

# SMT IN REVERSE ENGINEERING, FOR DUMMIES

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# ABOUT ME

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# REVERSE ENGINEERING IN 15 SECONDS?

- Take stuff, e.g. software, apart
- Understand how it works
- Many possible goals
  - How can I reach a specific state?

# WHAT IS SMT?

- Satisfiability modulo theories, SMT
- A bunch of variables
- A bunch of theories
  - Theory = A bunch of rules
- A bunch of formulas
- Can we find values for all values s.t. all formulas are satisfied?

## SMT: EXAMPLE 1

$$x + 13 = 37$$



## SMT: EXAMPLE 2

$$x + y + 13 = 37 - z$$

$$x - 2 \cdot y + 10 = 10 \cdot z$$

$$4 \cdot x - z + 13 = 37 + y$$



# SMT: EXAMPLE 3

$$|\Omega(T, \varepsilon, a, b)| \leq 2$$

$$\varphi(\Omega, \varepsilon) = \int_0^T \int_{\mathbb{R}^d} \left( \int_0^t \Psi_k^*(x) dx \right) dt - \int_0^T \int_{\mathbb{R}^d} \Psi_k^*(x) dt - \sum_{k=1}^{\infty} \beta_k(x) + \int_0^T (x-a) \sum_{k=1}^{\infty} \Psi_k^*(u) du$$

$$\rho(u) = \sum_{k=1}^{\infty} \rho_k^* \log \frac{f}{f_k}$$

$$c_k \gamma_k^* = \lambda_i c_i e^{-\frac{1}{2} u_k^2}$$

$$\eta_{ij} = \sum_{k=1}^{\infty} a_{kj} \frac{f_k}{f}$$

$$\log \varphi(u) = -\frac{\sigma^2 u^2}{2}$$

$$i^2 = -1, j^2 = -1, k^2 = -1$$

$$\lim_{n \rightarrow \infty} \frac{(2n)!}{(2n+1)!} = e^{-2}$$

$$P(\omega) = \sum_{k=1}^{\infty} \rho_k^* \int_{\mathbb{R}^d} e^{-\frac{1}{2} u^2} du$$

$$S(\omega, T) = \frac{2}{\pi} \int_0^T \int_{\mathbb{R}^d} \sin(xt) dt$$

$$P(\eta_{ij} < x) = F(x)$$

$$W_k = \binom{n}{k} p^k (1-p)^{n-k}$$

$$P(\eta_{ij} \neq x) = \sup_{y \in \mathbb{R}^d, y \neq x} P(\eta_{ij} \neq y)$$

$$|A_m| = \frac{m!}{2^m} \int_{\mathbb{R}^m} f(x) \log \frac{f}{f(x)} dx \leq \varepsilon$$

$$g^{-1}(g) = e$$

$$J = \frac{1}{\sqrt{m}} \int_{\mathbb{R}^m} \left( \frac{f(x) + g(x) - f(x)}{\sqrt{m}} \right)^2 dx$$

$$\prod_{i=1}^m H_i = \bigcap_{i=1}^m H_i$$

$$\prod_{i=1}^m X_i = \bigcap_{i=1}^m X_i$$

$$H_n(x) = \frac{G_n(x)}{A_n G_n(x)}$$

$$\int d\mu_n(x) \geq \frac{1}{2} \int_{\mathbb{R}^{2m}}$$

$$f_n(t) = \frac{2e^{nt} - e^{-2t}}{(n-1)!}$$

$$R = \int_{-\infty}^{\infty} \varphi(t) dt$$

$$\lim_{n \rightarrow \infty} f_n(t) = \int_{\mathbb{R}^m} f(u) f(t-u) du = \frac{2 \lim_{n \rightarrow \infty} t^n e^{-2t}}{n!} = 0$$

$$\lim_{n \rightarrow \infty} \frac{1}{n!} = P_\varepsilon$$

$$\log \varphi(z) = i \bar{z} - c |z|^2 \left[ 1 + \frac{1}{2} \int_{\mathbb{R}^d} \psi^*(x) dx \right]$$

$$C_{ir} = \sum_{j=1}^r a_{ij} b_{rj}$$

$$\lim_{n \rightarrow \infty} \frac{\ln n!}{n} = \frac{1}{2}$$

$$\int_{-\infty}^{\infty} \frac{dt}{t^2} dt = F(x) = \frac{1}{2} \int_{-\infty}^x e^{-t^2} dt$$

$$|\psi_{ij}(z)| = \left| \int_{\mathbb{R}^d} e^{izx} dF(x) \right| \leq \int_{\mathbb{R}^d} e^{-|zx|} dF(x) = \psi(x)$$

$$\Gamma_m = \Gamma_r / \Gamma_{m-r}$$

$$g^{-1} N_g = \{g^{-1} n g \mid n \in V\}$$

$$Q(A) = \sum_{j=1}^r \int_{\mathbb{R}^d} \frac{d\theta_j}{f(x)} \ell(x) = -\log \left( \frac{\sum_{k=1}^r \rho_k^* \log \frac{f}{f_k}}{\sum_{k=1}^r \rho_k^*} \right)^2$$

$$f(g(u)) = f\left(\sum_{j=1}^r a_{ij} b_{rj}\right) = \sum_{j=1}^r a_{ij} \left(\sum_{k=1}^m b_{kj} w_k\right) = \sum_{j=1}^r a_{ij} \frac{(w_j)}{2^m} \approx \frac{1}{2^m}$$

$$P_{j,k}^{(m)} = \sum_{r=0}^m P_{j,k}^{(r)} P_{k,m-r}^{(m-r)} \frac{1}{2^m} \int_{-\infty}^{\infty} \operatorname{Re} \left\{ \varphi(t) \frac{e^{itx} - e^{-itx}}{it} \right\} dt$$

$$P(\text{loss}) \leq \frac{C_p}{\log N}$$

$$q\left(e^{-\frac{|x-y|}{nq}} - 1\right) \geq \frac{q(|x-y|)}{nq} + O\left(\frac{1}{n}\right)$$

$$\prod_{k=1}^m \left[ q_k \left( \frac{x}{nq} \right) \right]^{N_k} = e^{-\frac{1}{2}}$$

$$\liminf_{N \rightarrow \infty} \int_{\mathbb{R}^d} f(x)^N dx \geq \int_{\mathbb{R}^d} f(x)^m dx$$

$$\lim_{N \rightarrow \infty} \int_{-1}^1 f(x) \log_2 \frac{1}{f(x)} dx = \int_{-1}^1 f(x) \log_2 f(x) dx$$

$$M(1/\delta_0 - 1/\delta_1) = \int_{k=1}^{\infty} k^{-1} e^{-kx} dx$$

$$N_{\delta_0 - \delta_1} \left( \frac{2x}{\delta_0 + \delta_1} \right) = \left( \frac{2x}{\delta_0 + \delta_1} \right)^{\frac{2x}{\delta_0 + \delta_1}}$$

$$D^2(J_m) \leq \frac{K}{m} + 2K \left( \frac{1}{k} \sum_{i=1}^k Q_i(a_i) \right)$$

$$\det(M') = \det(M) + \det(M'') = \det(M)$$

$$h(x,y) = \frac{1}{4\pi} \int_{\mathbb{R}^2} \left[ \frac{1}{2} e^{-\frac{|x-y|^2}{4}} - e^{-\frac{|x-y|^2}{4}} \right] I_M(\varepsilon_m, \delta_m) \leq C_2 \frac{1}{m-n}$$



## MICROSOFT TO THE RESCUE

- Can we automate? Yes!
- Microsoft Research
- Z3 Theorem Prover
  - General purpose
  - Own language
  - Bindings for several languages
  - Open source & cross platform



## THROWBACK THURSDAY: STARCRAFT

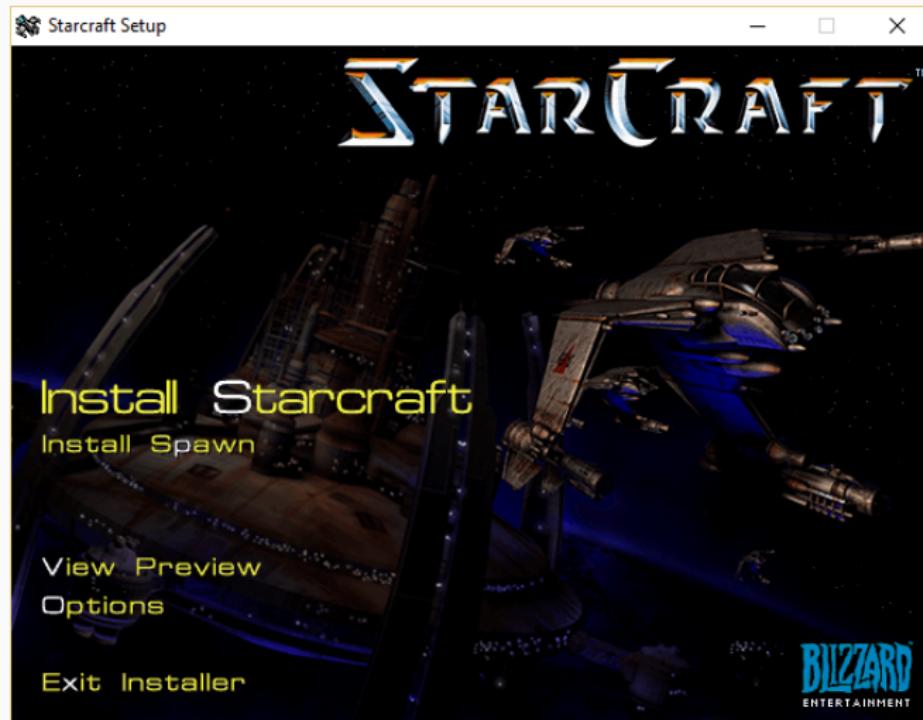
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## THROWBACK THURSDAY: STARCRAFT

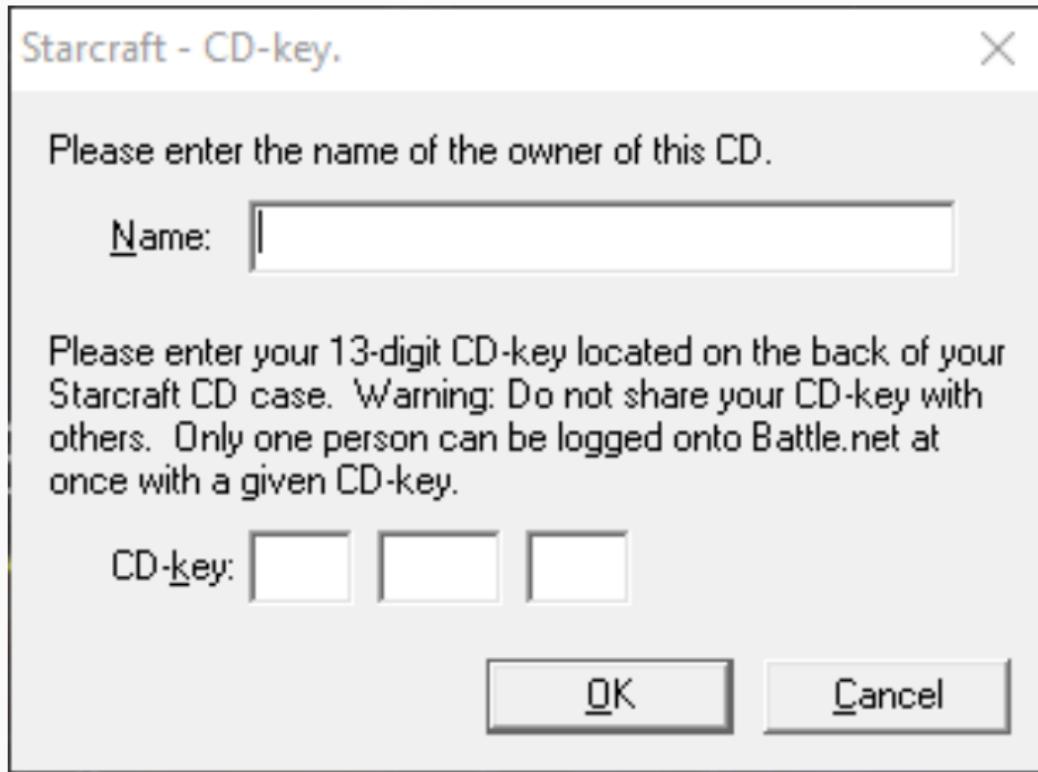
- Commercial software
- Released in 1998
  - Simple protections
  - Good starting point
- Requires a serial key
- Can we create our own?



## GETTING TO THE CORE: INSTALLER



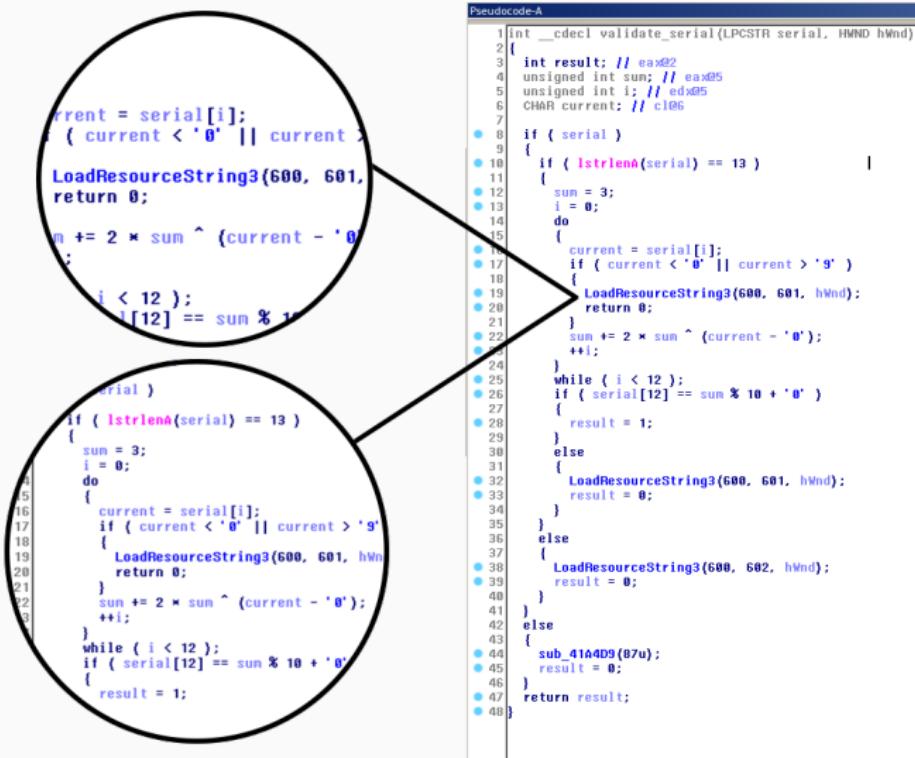
## GETTING TO THE CORE: SERIAL KEY INPUT



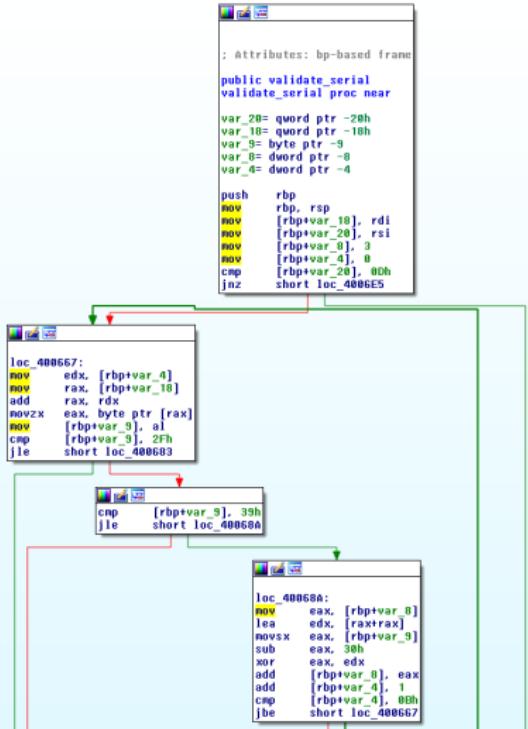
## GETTING TO THE CORE: RESOURCE STRINGS

```
... it is not necessary to install DirectX on Windows NT version 4.0 or greater.  
46 DirectX is built into Windows NT.  
47 507 A DLL required to install DirectX is missing or corrupt.  
48 DirectX installation aborted.  
49 600 Invalid CD-Key  
50 601 You entered an invalid CD-Key. Please check to ensure that  
51 you have entered the CD-Key as it appears on the CD-case.  
52 602 You entered an invalid CD-Key. The CD-Key you entered was too short.  
53 Please check to ensure that you have entered all 13 digits of your CD-Key.  
54 603 Invalid Name  
55 604 You must enter a name to continue with installation.  
56 605 Please enter a name that is less than 127 characters long.  
57 606 Please enter a name that does not contain quotes (").
```

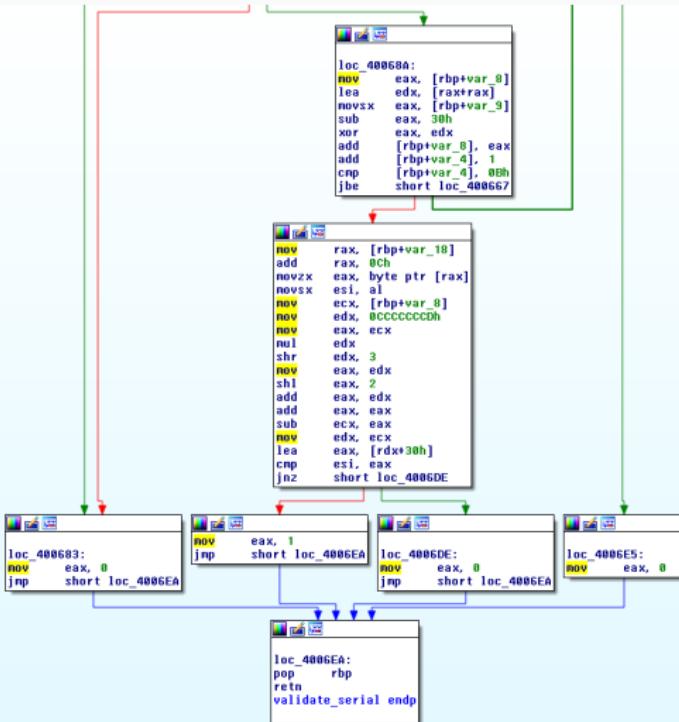
# GETTING TO THE CORE: DECOMPILATION



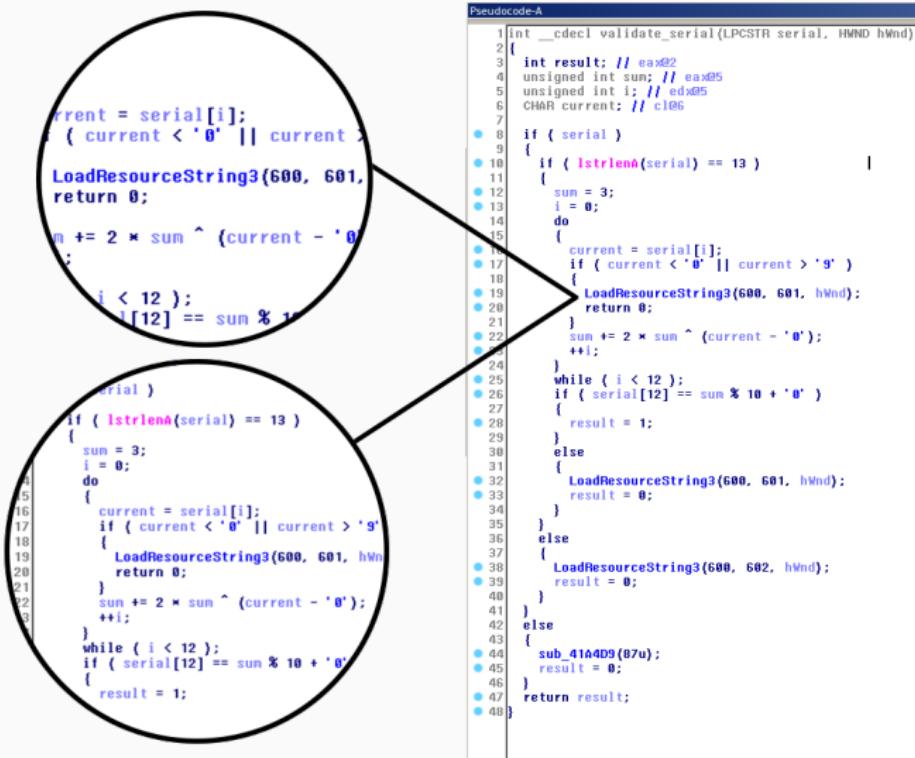
# GETTING TO THE CORE: CALL GRAPH



# GETTING TO THE CORE: CALL GRAPH



# GETTING TO THE CORE: DECOMPILATION



## Z3: FORMULATING FORMULAS

```
< > solve.py ×  
1 from z3 import *  
2  
3 s = Solver()  
4  
5 # Serial is 13 digits  
6 serial = [BitVec('c%d' % i, 32) for i in range(13)]  
7 for c in serial:  
8     s.add(c >= 0)  
9     s.add(c < 10)  
10  
11 # Partial sum  
12 partials = [3]  
13 for i in range(len(serial)-1):  
14     p = BitVec('p%d' % i, 32)  
15     s.add(p == partials[-1] + ((2*partials[-1]) ^ (serial[i])))  
16     partials.append(p)
```

## Z3: FORMULATING FORMULAS

```
17
18 # Final check
19 s.add(serial[-1] == (partials[-1] % 10))
20
21 # Print model
22 if s.check() == sat:
23     m = s.model()
24     res = map(Lambda s: m[s].as_long(), serial)
25     res = map(Lambda n: chr(n+ord('0')), res)
26     print(''.join(res))
27
```

## ONCE AGAIN, WITH FEE... ANGR

- "python framework for analyzing binaries"
- "both static and dynamic symbolic (concolic)"
- Computer Security Lab at UC Santa Barbara
- Uses Z3 internally



# ANGR MANAGEMENT: EXTRACTING THE CODE

```
< > validate.c x
1 int __cdecl validate_serial(LPCSTR serial, HWND hWnd)
2 {
3     int result; // eax@2
4     unsigned int v3; // eax@5
5     unsigned int v4; // edx@5
6     CHAR v5; // cl@6
7
8     if ( serial )
9     {
10         if ( lstrlenA(serial) == 13 )
11         {
12             v3 = 3;
13             v4 = 0;
14             do
15             {
16                 v5 = serial[v4];
17                 if ( v5 < '0' || v5 > '9' )
18                 {
19                     LoadResourceString3(600, 601, hWnd);
20                     return 0;
21                 }
22                 v3 += 2 * v3 ^ (v5 - '0');
23                 ++v4;
24             }
25         }
26         while ( v4 < 12 );
27         if ( serial[12] == v3 % 10 + '0' )
28         {
29             result = 1;
30         }
31         else
32         {
33             LoadResourceString3(600, 601, hWnd);
34             result = 0;
35         }
36     }
37     else
38     {
39         LoadResourceString3(600, 602, hWnd);
40         result = 0;
41     }
42 }
43 else
44 {
45     sub_41A4D9(0x57u);
46     result = 0;
47 }
48 }
```

# ANGR MANAGEMENT: MINIMIZING THE CODE

```
< > validate_clean.c x
1 #include <stdio.h>
2 #include <string.h>
3
4 int validate_serial(char *serial, size_t len)
5 {
6     int result;
7     unsigned int sum = 3;
8     unsigned int i = 0;
9     char current;
10
11    if ( len == 13 )
12    {
13        do
14        {
15            current = serial[i];
16            if ( current < '0' || current > '9' )
17            {
18                return 0;
19            }
20            sum += 2 * sum ^ (current - '0');
21            ++i;
22        }
23        while ( i < 12 );
24    }
25
26    if ( serial[12] == sum % 10 + '0' )
27    {
28        return 1;
29    }
30    else
31    {
32        return 0;
33    }
34    else
35    {
36        return 0;
37    }
38
39 int main(int argc, char **argv) {
40     char serial[1024];
41     scanf("%s", serial);
42     printf("Serial: %s\nValid: %d\n", serial, validate_serial(serial, strlen(serial)));
43
44     return 0;
45 }
```

# ANGR MANAGEMENT: WRITING THE EXPLORER

```
< > solve_angr.py x
1 #!/usr/bin/python
2
3 import angr
4
5 def main():
6     p = angr.Project('./validator2', load_options={"auto_load_libs": False})
7     pg = p.factory.path_group()
8
9     pg.explore(find=(0x4006d7,), avoid=(0x400683,0x4006de,0x4006e5,))
10
11    found = pg.found[0]
12    return found.state.posix.dumps(0).split('\0')[0]
13
14 if __name__ == '__main__':
15     print(main())
16
```

THANKS FOR LISTENING!