

Unification modulo Boolean Rings

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Structure

luiuh

(Axiom)

$$\Gamma, A \vdash A$$

 $(\rightarrow$ -Introduction)

$$\frac{\Gamma, A \vdash B}{\Gamma \vdash A \rightarrow B}$$

 $(\rightarrow$ -Elimination)

$$\frac{\Gamma \vdash A \rightarrow B \quad \Gamma \vdash A}{\Gamma \vdash B}$$

 $(\forall$ -Introduction)

$$\frac{\Gamma \vdash B}{\Gamma \vdash \forall \alpha B}$$

$$\alpha \notin \text{FV}(\Gamma)$$

 $(\forall$ -Elimination)

$$\frac{\Gamma \vdash \forall \alpha B}{\Gamma \vdash B[\alpha := b]}$$

$$b \in \mathcal{V}_P$$

(Axiom) $\Gamma, x : t \vdash x : t$

(λ -Introduction)
$$\frac{\Gamma, x : t_1 \vdash M : t_2}{\Gamma \vdash \lambda x : t_1. M : t_1 \rightarrow t_2}$$

(λ -Elimination)
$$\frac{\Gamma \vdash M_1 : t_1 \rightarrow t_2 \quad \Gamma \vdash M_2 : t_1}{\Gamma \vdash M_1 M_2 : t_2}$$

(\forall -Introduction)
$$\frac{\Gamma \vdash M : t}{\Gamma \vdash \Lambda \alpha. M : \forall \alpha. t} \quad \alpha \notin \text{FV}(\Gamma)$$

(\forall -Elimination)
$$\frac{\Gamma \vdash M : \forall \alpha. t}{\Gamma \vdash M t' : t [\alpha := t']}$$

$$\begin{array}{c}
\overline{\Gamma} \vdash x : \forall \vec{a} (\overline{A_1} \rightarrow \dots \rightarrow \overline{A_n} \rightarrow \mathbf{false}) \\
\hline
\overline{\Gamma} \vdash x \vec{t} : P_{\tilde{a}_1 \tilde{b}_1}^1 \rightarrow \dots \rightarrow P_{\tilde{a}_n \tilde{b}_n}^n \rightarrow \mathbf{false} \quad \overline{\Gamma} \vdash N_1 : P_{\tilde{a}_1 \tilde{b}_1}^1 \\
\hline
\vdots \\
\hline
\overline{\Gamma} \vdash x \vec{t} N_1 \dots N_{n-1} : P_{\tilde{a}_n \tilde{b}_n}^n \rightarrow \mathbf{false} \quad \overline{\Gamma} \vdash N_n : P_{\tilde{a}_n \tilde{b}_n}^n \\
\hline
\overline{\Gamma} \vdash (x \vec{t} N_1 \dots N_{n-1}) N_n : \mathbf{false}
\end{array}$$