

• Lemma 1: M is midpoint of PA.

$$\rightarrow AF^2 = FM \cdot FN = FB^2 \Rightarrow$$

$\Rightarrow F$ is mid point of AB

$\Rightarrow M$ is midpoint of PA

• Lemma 2: $EM \perp PA$

$$\text{Arc } \widehat{MB} = \text{Arc } \widehat{BD} \Rightarrow$$

$$\Rightarrow \angle DMB = \angle MDB \Rightarrow$$

$$\Rightarrow \angle ABE = \angle ABM.$$

Analogy: $\angle BAE = \angle BAM.$

$\Rightarrow M$ is symmetric of E, through AB.

$\rightarrow ME \perp AB \parallel PA.$

Lemmas 1 and 2:

$\Rightarrow E$ in perpendicular bisector of PA. \square

