# A Model Checker for Bilateral State-based Modal Logic (BSML)

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#### Abstract

Bilateral State-based Modal Logic (BSML), which proposed by [Aloni(2022)], extends classical modal logic by adopting state-based semantics and introducing a non-emptiness atom to account for free choice inferences in natural language. Despite its expressive power, no automated verification tool exists for BSML. This project aims to develop a model checker for BSML, enabling automated reasoning over its logical properties.

## Contents

1	Introduction	2
2	Motivation	2
3	The Syntax of BSML	2
4	Semantics	3
5	Web frontend for the model checker	7
	5.1 Web-Based User Interface	8
	5.2 Formula Evaluation	8
	5.3 Web server configuration	9
	5.4 Usage	10
6	Conclusion	11
Bi	ibliography	11

## 1 Introduction

## 2 Motivation

BSML was developed to account for *Free Choice* (FC) inferences, where disjunctive sentences give rise to conjunctive interpretations. For example, the sentence "You may go to the beach or to the cinema" typically implies that "You may go to the beach and you may go to the cinema" This inference is unexpected from a classical logical perspective, as disjunction does not typically imply conjunction.

The key idea in BSML is the *neglect-zero tendency*, which posits that humans tend to disregard models that verify sentences by virtue of some empty configuration. BSML formalizes this tendency by introducing the *nonemptiness atom* (NE), which ensures that only nonempty states are considered in the interpretation of sentences. This leads to the prediction of both narrow-scope and wide-scope FC inferences, as well as their cancellation under negation.

BSML has been extended in two ways:

- BSML $^{\mathbb{W}}$ : This extension adds the *global disjunction*  $\mathbb{W}$ , which allows for the expression of properties that are invariant under bounded bisimulation.
- $\mathbf{BSML}^{\odot}$ : This extension adds the *emptiness operator*  $\odot$ , which can be used to cancel out the effects of the nonemptiness atom (NE).

These extensions are expressively complete for certain classes of state properties, and natural deduction axiomatizations have been developed for each of these logics.

# 3 The Syntax of BSML

The syntax of **BSML** is defined over a set of propositional variables Prop. The formulas of BSML are generated by the following grammar:

$$\varphi ::= p \mid \bot \mid \neg \varphi \mid (\varphi \land \varphi) \mid (\varphi \lor \varphi) \mid \Diamond \varphi \mid \text{NE}$$

where  $p \in \text{Prop}$ .

**BSML** with global disjunction  $\vee$  by adding the clause  $\varphi \vee \varphi$ .

The classical modal logic **ML** is the NE-free fragment of BSML.

Below is the implementation of the syntax of BSML<sup>\newtilde{\neq}}}}}. We use Int to index the set of propositional variables.</sup>

```
module Syntax where

type Prop = Int

data BSMLForm = P Prop | Bot | Neg BSMLForm | Con BSMLForm BSMLForm | Dis BSMLForm BSMLForm | Dia BSMLForm | NE | Gdis BSMLForm BSMLForm deriving (Eq,Ord,Show)
```

Note that Dis is the "V" disjunction, while Gdis is the "W" disjunction.

The box modality  $\square$  is defined as the dual of the  $\lozenge$ :  $\square \varphi := \neg \lozenge \neg \varphi$ .

```
box :: BSMLForm -> BSMLForm
box = Neg . Dia . Neg
```

The pragmatic enrichment function  $[ ]^+$ :  $ML \to BSML$  is recursively defined as:

$$[p]^{+} := p \wedge NE$$

$$[\bigcirc a]^{+} := \bigcirc ([a]^{+}) \wedge NE \quad \text{for } \bigcirc \in \{\neg, \diamondsuit, \square\}$$

$$[\alpha \triangle \beta]^{+} := ([\alpha]^{+} \triangle [\beta]^{+}) \wedge NE \quad \text{for } \triangle \in \{\land, \lor\}$$

We implement pragmatic enrichment prag as a function BSMLForm -> BSMLForm, as the ML formulas are not used anywhere else in this project.

```
prag :: BSMLForm -> BSMLForm
prag (P n) = Con (P n) NE
prag (Neg f) = Con (Neg $ prag f) NE
prag (Con f g) = Con (Con (prag f) (prag g)) NE
prag (Dis f g) = Con (Dis (prag f) (prag g)) NE
prag (Dia f) = Con (Dia (prag f)) NE
prag (Gdis f g) = Con (Gdis (prag f) (prag g)) NE
prag Bot = Con Bot NE
prag NE = NE
```

## 4 Semantics

The semantics of BSML is based on team semantics, where formulas are interpreted with respect to sets of possible worlds, which called states or teams rather than single worlds. A model M is a triple (W, R, V), where:

- W is a nonempty set of possible worlds,
- $R \subseteq W \times W$  is an accessibility relation,
- $V: \text{Prop} \to \mathcal{P}(W)$  is a valuation function.

A state s is a subset of W, interpreted as an information state. The semantics of **BSML** is bilateral, with separate conditions for support ( $\models$ ), meaning assertion, and anti-support ( $\models$ ), meaning rejection. The conditions are defined recursively as follows:

$$M, s \models p \quad \text{iff} \quad \forall w \in s, w \in V(p)$$

$$M, s \rightleftharpoons p \quad \text{iff} \quad \forall w \in s, w \notin V(p)$$

$$M, s \models \bot \quad \text{iff} \quad s = \emptyset$$

$$M, s \rightleftharpoons \bot \quad \text{always}$$

$$M, s \models \neg \varphi \quad \text{iff} \quad M, s \rightleftharpoons \varphi$$

$$M, s \rightleftharpoons \neg \varphi \quad \text{iff} \quad M, s \models \varphi$$

An atomic proposition is supported at a state if it holds at every world of that state, and is anti-supported if every world falsifies it. From this, we can already see that = is not the same as  $\not\models$ . This extends to the clauses for falsum  $\bot$ . Negation is then defined in terms of anti-support.

```
\begin{array}{lll} M,s\models\varphi\wedge\psi & \text{iff} & M,s\models\varphi \text{ and } M,s\models\psi \\ M,s\models\varphi\wedge\psi & \text{iff} & \exists t,u\subseteq s \text{ s.t. } s=t\cup u \text{ and } M,t\models\varphi \text{ and } M,u\models\psi \\ M,s\models\varphi\vee\psi & \text{iff} & \exists t,u\subseteq s \text{ s.t. } s=t\cup u \text{ and } M,t\models\varphi \text{ and } M,u\models\psi \\ M,s\models\varphi\vee\psi & \text{iff} & M,s\models\varphi \text{ and } M,s\models\psi \end{array}
```

A state supports a disjunction if it is a union of two substates, each supporting one of the disjuncts. The intuition is that a disjunction is supported when the information state contains evidence for both of the disjuncts. This is also known as *split disjunction*, since it requires splitting the state into substates. Dually, a conjunction is anti-suported when there is evidence falsifying both of the conjuncts.

$$\begin{array}{ll} M,s \models \Diamond \varphi & \text{iff} \quad \forall w \in s, \exists t \subseteq R[w] \text{ s.t. } t \neq \emptyset \text{ and } M,t \models \varphi \\ M,s \models \Diamond \varphi & \text{iff} \quad \forall w \in s, \ M,R[w] \models \varphi \\ M,s \models \Box \varphi & \text{iff} \quad \forall w \in s, \ M,R[w] \models \varphi \\ M,s \models \Box \varphi & \text{iff} \quad \forall w \in s, \exists t \subseteq R[w] \text{ s.t. } t \neq \emptyset \text{ and } M,t \models \varphi \end{array}$$

A state supports a diamond formula  $\diamond \varphi$  if each word sees a (non-empty) state supporting  $\varphi$ ; A state anti-supports  $\diamond \varphi$  if all worlds accessible from the state together anti-supports  $\varphi$ . The clauses for  $\Box$  are derived from the clauses for  $\neg$  and  $\diamond$ .

$$M, s \models NE \text{ iff } s \neq \emptyset$$
  
 $M, s \models NE \text{ iff } s = \emptyset$ 

As the name suggests, the nonemptiness atom is supported when the state is empty, and is rejected otherwise. When combined with disjunction in the form of pragmatic enrichment, a state supports an enriched disjunction  $[\varphi \lor \psi]^+$  when it is a union of two *non-empty* substates, each supporting one of the disjuncts. This is what enables **BSML** to derive FC inferences.

$$M, s \models \varphi \lor \psi \text{ iff } M, s \models \varphi \text{ or } M, s \models \psi$$
  
 $M, s \models \varphi \lor \psi \text{ iff } M, s \models \varphi \text{ and } M, s \models \psi$ 

more to add...

The following is the definition of our Data Type for Model Checker.

```
-- Based on the Homework

-- {-# LANGUAGE InstanceSigs #-}
module Semantics where

import Test.QuickCheck
import Data.List

import Syntax
import Data.Maybe

type World = Integer
type Universe = [World]
type Proposition = Int
type State = [World]

type Valuation = World -> [Proposition]
```

```
type Relation = [(World, World)]
data KripkeModel = KrM Universe Valuation Relation

data ModelState = MS KripkeModel State

instance Show KripkeModel where
   show (KrM u v r) = "KrM " ++ show u ++ " " ++ vstr ++ " " ++ show r where
   vstr = "(fromJust . flip lookup " ++ show [(w, v w) | w <- u] ++ ")"

instance Show ModelState where
   show (MS k s) = "MS" ++ show k ++ " " ++ show s</pre>
```

The following helper function defines the set of all successors of a world:

```
(!) :: Relation -> World -> [World]
(!) r w = map snd $ filter ((==) w . fst) r
```

Here we define the semantics of **BSML** ...

```
-- helper function to find all pairs of worlds t and u that the union of t and u is the
    input s
allPairs :: [World] -> [([World], [World])]
allPairs [] = [([],[])]
allPairs (x:xs) =
  [ (x:ts, x:us) | (ts,us) <- allPairs xs ] ++
  [ (x:ts, us) | (ts,us) <- allPairs xs ] ++
 [ (ts, x:us) | (ts,us) <- allPairs xs ]
-- helper function to find all non-empty subsets of a list
subsetsNonEmpty :: [World] -> [[World]]
subsetsNonEmpty [] = []
subsetsNonEmpty (x:xs) =
 let rest = subsetsNonEmpty xs
 in [[x]] ++ rest ++ map (x:) rest
(|=) :: ModelState -> BSMLForm -> Bool
(MS (KrM _ v _) s) |= (P n) = all (\w -> n 'elem' v w) s
(MS _ s) |= Bot = null s
(MS _s) \mid = NE = not $ null s
(MS (KrM u v r) s) \mid = (Neg f) = MS (KrM u v r) s = \mid f
m \mid = (Con f g) = m \mid = f \&\& m \mid = g
(MS k s) \mid (Dis f g) = any (\((ts,us) -> MS k ts \mid = f && MS k us \mid = g) (allPairs s)
m \mid = (Gdis f g) = m \mid = f \mid \mid m \mid = g
(MS (KrM u v r) s) \mid = (Dia f) = all (\setminusw -> any (\setminus1 -> MS (KrM u v r) 1 \mid = f) (
   subsetsNonEmpty (r ! w))) s
(=|) :: ModelState -> BSMLForm -> Bool
(MS (KrM _{v} _{v} _{s}) _{s}) _{s} _{s} (P _{n}) _{s} all (_{v} _{s} _{s} _{s}
(MS \_ \_) =| Bot = True
(MS _s) = | NE = null s
(MS (KrM u v r) s) = | (Neg f) = MS (KrM u v r) s | = f
(MS k s) = | (Con f g) = any (\((ts,us) -> MS k ts = | f && MS k us = | g) (allPairs s)
m = | (Dis f g) = m = | f &  m = | g
m = | (Gdis fg) = m = | f &  m = | g
 (MS (KrM u v r) s) = | (Dia f) = all (\w -> MS (KrM u v r) (r ! w) = | f) s
```

The following provide QuickCheck properties for the ModelState.

```
-- Based on homework

instance Arbitrary ModelState where
arbitrary = sized modelStateGen

modelStateGen :: Int -> Gen ModelState
modelStateGen n = do
model@(KrM u _ _) <- modelGen n
state <- sublistOf u -- choose a set from universe as state
```

```
return (MS model state)
modelGen :: Int -> Gen KripkeModel
modelGen n = do
 size <- choose (1, n)
 let u = [0 .. fromIntegral size - 1]
 v \leftarrow arbitraryValuation u
 r <- arbitraryRelation u
 return $ KrM u v r
arbitraryValuation :: Universe -> Gen Valuation
arbitraryValuation u = do
 props <- vectorOf (length u) (sublistOf [0..10]) -- fixed vocabulary
 let val w = props !! fromIntegral w -- function
 return val
arbitraryRelation :: Universe -> Gen Relation
arbitraryRelation u = do
 pairs <- sublistOf [(x, y) | x <- u, y <- u]
  return (nub pairs)
```

A model state pair (M, s) is indisputable if for all  $w, v \in s, R[w] = R[v]$ .

```
isIndisputable :: ModelState -> Bool
isIndisputable (MS (KrM _ r) s) = all (\w -> all (\v -> sort (r ! w) == sort (r ! v )) s
) s
```

A model state pair is state-based if for all  $w \in s$ , R[w] = s.

```
isStateBased :: ModelState -> Bool
isStateBased (MS (KrM _ r) s) = all (\w -> sort (r ! w) == sort s) s
```

```
example1 :: KripkeModel
example1 = KrM [0,1,2] myVal [(0,1), (1,2), (2,1)] where
  myVal 0 = [0]
  myVal _ = [4]

example2 :: KripkeModel
example2 = KrM [0,1] myVal [(0,1), (1,1)] where
  myVal 0 = [0]
  myVal _ = [0, 4]

example11 :: ModelState
example11 = MS example1 [0,1,2]

example12 :: ModelState
example12 = MS example2 [0,1]
```

Here, we encode the example in Figure 2, [Aloni(2018)]. Here, a = P 2, b = P 3:

```
w0, wa, wb, wab :: Integer
(w0, wa, wb, wab) = (0,1,2,3)
val2a18 :: Valuation
val2a18 = fromJust . flip lookup [(w0,[]), (wa,[2]),(wb,[3]),(wab,[2,3])]

m2a18 :: KripkeModel
m2a18 = KrM [w0,wa,wb,wab] val2a18 []

ms2a18, ms2b18 :: ModelState
ms2a18 = MS m2a18 [wa, wb]
ms2b18 = MS m2a18 [wa]
```

Here is another example, from Figure 2(c), [Aloni et al.(2024)Aloni, Anttila, and Yang]. Here p = P 0, q = P 1:

```
wp, wq, wpq :: Integer
(wp, wq, wpq) = (1,2,3) -- same w0 as above
val2c24 :: Valuation
```

```
val2c24 = fromJust . flip lookup [(w0,[]),(wp,[0]),(wq,[1]),(wpq,[0,1])]
rel2c24 :: Relation
rel2c24 = [(w0,wq), (wpq,wp), (wpq,wq)]

m2c24 :: KripkeModel
m2c24 = KrM [w0,wp,wq,wpq] val2c24 rel2c24

ms2c241, ms2c242 :: ModelState
ms2c241 = MS m2c24 [w0]
ms2c242 = MS m2c24 [wpq]
```

The following example is from Figure 3(a), [Aloni(2022)]

```
val3a22 :: Valuation
val3a22 = val2a18
rel3a22 :: Relation
re13a22 = [(wa, w0), (wa, wab), (wb, w0), (wb, wab)]
m3a22 :: KripkeModel
m3a22 = KrM [w0,wa,wb,wab] val3a22 rel3a22
ms3a22 :: ModelState
ms3a22 = MS m3a22 [wa,wb]
counterexamplews1 :: ModelState
counterexamplews1 = MS (KrM [0,1,2,3,4] (fromJust . flip lookup [(0,[0,4,6,8,9,10])
    (1,[1,4,6,8]),(2,[0,3,5,8,9]),(3,[0,1,4,6,8]),(4,[1,2,3,7,8]))) [(0,0),(1,1),(1,4)
    ,(2,1),(2,4),(3,1),(3,2),(4,1)] ) [0,2,3]
counterexamplewmd :: ModelState
counterexamplewmd = MS (KrM [0,1,2] (fromJust . flip lookup [(0,[1,3,4,7,9])
    (1,[0,2,6,7,8,9,10]),(2,[1,6,8,9])) [(1,0),(1,1),(2,1),(2,2)]) [0,1]
p :: BSMLForm
p = P 0
q :: BSMLForm
q = P 1
```

The following is a QuickCheck example, change this to a better tautology test.

```
badTautology :: BSMLForm
badTautology = Neg(Bot 'Con' NE)

prop_tautologyHolds :: ModelState -> Bool
prop_tautologyHolds m = m |= badTautology
```

## 5 Web frontend for the model checker

To enhance the usability of the BSML model checker, we have developed a web-based interface using Haskell for the backend and various modern web technologies for the frontend. The web application allows users to input modal logic formulas, visualize Kripke models, and dynamically view verification results. The process works as follows:

We implemented the frontend using Next.js, KaTeX [KaTeX Contributors(2025)], and HTML5 Canvas [W3Schools(2025)]. Users can enter models, states, and formulas through input fields, and the web application submits model-checking queries via HTTP requests to the backend.

On the backend, we use Scotty, a lightweight Haskell web framework, to handle requests from the frontend and run the model checker. Once the computation is complete, the backend returns the verification result (True/False) to the frontend.

Additionally, the frontend generates a graph representation of the Kripke model and states, providing users with a visual understanding of the verification process.

This web server makes the BSML model checker more accessible and user-friendly, allowing users to verify modal logic formulas without writing any Haskell code.

#### 5.1 Web-Based User Interface

We developed a Next.js frontend that provides an intuitive user interface for building and evaluating logical models. To handle mathematical formulas, we integrated KaTeX, a JavaScript library, which dynamically renders user-entered LaTeX formulas into HTML for clear and precise display. For visualizing Kripke models, we utilized HTML5 Canvas to dynamically draw the worlds (nodes) and relationships (edges) of the logical model. The nodes are color-coded to represent different states, and the graph updates in real-time based on user input, providing an interactive and responsive experience.

To facilitate communication with the Haskell backend, we defined a structured interface, ModelEvaluationRequest, which encapsulates the essential elements of Kripke models and logical formulas. This interface includes:

- universe: A list of world identifiers.
- valuation: A mapping of worlds to the propositions that hold true in them.
- relation: A list of relationships (edges) between worlds.
- state: The selected states (worlds) for evaluation.
- formula: The logical formula to be evaluated.
- isSupport: A boolean value, true means support(|=), false means not support (=).

The frontend sends this data as a POST request to the backend, enabling seamless evaluation and retrieval of results.

#### 5.2 Formula Evaluation

The Parser module is responsible for parsing logical formulas into the internal BSMLForm representation. It supports:

- Atomic propositions: e.g.,  $p_1, p_2$
- Negation: ! (not)
- Conjunction: &
- Disjunction:
- Global disjunction: /
- Diamond  $\Diamond$

```
module Parser where
import Syntax
import Text.Parsec
-- Based on the Parsec Homework
pForm :: Parsec String () BSMLForm pForm = spaces >> pCnt <* (spaces >> eof) where
 pCnt = chainl1 pDiaBox (spaces >> (pGdis <|> pDisj <|> pConj))
 pConj = char '&' >> return Con
 pDisj = char '|' >> return Dis
  pGdis = char '/' >> return Gdis
  -- Diamond operator has higher precedence than conjunction
  pDiaBox = spaces >> ( try (pDiaOp <|> pBoxOp) <|> pAtom)
  pDiaOp = char '<' >> char '>' >> Dia <$> pDiaBox
  pBoxOp = char '[' >> char ']' >> box <$> pDiaBox
 -- An atom is a variable, negation, or a parenthesized formula pAtom = spaces >> (pBot <|> pNE <|> pVar <|> pNeg <|> (spaces >> char '(' *> pCnt <* char ')' <* spaces))
  -- A variable is 'p' followed by digits
 pVar = char 'p' >> P . read <$> many1 digit <* spaces
 pBot = string "bot" >> return Bot
 pNE = string "ne" >> return NE
  -- A negation is '!' followed by an atom
 pNeg = char '!' >> Neg <$> pDiaBox
parseForm :: String -> Either ParseError BSMLForm
parseForm = parse pForm "input"
parseForm' :: String -> BSMLForm
parseForm's = case parseForm s of
  Left e -> error $ show e
  Right f -> f
```

# 5.3 Web server configuration

The server is built using Scotty [Hackage(2025)] and listens for POST requests at /input:

```
main :: IO ()
main = scotty 3001 $ do
   middleware allowCors
    post "/input" $ do
        input <- jsonData :: ActionM Input
        let modelState = inputToModelState input
            (MS kripkeModel state') = modelState
            KrM _ _ relation' = kripkeModel
            -- Parse and Check Formula
            result = do
              parsedFormula <- parseForm (formula input)</pre>
              let finalFormula = if isPrag input then prag parsedFormula else parsedFormula
              return $ if isSupport input
                         then modelState |= finalFormula
                         else modelState =| finalFormula
            -- Generate response
            finalResult = case result of
              Left err -> object [
                  "error" .= show err
                , "formula" .= formula input
                , "state" .= state;
```

```
Right checkResult -> object [
              "result" .= checkResult
"formula" .= formula input
             , "state" .= state,
              "relation" .= show relation;
             , "relation_type" .= (if isSupport input then "support |=" else "reject =|"
                  :: String)
             ]
    json finalResult
post "/quickcheck" $ do
    inputQuickCheck <- jsonData :: ActionM InputQuickCheck</pre>
     -- Parse both formulas
    let pf1 = parseForm (formulaL inputQuickCheck)
        pf2 = parseForm (formulaR inputQuickCheck)
    case (pf1, pf2) of
      (Right f1, Right f2) -> do
        let finalF1 = if isPragL inputQuickCheck then prag f1 else f1
             finalF2 = if isPragR inputQuickCheck then prag f2 else f2
             prop m = prop_implicationHolds finalF1 finalF2 m
        result <- liftIO $ quickCheckWithResult stdArgs { maxSuccess = 30 } prop
        let jsonResult = case result of
               Success {} -> object [
                    "status" .= ("passed" :: String),
                   "numTests" .= numTests result
               GaveUp {} -> object [
                    "status" .= ("gave up" :: String),
                    "reason" .= reason result
               Failure { output = out, usedSeed = _ } -> object [
                   "status" .= ("failed" :: String),
"reason" .= reason result,
"output" .= out
               NoExpectedFailure {} -> object [
                    status" .= ("unexpected success" :: String)
        ison isonResult
       _ -> json $ object [
          "status" .= ("parse error" :: String),
"errorL" .= show pf1,
           "errorR" .= show pf2
```

## 5.4 Usage

Our BSML model checker web application is available at https://bsmlmc.seit.me.

Here we give an example to illustrate how to use the web application.

We define a model with universe:  $\{W1,W2,W3,W4\}$ , state:  $\{W2,W3\}$ . In W1, p1 and p2 are true; in W2, p1 is true; in W3, p2 is true; W4 is empty. W2 and W3 are reflexive and mutually related. We test whether formula  $\Diamond p1 \land \Diamond p2$  holds in this model. Figure 1 shows how to input worlds, valuations and relations in interface the. Figure 2 shows how to choose worlds in the state and input the formula. By clicking **Evaluate** bottow, web can return model-checking results. Figure 3 displays a graphical representation of the model and state.

#### **BSML Model Checker**

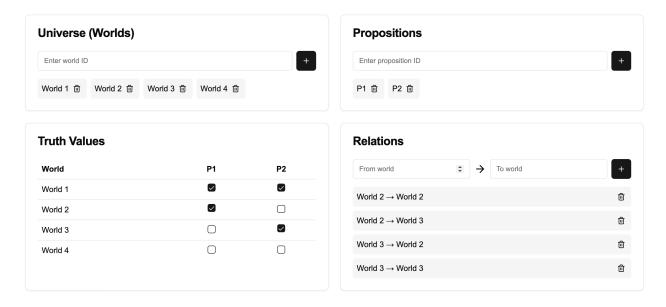


Figure 1: interface1

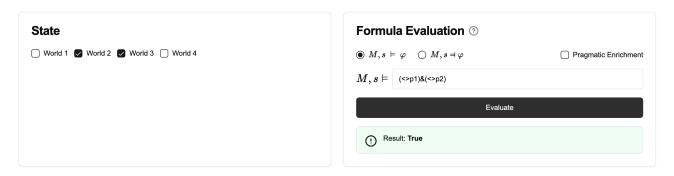


Figure 2: interface2

## 6 Conclusion

## References

[Aloni(2018)] Maria Aloni. FC disjunction in state-based semantics. Accessed: 2025-03-27, 2018. URL https://www.marialoni.org/resources/Aloni2018.pdf.

[Aloni(2022)] Maria Aloni. Logic and conversation: The case of free choice. Semantics & Pragmatics, 15:1–60, 2022. doi: 10.3765/sp.15.5. URL https://doi.org/10.3765/sp.15.5.

[Aloni et al.(2024)Aloni, Anttila, and Yang] Maria Aloni, Aleksi Anttila, and Fan Yang. State-based modal logics for free choice. *Notre Dame Journal of Formal Logic*, 65(4):367–413, 2024. doi: 10.1215/00294527-2024-0027.

[Hackage(2025)] Hackage. Scotty 0.22 - web.scotty documentation, 2025. URL https://hackage.haskell.org/package/scotty-0.22/docs/Web-Scotty.html. Accessed: 2025-03-25.

Model Visualization

Generate Visualization

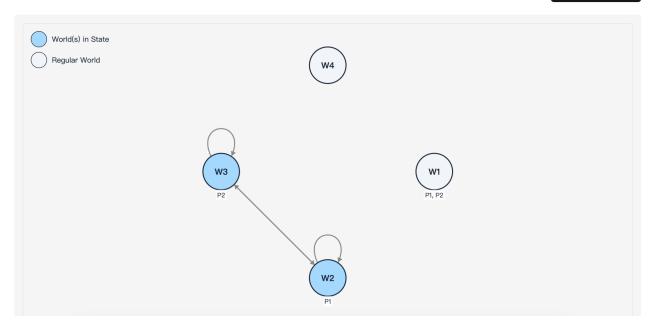


Figure 3: model graph

[KaTeX Contributors(2025)] KaTeX Contributors. Katex: Fast math typesetting for the web, 2025. URL https://katex.org/. Accessed: 2025-03-25.

[W3Schools(2025)] W3Schools. Html5 canvas tutorial, 2025. URL https://www.w3schools.com/html/html5\_canvas.asp. Accessed: 2025-03-25.