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Geometria 3  
Guilherme Zeus Moura  
zeusdanmou@gmail.com

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**Problema 1 (IMO 1986, 2)** Given a point  $P_0$  in the plane of the triangle  $A_1A_2A_3$ . Define  $A_s = A_{s-3}$  for all  $s \geq 4$ . Construct a set of points  $P_1, P_2, P_3, \dots$  such that  $P_{k+1}$  is the image of  $P_k$  under a rotation center  $A_{k+1}$  through an angle  $120^\circ$  clockwise for  $k = 0, 1, 2, \dots$ . Prove that if  $P_{1986} = P_0$ , then the triangle  $A_1A_2A_3$  is equilateral.