

Backpropagation Preparation

- $e_j(n) = d_j(n) - y_j(n)$

$$E(n) = \frac{1}{2} \sum_{j \in c} e_j^2(n) \quad E_{AV} = \frac{1}{N} \sum_{n=1}^N E(n)$$

$$v_j(n) = \sum_{i=0}^p w_{ji}(n) y_i(n) \quad y_j(n) = \varphi_j(v_j(n))$$

$$\frac{\partial E(n)}{\partial w_{ji}(n)} = \frac{\partial E(n)}{\partial e_j(n)} \frac{\partial e_j(n)}{\partial y_j(n)} \frac{\partial y_j(n)}{\partial v_j(n)} \frac{\partial v_j(n)}{\partial w_{ji}(n)}$$

$$\frac{\partial E(n)}{\partial e_j(n)} = e_j(n), \quad \frac{\partial e_j(n)}{\partial y_j(n)} = -1, \quad \frac{\partial y_j(n)}{\partial v_j(n)} = \varphi'_j(v_j(n)), \quad \frac{\partial v_j(n)}{\partial w_{ji}(n)} = y_j(n)$$

$$\frac{\partial E(n)}{\partial w_{ji}(n)} = -e_j(n) \varphi'_j(v_j(n)) y_j(n)$$

