

C2/2016

Let $1=d_1 < d_2 < \dots < d_k = n$ be the divisors of n .

Let the table be $a \times b$. Thus, $a \cdot b = k$. S.P.G, $a \geq b \Rightarrow a \geq \sqrt{k}$.
 $b \leq \sqrt{k}$

The numbers $d_k, d_{k-1}, d_{k-2}, \dots, d_{k-a+1}$ ($a-1$ numbers) occupy,

at most, $a-1$ rows. Then, there's a row without those numbers.

The sum of those b numbers in that row is, at most,

$$d_{k-a} + d_{k-a-1} + \dots + d_{k-a-b+1} \stackrel{\textcircled{*}}{\leq}$$

$$\stackrel{\textcircled{*}}{\leq} b \cdot d_{k-a} \stackrel{\textcircled{*}}{\leq} a \cdot d_{k-a} \stackrel{\textcircled{*}}{\leq} d_a \cdot d_{k-a} = n.$$

But the row that contains n has sum at least n .

Thus, the sum on each row is n . $\Rightarrow a=1$ and inequalities $\textcircled{*}$ hold equality.

$$\Rightarrow a=b=1 \Rightarrow \boxed{n=1}$$

$n=1$ works!

□