TTIC 31230 Fundamentals of Deep Learning

Problems For Fundamental Equations.

problem 1. This problem is on a CTC-like algorithm for image labeling.

Suppose that the training data consists of pairs (I[X,Y],S) where I is an image and S is a set of object types occurring in the image. For example S might be {Person, Dog, Car}. To be concrete we can take C to be the set of image labels used in CIFAR 100 and take S to be a subset of C containing no more than five labels $(|S| \leq 5)$. We want to do SGD on a model defining $P_{\Phi}(S \mid I[X,Y])$.

We will use a latent variable z[X,Y] such that for pixel coordinates (x,y) we have $z[x,y] \in \mathcal{C} \cup \{\bot\}$. For a given z[X,Y] define S(z[X,Y]) to be the set of classes appearing in z[X,Y], i.e., $S(z[X,Y]) = \{c \exists x,y \ z(x,y) = c\}$. Here the "semantic segmentation" Z[X,Y] is analogous to the phoneme sequence z[T] in CTC. Unlike the CTC model, the label S is a set rather than a sequence.

We assume a CNN (with convolutions of stride 1 to preserve spatial dimensions) followed by a softmax at each pixel to get a probability $P_{\Phi}(z[x,y]=c)$ for each pixel location (x,y) and each $c \in \mathcal{C} \cup \{\bot\}$ and where each pixel location has an independent probability distribution over classes. To simplify notation we can reshape the pixel locations into a linear sequence and replace z[X,Y] by z[T] with $T = X \times Y$.

Define

$$S_t = \{ c \in \mathcal{C} \ \exists t \le T \ z[t] = c \}$$

For $U \subseteq S$ define

$$F[U,t] = P(S_t = U)$$

Note that for $|S| \leq 5$ there are at most 32 possible values of U. Give dynamic programming equations defining F[U,0] and defining F[U,t+1] in term of F[U,t].