

Block-Diagonal Coding for Distributed Computing With Straggling Servers

Albin Severinson^{†‡}, Alexandre Graell i Amat[†], and Eirik Rosnes[‡]

[†] Department of Electrical Engineering, Chalmers University of Technology, Gothenburg, Sweden

[‡] University of Bergen/Simula Research Lab, Bergen, Norway

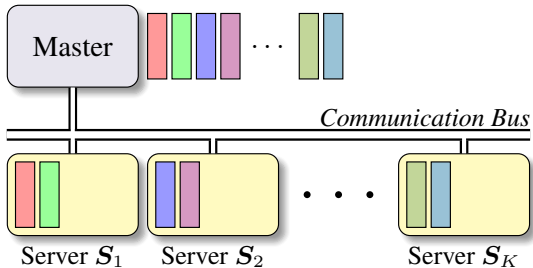
IEEE ITW
Kaohsiung, November, 2017

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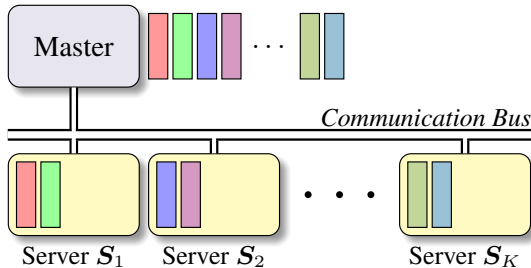


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Motivation



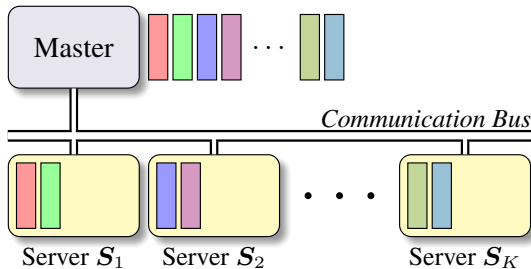
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Problem addressed

- Given an $m \times n$ matrix A and N vectors x_1, \dots, x_N , we want to compute $y_1 = Ax_1, \dots, y_N = Ax_N$ using K servers.

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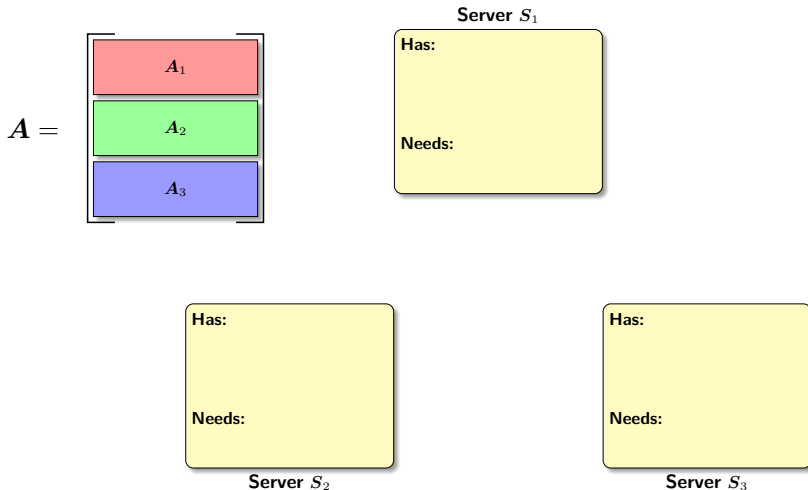
Performance metrics

- Communication load:** Average number of messages sent over the network
- Computational delay:** Average overall runtime of the computation

Bandwidth Scarcity

(Coded MapReduce, Li *et al.*, 2015)

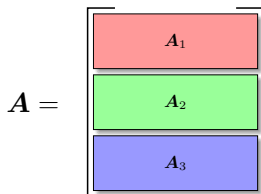
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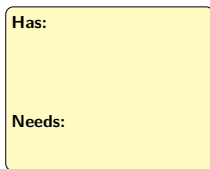
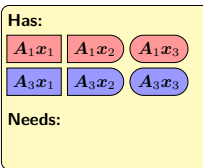
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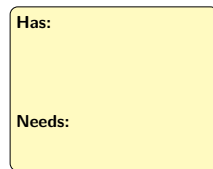
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Server S_1



Server S_2

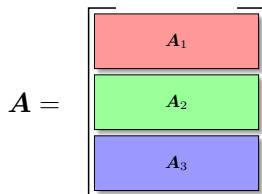


Server S_3

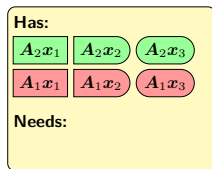
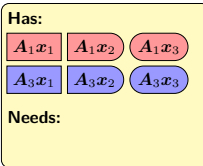
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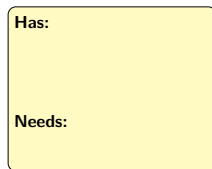
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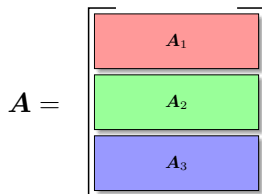


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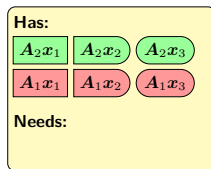
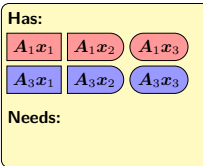
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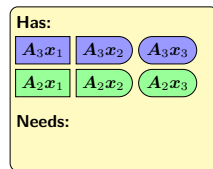
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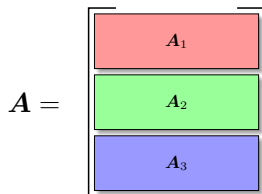


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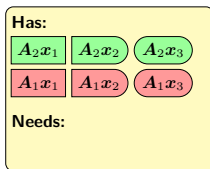
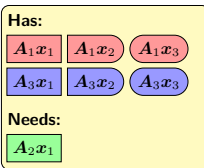
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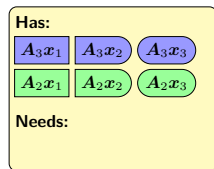
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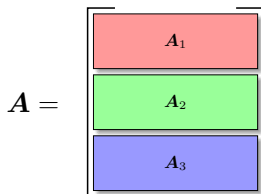


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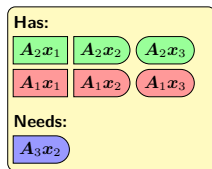
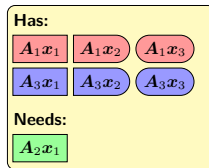
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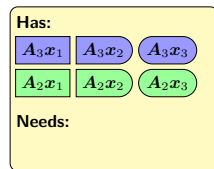
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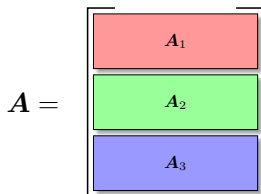


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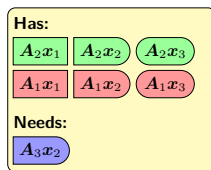
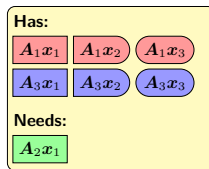
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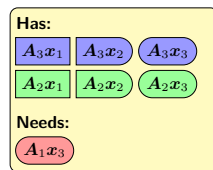
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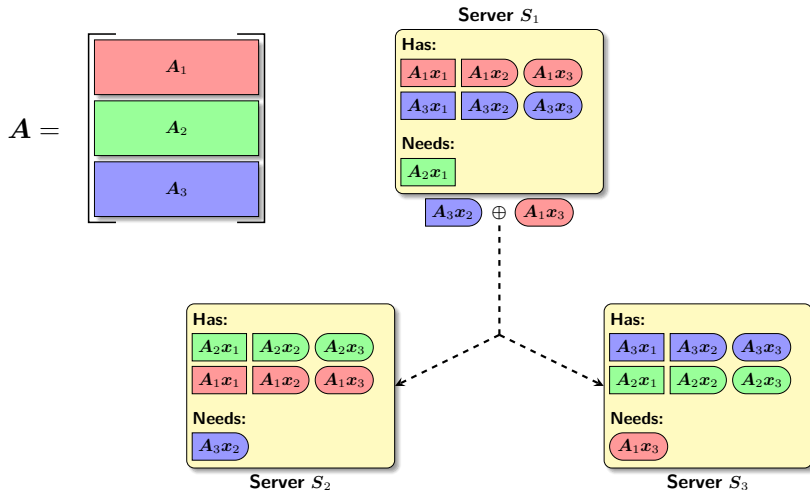


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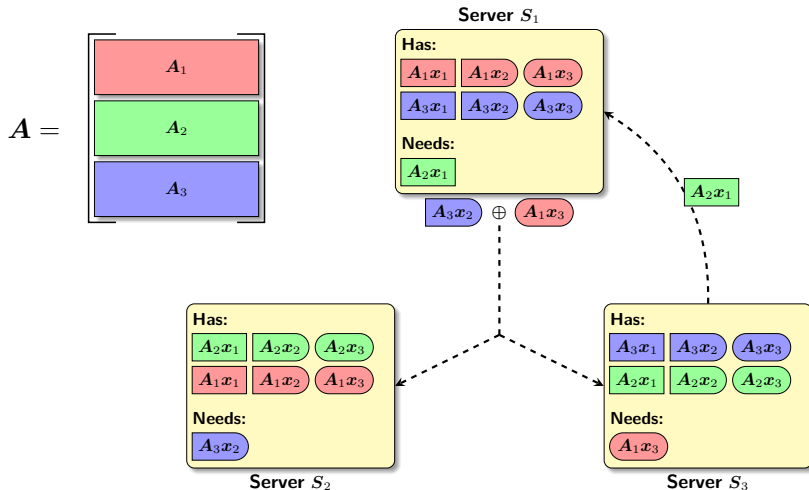
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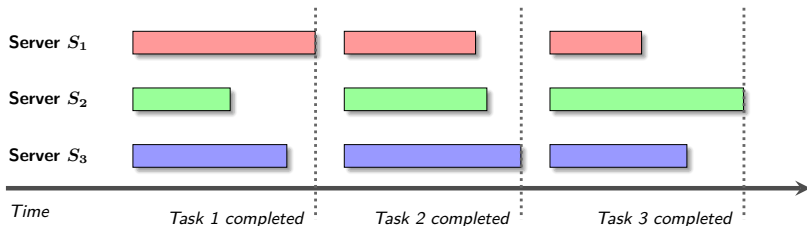


The straggler problem

(Speeding up Distributed Machine Learning Using Codes, Lee *et al.*, 2016)

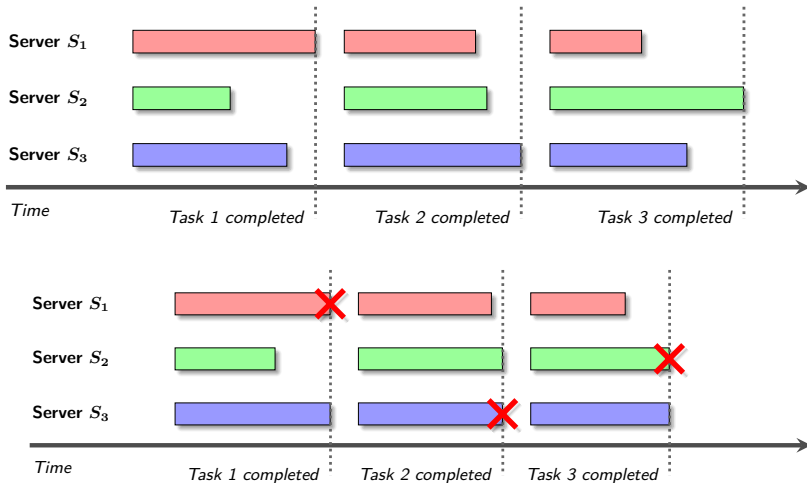
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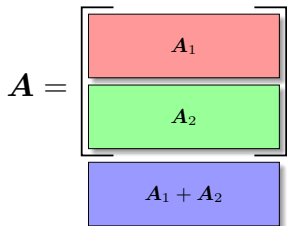
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$$y = Ax$$

$$A = \begin{bmatrix} A_1 \\ A_2 \end{bmatrix}$$

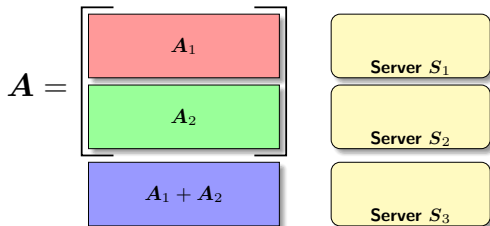
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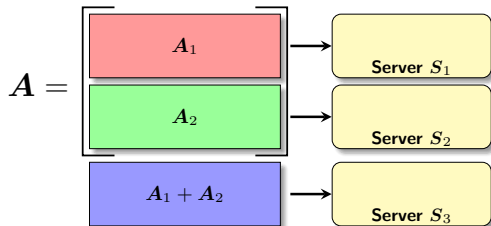
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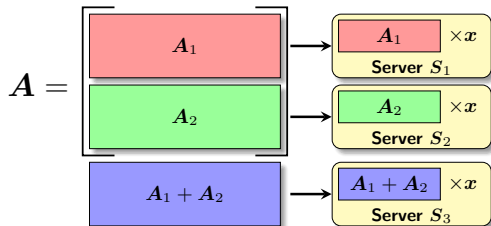
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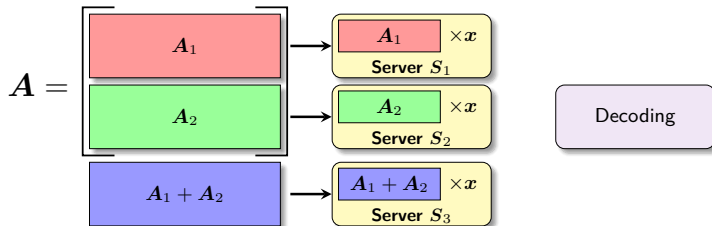
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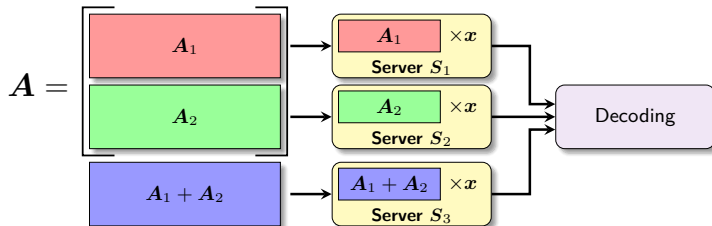
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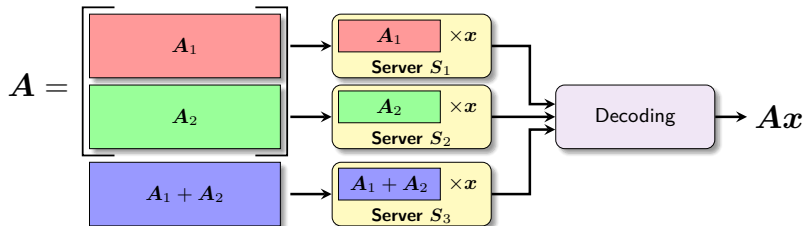
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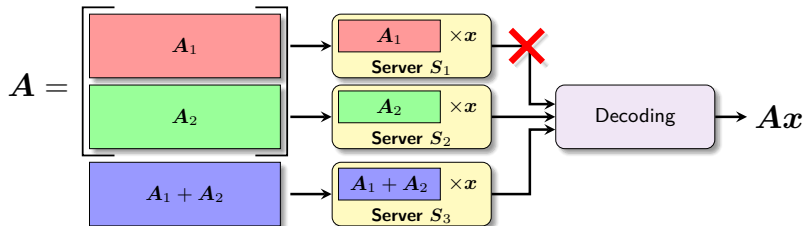
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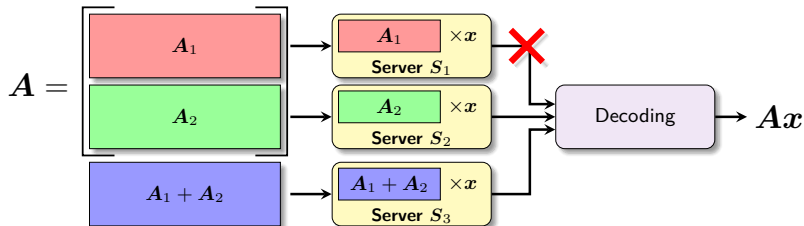
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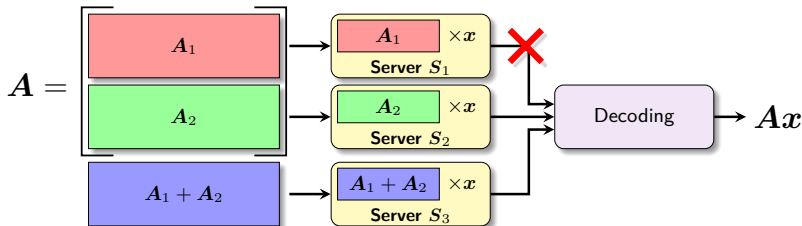


In general

- Introduce redundancy by encoding the input matrix A .

The Straggler Problem

$$y = Ax$$



In general

- Introduce redundancy by encoding the input matrix A .
- Each server is given **more work**. However, this may still **lower the computational delay!**

The Unified Coded Framework

(A Unified Coding Framework for Distributed Computing with Straggling Servers, Li *et al.*, 2016)

Coded approach by *Li et al.*

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Coded approach by Li *et al.*

- Encode the columns of $\mathbf{A} \in \mathbb{F}^{m \times n}$ using an (r, m) MDS code by multiplying \mathbf{A} with an $r \times n$ encoding matrix Ψ_{MDS} , i.e., $\mathbf{C} = \Psi_{\text{MDS}} \mathbf{A}$.

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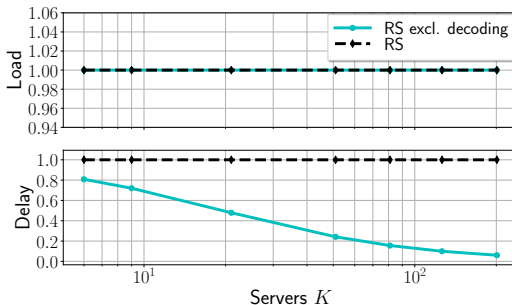
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- 2000 rows assigned to each server, $n = 10000$ columns, and code rate $m/r = 2/3$.

In this talk

Block-Diagonal Coding

- We propose a **block-diagonal** encoding scheme with lower decoding complexity.

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Idea

- **Partition** \mathbf{A} into T disjoint submatrices and apply **smaller MDS codes** to each submatrix,

$$\mathbf{C} = \mathbf{\Psi}_{\text{BDC}} \mathbf{A}, \quad \mathbf{\Psi}_{\text{BDC}} = \begin{bmatrix} \psi_1 & & \\ & \ddots & \\ & & \psi_T \end{bmatrix}.$$

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- Overall **computational delay** is lower than that of the scheme by Li *et al.*
- Larger T may reduce **computational delay** further at the expense of higher **communication load**.

Block-Diagonal Coding

$$\Psi_{\text{BDC}} = \begin{bmatrix} \psi_1 & & \\ & \psi_2 & \\ & & \psi_3 \end{bmatrix}$$

$r \times m$

- Block-diagonal encoding with $T = 3$ partitions.

Block-Diagonal Coding

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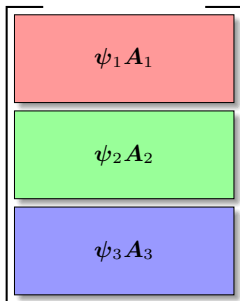
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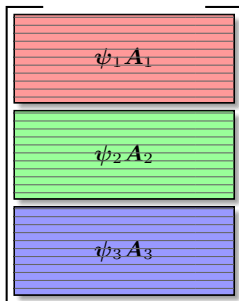
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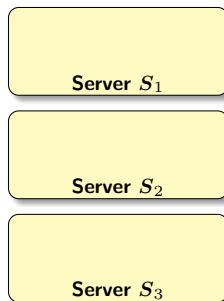
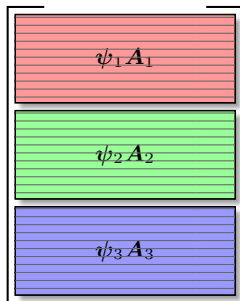
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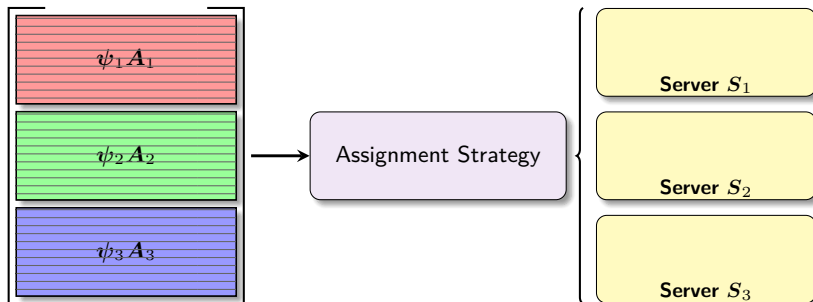
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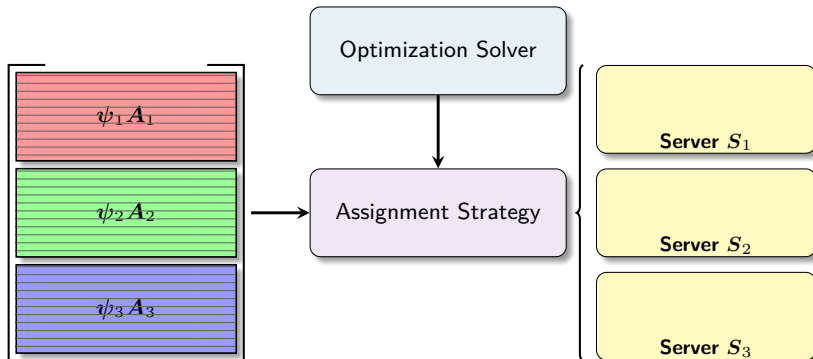
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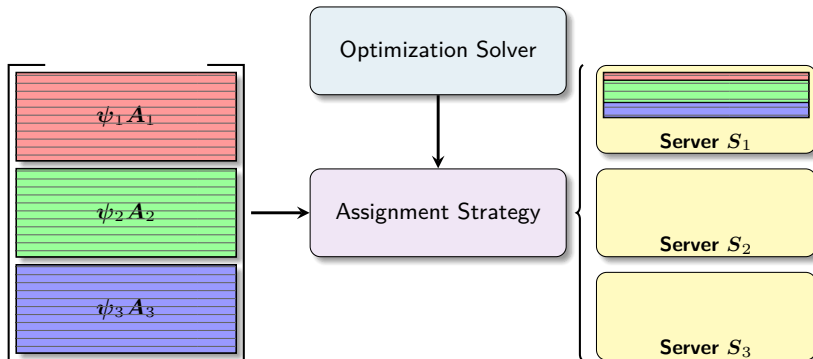
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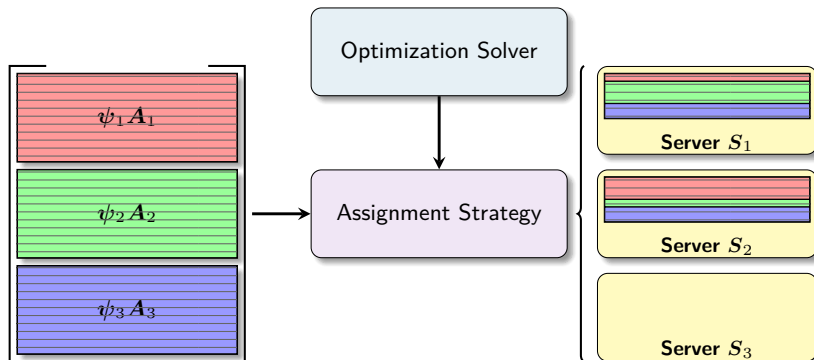
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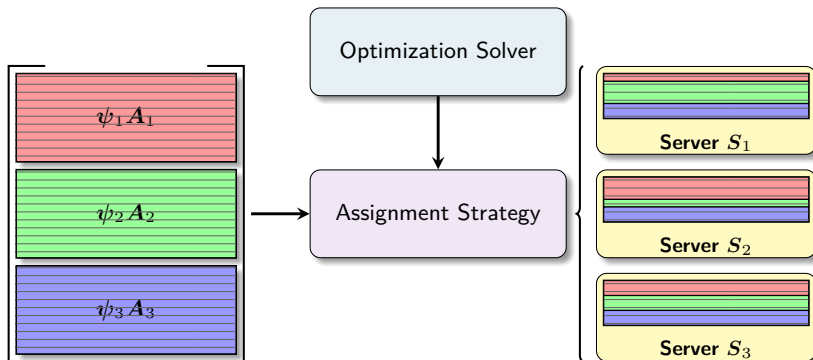
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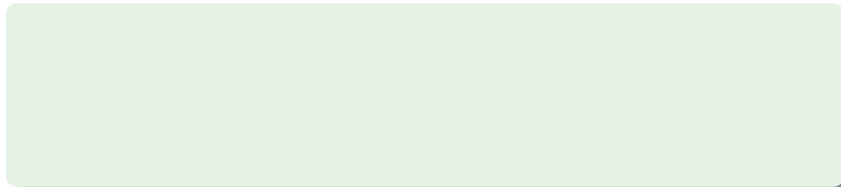
- Block-diagonal encoding with $T = 3$ partitions.
- Need any m/T out of r/T rows from **each partition** to decode.
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 \end{array}
 \begin{pmatrix}
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 & & & & & \\
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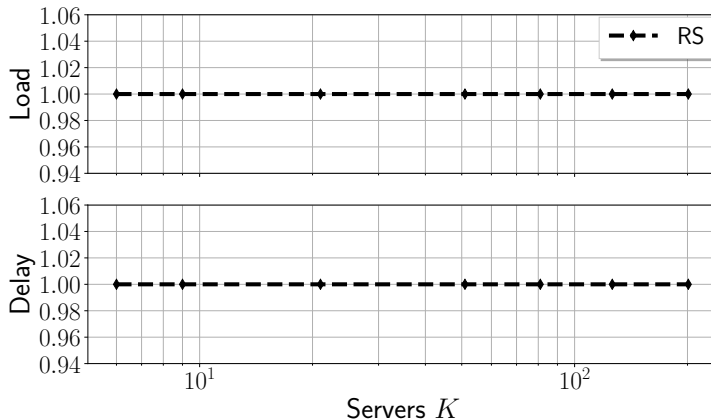
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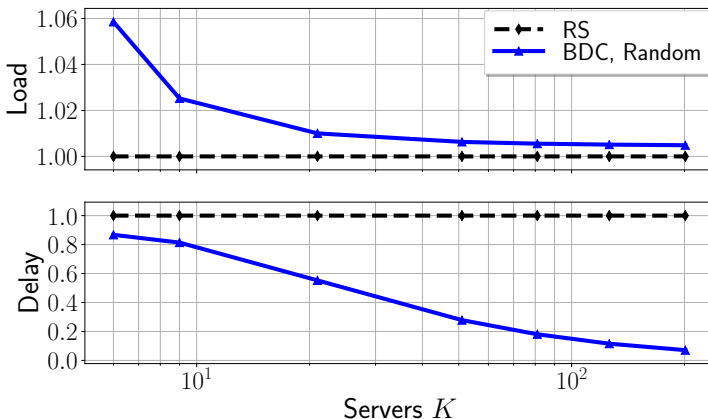
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Numerical results



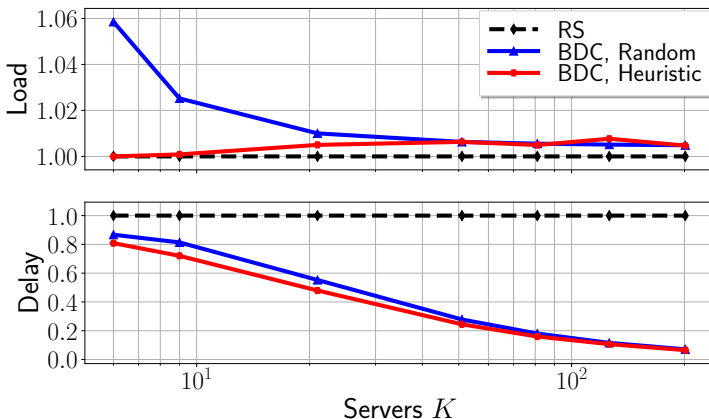
- 2000 rows assigned to each server, $n = 10000$ columns, $m/T = 10$ rows per partition, and code rate $m/r = 2/3$.

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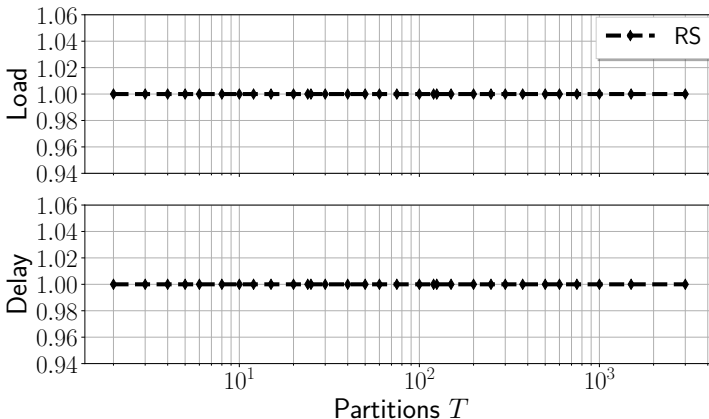
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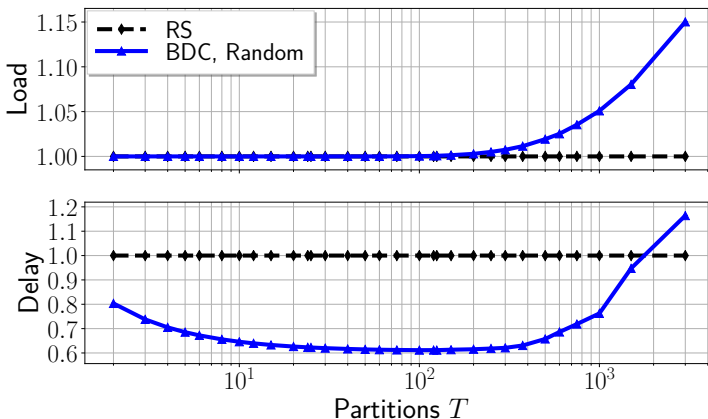
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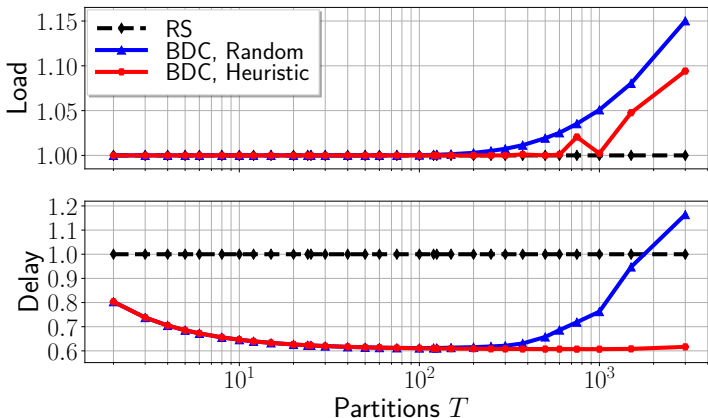
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Theorem

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The overall **computational delay** of our scheme is much lower than that of the scheme by Li *et al.* due to its lower decoding complexity.

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Take-home message...

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- Slides and code on Github: github.com/severinson/coded-computing-tools

References

- [1] K. Lee et al. “Speeding up distributed machine learning using codes”. In: *Proc. IEEE Int. Symp. Inf. Theory*. Barcelona, Spain, July 2016, pp. 1143–1147. DOI: 10.1109/ISIT.2016.7541478.
- [2] S. Li, M. A. Maddah-Ali, and A. S. Avestimehr. “Coded MapReduce”. In: *Proc. Annual Allerton Conf. Commun., Control, and Computing*. Monticello, IL, Sept. 2015, pp. 964–971. DOI: 10.1109/ALLERTON.2015.7447112.
- [3] Songze Li, Mohammad Ali Maddah-Ali, and Amir Salman Avestimehr. “A Unified Coding Framework for Distributed Computing with Straggling Servers”. In: *Proc. Workshop Network Coding and Appl.* Washington, DC, Dec. 2016. DOI: 10.1109/GLOCOMW.2016.7848828.