Algorithm	Program		
Algorithms are written at design phase	Programs are written at Implementation Stage		
Algorithms are programming syntax independent	Programs are programming syntax dependent		
Algorithms are not dependant on operating system architecture and hardware	Programs are dependent on operating system architecture and hardware		
Algorithms are analysed on efficiency in terms of completion time and the space used.	We just test the program to see if it will scale in production		

#### A POSTERIORI

KNOWLEDGE IS OBTAINED THROUGH EXPERIENCE

#### A PRIORI

KNOWLEDGE IS OBTAINED BY ANALYZING CONCEPTS INDEPENDENT OF EXPERIENCE

#### ANALYSIS OF ALGORITHM

#### PRIORI

- 1.Done priori to run algorithm 1.Analysis after running on a specific system
- 2.Hardware independent
- 3.Approximate analysis
- 4.Dependent on no of time statements are executed

#### POSTERIORI

- it on system.
- 2.Dependent on hardware
- 3.Actual statistics of an algorithm
- 4. They do not do posteriori analysis

#### Characteristics of Algorithm

Unambiguous:

Algorithm should be clear and unambiguous. Each of its steps (or phases), one and their inputs/outputs should be clear and must lead to only meaning.

Input:

An algorithm should have 0 or more well-defined inputs.

Output:

An algorithm should have 1 or more well-defined outputs, and should match the desired output.

· Finiteness:

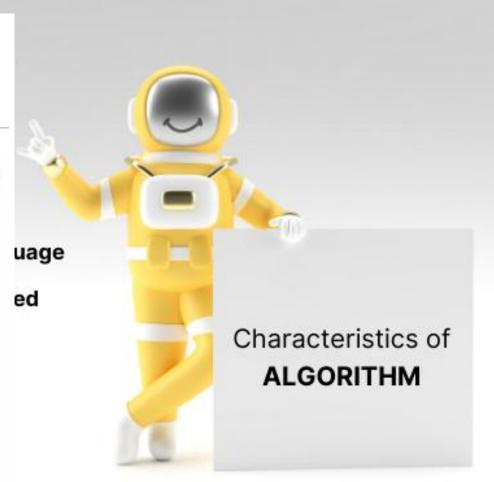
Algorithms must terminate after a finite number of steps.

Feasibility:

Should be feasible with the available resources.

Independent:

An algorithm should have step-by-step directions, which should be independent of any programming code.



## Time complexity



WHY ..?

SEARCHING, SORTING, ETC ....



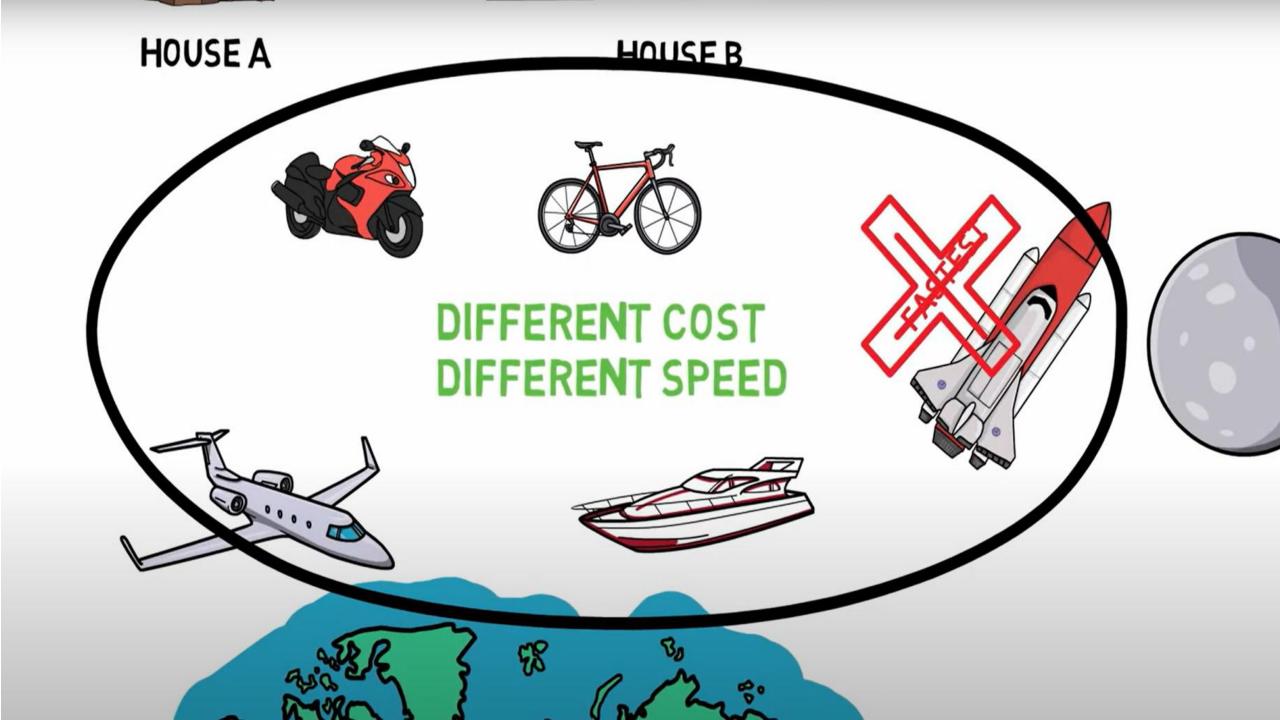
**HOUSE A** 



**HOUSE B** 









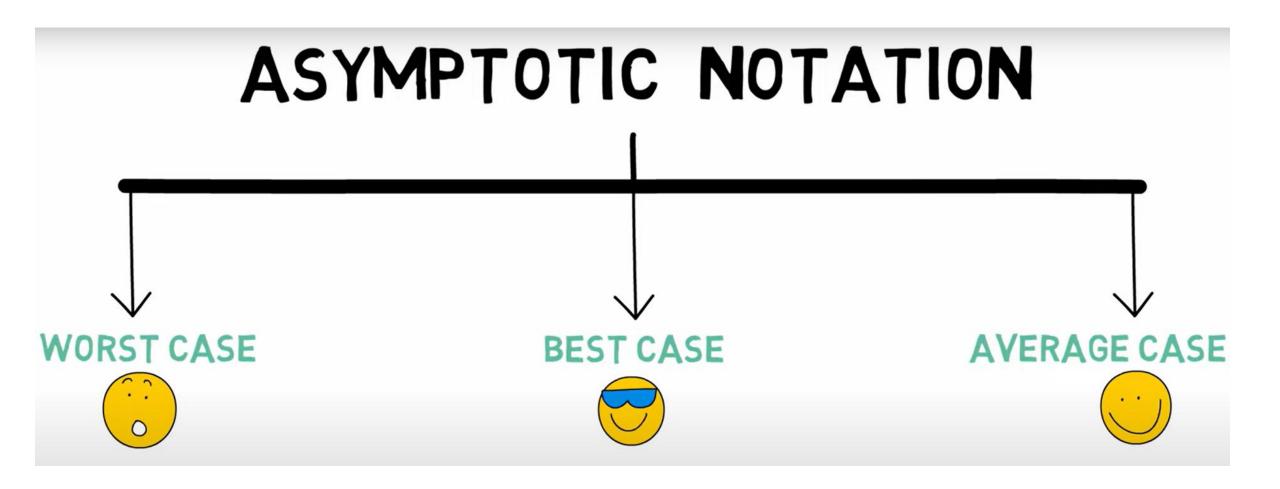
# ALGORITHMS..?





STRENGTH

WEAKNESS

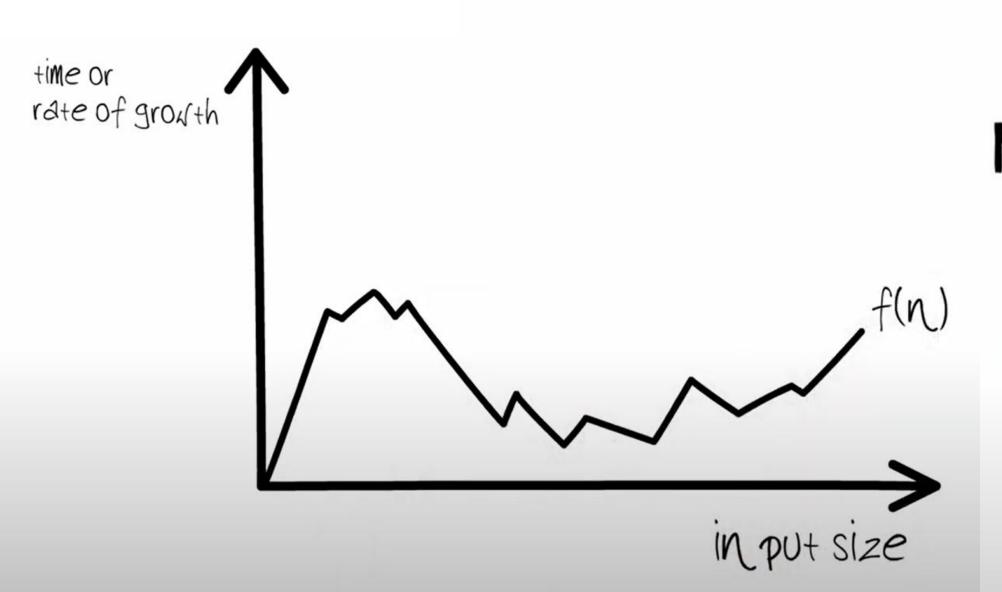


# WORST CASE



Big Oh Notation O

# f(n) = Our Algorithm



### MATHS....

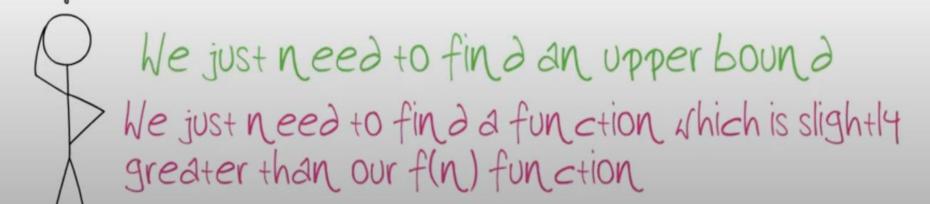


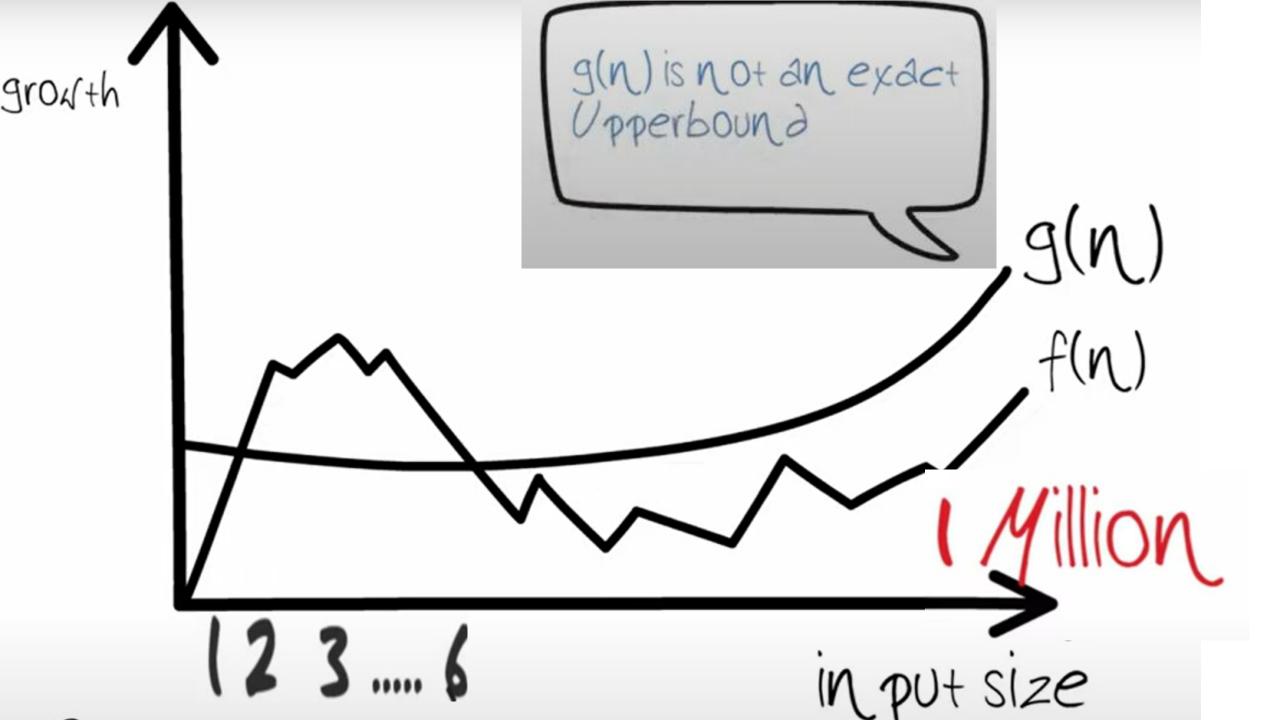
rate of growth

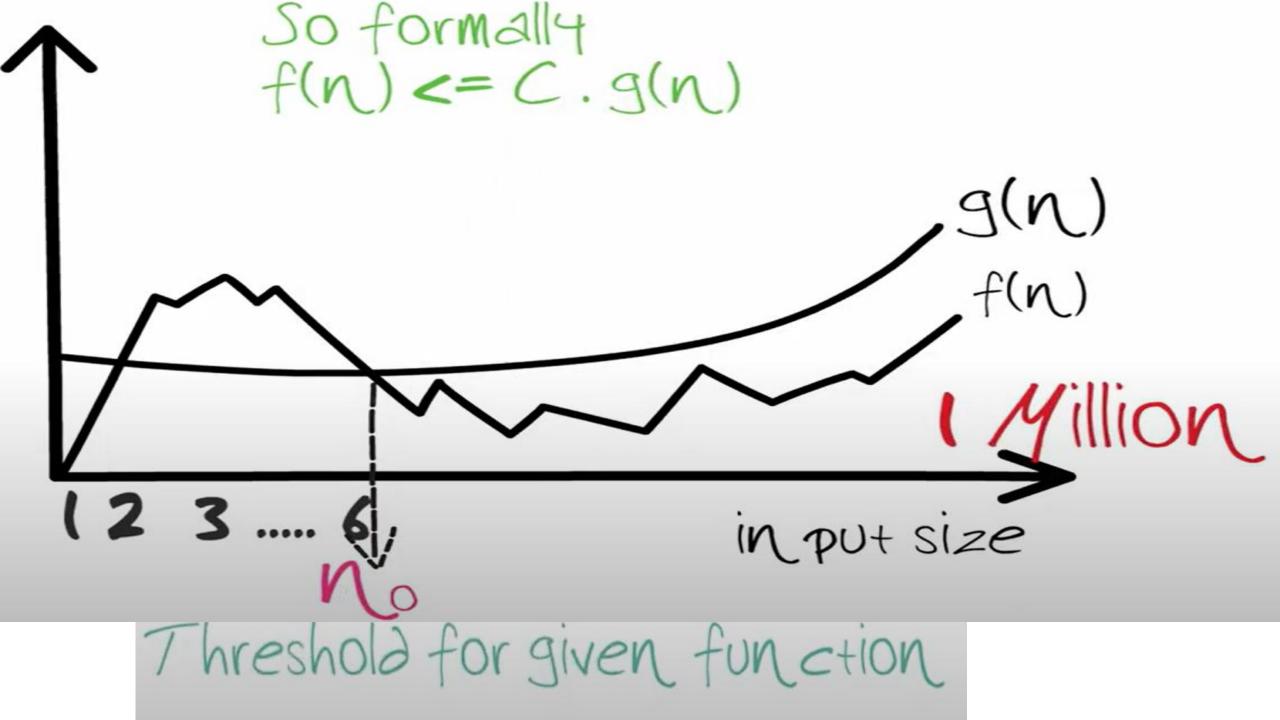
Let's call it as g(n)

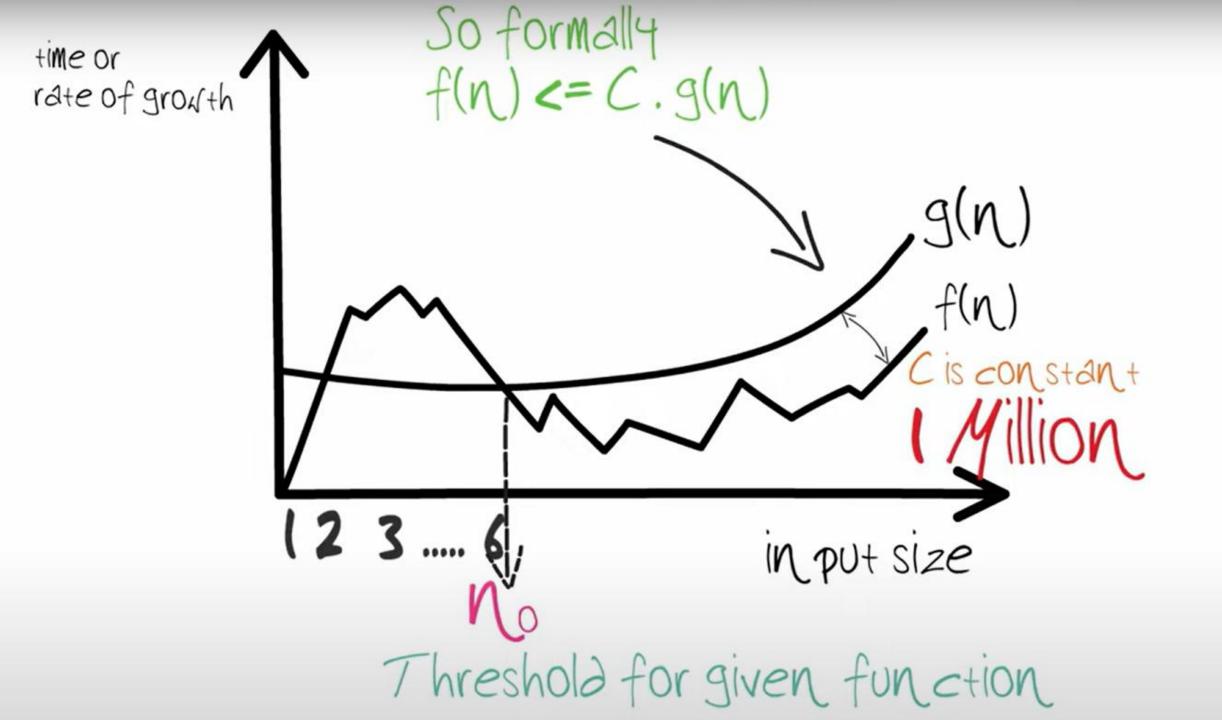


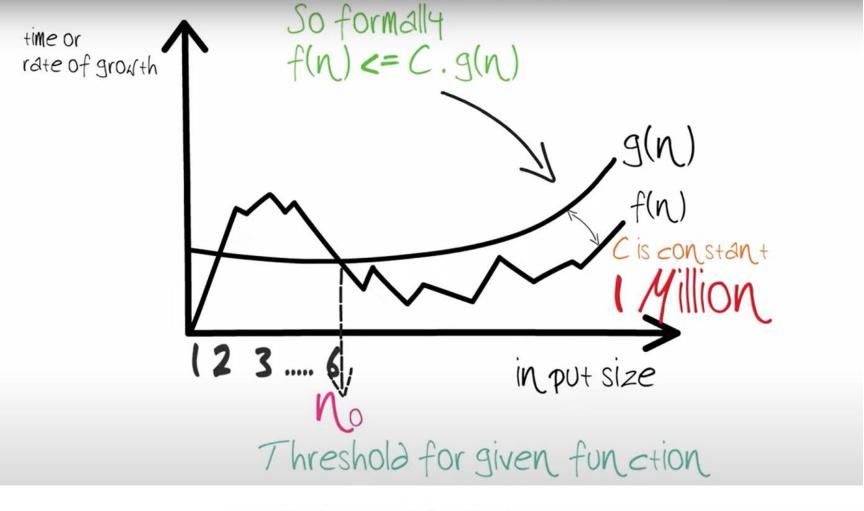












$$f(n) = O(g(n))$$
  
means  $c \cdot g(n)$  is an upper bound on  $f(n)$ .  
C and  $n_o$  are constant

### Find upper bound for $f(n) = n^2 + 1$

$$f(n) \leq c.g(n)$$



$$n^2 + 1 \le c. n^2$$

$$n^2 + 1 \le 2 \cdot n^2$$
, for  $n \ge 1$ 

$$n^2 + 1 = O(n^2)$$
 for c = 2 and n0 >= 1

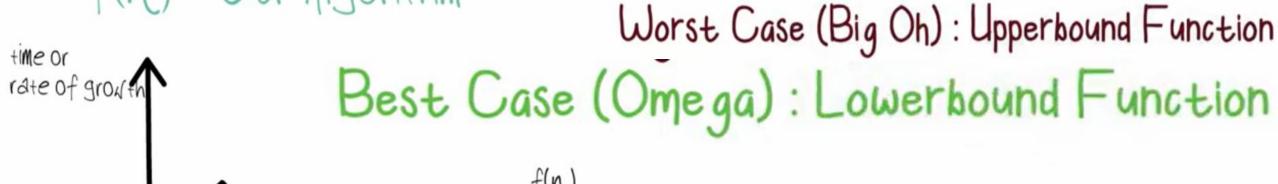
This is Big Oh Notation

# BEST CASE

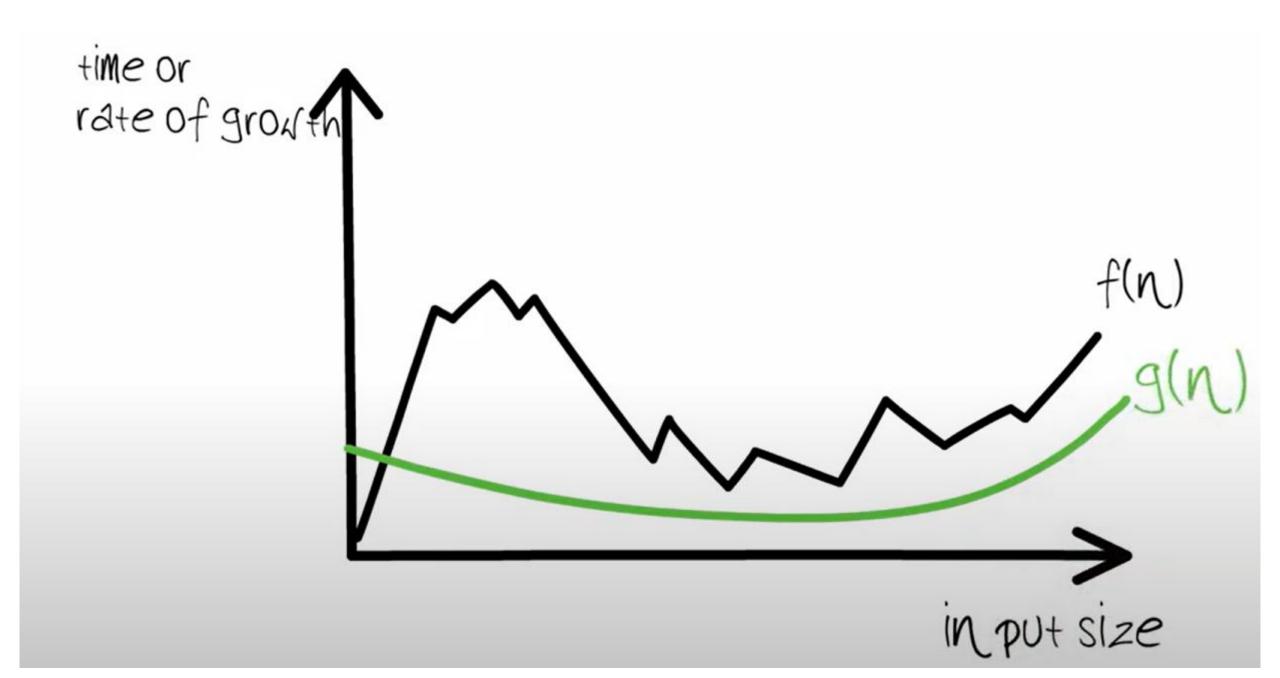


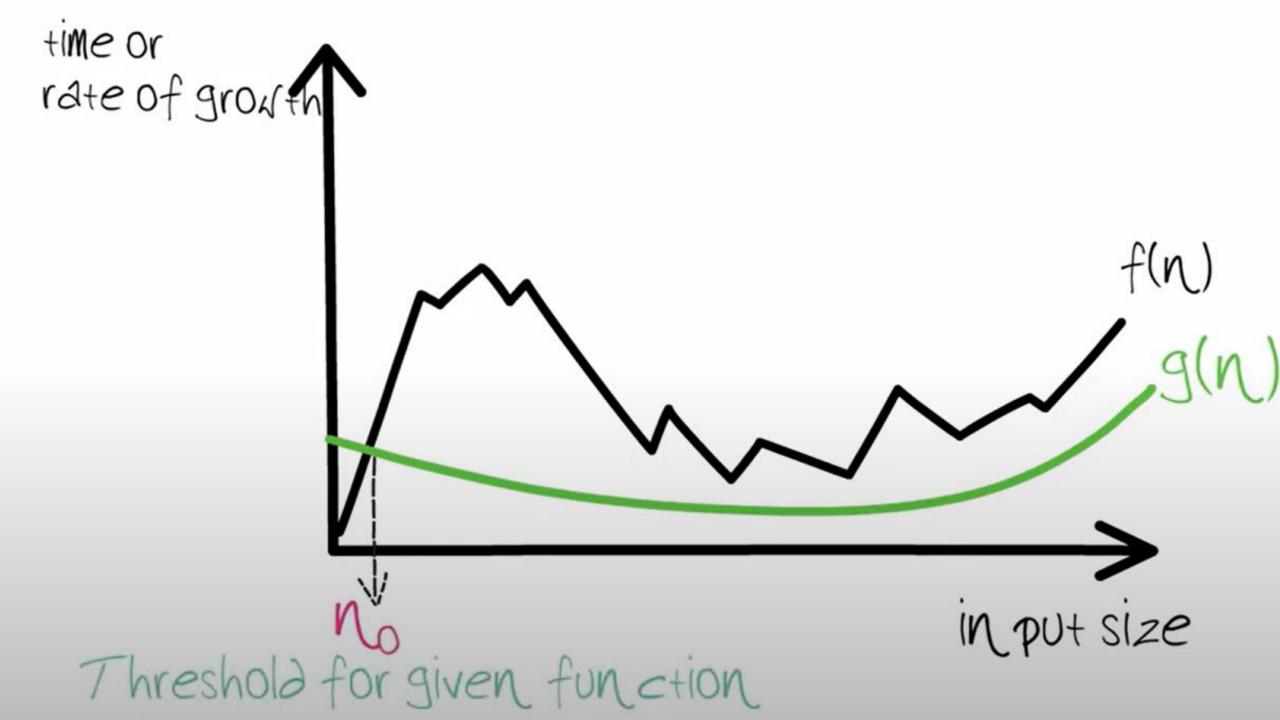
Omega-Q Notation

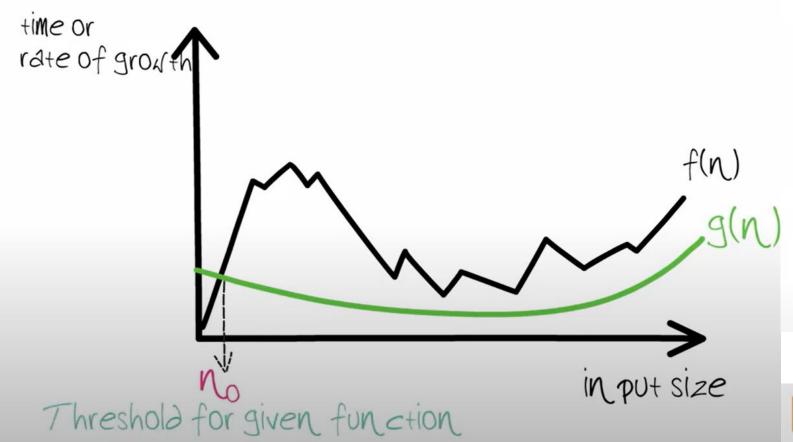
Omega-Q Notation 
$$\Omega$$
  
 $f(n) = Our Algorithm$ 



in put size







So formally 
$$f(n) >= C \cdot g(n)$$

$$f(n) = \Omega(g(n))$$

Find lower bound for  $f(n) = 5n^2$ 

#### Find lower bound for $f(n) = 5n^2$

So 
$$5n^2 = \Omega(n^2)$$

$$f(n) \ge c.g(n)$$

$$5n^2 > = c n^2$$

from c = 5 and n =1 it hold true

## **AVERAGE CASE**

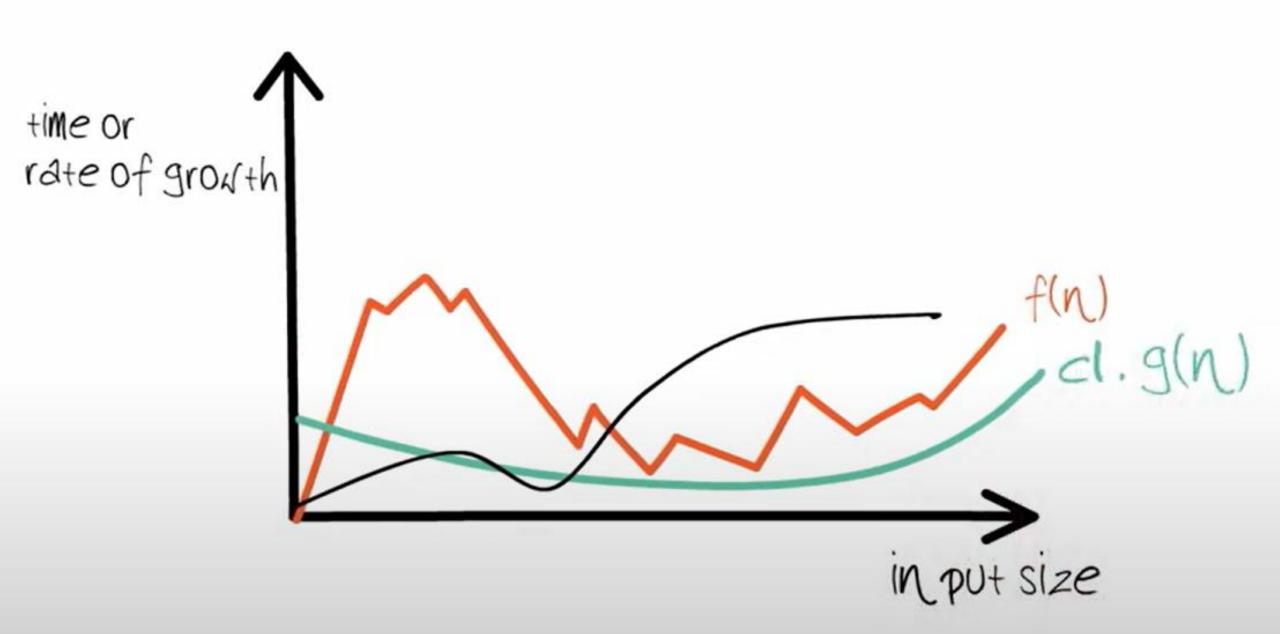


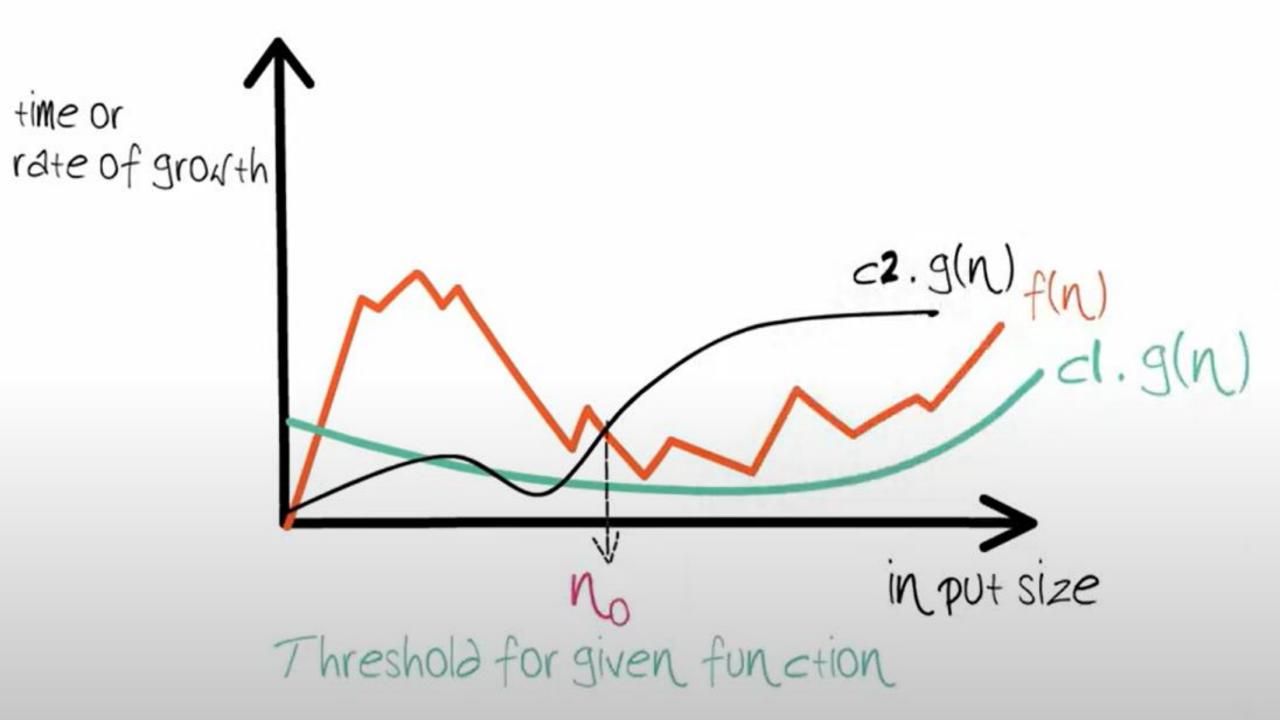
Theta Notation 0

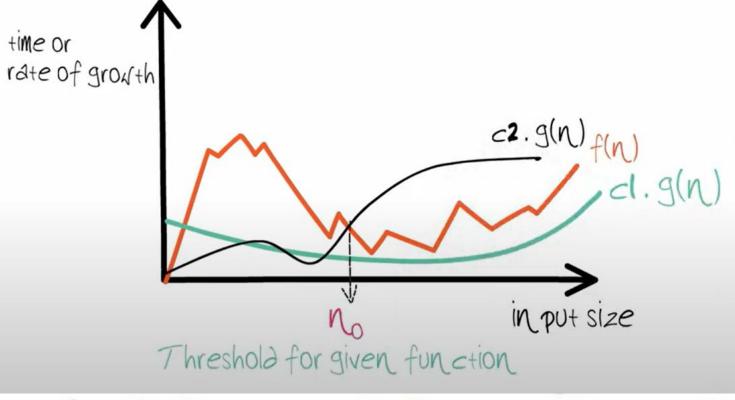
Theta Notation 
$$\Theta$$
  
 $f(n) = Our Algorithm$ 











$$c1.g(n) \leftarrow f(n) \leftarrow c2.g(n)$$
$$f(n) = \theta g(n)$$

where c1, c2, n > 0

## Prove that $f(n) = \Theta$ g(n) where

$$f(n) = 3n + 2$$
 and  $g(n) = n$ 

Lowerbound: c1.  $g(n) \le f(n)$ 

c1. 
$$n \le 3n + 2$$
  
c1 = 1 and  $n \ge 1$ 

 $n \le 3n+2$  for  $n \ge 1$  is True

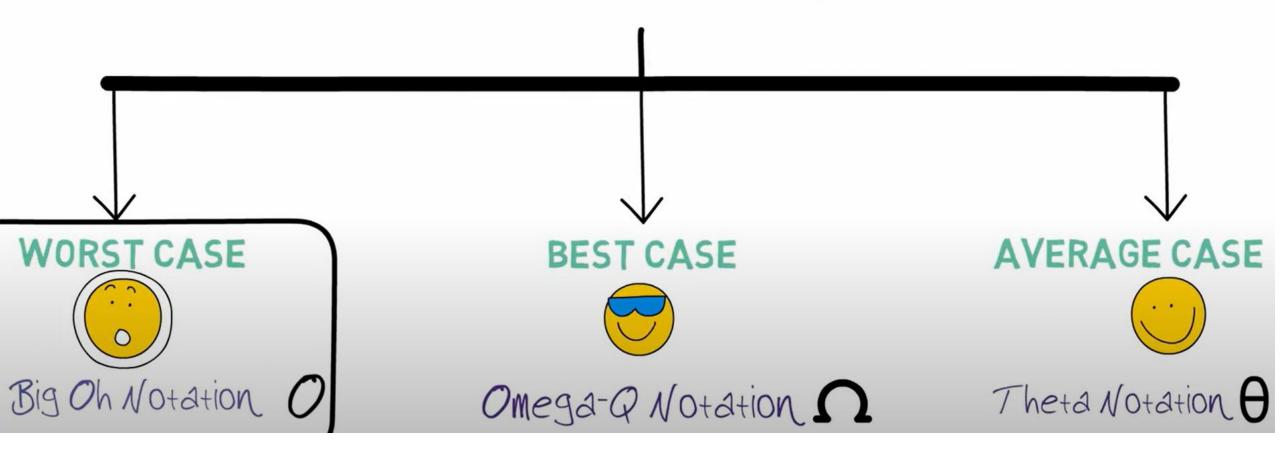
Upperbound:  $f(n) \le c2$ . g(n)

$$3n + 2 \le c2 \cdot n$$
  
for  $c2 = 4$  and  $n \ge 1$ 

$$3n + 2 \le 4n$$
  
for  $n \ge 1$  is True

$$3n+2=\Theta(n)$$

## ASYMPTOTIC NOTATION



#### Some Common Algo's Complexities

	n - f(n)	$\lg n$	n	$n \lg n$	$n^2$	$2^n$	n!
	10	$0.003~\mu {\rm s}$	$0.01~\mu \mathrm{s}$	$0.033~\mu { m s}$	$0.1~\mu \mathrm{s}$	$1~\mu \mathrm{s}$	$3.63 \mathrm{\ ms}$
	20	$0.004~\mu s$	$0.02~\mu \mathrm{s}$	$0.086 \; \mu { m s}$	$0.4~\mu \mathrm{s}$	1  ms	77.1 years
	30	$0.005 \; \mu { m s}$	$0.03~\mu \mathrm{s}$	$0.147 \; \mu { m s}$	$0.9~\mu s$	1 sec	$8.4 \times 10^{15} \text{ yrs}$
	40	$0.005 \; \mu { m s}$	$0.04~\mu \mathrm{s}$	$0.213 \; \mu { m s}$	$1.6~\mu s$	18.3 min	130
₹ 2×	50	$0.006~\mu \mathrm{s}$	$0.05~\mu \mathrm{s}$	$0.282 \ \mu s$	$2.5~\mu \mathrm{s}$	13 days	
1	100	$0.007 \; \mu { m s}$	$0.1~\mu \mathrm{s}$	$0.644~\mu { m s}$	$10 \ \mu s$	$4 \times 10^{13} \text{ yrs}$	
۱ ۱	1,000	$0.010 \; \mu { m s}$	$1.00~\mu \mathrm{s}$	$9.966 \ \mu s$	$1 \mathrm{\ ms}$		
	10,000	$0.013~\mu { m s}$	$10 \ \mu s$	$130~\mu s$	100  ms		
	100,000	$0.017 \; \mu s$	$0.10~\mathrm{ms}$	$1.67~\mathrm{ms}$	10 sec		
	1,000,000	$0.020 \; \mu s$	1  ms	19.93  ms	$16.7 \min$		
	10,000,000	$0.023~\mu { m s}$	$0.01  \mathrm{sec}$	$0.23  \sec$	$1.16  \mathrm{days}$		
	100,000,000	$0.027~\mu s$	$0.10  \sec$	$2.66  \mathrm{sec}$	115.7 days		
	1,000,000,000	$0.030 \; \mu s$	1 sec	$29.90  \mathrm{sec}$	31.7 years		

Figure 2.4: Growth rates of common functions measured in nanoseconds

Book: Algorithm Design Manual by Skiena

mas and