

TTIC 31230 Fundamentals of Deep Learning, winter 2019
Framework Problems

Problem 1: Consider the following softmax.

$$\begin{aligned} Z[b] &= \sum_j \exp(s[b, j]) \\ p[b, j] &= \exp(s[b, j]) / Z[b] \end{aligned}$$

Give a back-propagation += update based on the second equation for adding to $s.\text{grad}$ using $p.\text{grad}$ (and using the forward-computed tensors Z and s).

Give a back-propagation += update based on the second equation for adding to $Z.\text{grad}$ using $p.\text{grad}$ (and using the forward-computed tensors s and Z).

Give a back-propagation += update based on the first equation for adding to $s.\text{grad}$ using $Z.\text{grad}$ (and using the forward-computed tensor s).

Problem 2: For the softmax in problem 1 show that we can instead use

$$\begin{aligned} e[b] &= \sum_j p[b, j] p.\text{grad}[b, j] \\ s.\text{grad}[b, j] &= p[b, j] (p.\text{grad}[b, j] - e[b]) \end{aligned}$$

This formula shows how hand-written back-propagation methods for “layers” such as softmax can be more efficient than compiler-generated back-propagation code. While optimizing compilers can of course be written, one must keep in mind the trade-off between the abstraction level of the programming language and the efficiency of the generated code.