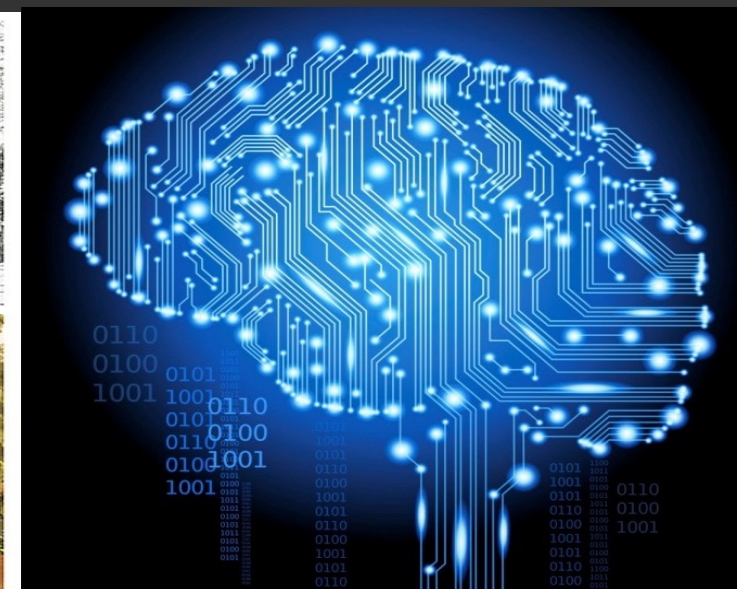
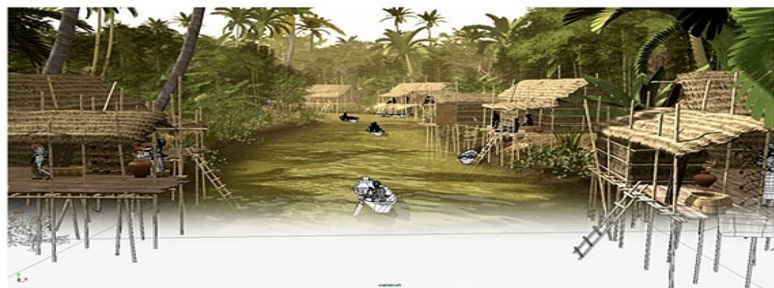
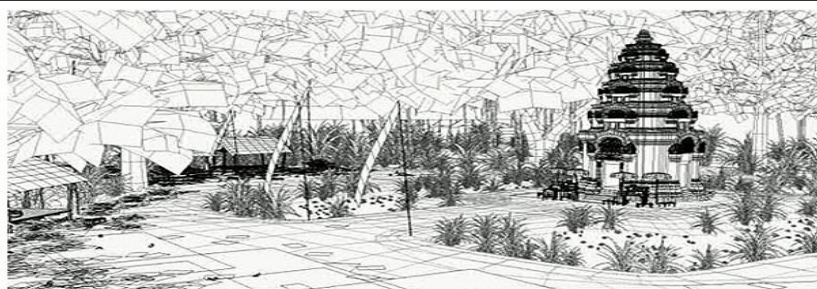




# Linked Lists and Iterators

Prepared by Maria Garcia de la Banda  
Updated by Brendon Taylor



# Objectives for today lesson

- To understand the importance of **iterators**
- To learn how to implement and use them
- To learn to make our classes **iterable** by creating **iterators** on them
- We will probably not have time for a brief look at higher-order programming but, for those interested, have a look at how to implement functions/methods that:
  - Receive functions as arguments
  - Return functions

# Recap: When to use linked nodes, when arrays for lists?

## ▪ Linked Storage

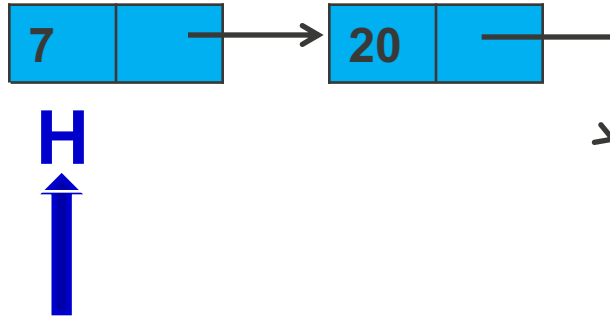
- Unknown list size (no need to resize by copying)
  - If memory is a huge issue though and time is not a problem at all...
- Many insertions and deletions needed within (rather than at the end)
  - If one does not have direct access to the positions though...
- Most operations need traversal of the list from the first element

## ▪ Contiguous Storage

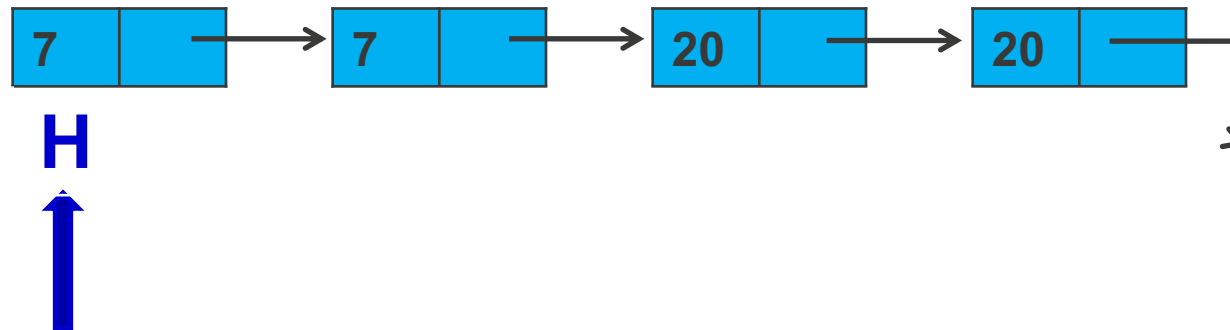
- Known number of elements (no need for links)
- Few insertions and deletions needed within (no shuffling)
- Lots of searches on a sorted list (can use binary search, which is faster)
- Access to elements by their positions (constant time)

# Motivating Iterators

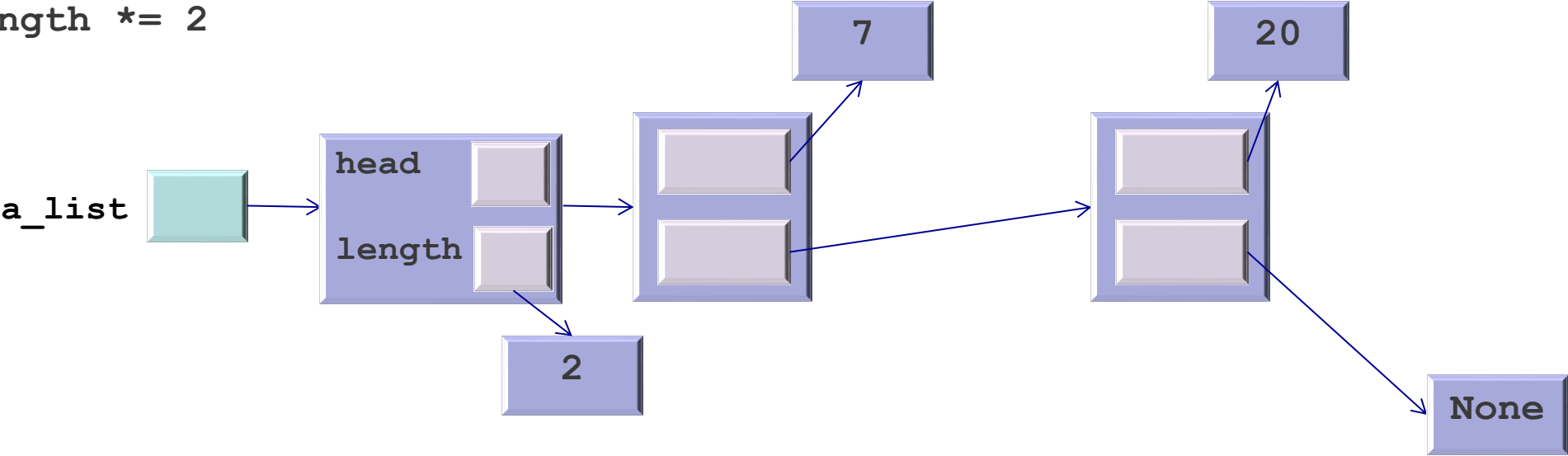
Define a method **inside** the linked class **List** that **modifies** the list by doubling every node. For example, if **a\_list** is:



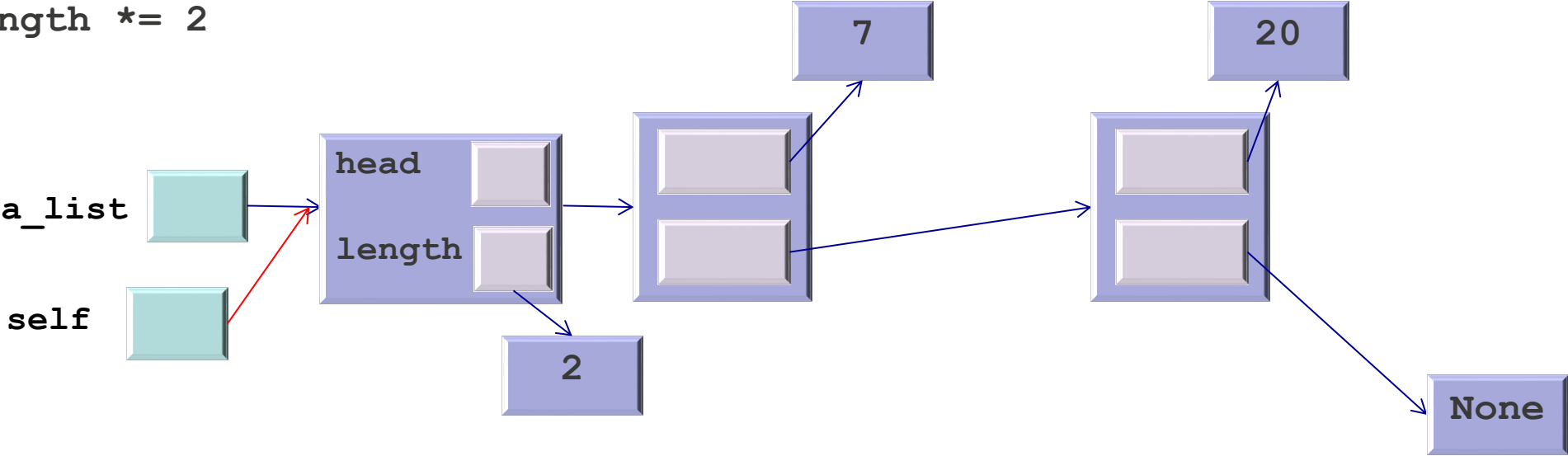
A call to **a\_list.double()** will



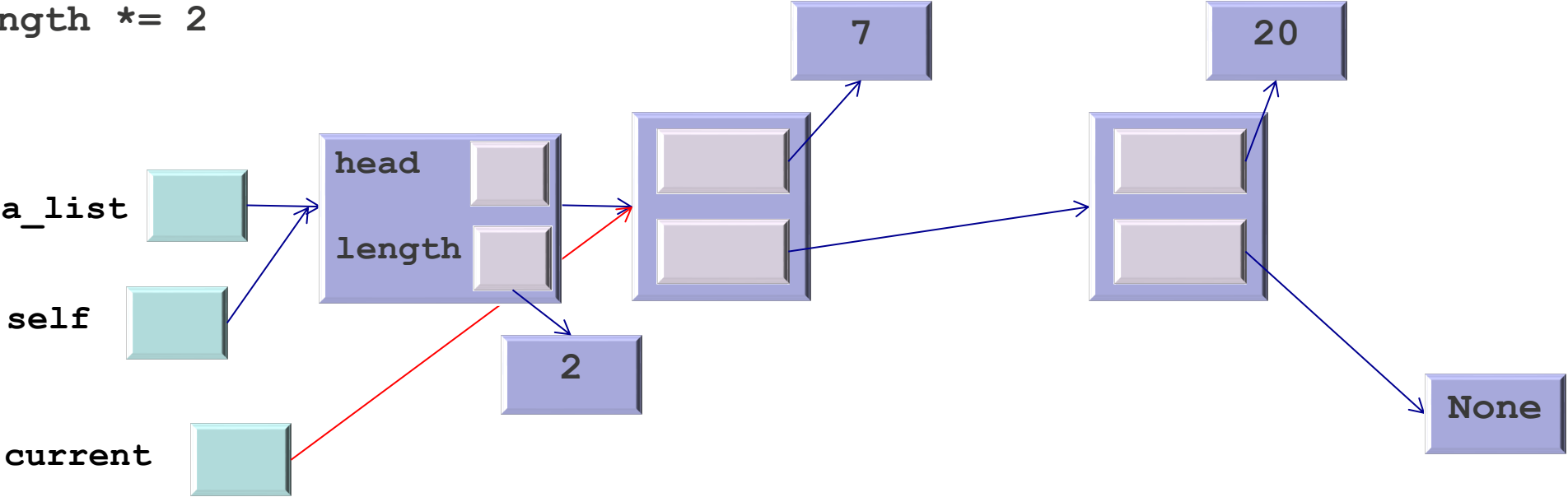
```
def double(self) -> None:
    current = self.head
    for _ in range(len(self)):
        new_node = Node(current.item)
        new_node.link = current.link
        current.link = new_node
        current = new_node.link
    self.length *= 2
```



```
def double(self) -> None:
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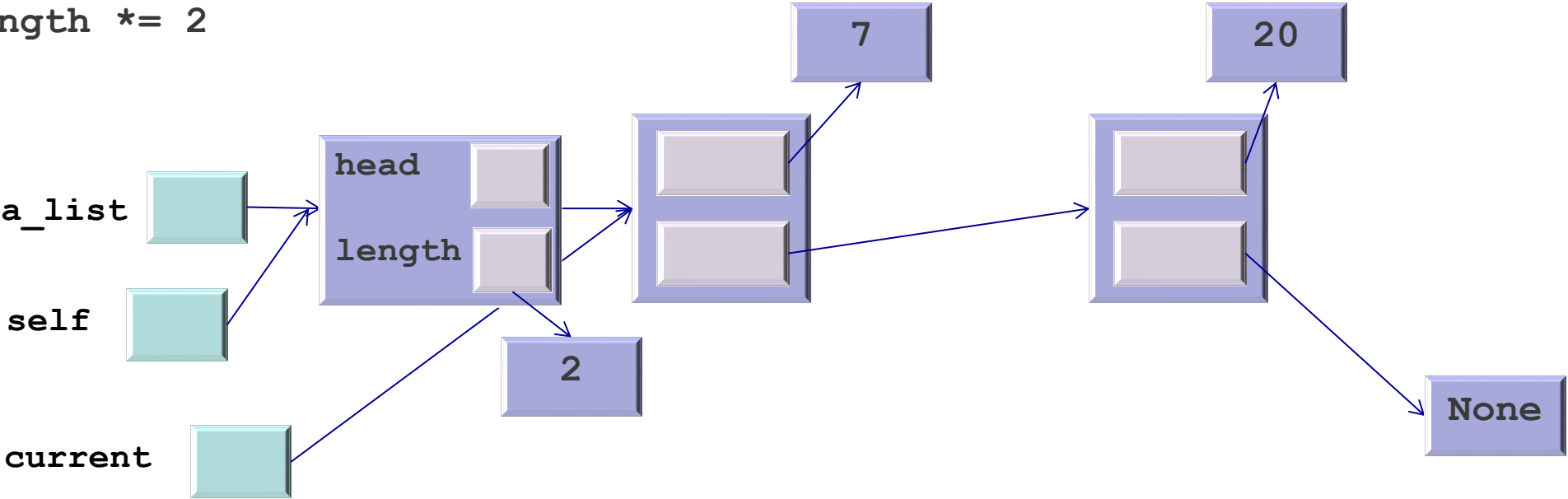


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```

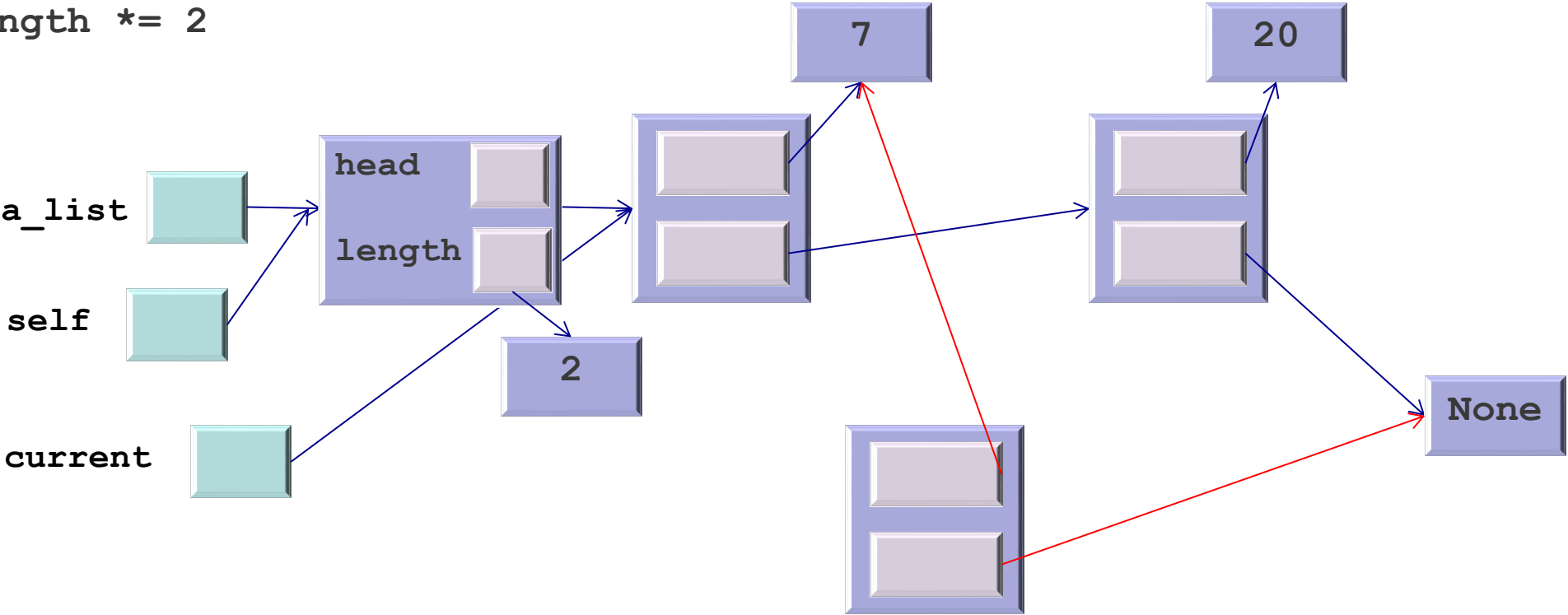




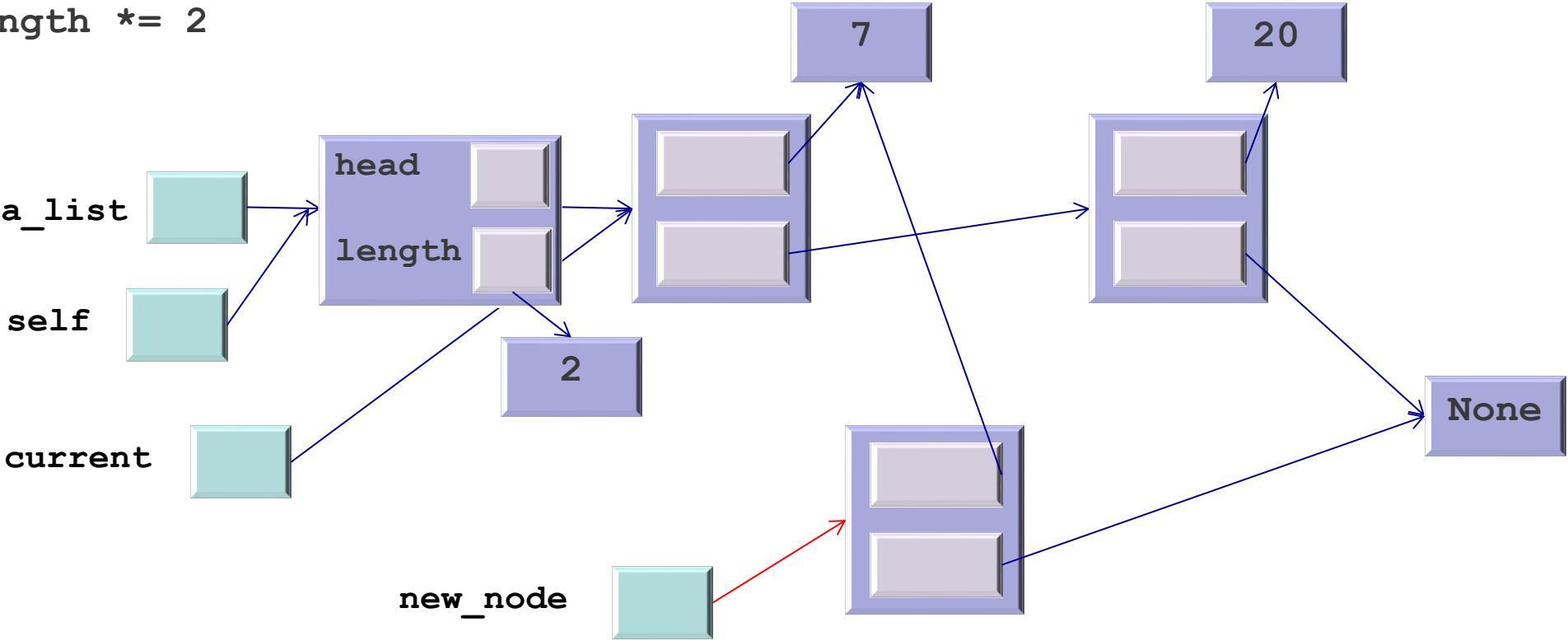
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```



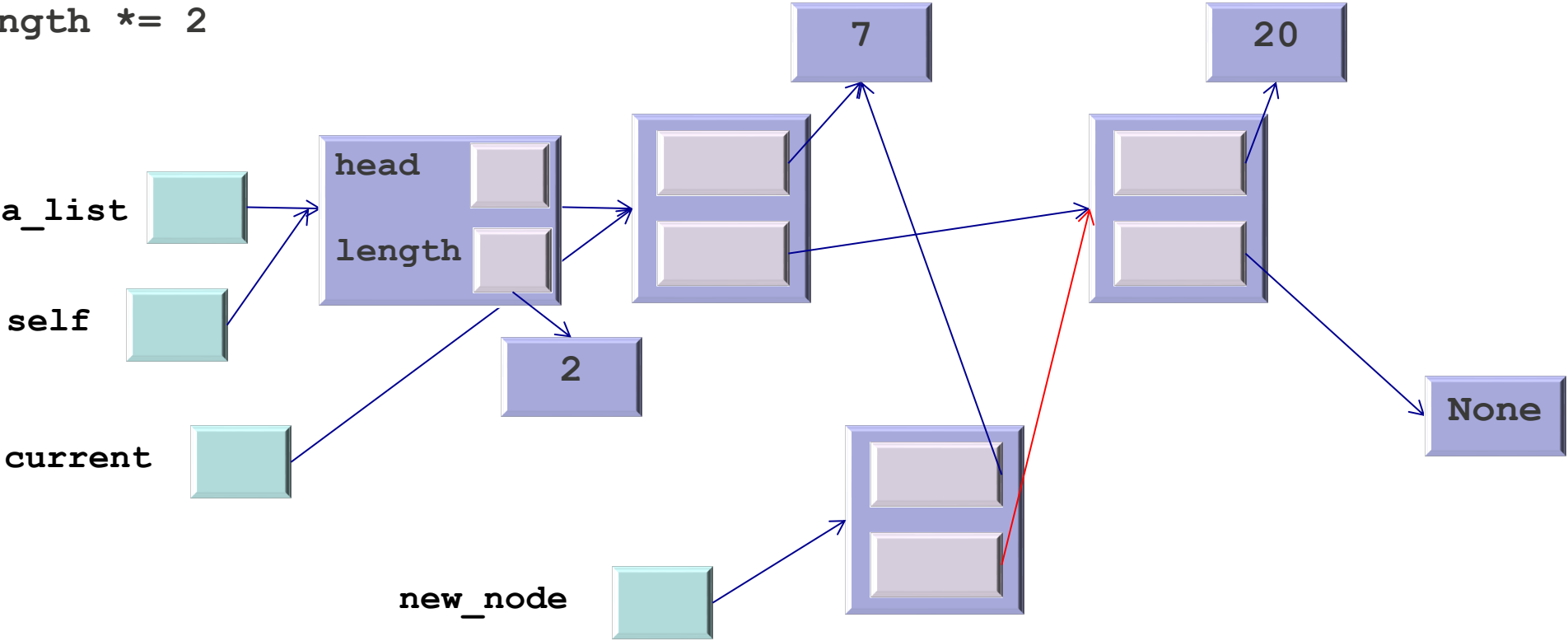
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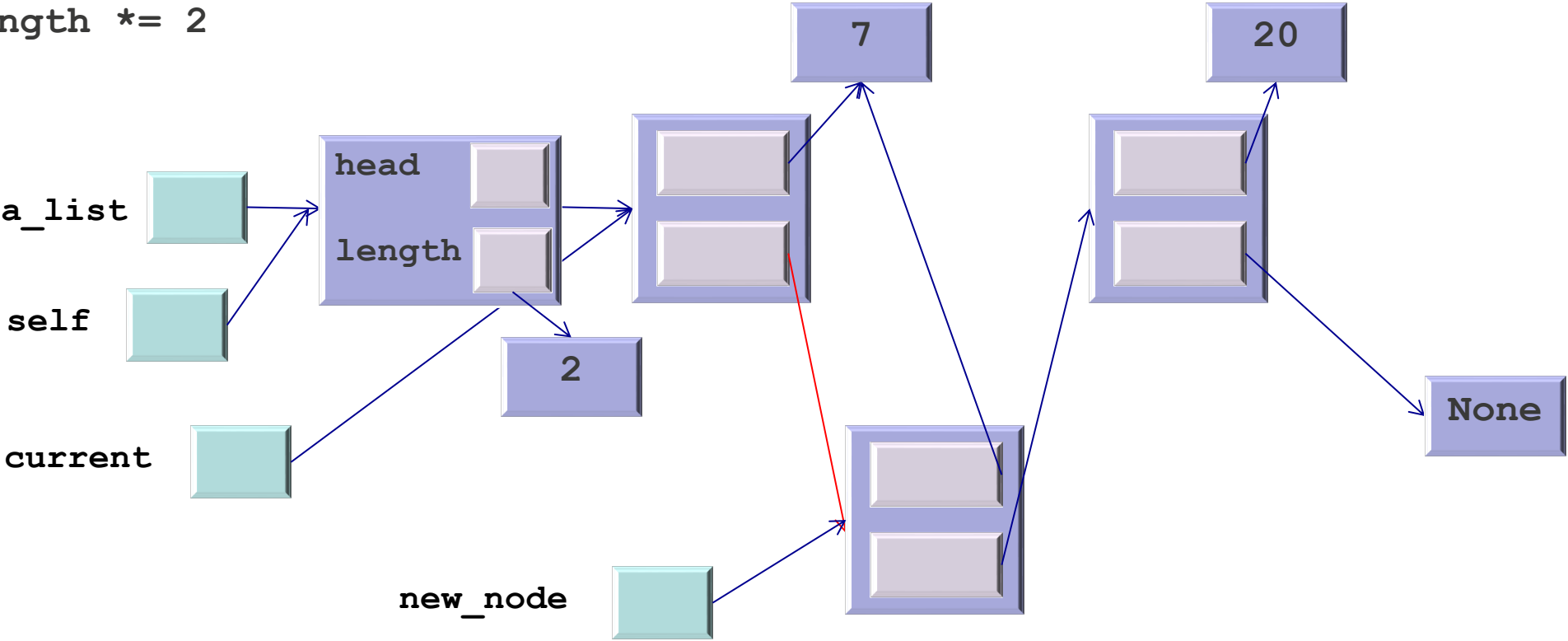
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```



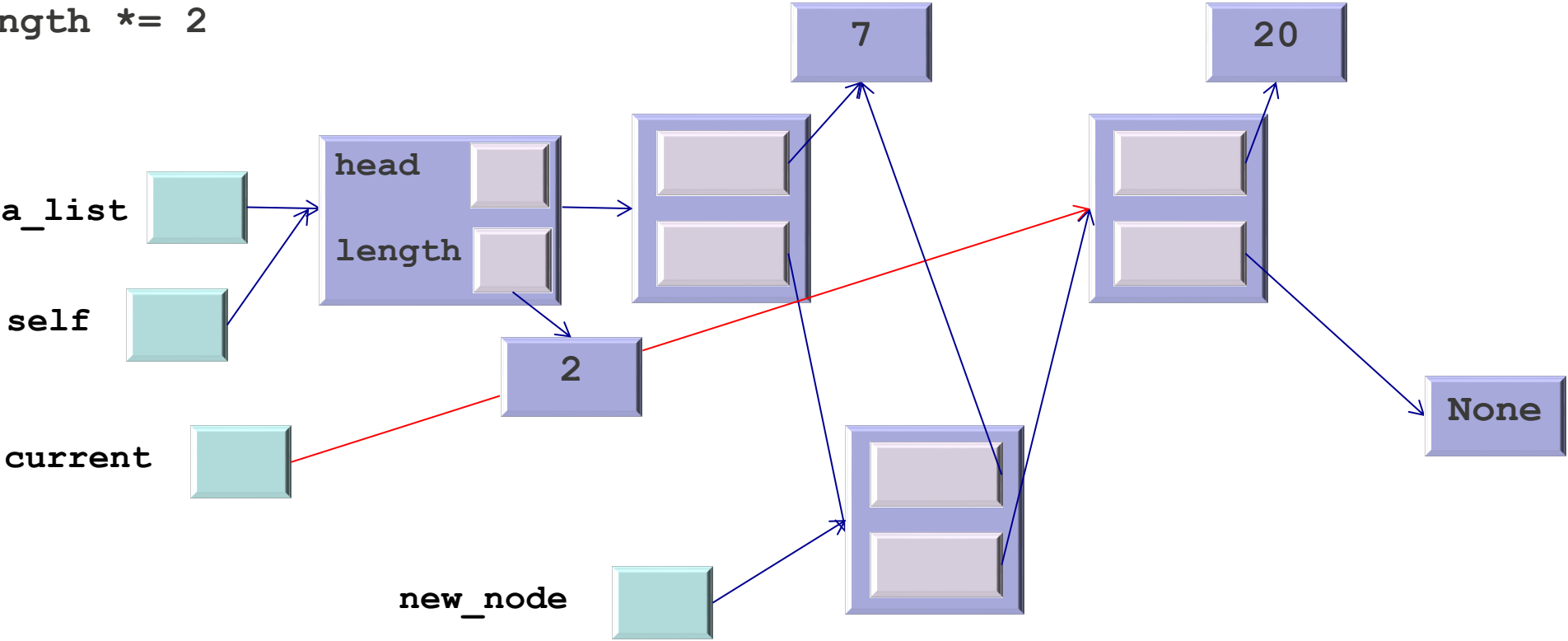
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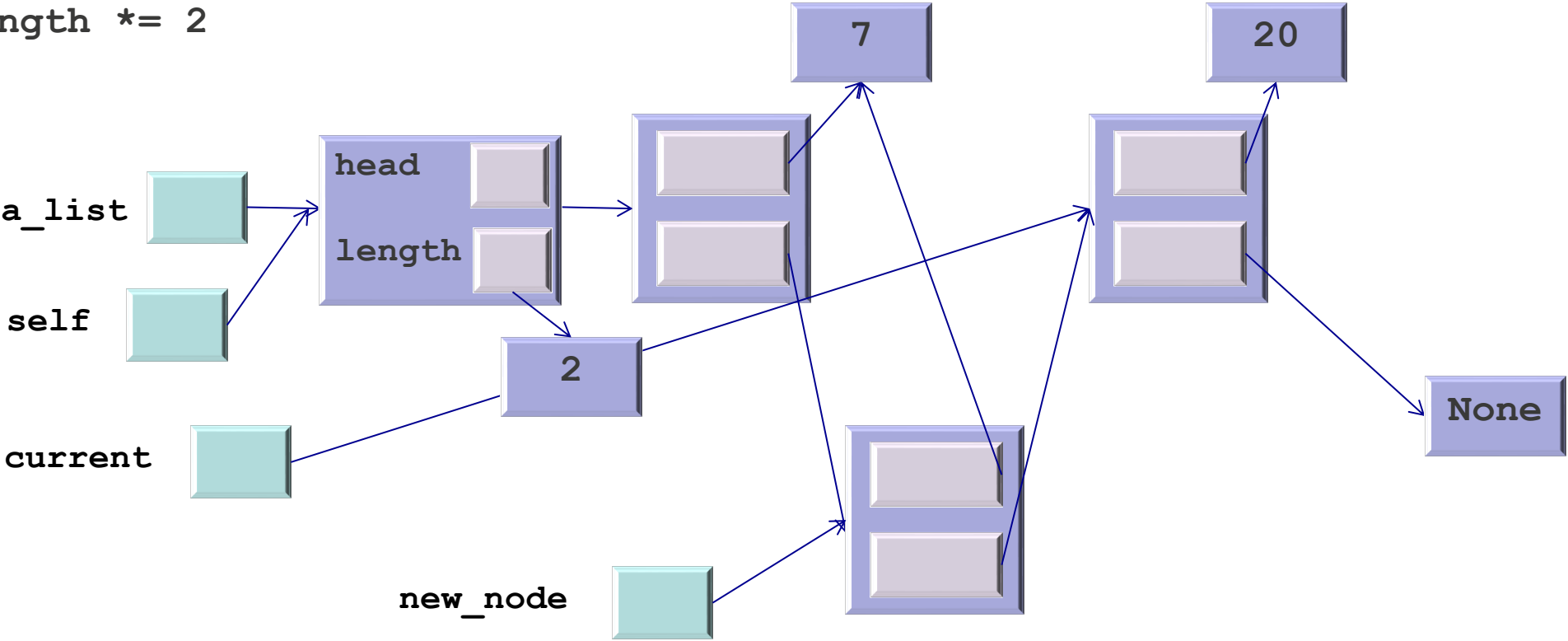
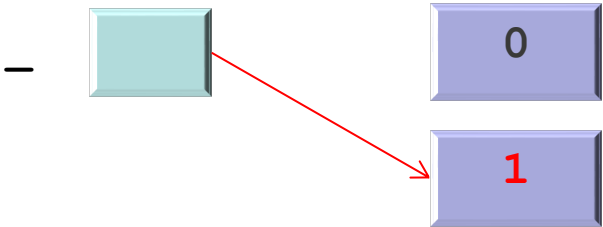
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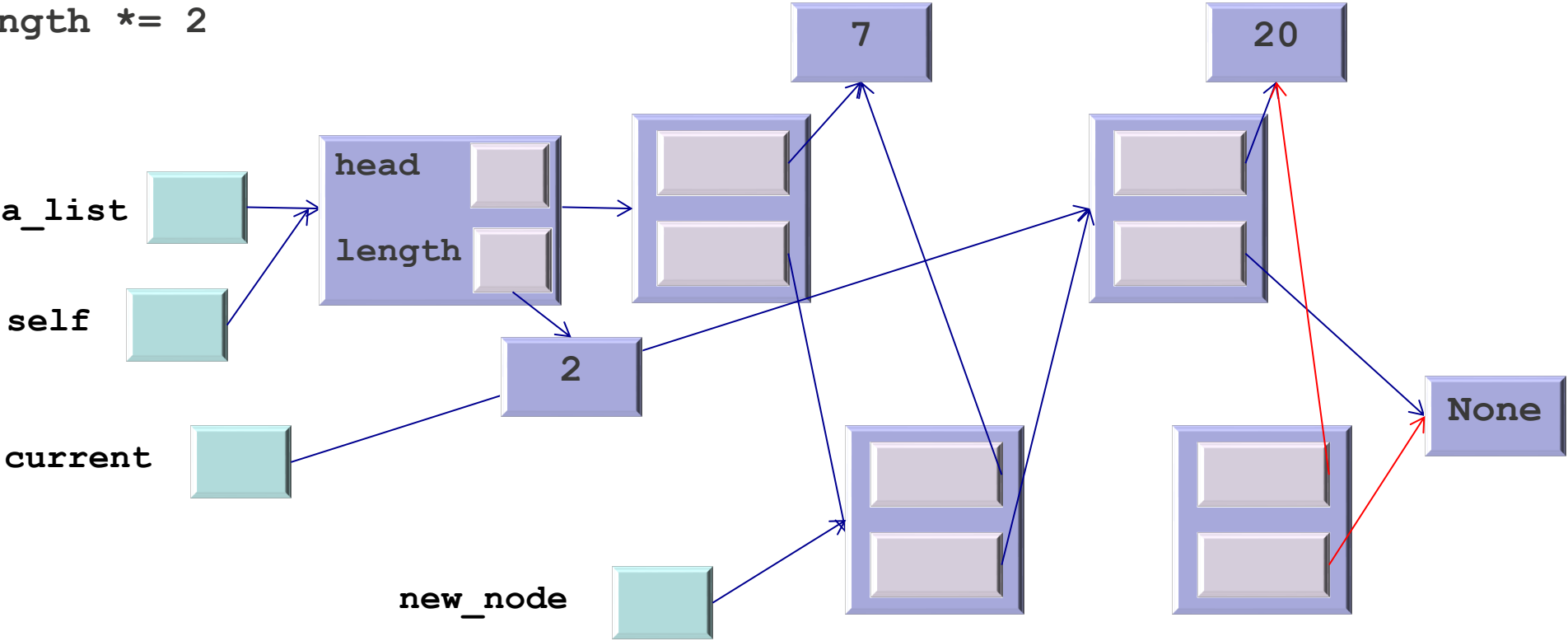
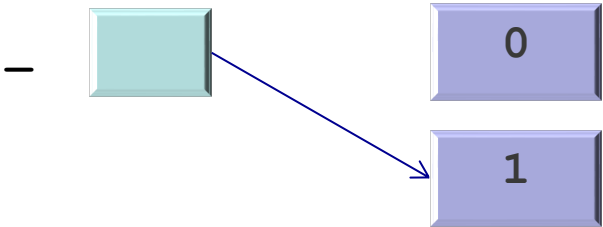
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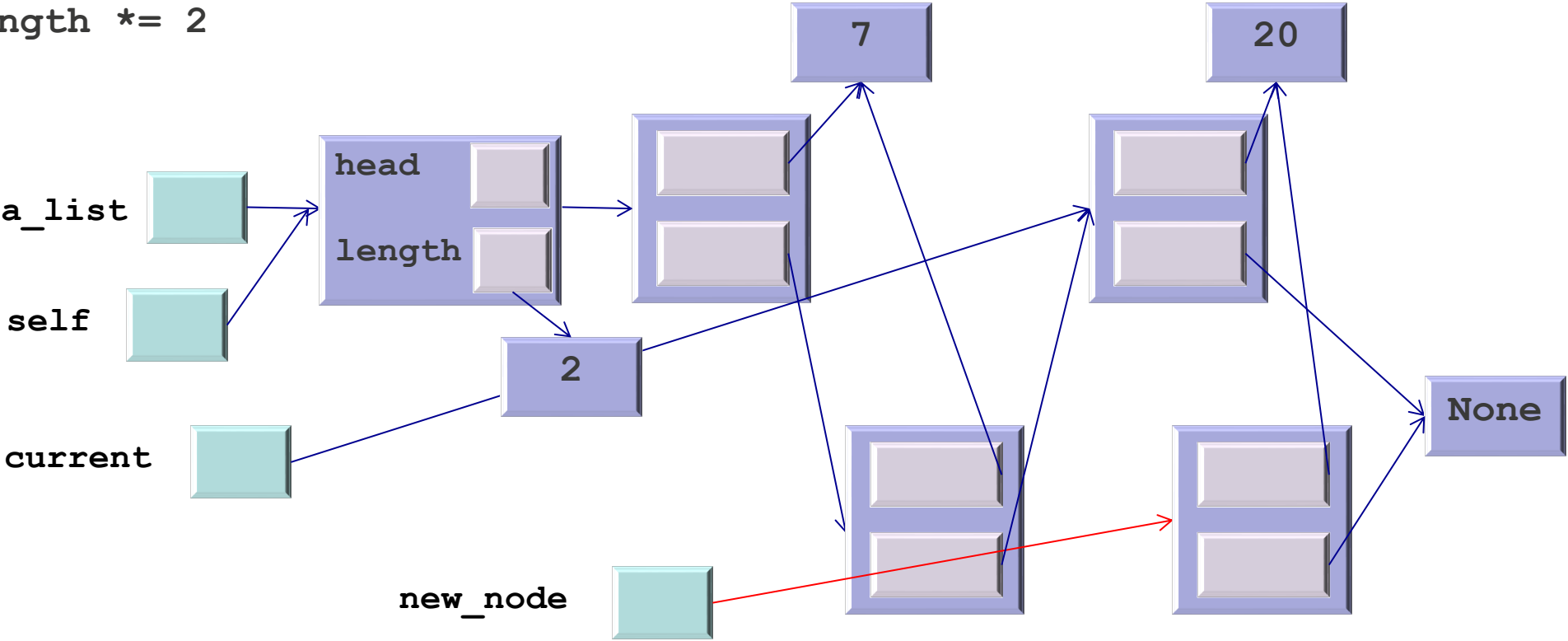
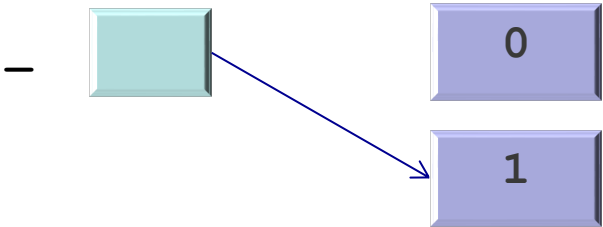


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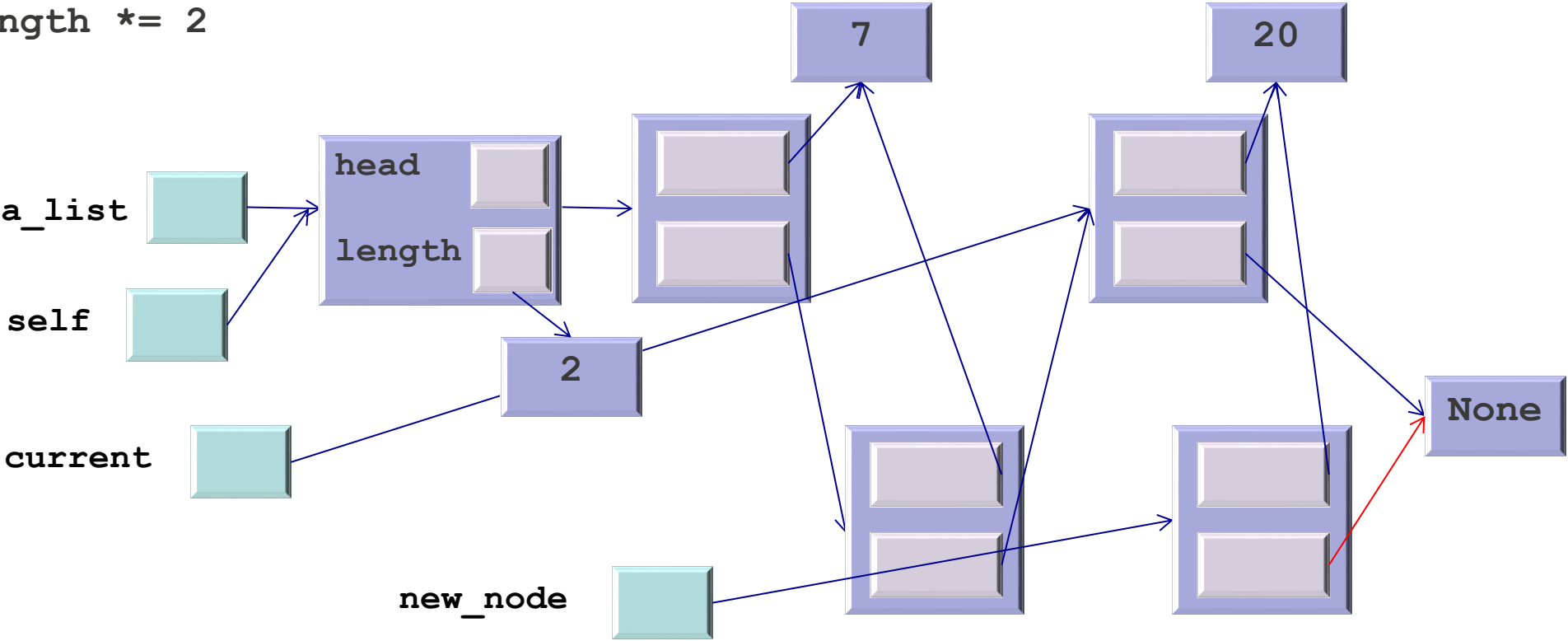
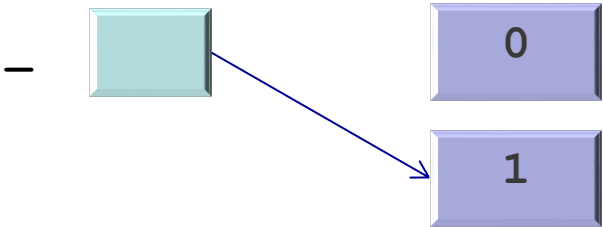




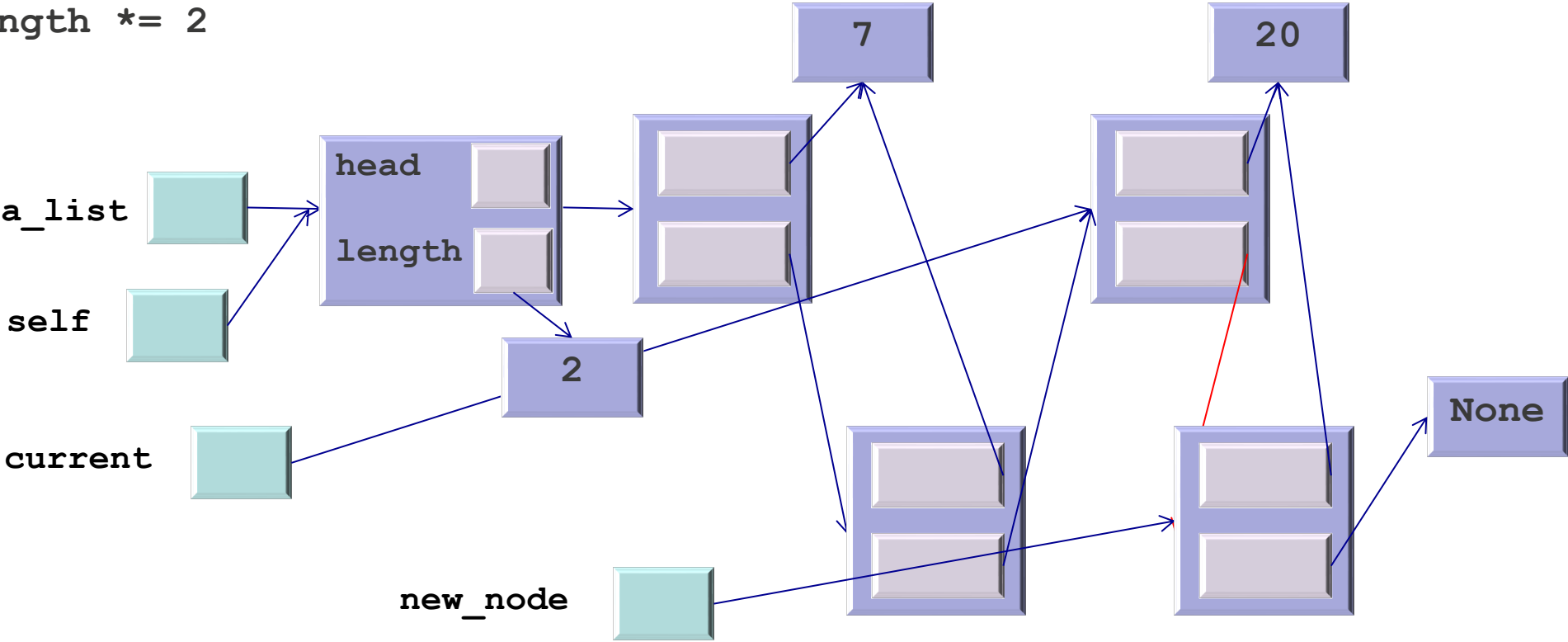
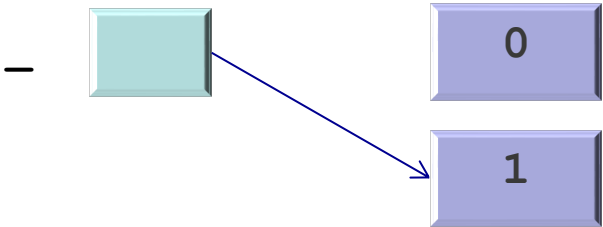
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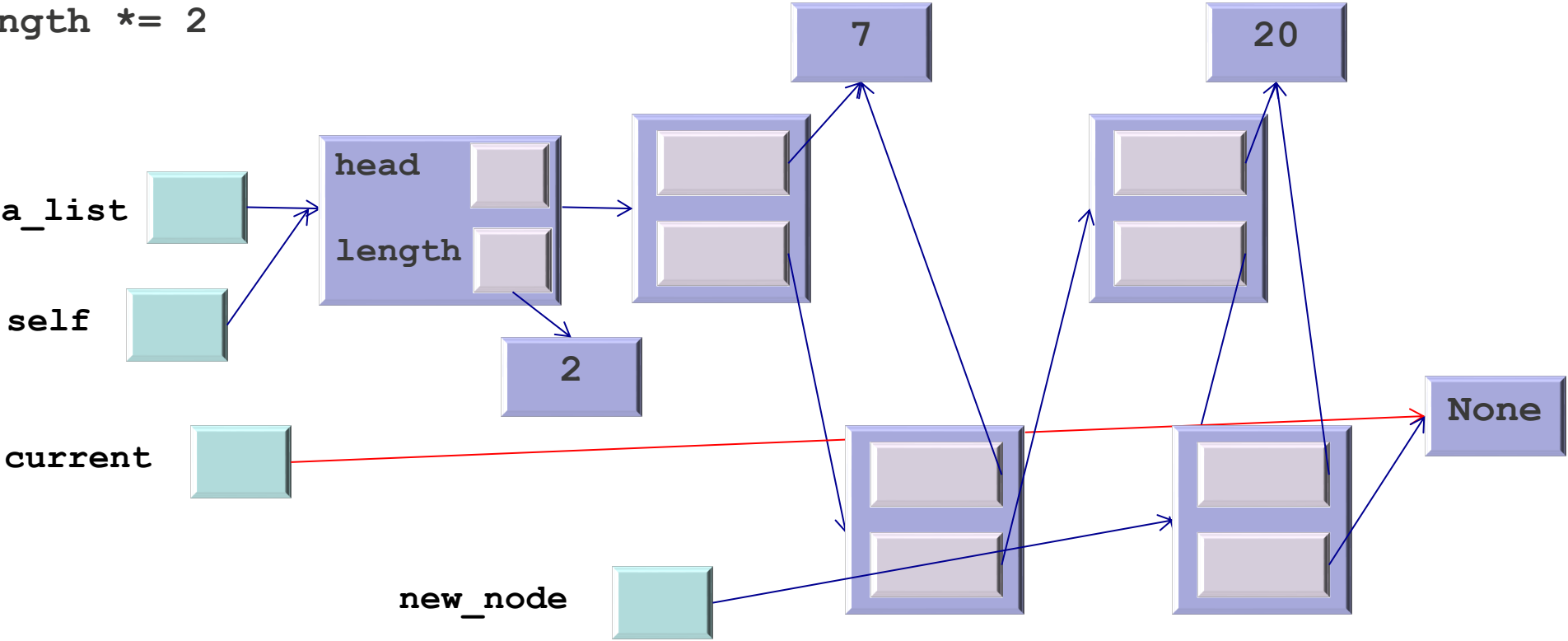
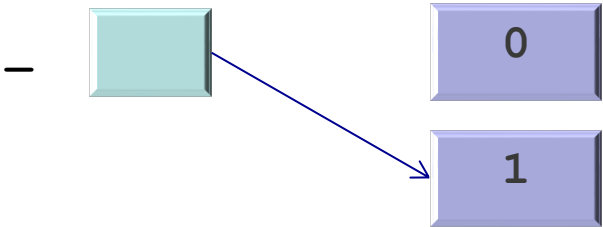
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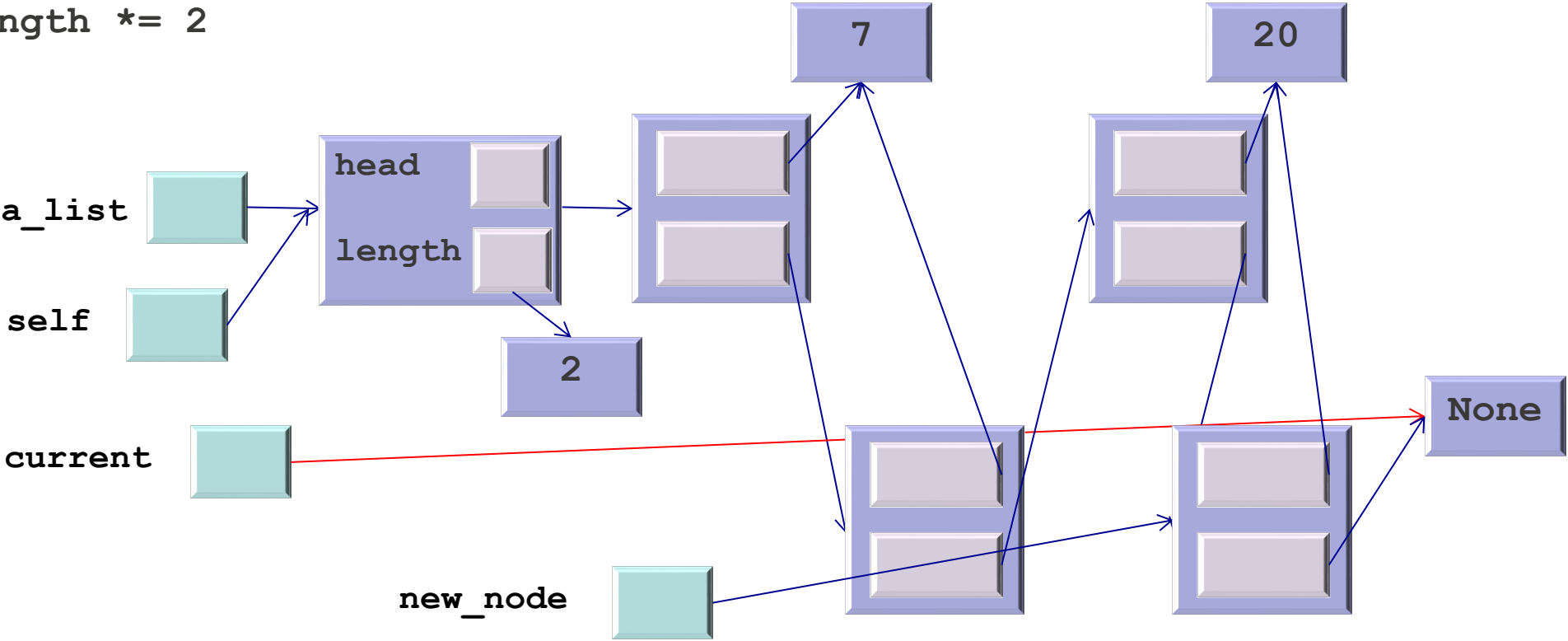
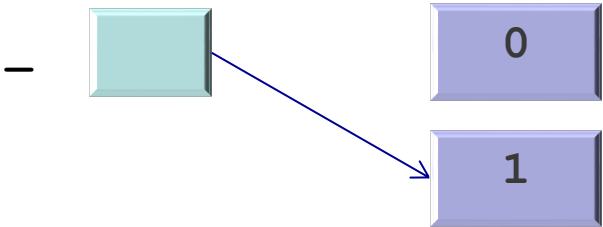


Diagram illustrating a subtraction operation. A minus sign is followed by a light blue square box. An arrow points from the box to a purple box labeled '0'. Below the arrow is a purple box labeled '1'.

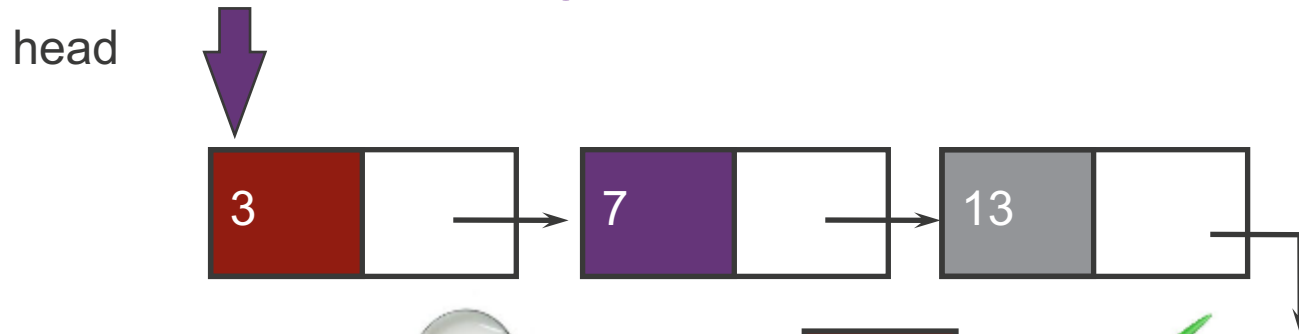


# Motivation for iterators

- **How can we define `double()` from outside the class?**
  - Need to traverse the list
  - Need to add nodes into a list
- **How would we even traverse the list from outside the class?**
  - We would have to access `self.link`
  - This means accessing the implementation (not very abstract!)

# Traversing a list as a user

- What do users do when they need to check all elements are  $>0$ ?



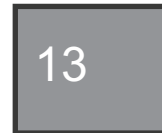
Next!



Next!



Next!



Next! No more!

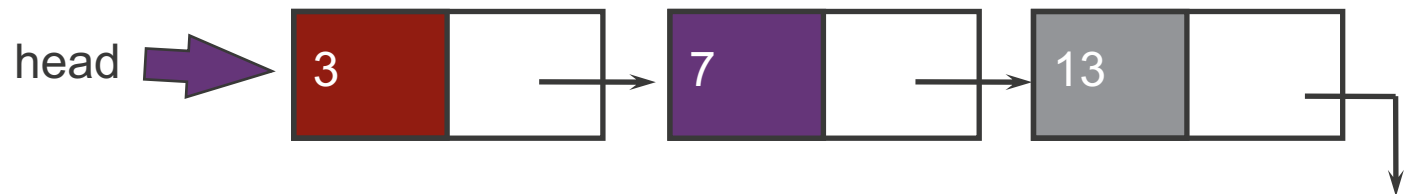
Handled differently in different languages. In Python: raise `StopIteration`



# Implementing Iterators

# How do we do this?

- **We need a way of creating an iterator object to start the iterations**
  - An object **other than the list** because:
    - It needs to change (move through the list) without changing the list
    - We might need several iterators on a list
  - In Python, iterator objects are returned by method `__iter__`
- **This means we need an iterator class to create the objects:**
  - Its `__init__` performs the “beginning-of-iteration” initialisation
    - In our example: it makes sure we start from 3
- **The class needs a way of returning the next element**
  - In our example, first 3, then 7, then 13, and then `StopIteration`
  - In Python, this is implemented by the `__next__` method



# How does this work from the outside?

- Python lists and strings (among others) are **iterable**:

Overloaded function. Python finds the `__iter__` from the `String` class

```
>>> x = "abc"
>>> it1 = iter(x)
>>> it1
<iterator object at 0x10a9f2>
>>> next(it1)
'a'
>>> next(it1)
'b'
>>> it2 = iter(x)
>>> next(it2)
'a'
>>> next(it1)
'c'
```

it1 is an  
iterator, not  
a list

it1 and it2 are different  
objects and, thus, independent

```
>>> next(it1)
Traceback (most recent call last):
  File "<stdin>", line 1, in
<module>
StopIteration
>>> next(it2)
'b'
>>> next(it2)
'c'
>>> next(it2)
Traceback ...StopIteration
>>> x
'abc'
```

x has not changed at all!

# How do we make the LinkedList class **iterable**?

- We need to create an **iterator class** for the list
  - A class with the `__init__`, `__iter__` and `__next__` methods

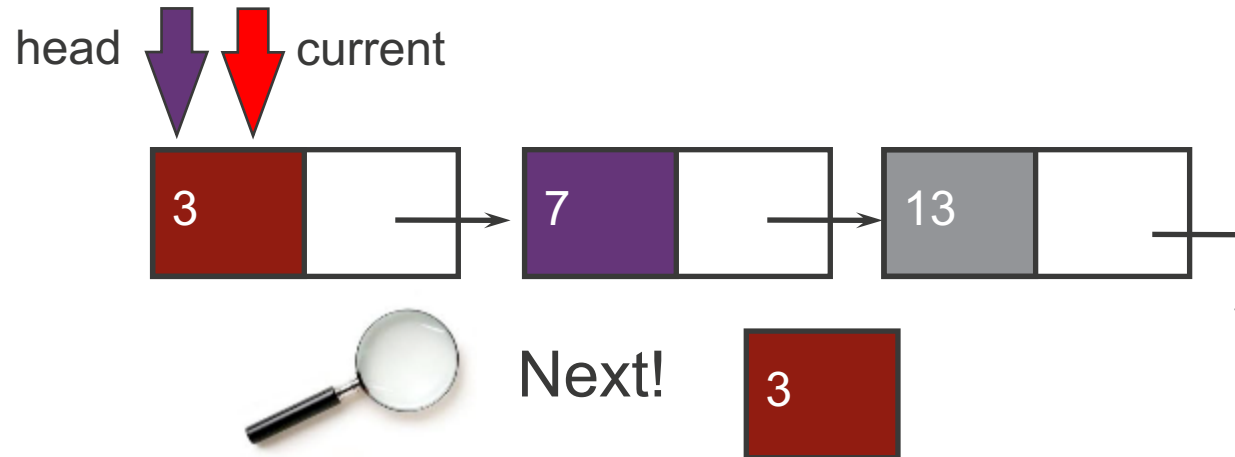
```
class LinkedListIterator(Generic[T]):  
    def __init__(self, node: Node[T]) -> None:  
        self.current = node  
  
    def __iter__(self):  
        return self  
  
    def __next__(self) -> T:
```

Takes a list node as argument, and initialises the iterator to start at that node

Must return an object with a `__next__` method. This one simply returns itself

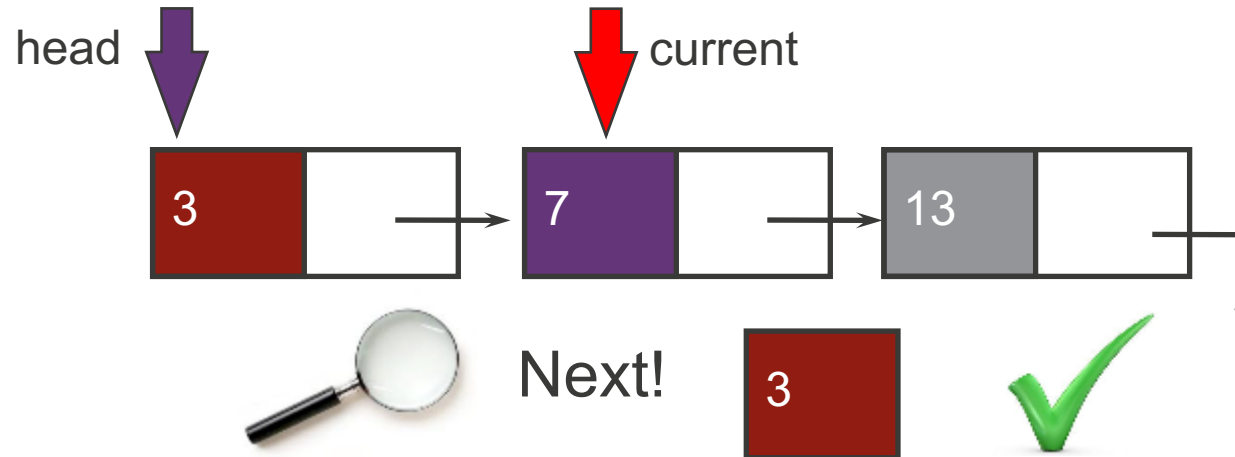
# How do we implement `__next__`?

- We need a reference **current** that starts at the **head**



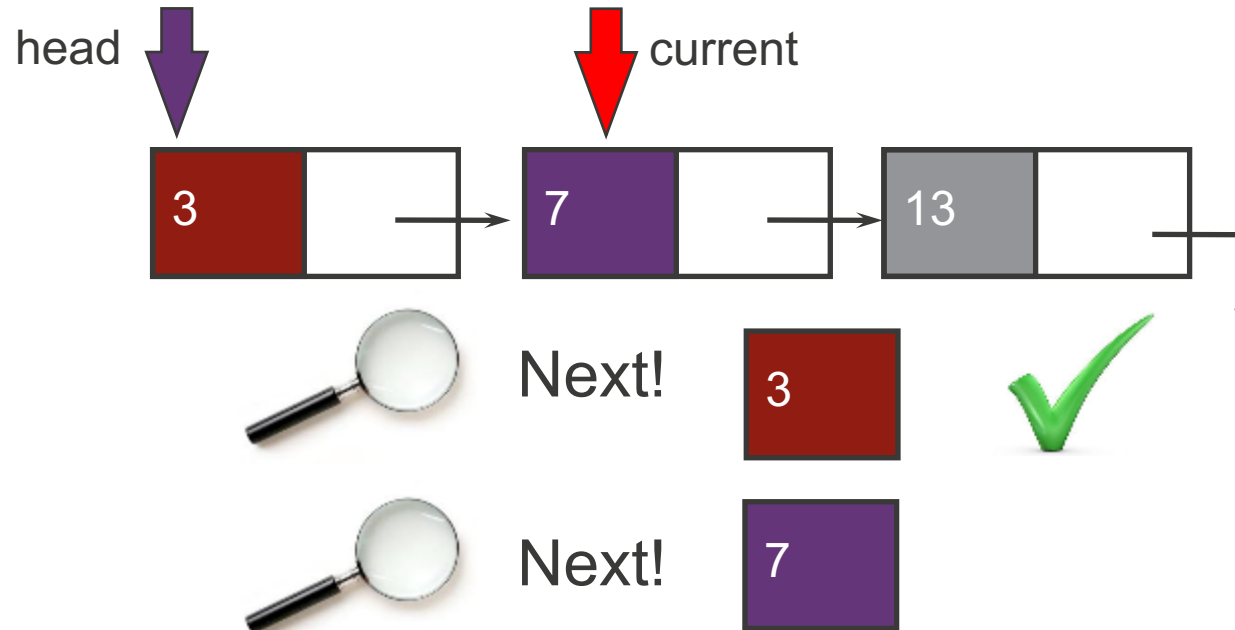
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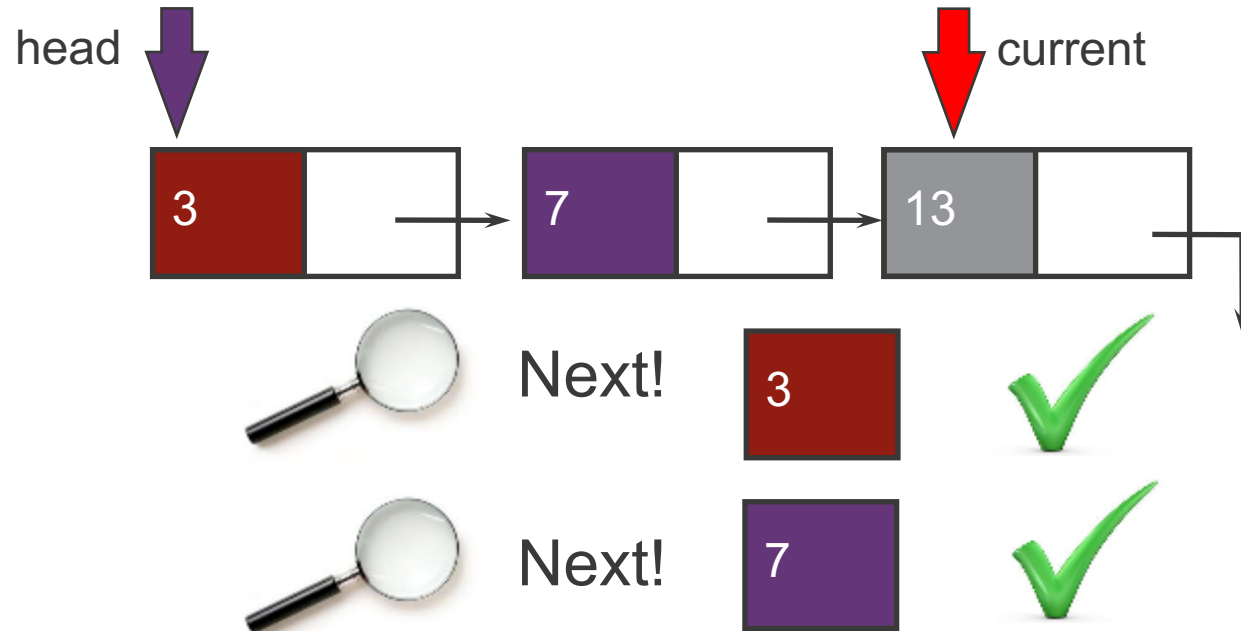
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# How do we implement `__next__`?

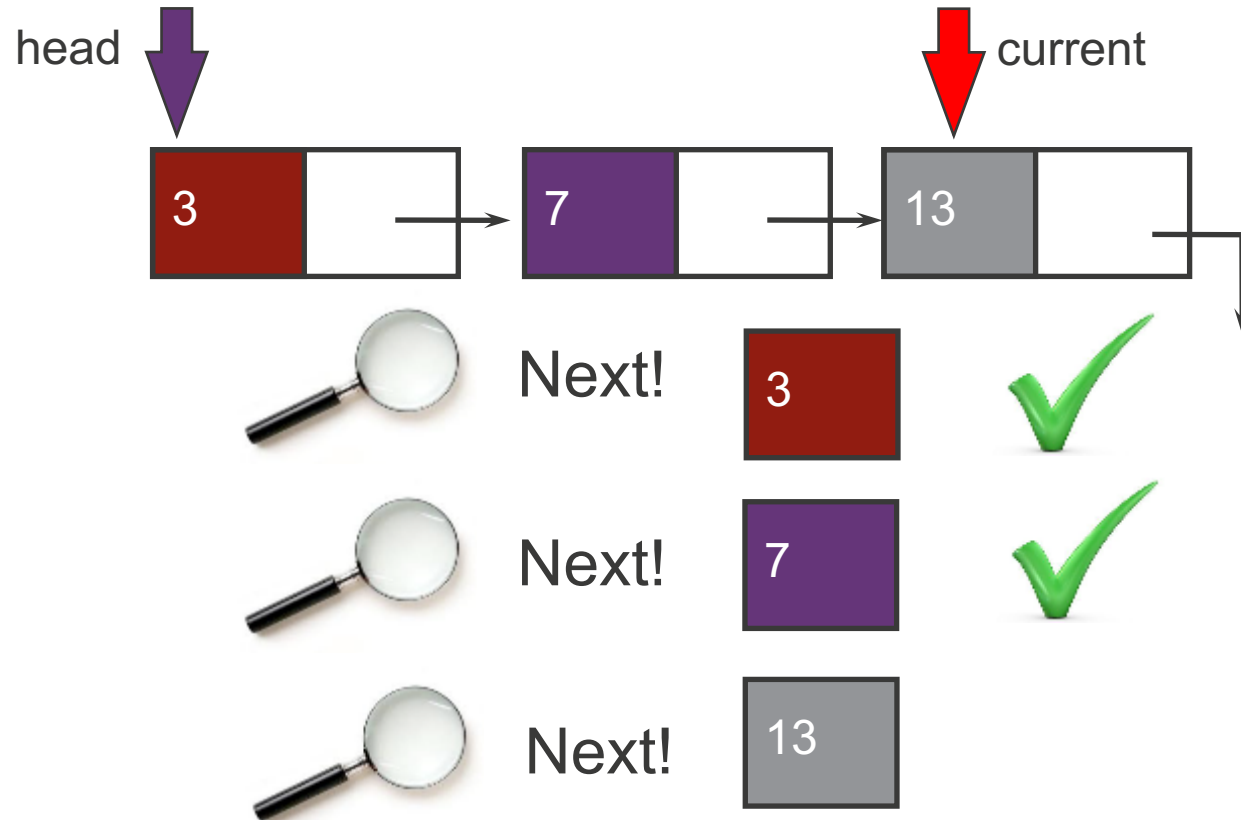
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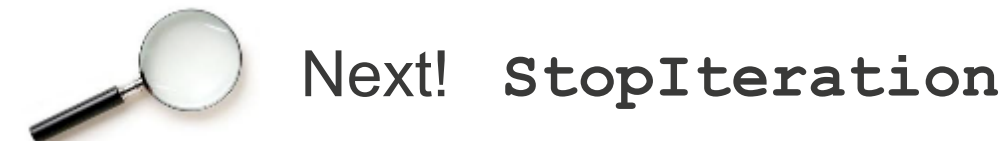
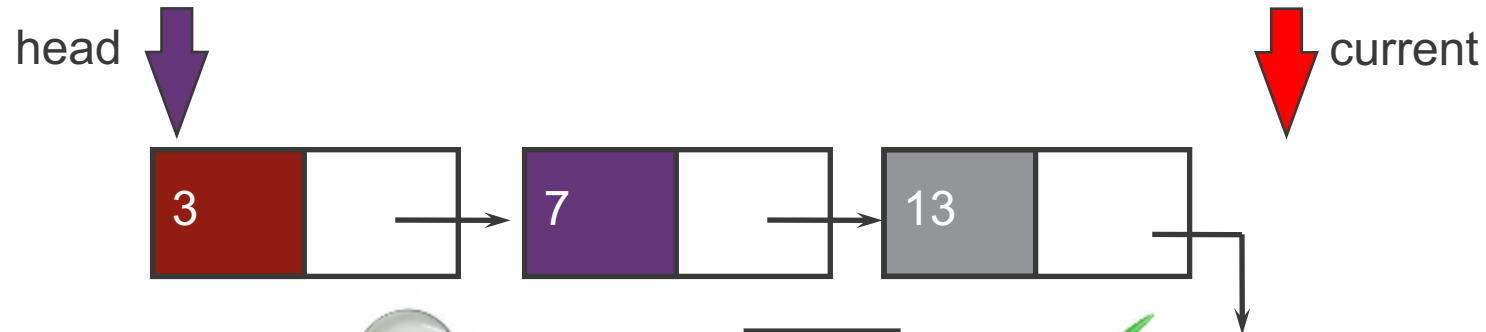
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- We need a reference **current** that starts at the **head**



# How do we implement `__next__`?

- We need a reference `current` that starts at the `head`



# How do we make the List class **iterable**?

- We need to create an **iterator class** for the list

- A class with the `__init__`, `__iter__` and `__next__` methods

```
class LinkedListIterator(Generic[T]):  
    def __init__(self, node: Node[T]) -> None:  
        self.current = node  
  
    def __iter__(self):  
        return self  
  
    def __next__(self) -> T:  
        if self.current is not None:  
            item = self.current.item  
            self.current = self.current.link  
            return item  
        else:  
            raise StopIteration
```

Takes a list node as argument, and initialises the iterator to start at that node

Must return an object with a `__next__` method. This one simply returns itself

If not finished, remember current item and advance

Why not `self.current != None`?

Because users might have re-defined `__eq__(self, rhs)`

If finished, raise `StopIteration`

# An equivalent way of defining `__next__`

- We have defined `__next__` as:

```
def __next__(self) -> T:
    if self.current is not None:
        item = self.current.item
        self.current = self.current.link
        return item
    else:
        raise StopIteration
```

- But we could also have said:

```
def __next__(self) -> T:
    try:
        item = self.current.item
    except AttributeError:
        raise StopIteration
    else:
        self.current = self.current.link
        return item
```

Which one is better? Whichever one is clearer (different people...)

# How is this connected to the LinkList class?

- The `LinkList` class needs to have an `__iter__` method too
- Which does what?
  - Return a list iterator object initialised to the head of the list

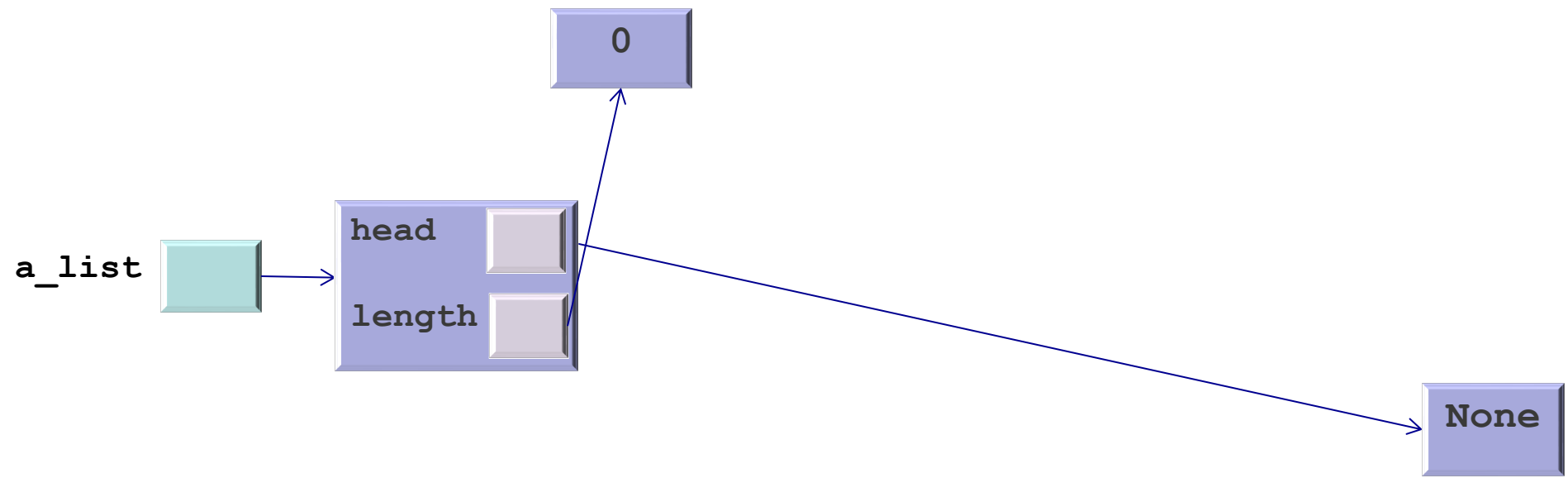
```
class LinkList(List[T]):
```

```
    ...  
    def __iter__(self) -> LinkListIterator[T]:  
        return LinkListIterator(self.head)
```

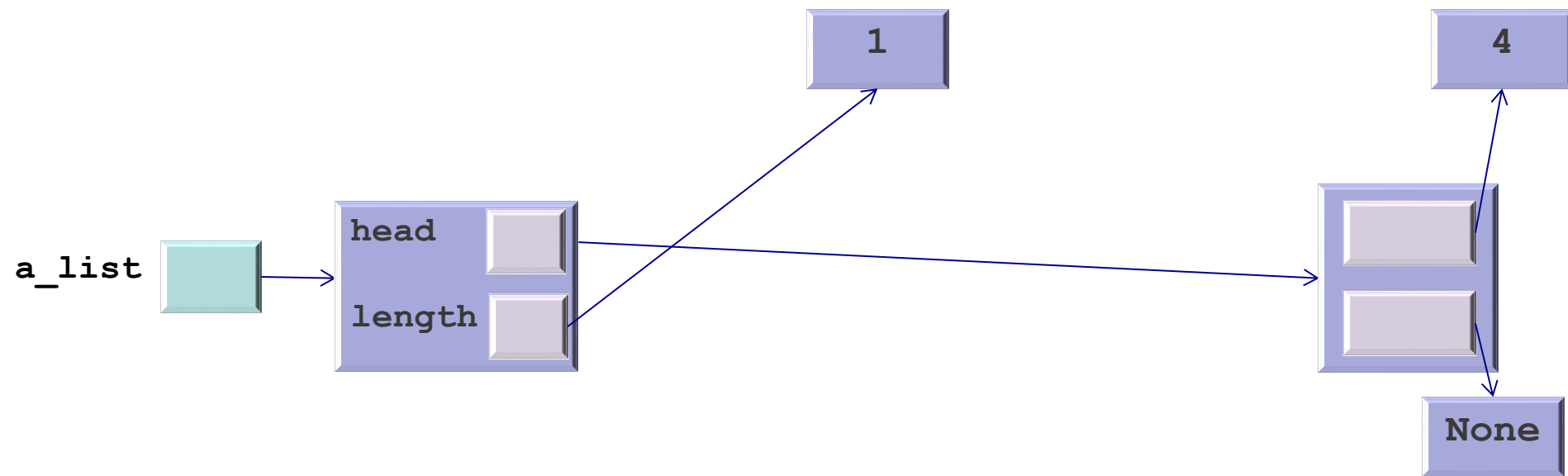
Somewhere inside the `List` class

This points to the `List` object

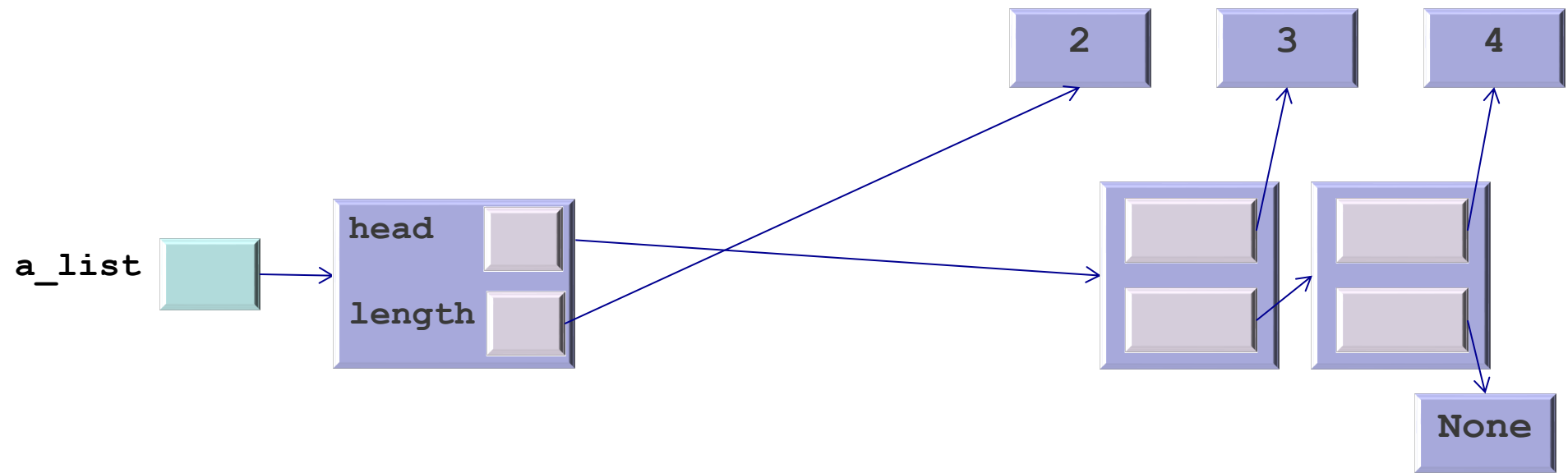
This points to a `Node` object (the one at the head of the list), which remember, is the input argument for the `__init__` in the `LinkListIterator` class



```
>>> a_list = LinkedList()
>>> a_list.insert(0,4)
```

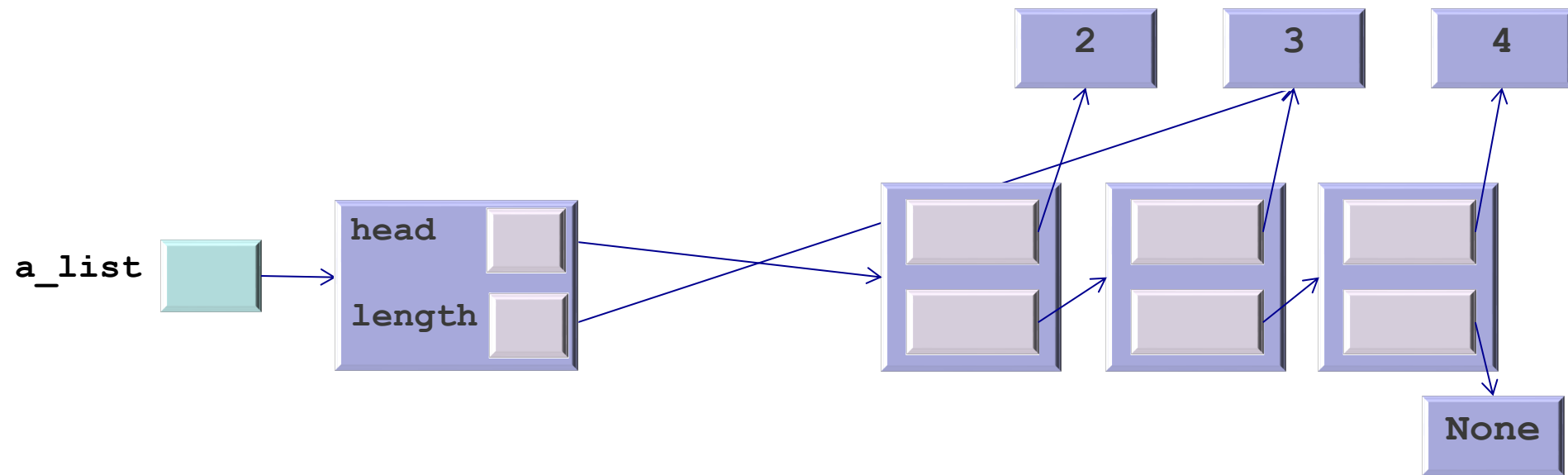


```
>>> a_list = LinkedList()
>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
```

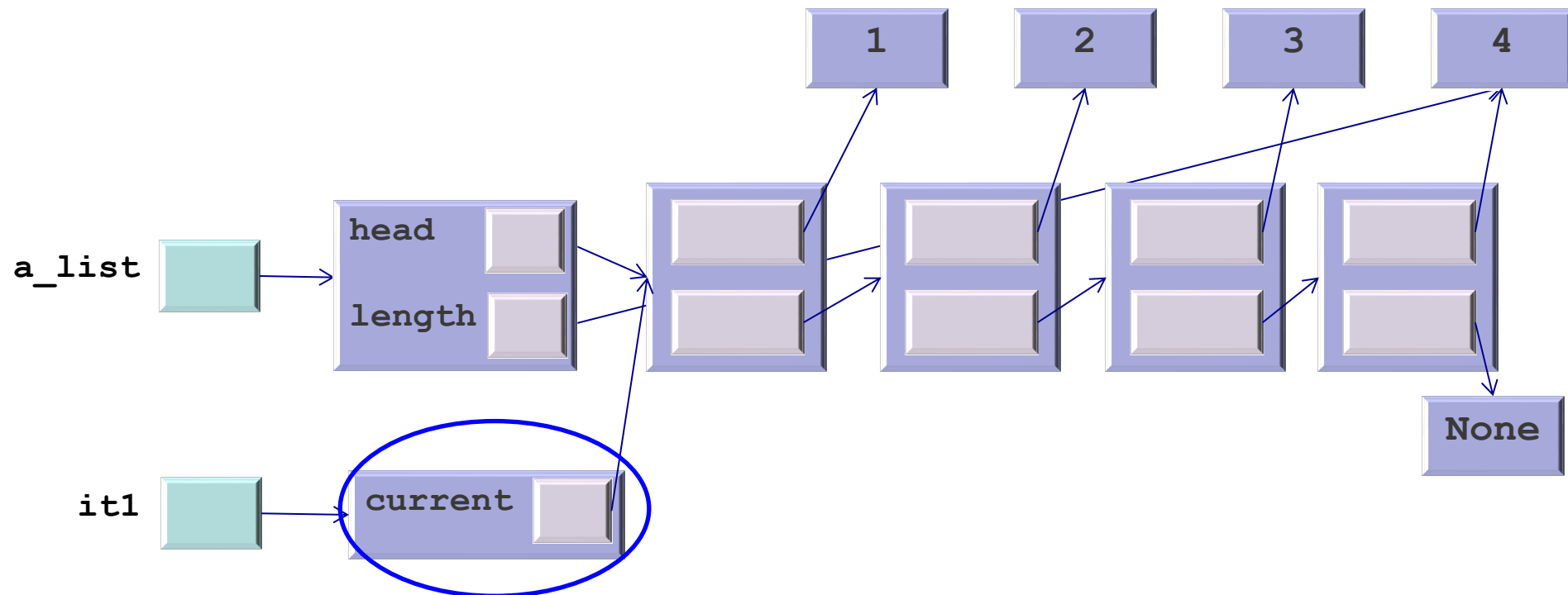


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>>> a_list = LinkList()
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>>> a_list.insert(0,2)
```





```
>>> a_list = LinkList()
>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
>>> a_list.insert(0,2)
>>> a_list.insert(0,1)
```



This is my `LinkListIterator` object

```

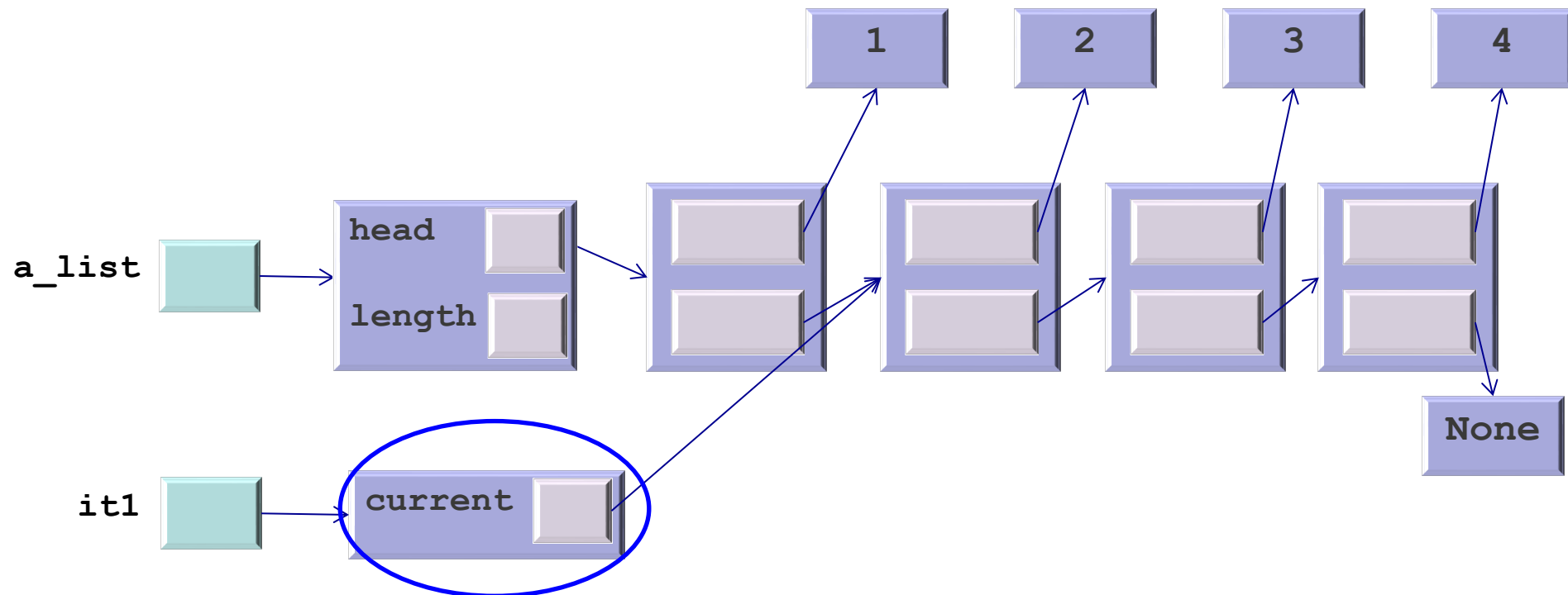
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>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
>>> a_list.insert(0,2)
>>> a_list.insert(0,1)
>>> it1 = iter(a_list)
>>> next(it1)

```

```

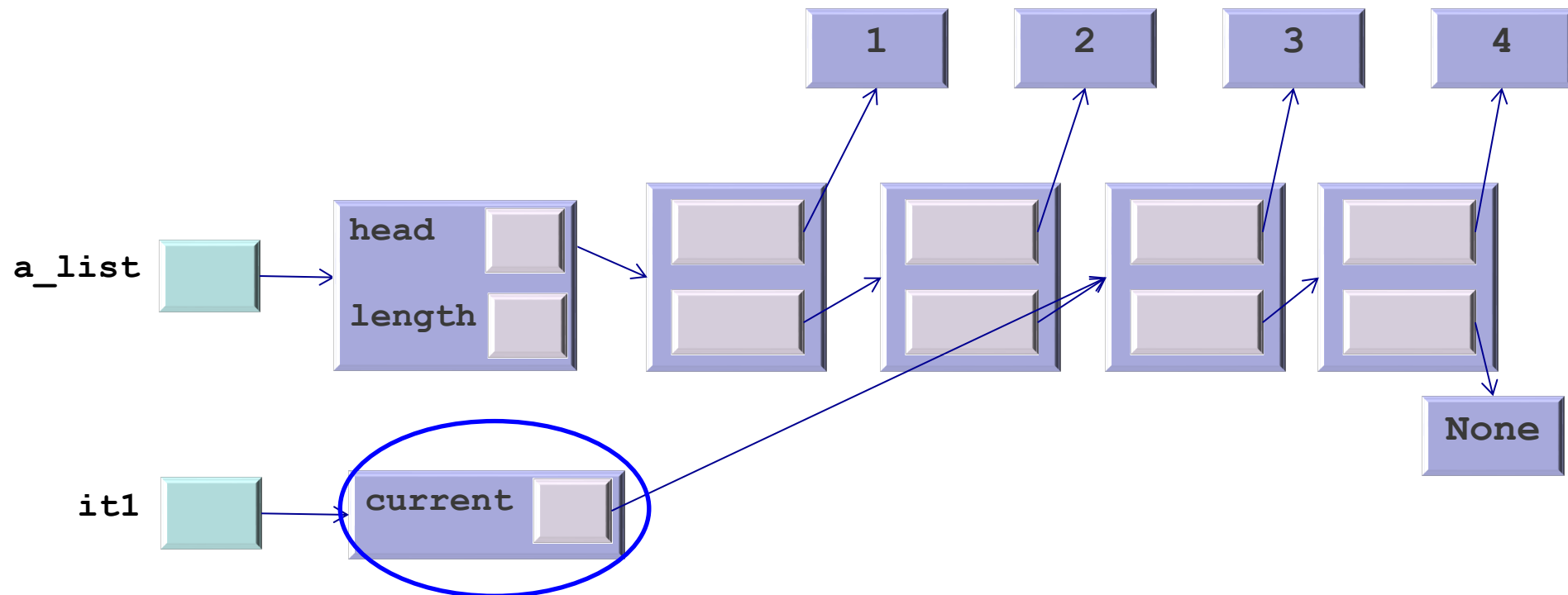
def __next__(self) -> T:
    if self.current is not None:
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        return item
    else:
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```



This is my `LinkListIterator` object

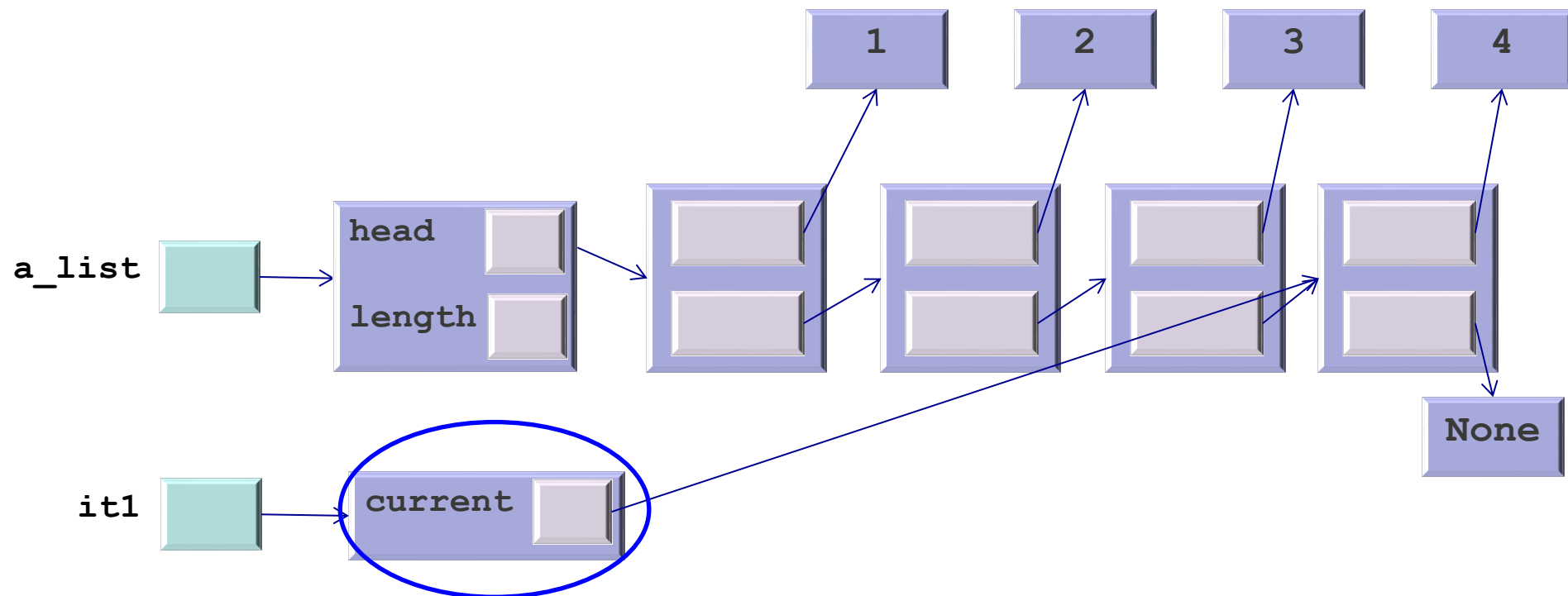
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>>> next(it1)
1
>>> next(it1)
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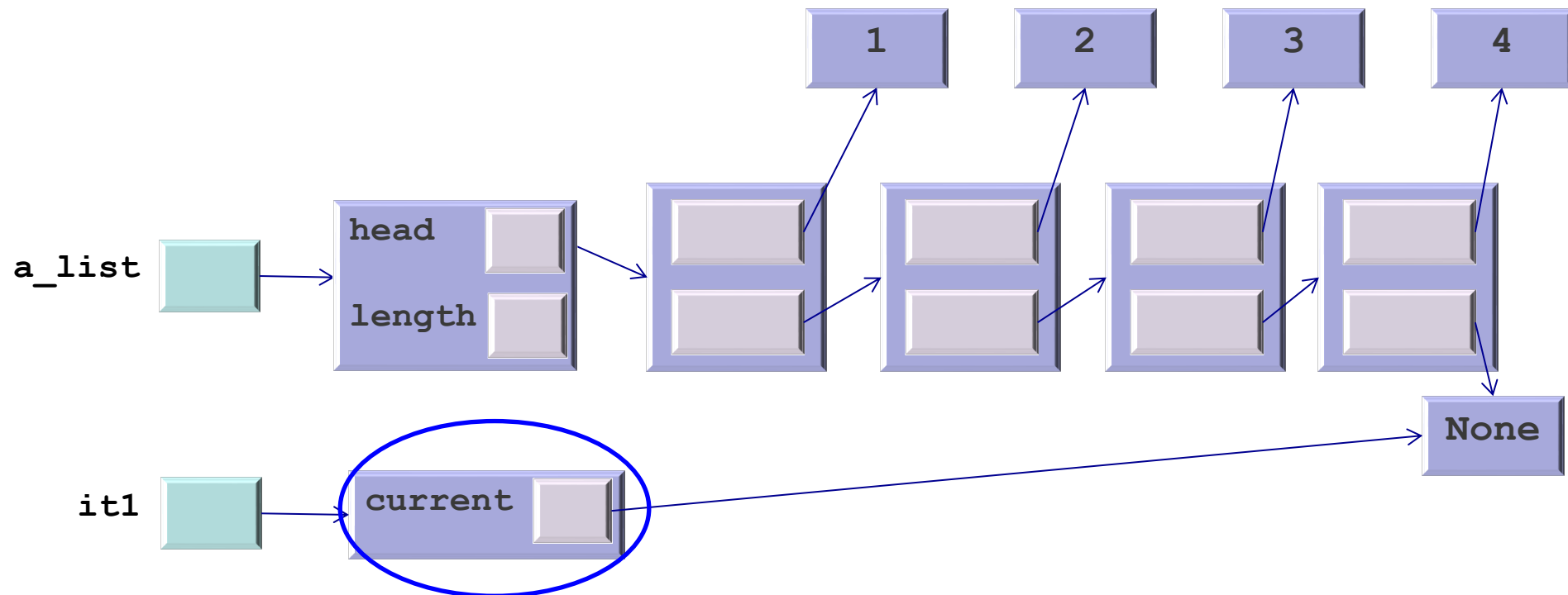
```
2
>>> next(it1)
```



This is my `LinkedListIterator` object

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1
>>> next(it1)
```

```
2
>>> next(it1)
3
>>> next(it1)
```



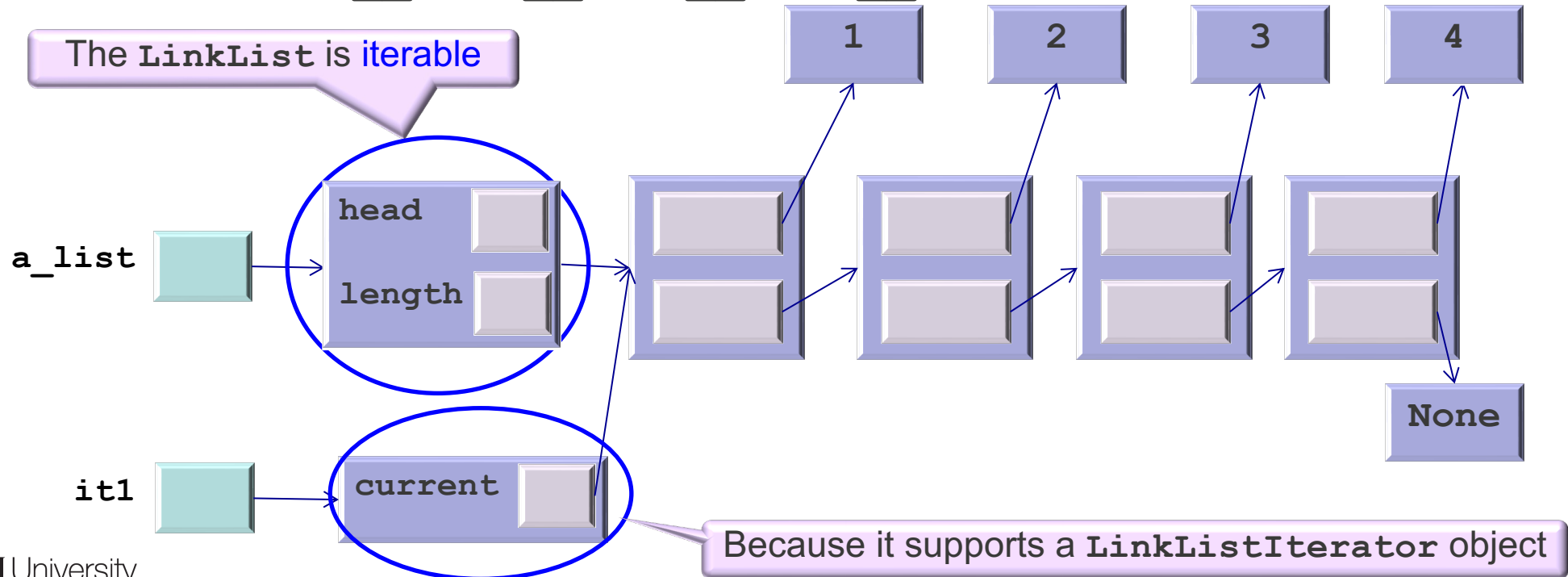
This is my `LinkListIterator` object

```
>>> a_list = LinkList()
>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
>>> a_list.insert(0,2)
>>> a_list.insert(0,1)
>>> it1 = iter(a_list)
>>> next(it1)
1
>>> next(it1)
```

```
2
>>> next(it1)
3
>>> next(it1)
4
>>> next(it1)
Traceback ...:
  File ... in __next__
    raise StopIteration
```

# Iterables versus iterators

- We have made our `List` class **iterable**, since
  - It defines an `__iter__` method that returns an **iterator** on the list
- The objects of the `LinkedListIterator` class are **iterators**, since
  - They support the `__iter__` and `__next__`



# Now that our `LinkedList` class is iterable...

- We can use the `for` notation on it:

```
>>> a_list = LinkedList()
>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
>>> a_list.insert(0,2)
>>> a_list.insert(0,1)
>>> for item in a_list
...     print(item)
...
1
2
3
4
>>>
```

So easy!



# Using Iterators

## So let's use it

- Define `positive(a_list)` which returns `True` if all items are `>0`
- Assume you are a **user**: outside the class, no access to internals
- One possible solution is:

```
def positive(a_list: LinkedList[T]) -> bool:
    for item in a_list:
        if item <= 0:
            return False
    return True
```

Too easy! Not even have to explicitly call `iter` or `next`

**Complexity?**

**Best:  $O(1)$  when the first element is  $\leq 0$**

**Worst :  $O(N)$  when all elements are  $>0$**

# List comprehensions and Iterable classes

- **List comprehension: create a list from another list using mathematic-like notation:**

```
>>> A = [3*x for x in range(10)]
>>> B = [x for x in A if x % 2 == 0]
>>> A;B
[0, 3, 6, 9, 12, 15, 18, 21, 24, 27]
[0, 6, 12, 18, 24]
```

Both `range()` and list `A` are **iterable**

- **Common operations on an iterator's output include:**
  - Perform some operation for every element (e.g., `3*x`)
  - Select a subset of elements that meet a condition (e.g., `x % 2 == 0`)
- **List comprehensions allow you to do that AND return a list**
- **Generator expressions allow you to do that AND return an iterator**

```
>>> A = (3*x for x in range(10))
>>> next(A)
0
```

You can now do things like this

# Equivalent definition

- We said one possible solution for `positive(a_list)` was:

```
def positive(a_list: LinkedList[T]) -> bool:
    for item in a_list:
        if item <= 0:
            return False
    return True
```

- Another (more pythonic) solution is:

```
def positive(a_list: LinkedList[T]) -> bool:
    return [] == [e for e in a_list if e <= 0]
```

I do not expect you to program like this though... not just yet

## Let's use it again

- Define `max(a_list)` to compute the maximum item `a_list`
- Assume you are a **user**: outside the class, no access to internals
- One could write the following:

```
def max(a_list: LinkList[T]) -> int:
    for item in a_list:
        if max < item:
            max = item
    return max
```

But this does not work. Why?

Local variable `max` has not been initialised before the comparison. Python will say:  
`UnboundLocalError: local variable 'max' referenced before assignment`

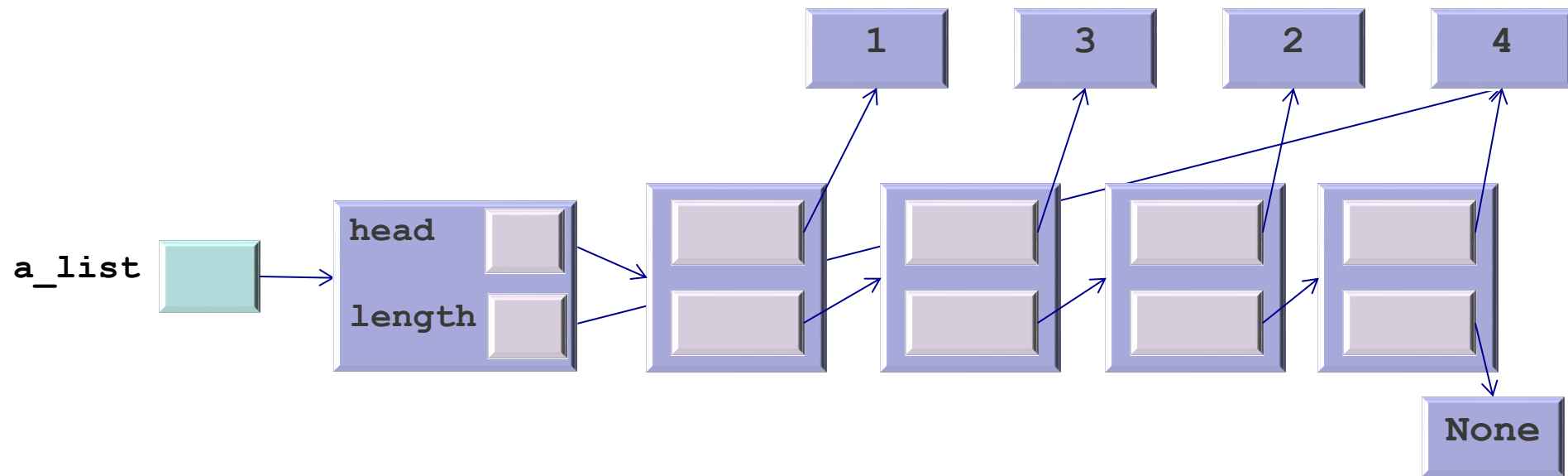
- What do you need to do to fix it?
  - Give a (reasonable) initial value to `max` (that of an element of the list)
- What does the function do if the list is empty?
  - Raise an exception

# Let's use it again (cont)

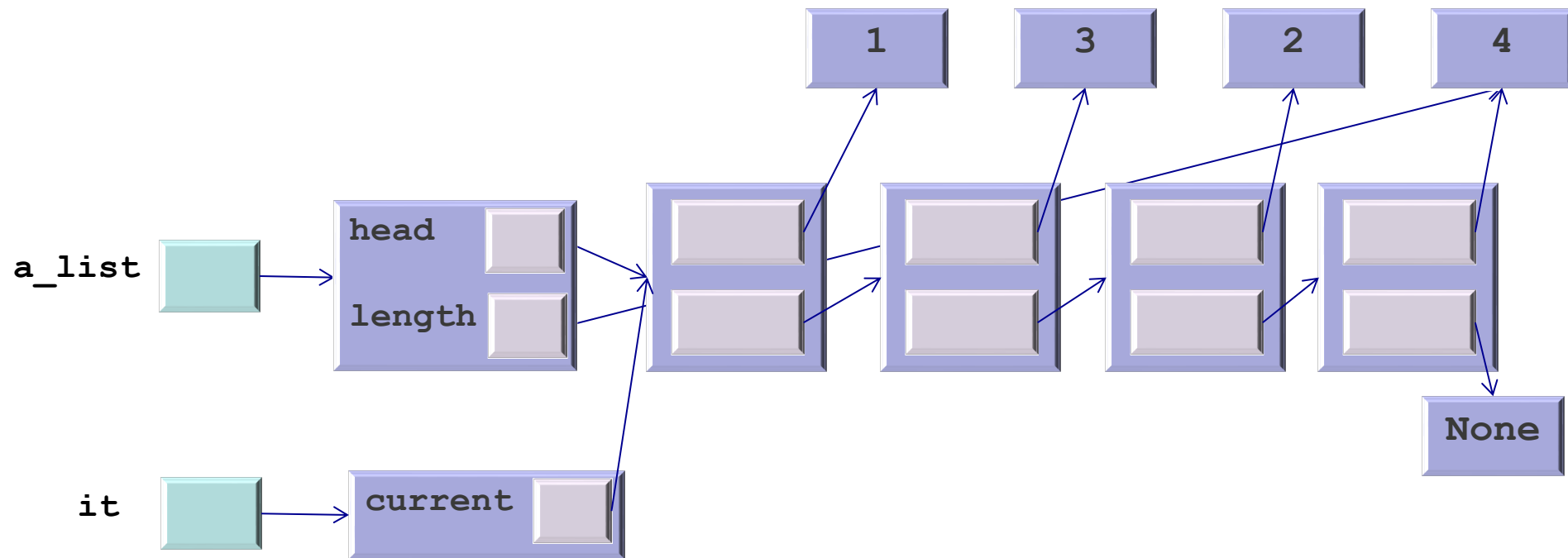
- One possibility (there are many!):

Iterators are also iterable!

```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list) # construct an iterator
    try:
        max = next(it) # get the first element
    except StopIteration: # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it: # traverse the rest of the list
            if max < item:
                max = item
        return max
```

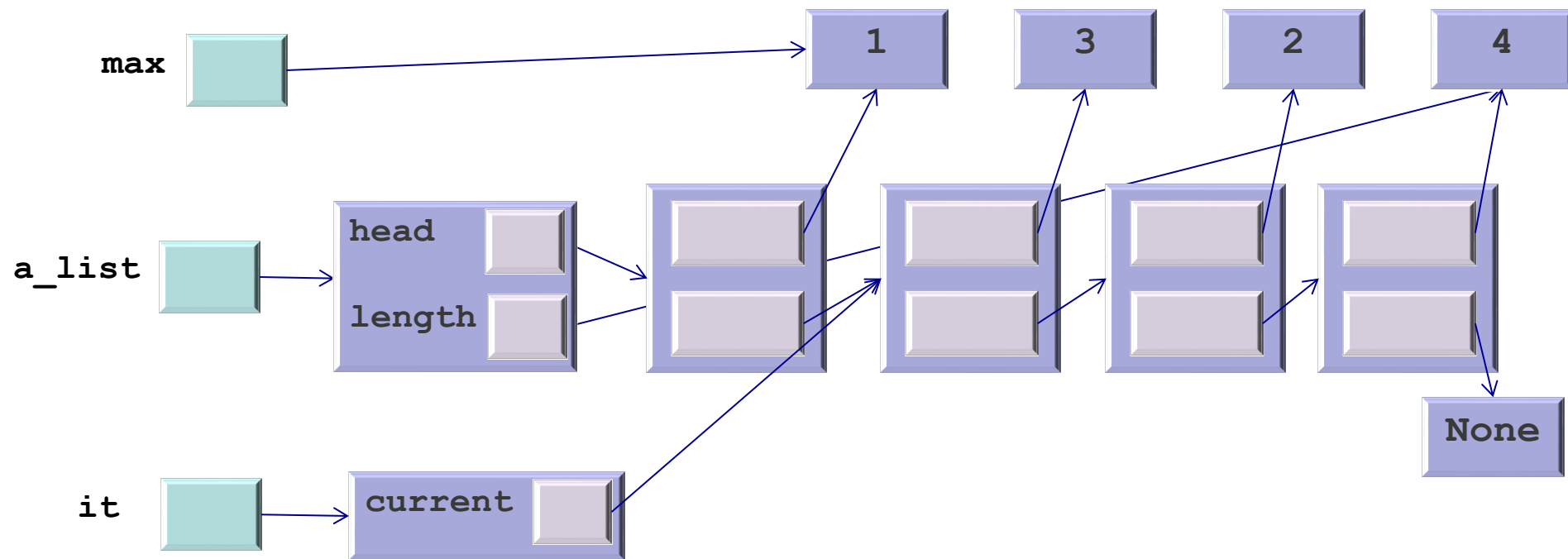


```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```

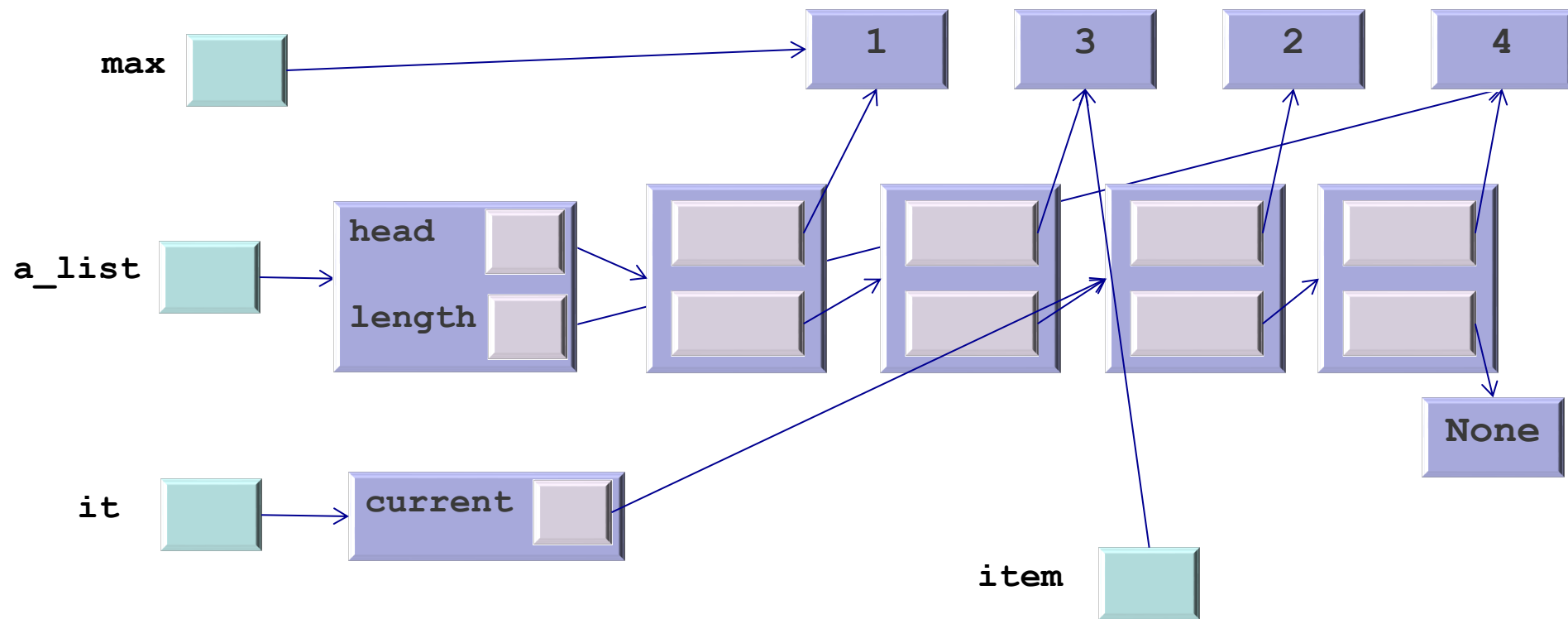


```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)         # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```

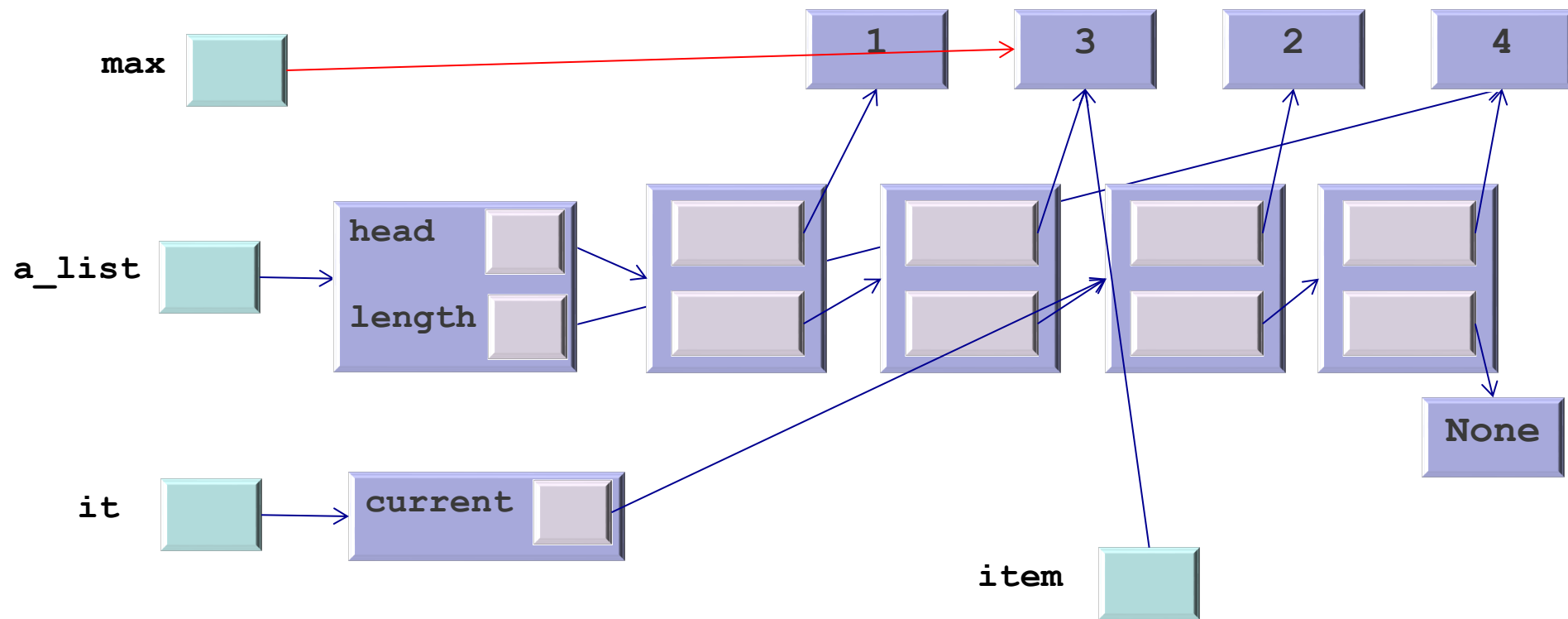




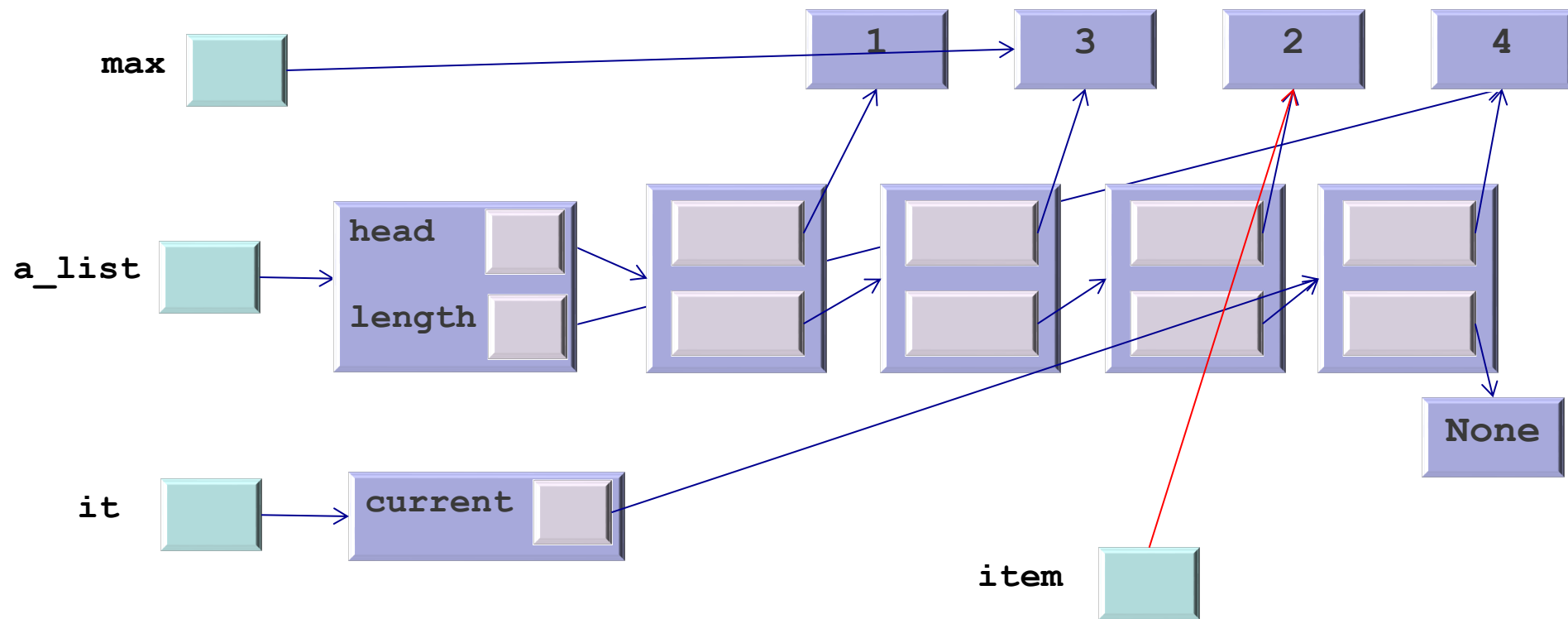
```
def max(a_list: LinkList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```



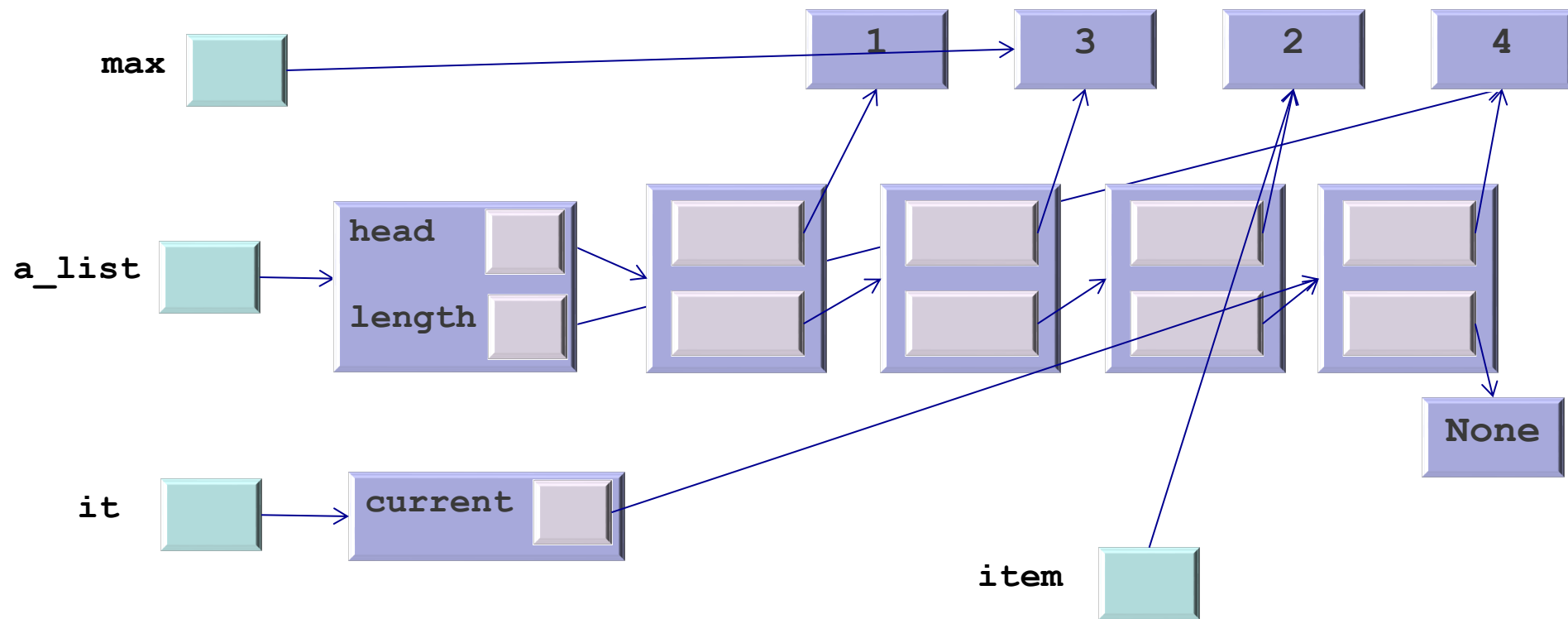
```
def max(a_list: LinkList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```



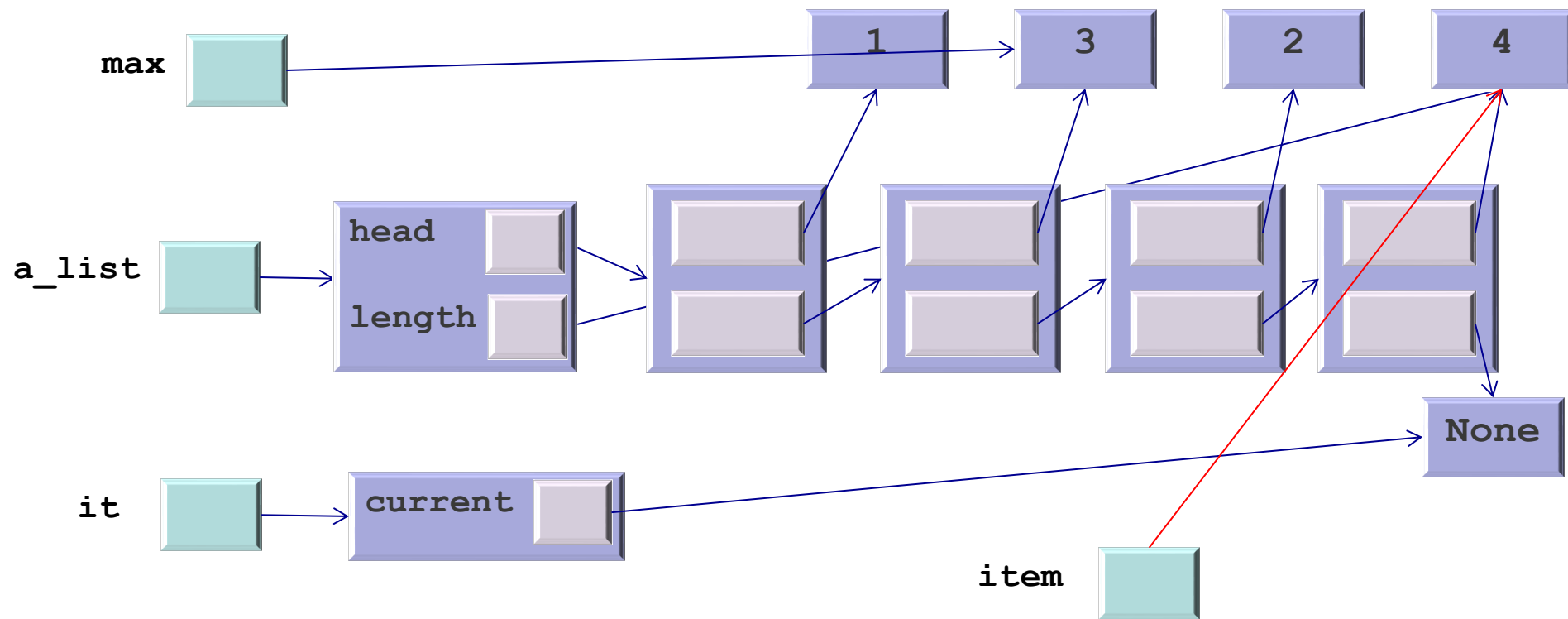
```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)         # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```



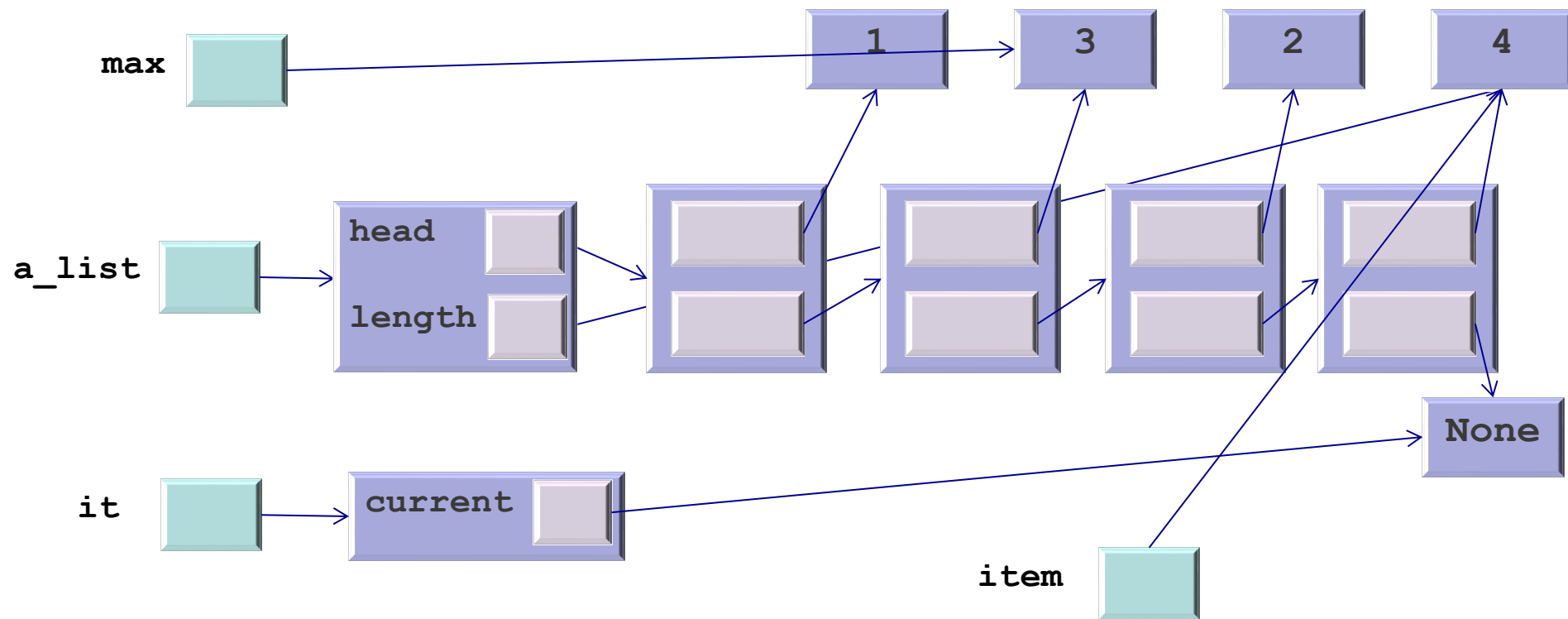
```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)         # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
        return max
```



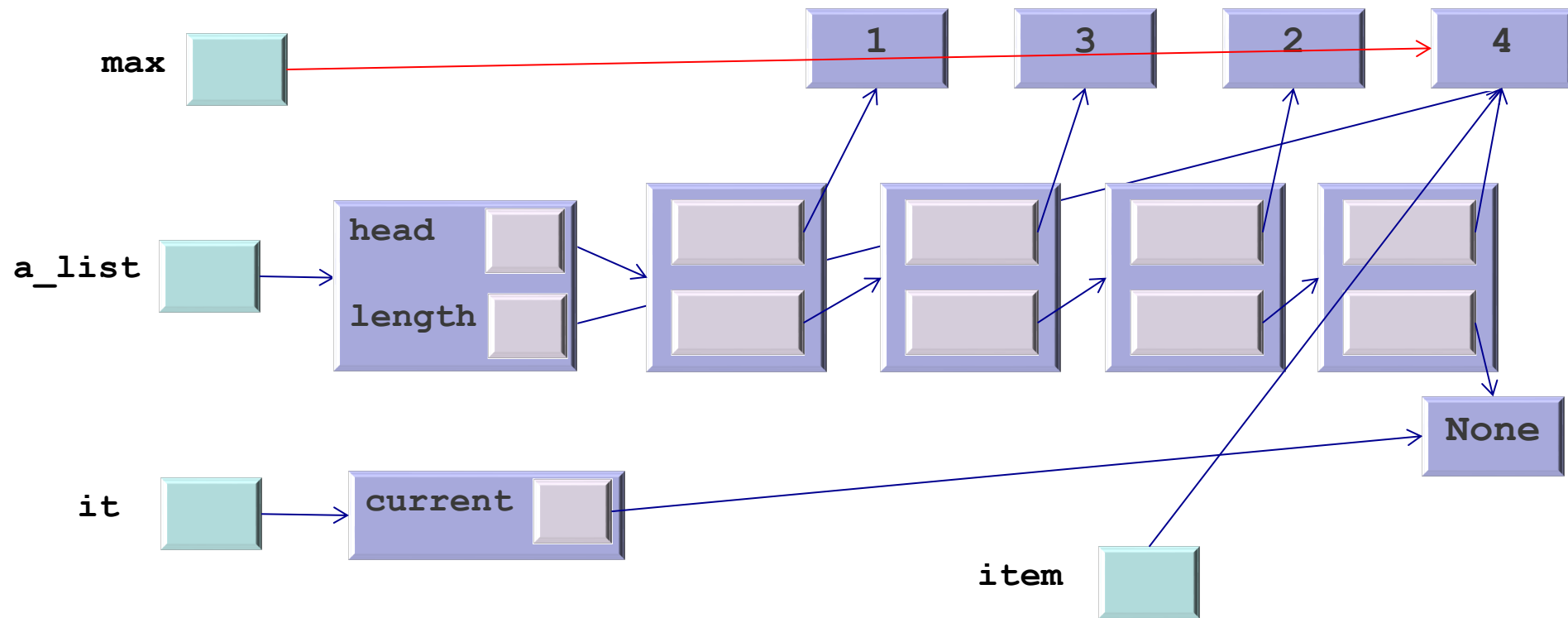
```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)         # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
        return max
```



```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
        return max
```

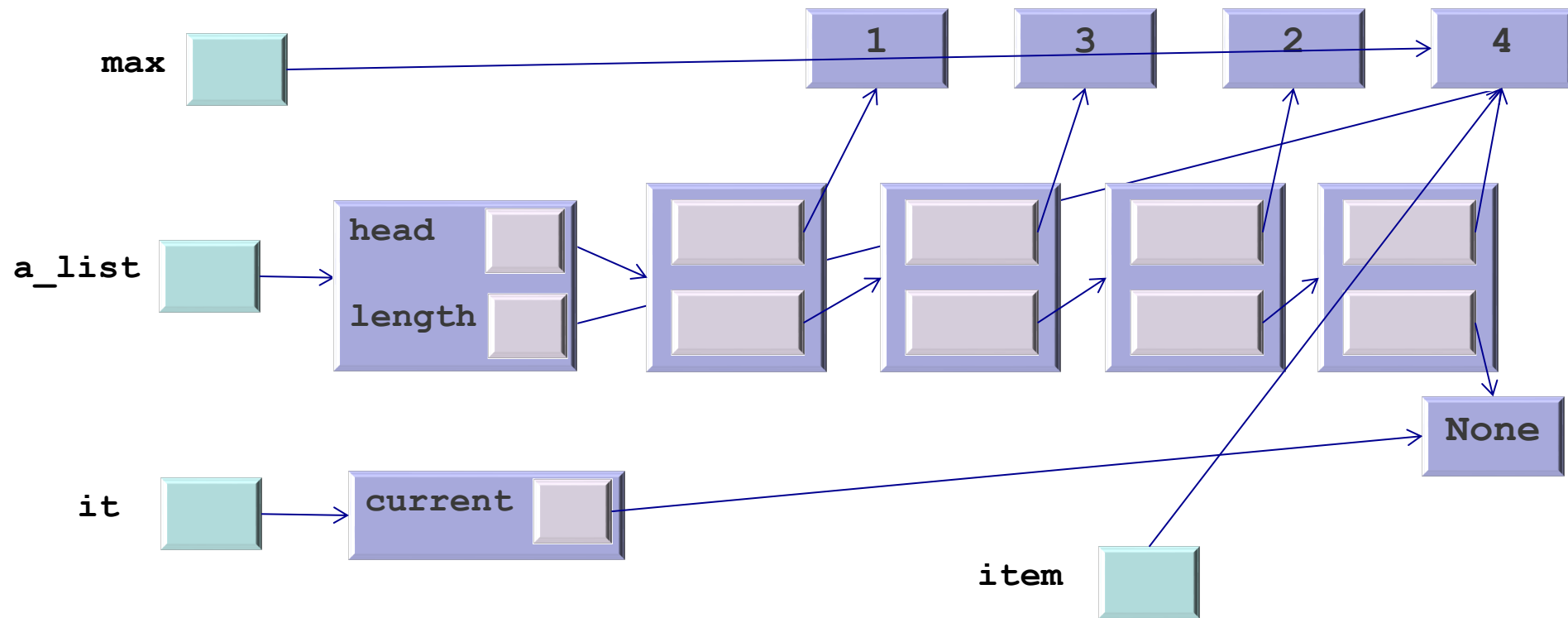


```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
        return max
```

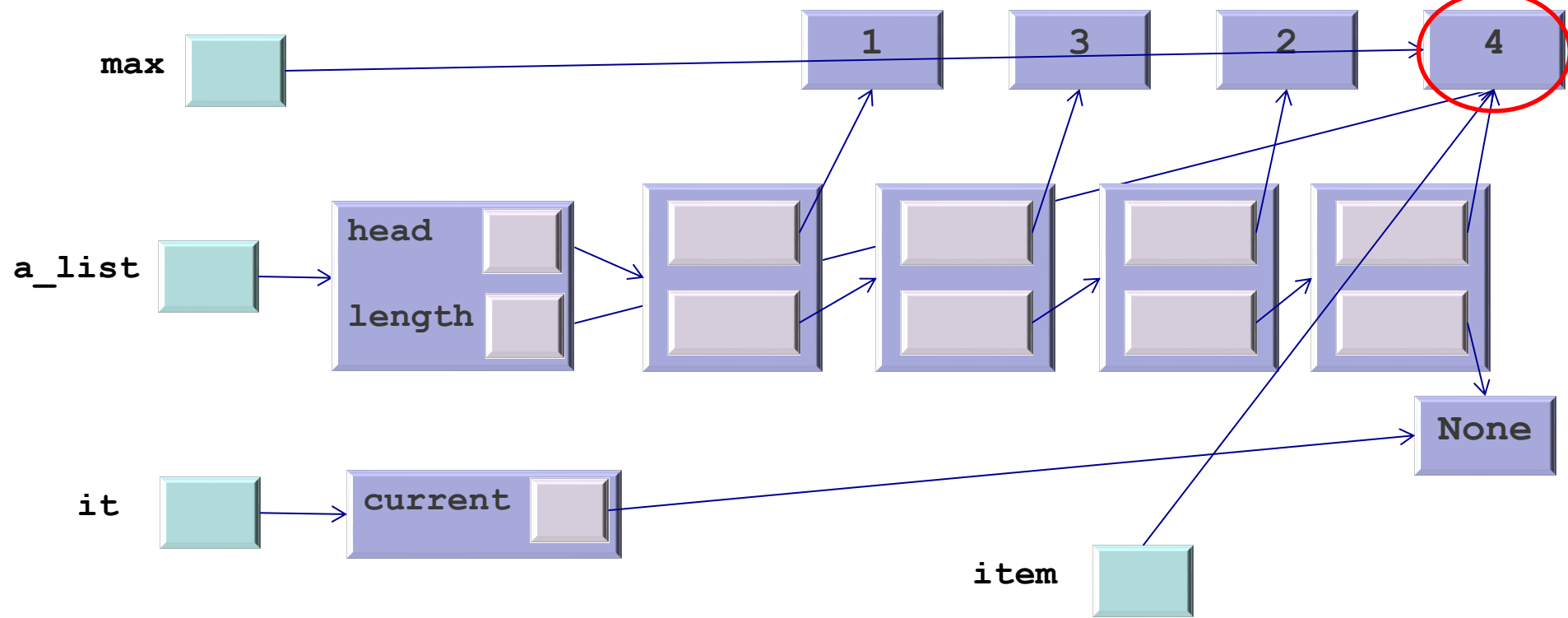


```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```





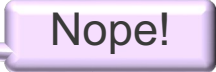
```
def max(a_list: LinkList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)        # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```



```
def max(a_list: LinkedList[T]) -> int:
    it = iter(a_list)          # construct an iterator
    try:
        max = next(it)         # get the first element
    except StopIteration:      # if empty, next(it) raises an exception
        raise Exception("The list is empty")
    else:
        for item in it:        # traverse the rest of the list
            if max < item:
                max = item
    return max
```

# A Modifying Iterator

# Can we now do double as users?

- **We started this to be able to define the function `double(a_list)`**
  - And do so from **outside** the class
- **Can we now do that? What do we need?**
  - To traverse the list **and add new nodes** as we do so
- **Can our iterator add nodes?** 
- **So we need to create a different kind of iterator**
  - One that allows us to **modify the iterable object**

# A more versatile `LinkedListIterator` class

## ▪ Additional operations we will define:

- `delete`: returns the item pointed by `current` and deletes the node
- `add`: adds an item right before `current` (to do in the pracs)
- `has_next`: returns `True` if there is a next item to be processed (i.e., if `current` is not at the end of list)
- `peek`: returns the next item (the one pointed by `current`) without moving along.  
Raises `stopIteration` if there is no next.

## ▪ Since we need to add and delete:

- We are going to need not only a `current` but also a `previous`
- Plus some times we will need to change the head of the list
  - We are also going to `keep the list itself`

```
class LinkedList(List[T]):
```

```
...
```

```
def __iter__(self) -> LinkedListIterator[T]:
```

```
    return LinkedListIterator(self)
```

The list, not just the head node

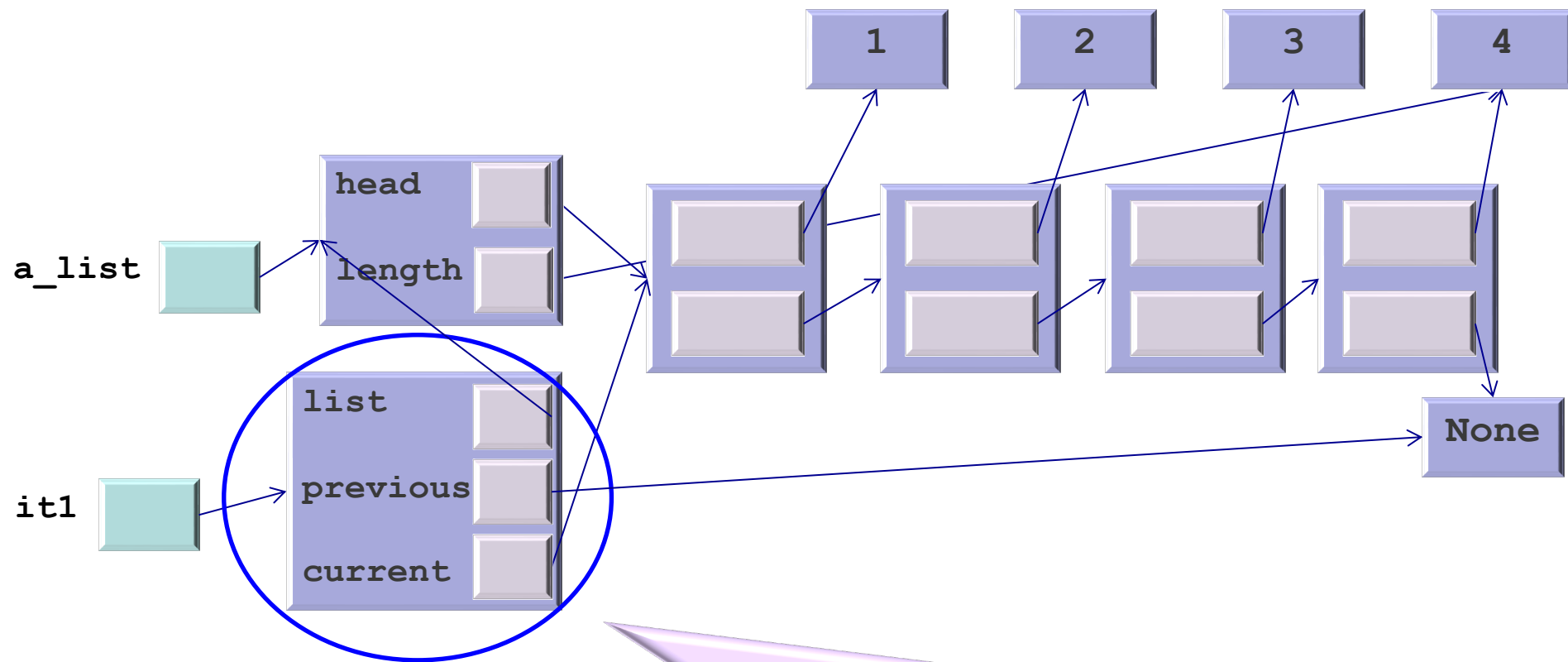
# Rethinking LinkedListIterator

```
class LinkedListIterator(Generic[T]):  
    def __init__(self, a_list: LinkedList[T]) -> None:  
        self.list = a_list  
        self.previous = None  
        self.current = a_list.head  
  
    def __iter__(self):  
        return self  
  
    def __next__(self) -> T:  
        if self.current is not None:  
            item = self.current.item  
            self.previous = self.current  
            self.current = self.current.link  
            return item  
        else:  
            raise StopIteration
```

The list, not just the head node

We store the list, previous and current

Differences marked in red



This is my new more versatile **LinkListIterator** object

```
>>> a_list = List()
>>> a_list.insert(0,4)
>>> a_list.insert(0,3)
>>> a_list.insert(0,2)
>>> a_list.insert(0,1)
>>> it1 = iter(a_list)
>>>
```

# Rethinking LinkedListIterator (cont)

```
def has_next(self):
```

True if there is at least one item to process

```
    return self.current is not None
```

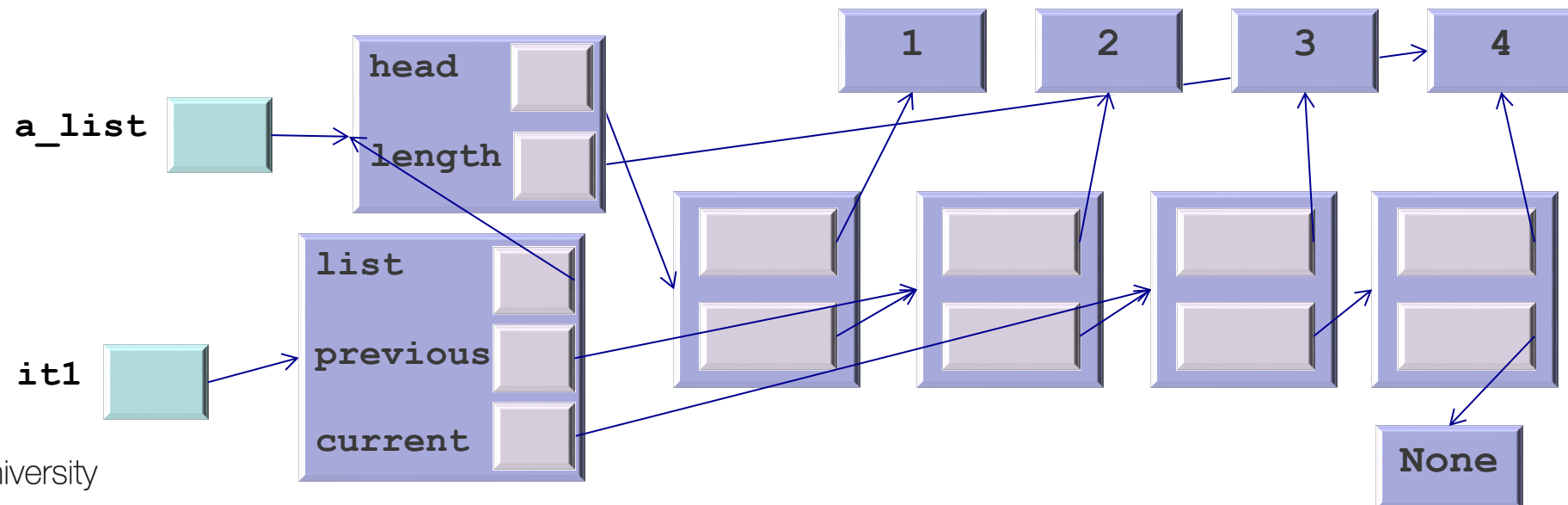
```
def peek(self):
```

Returns the next item without moving along. Raises StopIteration if no next.

```
    try: # In case someone tries to peek over the line
        return self.current.item
```

```
    except AttributeError:
```

```
        raise StopIteration("no more elements in list")
```





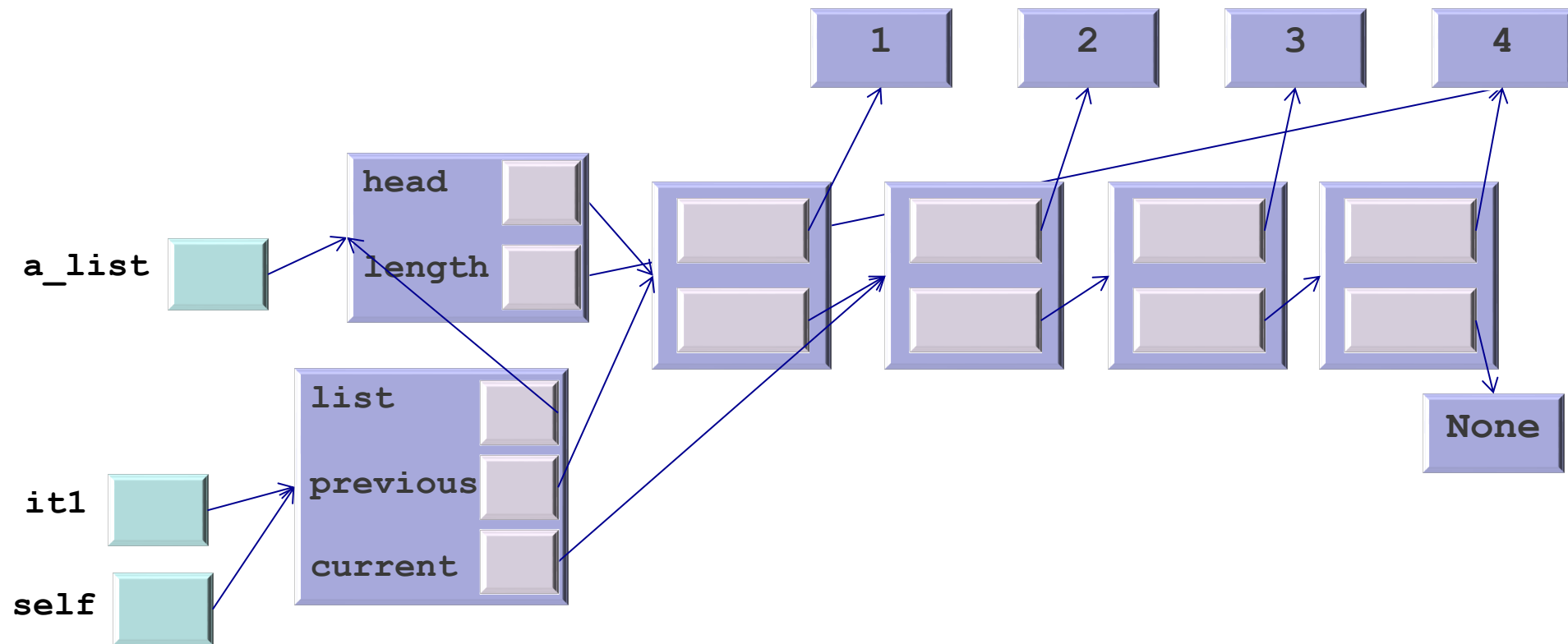
# Rethinking LinkedListIterator (cont)

Returns the next item and deletes the associated node. Raises `StopIteration` if no next.

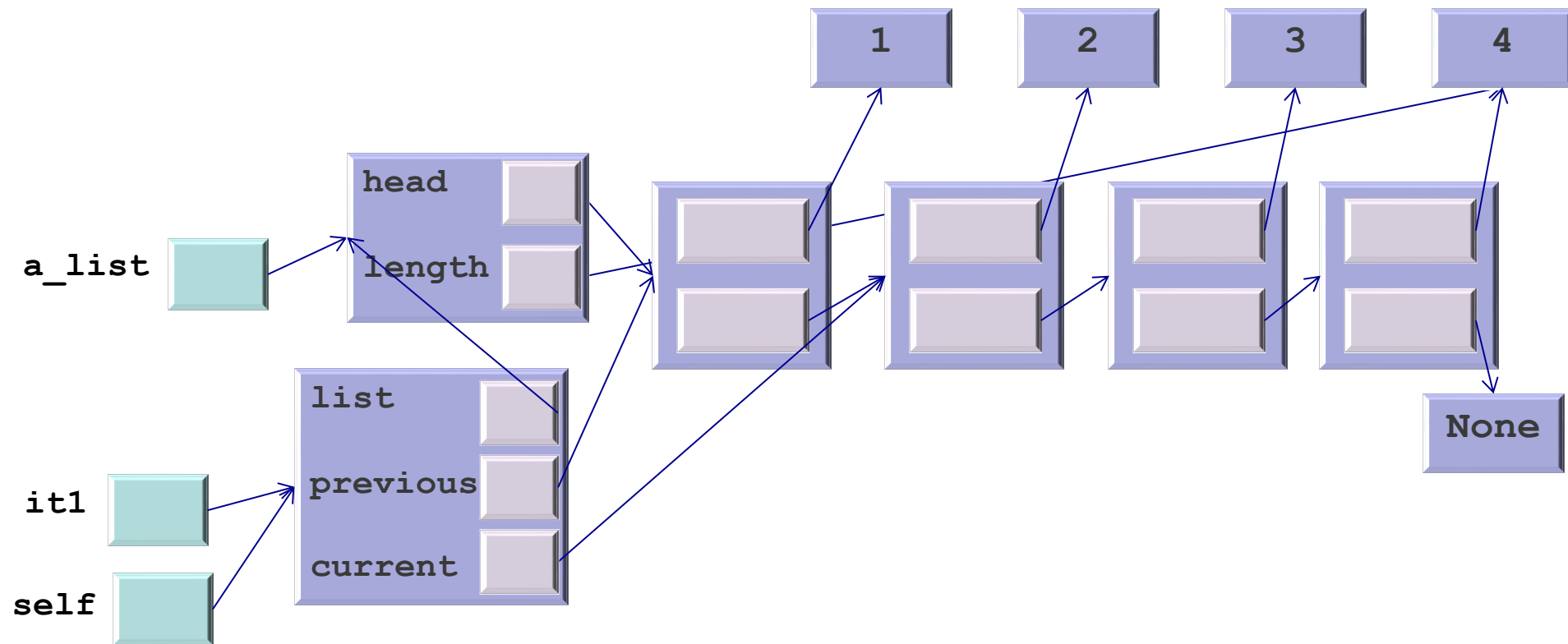
```
def delete(self) -> T:
    if not self.has_next(): # we reached the end
        raise StopIteration("no more elements in list")
    else:
        item = self.current.item
        self.current = self.current.link

        if self.previous is None: #it is the first element
            self.list.head = self.current
        else: #not the first element
            self.previous.link = self.current
        self.list.length -= 1

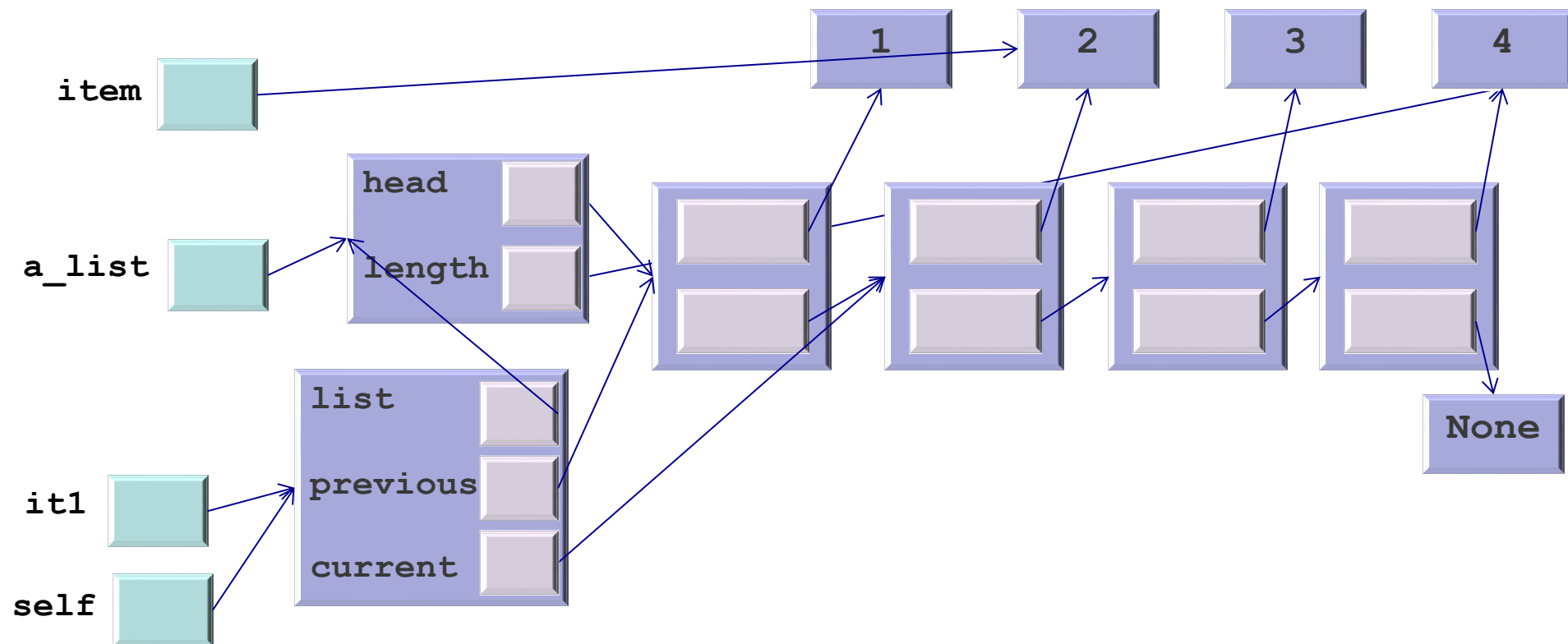
    return item
```



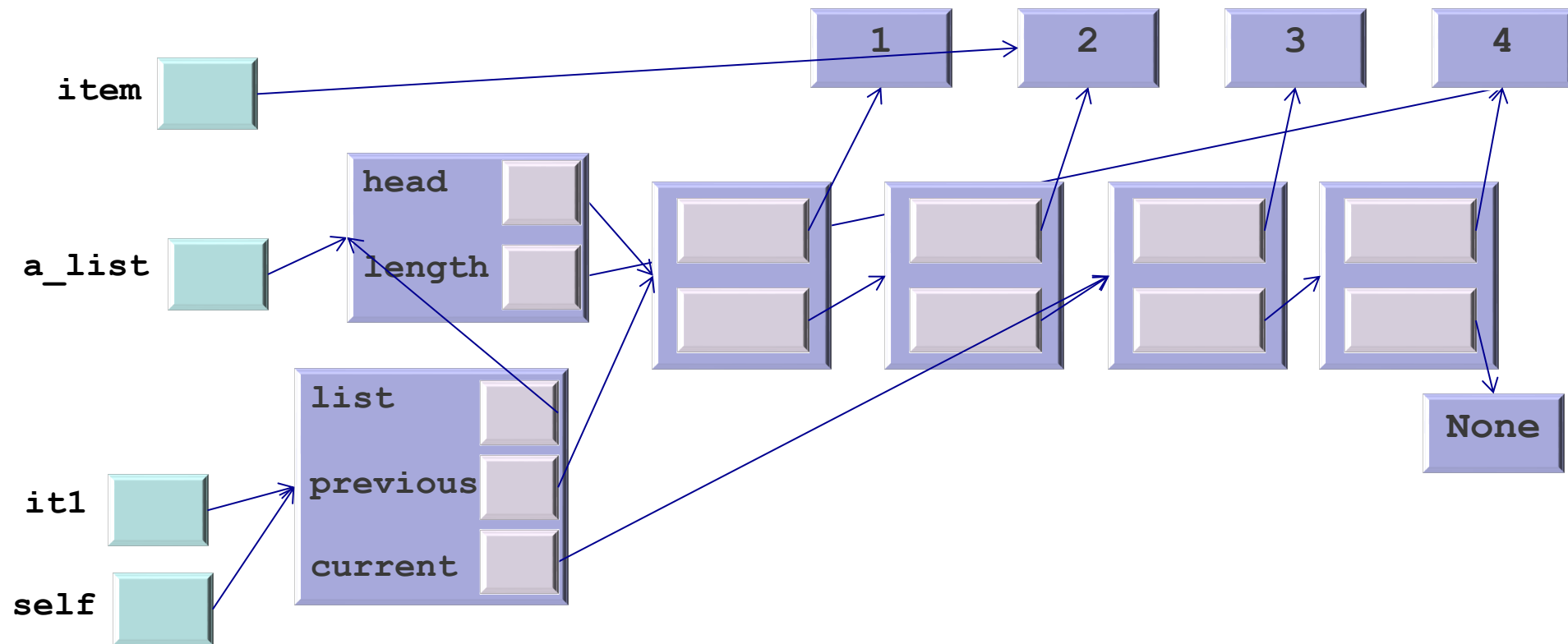
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def delete(self) -> T:
    if not self.has_next(): # we reached the end
        raise StopIteration("no more elements in list")
    else:
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            self.list.head = self.current
        else: #not the first element
            self.previous.link = self.current
        self.list.length -= 1
        return item
```



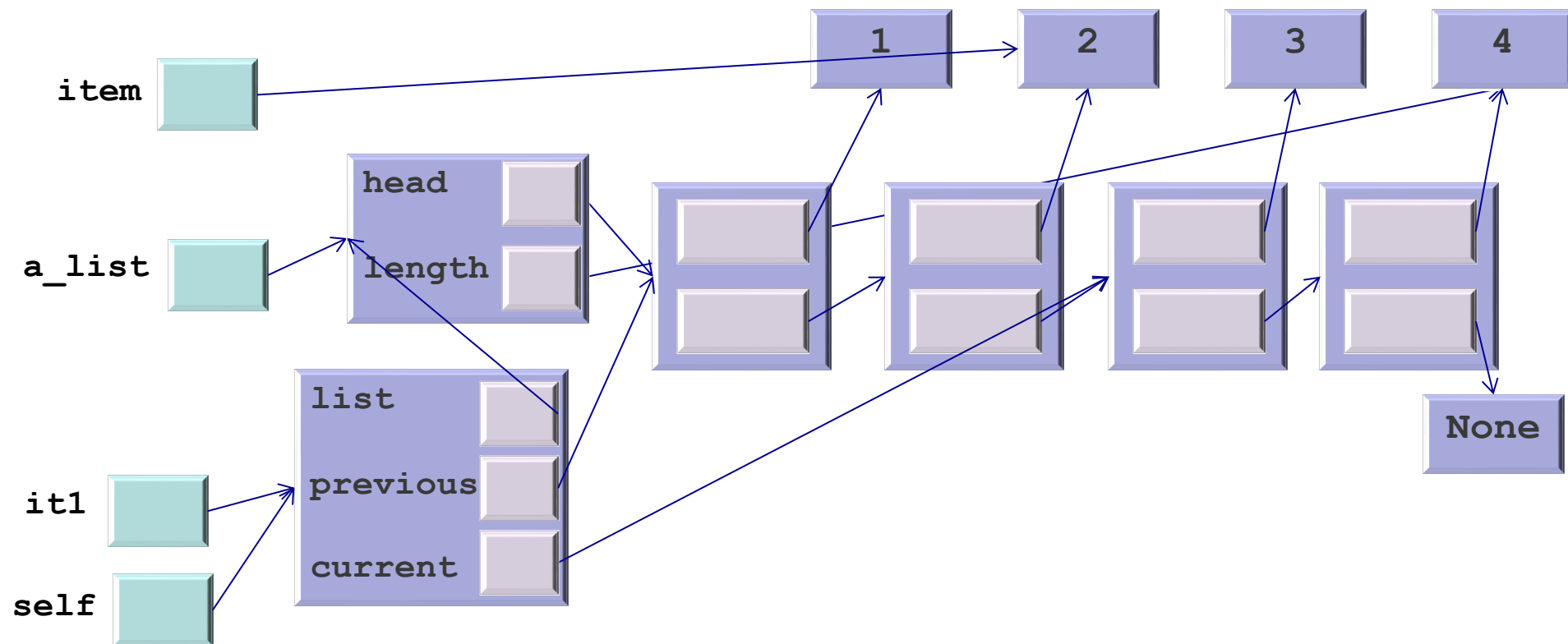
```
def delete(self) -> T:
    if not self.has_next(): # we reached the end
        raise StopIteration("no more elements in list")
    else:
        item = self.current.item
        self.current = self.current.link
        if self.previous is None: #it is the first element
            self.list.head = self.current
        else: #not the first element
            self.previous.link = self.current
        self.list.length -= 1
        return item
```



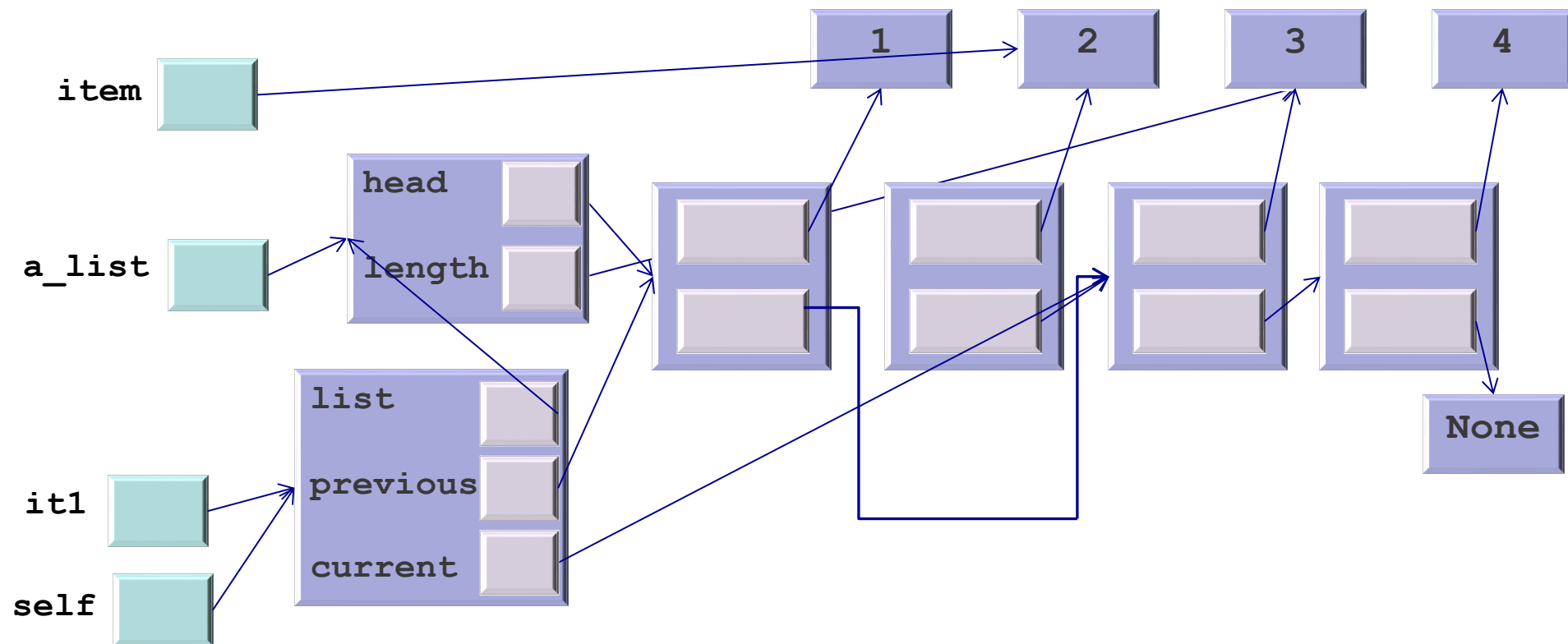
```
def delete(self) -> T:
    if not self.has_next(): # we reached the end
        raise StopIteration("no more elements in list")
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        self.current = self.current.link
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            self.previous.link = self.current
        self.list.length -= 1
        return item
```



```
def delete(self) -> T:
    if not self.has_next(): # we reached the end
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    else:
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        self.current = self.current.link
        if self.previous is None: #it is the first element
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```



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def delete(self) -> T:
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        else: #not the first element
            self.previous.link = self.current
        self.list.length -= 1
        return item
```



```
def delete(self) -> T:
    if not self.has_next(): # we reached the end
        raise StopIteration("no more elements in list")
    else:
        item = self.current.item
        self.current = self.current.link
        if self.previous is None: #it is the first element
            self.list.head = self.current
        else: #not the first element
            self.previous.link = self.current
        self.list.length -= 1
    return item
```



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# Basics of Higher Order Functions in Python



# Functions as first-class objects/entity

- **Being a first-class object means being like any other object:**
  - Functions can then be **assigned** to variables
  - **Passed** as arguments to a function/method
  - **Returned** by a function/method
- **A higher order function is one that:**
  - **Takes** another function as argument and/or
  - **Returns** another function as argument
- **In Python functions (and thus methods) are first class objects**
  - So you can define higher order functions

```
>>> def my_call(f,x):  
...     f(x)  
...
```

```
>>> def my_function(x):  
...     print(x)  
...  
>>> my_call(my_function, "hello")  
hello
```

Takes a function  
as argument

# Functions as first-class objects (cont)

- You can also define a function that returns another function:

```
>>> def return_f(x):  
...     def f(y):  
...         return x+y  
...     return f  
...  
>>> g = return_f(30)  
>>> g  
<function return_f...>  
>>> g(2)  
32
```

`g` is bound to a function that  
adds 30 to its argument

```
>>> def return_h():  
...     def h(x,y):  
...         return x+y  
...     return h  
...  
>>> j = return_h()  
>>> j  
<function return_h...>  
>>> j(30,2)  
32
```

`j` is bound to a function that  
adds its two arguments

# Let's combine the two

- **Let's define a function that:**

- Receives a list `a_list` and a function `f` as input
- Returns a new function `h` that receives another function `g` and applies first `g` and then `f` to every element in `a_list`

```
def combine(f, a_list):  
    def h(g):  
        return [f(g(x)) for x in a_list]  
    return h
```

```
>>> def plus_10(x):  
...     return x + 10  
...  
>>> def mult_by2(x):  
...     return x*2  
...
```

```
>>> h = combine(plus_10, [1,2,3,4])  
>>> h(mult_by2)  
[12, 14, 16, 18]  
>>>
```

# Summary

- **We have looked at how to make lists iterable by implementing an iterator for them**
  - A simple traversal iterator
  - A modifying iterator (more Java like)
- **Briefly looked at higher order functions in Python**