaments_int}
          7772
                   \int_compare:nF {\l__knot_component_start_int == \g__knot_filaments_int}
          7773
          7774
          7775
                     7777
                      {filament \int_eval:n {\g_knot_filaments_int - 1}}
                   }
          7778
          7779
                   \tl_set:cx
                   {knot previous filament \int_use:N \l__knot_component_start_int}
          7780
                    {filament \int_use:N \g__knot_filaments_int}
          7781
          7782
               }
          7783
          7784
               {
          7785
               }
          7786 }
         (End definition for \knot_save_filament:N.)
         The user can redraw segments of the strands at specific locations.
\redraw
          7787 \NewDocumentCommand \redraw { m m }
          7788 {
                \tikz@scan@one@point\pgfutil@firstofone #2 \relax
          7789 %
               \tl_put_right:Nn \l__knot_redraws_tl {\knot_draw_crossing:nn}
          7790
               \tl_put_right:Nx \l_knot_redraws_tl {
                 { t^{#1} {#2}% {\dim_use:N \geq 0x} {\dim_use:N \geq 0}}
          7792
          7793
          7794 }
         (End definition for \redraw.)
          7795 \ExplSyntaxOff
```

7747

\l__knot_tmpa_tl

```
Add the extra anchors for the knot crossing nodes.
\pgf@sh__knotknotanchor
                                                                                                                                       \def\pgf@sh_knotknotanchor#1#2{%
                                                                                                                                                \anchor{#2 north west}{%
                                                                                                                                                         \csname pgf@anchor@knot #1@north west\endcsname%
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                        7800
                                                                                                                                               }%
                                                                                                                        7801
                                                                                                                                                \anchor{#2 north east}{%
                                                                                                                        7802
                                                                                                                                                         \csname pgf@anchor@knot #1@north east\endcsname%
                                                                                                                      7803
                                                                                                                                                         \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                                                                                                                      7804
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7805
                                                                                                                                               }%
                                                                                                                      7806
                                                                                                                                                 \anchor{#2 south west}{%
                                                                                                                      7807
                                                                                                                                                         \csname pgf@anchor@knot #1@south west\endcsname%
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                      7810
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7811
                                                                                                                                                 \anchor{#2 south east}{%
                                                                                                                      7812
                                                                                                                                                         \csname pgf@anchor@knot #1@south east\endcsname%
                                                                                                                      7813
                                                                                                                                                         \protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\protect\pro
                                                                                                                      7814
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7815
                                                                                                                      7816
                                                                                                                                                 \anchor{#2 north}{%
                                                                                                                      7817
                                                                                                                                                         \csname pgf@anchor@knot #1@north\endcsname%
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                                               }%
                                                                                                                      7821
                                                                                                                                                 \anchor{#2 east}{%
                                                                                                                      7822
                                                                                                                                                         \csname pgf@anchor@knot #1@east\endcsname%
                                                                                                                      7823
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                      7824
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7825
                                                                                                                      7826
                                                                                                                                                 \anchor{#2 west}{%
                                                                                                                      7827
                                                                                                                                                         \csname pgf@anchor@knot #1@west\endcsname%
                                                                                                                      7828
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7830
                                                                                                                      7831
                                                                                                                                                 \anchor{#2 south}{%
                                                                                                                      7832
                                                                                                                                                         \csname pgf@anchor@knot #1@south\endcsname%
                                                                                                                      7833
                                                                                                                                                         \pgf@x=#2\pgf@x%
                                                                                                                      7834
                                                                                                                                                         \pgf@y=#2\pgf@y%
                                                                                                                      7835
                                                                                                                                               }%
                                                                                                                      7836
                                                                                                                      7837 }
                                                                                                                    (End\ definition\ for\ \verb+\pgf@sh_-knotknotanchor.)
                                              knot⊔crossing
                                                                                                                      7838
                                                                                                                                      \pgfdeclareshape{knot crossing}
                                                                                                                                                 \inheritsavedanchors[from=circle] % this is nearly a circle
```

\inheritanchorborder[from=circle]
\inheritanchor[from=circle] {north}

```
\inheritanchor[from=circle]{north east}
                   7844
                         \inheritanchor[from=circle]{center}
                   7845
                         \inheritanchor[from=circle]{west}
                   7846
                         \inheritanchor[from=circle]{east}
                   7847
                         \inheritanchor[from=circle]{mid}
                   7848
                         \inheritanchor[from=circle]{mid west}
                   7849
                         \inheritanchor[from=circle]{mid east}
                   7850
                         \inheritanchor[from=circle]{base}
                   7851
                         \inheritanchor[from=circle]{base west}
                   7852
                         \inheritanchor[from=circle]{base east}
                   7853
                         \inheritanchor[from=circle]{south}
                   7854
                         \inheritanchor[from=circle]{south west}
                   7855
                         \inheritanchor[from=circle]{south east}
                   7856
                         \inheritanchorborder[from=circle]
                   7857
                         \pgf@sh__knotknotanchor{crossing}{2}
                   7858
                         \pgf@sh_knotknotanchor{crossing}{3}
                   7859
                         \pgf@sh__knotknotanchor{crossing}{4}
                         \pgf@sh__knotknotanchor{crossing}{8}
                         \pgf@sh_knotknotanchor{crossing}{16}
                         \pgf@sh__knotknotanchor{crossing}{32}
                         \backgroundpath{
                   7864
                           \pgfutil@tempdima=\radius%
                   7865
                           \pgfmathsetlength{\pgf@xb}{\pgfkeysvalueof{/pgf/outer xsep}}%
                   7866
                           \pgfmathsetlength{\pgf@yb}{\pgfkeysvalueof{/pgf/outer ysep}}%
                   7867
                           \ifdim\pgf@xb<\pgf@yb%
                   7868
                             \advance\pgfutil@tempdima by-\pgf@yb%
                   7869
                   7870
                             \advance\pgfutil@tempdima by-\pgf@xb%
                   7871
                   7872
                           \fi%
                        }
                   7873
                   7874 }
                  (End definition for knot crossing.)
knot⊔over⊔cross
                      \pgfdeclareshape{knot over cross}
                   7876
                         \inheritsavedanchors[from=rectangle] % this is nearly a circle
                   7877
                         \inheritanchorborder[from=rectangle]
                   7878
                         \inheritanchor[from=rectangle] {north}
                   7879
                         \inheritanchor[from=rectangle] {north west}
                   7880
                         \inheritanchor[from=rectangle] {north east}
                   7881
                         \inheritanchor[from=rectangle]{center}
                   7882
                         \inheritanchor[from=rectangle] {west}
                   7883
                         \inheritanchor[from=rectangle]{east}
                         \inheritanchor[from=rectangle]{mid}
                   7885
                         \inheritanchor[from=rectangle]{mid west}
                   7886
                         \inheritanchor[from=rectangle]{mid east}
                   7887
                         \inheritanchor[from=rectangle]{base}
                   7888
                         \inheritanchor[from=rectangle]{base west}
                   7889
                         \inheritanchor[from=rectangle]{base east}
                   7890
                         \inheritanchor[from=rectangle] {south}
                   7891
                         \inheritanchor[from=rectangle]{south west}
```

\inheritanchor[from=circle]{north west}

```
\inheritanchor[from=rectangle]{south east}
                          \inheritanchorborder[from=rectangle]
                    7894
                          \backgroundpath{
                    7895
                            \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
                    7896
                            \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
                    7897
                            \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@ya}}
                    7898
                            \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@yb}}
                    7899
                    7900
                          \foregroundpath{
                       % store lower right in xa/ya and upper right in xb/yb
                            \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
                    7903
                            \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
                    7904
                            \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@yb}}
                    7905
                            \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@ya}}
                    7906
                    7907
                    7908
                   (End definition for knot over cross.)
knot under cross
                       \pgfdeclareshape{knot under cross}
                    7909
                    7910
                          \inheritsavedanchors[from=rectangle] % this is nearly a circle
                    7911
                          \inheritanchorborder[from=rectangle]
                    7912
                          \inheritanchor[from=rectangle]{north}
                    7913
                          \inheritanchor[from=rectangle]{north west}
                    7914
                          \inheritanchor[from=rectangle] {north east}
                    7915
                          \inheritanchor[from=rectangle]{center}
                    7916
                          \inheritanchor[from=rectangle] {west}
                    7917
                          \inheritanchor[from=rectangle]{east}
                    7918
                          \inheritanchor[from=rectangle]{mid}
                    7919
                          \inheritanchor[from=rectangle]{mid west}
                    7920
                          \inheritanchor[from=rectangle]{mid east}
                    7921
                          \inheritanchor[from=rectangle]{base}
                          \inheritanchor[from=rectangle]{base west}
                          \inheritanchor[from=rectangle]{base east}
                          \inheritanchor[from=rectangle]{south}
                          \inheritanchor[from=rectangle]{south west}
                    7926
                          \inheritanchor[from=rectangle]{south east}
                    7927
                          \inheritanchorborder[from=rectangle]
                    7928
                          \backgroundpath{
                    7929
                            \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
                    7930
                            \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
                    7931
                            \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@yb}}
                    7932
                            \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@ya}}
                    7933
                    7934
                          \foregroundpath{
                    7935
                    7936
                       % store lower right in xa/ya and upper right in xb/yb
                            \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
                    7937
                            \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
                    7938
                            \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@ya}}
                    7939
                            \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@yb}}
                    7940
                    7941
                    7942 }
```

```
(End definition for knot under cross.)
 knot vert
             7943 \pgfdeclareshape{knot vert}
             7944 {
             7945
                    \inheritsavedanchors[from=rectangle] % this is nearly a circle
                   \inheritanchorborder[from=rectangle]
                   \inheritanchor[from=rectangle] {north}
             7947
                   \inheritanchor[from=rectangle]{north west}
             7948
                   \inheritanchor[from=rectangle]{north east}
             7949
                   \inheritanchor[from=rectangle]{center}
             7950
                   \inheritanchor[from=rectangle] {west}
             7951
                   \inheritanchor[from=rectangle]{east}
             7952
                   \inheritanchor[from=rectangle]{mid}
             7953
                   \inheritanchor[from=rectangle]{mid west}
             7954
                   \inheritanchor[from=rectangle]{mid east}
                   \inheritanchor[from=rectangle]{base}
                   \inheritanchor[from=rectangle]{base west}
             7957
                   \inheritanchor[from=rectangle]{base east}
             7958
                   \inheritanchor[from=rectangle]{south}
             7959
                   \inheritanchor[from=rectangle]{south west}
             7960
                   \inheritanchor[from=rectangle]{south east}
             7961
                   \inheritanchorborder[from=rectangle]
             7962
                   \backgroundpath{
             7963
                 % store lower right in xa/ya and upper right in xb/yb
             7964
                     \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
                     \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
                     \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@ya}}
                     \pgfpathlineto{\pgfqpoint{\pgf@xa}{\pgf@yb}}
             7968
                     \pgfpathmoveto{\pgfqpoint{\pgf@xb}{\pgf@yb}}
             7969
                     \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@ya}}
             7970
                  }
             7971
             7972 }
             (End definition for knot vert.)
knot horiz
                 \pgfdeclareshape{knot horiz}
             7973
             7974
             7975
                   \inheritsavedanchors[from=rectangle] % this is nearly a circle
             7976
                   \inheritanchorborder[from=rectangle]
                   \inheritanchor[from=rectangle] {north}
                   \inheritanchor[from=rectangle]{north west}
                   \inheritanchor[from=rectangle]{north east}
                   \inheritanchor[from=rectangle]{center}
              7980
                   \inheritanchor[from=rectangle]{west}
             7981
                   \inheritanchor[from=rectangle]{east}
             7982
                   \inheritanchor[from=rectangle]{mid}
             7983
                   \inheritanchor[from=rectangle] {mid west}
             7984
                   \inheritanchor[from=rectangle]{mid east}
             7985
             7986
                   \inheritanchor[from=rectangle]{base}
             7987
                   \inheritanchor[from=rectangle]{base west}
                   \inheritanchor[from=rectangle]{base east}
                   \inheritanchor[from=rectangle]{south}
```

```
\inheritanchor[from=rectangle]{south west}
      \inheritanchor[from=rectangle]{south east}
7991
      \inheritanchorborder[from=rectangle]
      \foregroundpath{
7993
    % store lower right in xa/ya and upper right in xb/yb
7994
        \southwest \pgf@xa=\pgf@x \pgf@ya=\pgf@y
7995
        \northeast \pgf@xb=\pgf@x \pgf@yb=\pgf@y
7996
        \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@ya}}
7997
        \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@ya}}
        \pgfpathmoveto{\pgfqpoint{\pgf@xa}{\pgf@yb}}
        \pgfpathlineto{\pgfqpoint{\pgf@xb}{\pgf@yb}}
8000
    }
8001
8002 }
(End definition for knot horiz.)
```