Contents

1 Equational Unification

In the following let E be a set of identities of the form $\{e_1 \approx f_1, \ldots, e_n \approx f_n\}$. Furthermore let $\mathcal{S}ig(E)$ denote the set of all function symbols occurring in E.

Definition 1.1. An E**-unification Problem** over Σ is a finite set S of the form $S = \left\{ s_1 \overset{?}{\approx}_E t_1, \ldots, s_n \overset{?}{\approx}_E t_n \right\}$ with $s_1, \ldots, s_n, t_1, \ldots, t_n \in T(\Sigma, V)$, V being a countable set of Variables.
A substitution σ is an E**-unifier** of S iff $\sigma(s_i) \approx_E \sigma(t_i)$ for all $1 \leq i \leq n$. The set of all E-unifiers of S is denoted by $\mathcal{U}_E(S)$. S is E**-unifiable** iff $\mathcal{U}_E(S) \neq \emptyset$.

Definition 1.2. Let S be an E-unification problem over Σ.

- S is an **elementary** E-unification problem iff $\mathcal{S}ig(E) = \Sigma$.
- S is an E-unification problem **with constants** iff $\Sigma - \mathcal{S}ig(E) \subseteq \Sigma^{(0)}$
- S is an **general** E-unification problem iff $\Sigma - \mathcal{S}ig(E)$ contains an at least unary function symbol.