

Predict Price Freeze Likelihood: A Bayesian Approach to predict Grocery Pricing in Canada*

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This article aims to study the possibility of Canada adopting a price freeze strategy for specific products from November to February of the following year. By selecting relevant data such as the historical price and current price of specific products in several major groceries, and fitting the Bayesian model for price prediction, the impact of historical prices and time changes on the current price trend is analysed. The flexibility of the Bayesian model enables it to quantify uncertainty stably and reliably, and is superior to the traditional linear regression model in terms of predicting accuracy and interpretability of future price changes. The Posterior predictive checks confirmed the consistency of the model with the observed price distribution, and the confidence interval further revealed the potential variability. The results of the study show that the price freeze may continue from November to February of the following year, but the differences between different suppliers, especially the price coordination and potential collusion between food retailers implied by the extreme values, need continuous attention.

1 Introduction

Implementing a price freeze on grocery products for a period of time has become a common annual strategy for Canadian retailers. During the price freeze period, these groceries would keep the prices of certain products unchanged for a period of time, without being affected by market fluctuation, cost changes or other factors, which is a short-term behavior implemented by major retailers in order to stabilize consumer prices and achieve benefits. Well-known supermarket chains such as Loblaws and Metro have always followed this strategy. These retailers aim to protect consumers' ability to pay in the event of economic fluctuations, so as to retain customers and obtain benefits. However, the bread price manipulation scandal that broke out a few years ago also raised questions about the consistency and sustainability

*Code and data are available at:

of the strategy(Charlebois 2023). Accusations of food price manipulation are also emerging in various countries, such as lowering the price to the original price or higher after the price increase, and using short-term price increases to create falsely high “original prices” to fake the illusion of discounts(Competition and Commission 2024).

The analysis uses data such as the history and current price of whole wheat bread from multiple suppliers, focussing on factors such as unit price and its historical changes. By analyzing historical price trends and using Bayesian modelling to predict current price stability, we will explore whether the price freeze strategies of major retail stores will be implemented from November to February of the following year as stated by Metro. By comparing the Bayesian model with the traditional linear regression model, it is shown that the Bayesian method has obvious advantages in integrating uncertainty and capturing the dynamics of price trends. In addition, the performance of the model on historical price data is tested through posterior distribution, so as to improve the reliability of future price forecasts(nature2020bayesia?). This study provides in-depth insights into understanding the factors affecting prices, and a reference for consumers, regulators, retailers and policymakers to ensure price stability under the pressure of inflation, ensure fair market competition, and prevent price manipulation from harming the interests of consumers.

1.0.1 Overview

This study explores whether some well-known Canadian food groceries follow the price freeze strategy when pricing whole wheat bread from November to February of the following year. By using old and current price data, we analyzed the relationship between old price, unit price, and current pricing trends of multiple vendors. The study uses the Bayesian regression model to capture these dynamic relationships, and by comparison with the linear regression model, the analysis shows the excellent performance of the Bayesian model through posterior predictive check and credible intervals.

1.0.2 Estimand

The primary estimand in this analysis is based on the historical price and unit price and the expected price of the whole wheat bread of different vendors from November to February of the following year. It aims to quantify the relationship between these predictors and the current price to assess whether the groceries comply with the price freeze strategy.

It reflects the size of the factors affecting the historical price ((old_price)) and unit price ((price_per_unit)) on the current price ((current_price)), while controlling the variability between vendors. In order to achieve this goal, the analysis adopts the Bayesian regression model, which combines a priori knowledge and evaluates the uncertainty in these relationships through credible intervals. And the phenomenon of deviating from the predicted pricing trend is interpreted as a possible inconsistency in the price freeze strategy.

1.0.3 Why It Matters

The analysis of the implementation of the price freeze from November to February of the following year is crucial to protecting consumers from inflationary pressure and price fraud. If this strategy can be implemented legally and in a standardized manner, it can not only ensure consumers' ability to pay, but also enhance the credibility and reputation of groceries, and establish trust between retailers and customers, so as to retain customers to achieve greater benefits. By revealing the performance of major vendors in terms of the consistency of pricing strategies, this study provides policymakers and industry stakeholders with important information about potential irregular behavior involving collusion during the period of price freeze.

In addition, the use of Bayesian modelling method enhances the reliability of research results, and by quantifying uncertainty, the analysis has strong applicability in a dynamic economic environment. The results of this study are especially important for policies and strategies aimed at promoting fair pricing and economic stability during the period of high consumer demand.

2 Data

2.1 Measurement

We use the statistical programming language R (R Core Team 2023) and its data analysis and visualization libraries to explore grocery pricing trends across multiple vendors. Our data (Filipp 2024) consists of historical and current prices for a variety of grocery items, collected from major Canadian retailers. Following the principles outlined in (Alexander 2023), we aim to provide a clear and insightful narrative about vendor adherence to seasonal price freeze policies. By leveraging Bayesian regression modeling, we quantify the relationships between historical prices, price per unit, and current pricing while incorporating uncertainty. This approach ensures a nuanced understanding of pricing behaviors during a critical consumer period.

The dataset records the pricing behavior of six major vendors for whole wheat bread: Voila, Loblaws, Metro, T&T, NoFrills, SaveOnFoods. The current price at each point in time in the dataset reflects the pricing strategies of different vendors, covering the period from April to June this year for comparative analysis and prediction.

In order to ensure accuracy, the price data has been standardized in the measurement unit, and the product is 675g of whole wheat bread, which makes the comparison between different products and vendors meaningful. For the missing old price data of some products, it is not cleaned and filtered in the initial analysis data to maintain the integrity of the dataset and avoid the introduction of significant deviations. And a few outliers are analyzed separately to assess their impact on the overall trend.

Table 1

	product_id		nowtime	current_price	old_price	other	price_per_unit
1	116800	2024-04-26	09:20:00	4.99	NA		0.01
2	116800	2024-04-27	09:38:00	4.99	NA		0.01
3	116800	2024-04-28	10:00:00	4.99	NA		0.01
4	116800	2024-04-29	09:56:00	4.99	NA		0.01
5	116800	2024-04-30	07:54:00	4.99	NA		0.01
6	116800	2024-05-01	14:44:00	4.99	NA		0.01
	product_description						vendor
1	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
2	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
3	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
4	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
5	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
6	Voila~Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g@675g^	Voila
	product_name		units				
1	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g
2	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g
3	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g
4	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g
5	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g
6	Dempster's	Whole	Wheat	Bread	Texas	Toast 675 g	675g

The following packages were used for this study:

- **tidyverse** (Wickham, Hester, et al. 2022): A collection of tools for data manipulation and visualization.
- **ggplot2** (Wickham, Chang, et al. 2022): Creates customizable, high-quality plots.
- **readr** (Wickham, Hester, and François 2022): Reads data files quickly and easily.
- **lubridate** (Grolemund and Wickham 2022): Simplifies handling dates and times.
- **dplyr** (Wickham, François, et al. 2022): Makes data manipulation fast and intuitive.
- **bayesplot** (Gabry, Goodrich, et al. 2022): Visualizes Bayesian model outputs.
- **rstanarm** (Goodrich et al. 2022): Enables Bayesian regression modeling with Stan.
- **knitr** (Xie 2022): Combines R code and text for reproducible reports.
- ***Telling Stories with Data*** (Alexander 2023): Referenced for its code and methodologies in data and statistical information.

2.2 Variables

- **product_id**: A unique identifier for each product in the dataset.
- **nowtime**: The timestamp indicating when the price was recorded.
- **current_pricet**: The price of the product at the time of data collection.
- **old_price**: The previous price of the product, if available.
- **other**: Promotion for the product in the specific time
- **price_per_unit**: The unit price of the product
- **product_description**: A detailed description of the product, including brand and product specifics.
- **vendor**: The name of the vendor supplying the product.
- **product_name**: The name of the product as displayed in the dataset.
- **units**: The quantity or size of the product in its packaging.

Detailed information about these variables and the data structure is presented in @.

Table 2: Summary statistics for current and old prices

Table 2: Summary of Current and Old Prices

Avg_Current_Price	Avg_Old_Price	Min_Current_Price	Max_Current_Price	Min_Old_Price	Max_Old_Price
3.914998	3.91093	0.5	10.99	2.49	4.99

Table 2 shows the summary statistics data of current and old price.

Figure 1 compares the current and old prices of five vendors, Loblaw's, Metro, No Frills, SaveOn-Foods and T&T, revealing the pricing trends and changes of each vendor. Among them, the current price of the whole wheat bread in Metro has not changed, indicating the continuity of

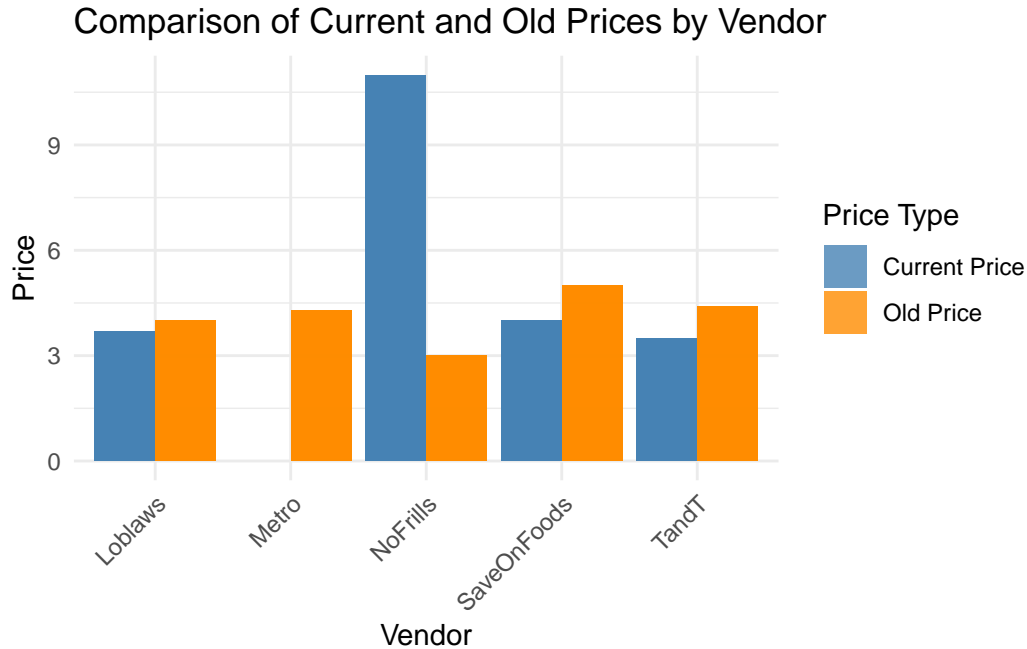


Figure 1: Comparison of current and old prices by vendor

its pricing, and there is no special offer during this period; the current price of the bread in No Frills is significantly higher than the old price, which shows that its pricing has changed significantly, but combined with the data analysis just now, it may be affected by extreme values; The current price of SaveOnFoods and T&T is lower than the old price, which may reflect the price adjustment during the promotion. Generally speaking, the price stability of the whole wheat bread in Metro provides consumers with a clear shopping experience, while the price fluctuations of No Frills need close attention. The price reduction trend of SaveOnFoods and T&T may be the result of market competition triggered by other groceries' promotional activities.

2.3 Predictor variables

Add graphs, tables and text.

Use sub-sub-headings for each outcome variable and feel free to combine a few into one if they go together naturally.

Table 3: Summary statistics for predictor variables

Table 3: Summary of Pricing by Vendor

vendor	Avg_Price	Min_Price	Max_Price	Count
Loblaws	4.042559	3.502	4.29	239
Metro	4.281892	3.990	4.29	224
NoFrills	3.163756	0.500	10.99	239
SaveOnFoods	4.625417	3.490	4.99	48
TandT	4.112110	3.470	4.39	237
Voila	4.990000	4.990	4.99	8

Table 3 summarizes the average price, lowest price and highest price of six suppliers of Loblaw, Metro, No Frills, SaveOnFoods, T&T and Voila in a fixed period of time.

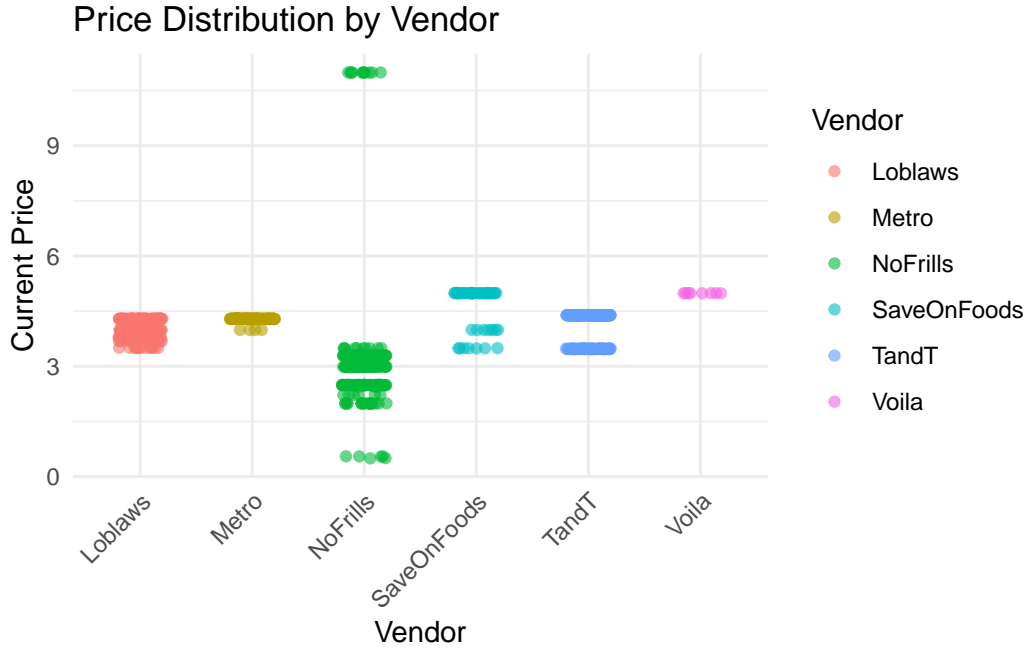


Figure 2: Price distribution by vendor

Figure 2 shows the price distribution of six vendors: Loblaws, Metro, No Frills, Save-On-Foods, T&T and Voila. The prices of Loblaws, Metro and T&T are concentrated between \$3 and \$4.5, with less volatility, indicating the stability of their pricing. The price of Save-On-Foods is concentrated in the range of \$4 to \$5, while the price of Voila is fixed at \$5, both of which reflect high stability and are consistent with the freezing policy. In comparison, the price of No Frills fluctuates significantly, from less than \$1 to nearly \$7, showing the possibility of

promotional or strategic pricing, indicating that it may have a lower degree of compliance with the price freeze policy in the future. In addition, No Frills still has obvious abnormal values, while other suppliers have fewer abnormal values. Overall, Loblaws, Metro, Save-On-Foods, T&T and Voila showed high compliance during the price freeze, while No Frills adopted a more flexible pricing strategy. This analysis reflects the important impact of supplier pricing strategies on consumer experience and emphasizes the need to focus on monitoring vendors with large price fluctuations such as No Frills.

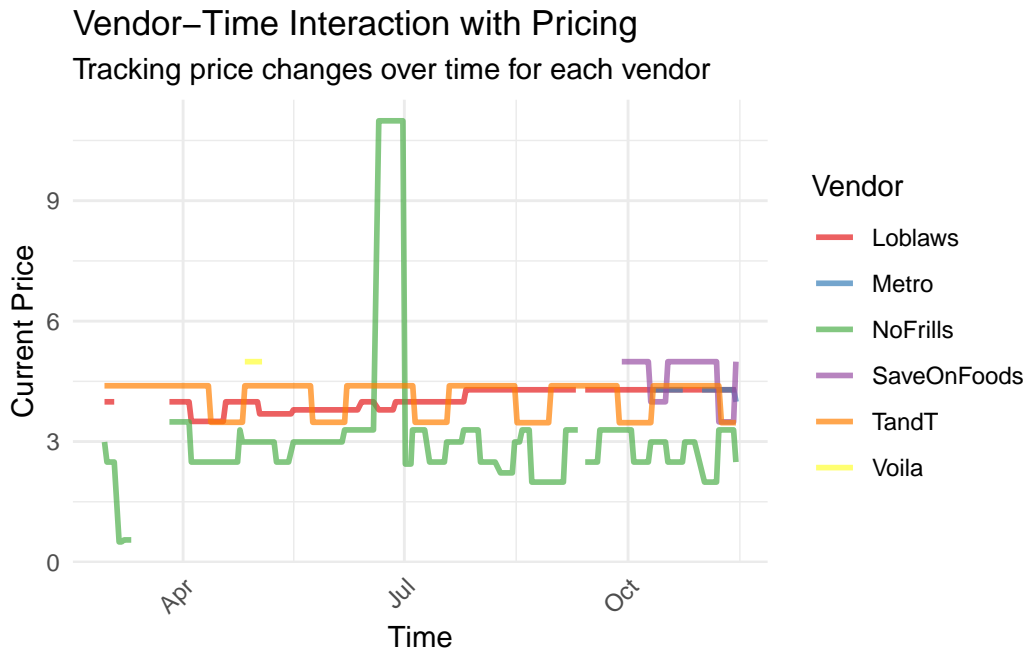


Figure 3: Interaction between vendor, time, and pricing

Figure 3 shows the price fluctuation trend of six vendors of Loblaw, Metro, No Frills, SaveOn-Foods, T&T and Voila. The price fluctuation of Loblaws and Metro is extremely small, showing remarkable stability. The price of No Frills fluctuates greatly, and there are significant peaks during this period, which shows that there may be challenges to its stability during the price freeze period. The price adjustment trend of SaveOnFoods and T&T is relatively moderate and fluctuates moderately. Voila’s price is the most consistent throughout the year, indicating that it has adopted a strict pricing strategy. On the whole, most vendors have achieved a stable price adjustment by November.

3 Model

Number of rows in the dataset: 50


```
# A tibble: 6 x 10
  product_id nowtime          current_price old_price other price_per_unit
    <dbl> <dtm>          <dbl>      <dbl> <chr>      <dbl>
1   2881302 2024-03-02 16:07:00         2.49      2.99 <NA>         0.37
2   2881302 2024-10-19 09:14:00         2.49      2.99 "sale\n~         0.37
3   1688554 2024-05-08 10:11:00         3.69      3.99 <NA>         0.55
4   2881302 2024-08-29 08:12:00         1.99      2.99 "$1.99"         0.29
5   3357383 2024-11-08 09:57:00         3.49      4.99 "$3.49 ~         0.52
6   2881302 2024-04-06 11:29:00         2.49      2.99 <NA>         0.37
# i 4 more variables: product_description <chr>, vendor <chr>,
#   product_name <chr>, units <chr>
```

SAMPLING FOR MODEL 'continuous' NOW (CHAIN 1).

Chain 1:

Chain 1: Gradient evaluation took 0.003095 seconds

Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 30.95 seconds.

Chain 1: Adjust your expectations accordingly!

Chain 1:

Chain 1:

Chain 1: Iteration: 1 / 2000 [0%] (Warmup)

Chain 1: Iteration: 200 / 2000 [10%] (Warmup)

Chain 1: Iteration: 400 / 2000 [20%] (Warmup)

Chain 1: Iteration: 600 / 2000 [30%] (Warmup)

Chain 1: Iteration: 800 / 2000 [40%] (Warmup)

Chain 1: Iteration: 1000 / 2000 [50%] (Warmup)

Chain 1: Iteration: 1001 / 2000 [50%] (Sampling)

Chain 1: Iteration: 1200 / 2000 [60%] (Sampling)

Chain 1: Iteration: 1400 / 2000 [70%] (Sampling)

Chain 1: Iteration: 1600 / 2000 [80%] (Sampling)

Chain 1: Iteration: 1800 / 2000 [90%] (Sampling)

Chain 1: Iteration: 2000 / 2000 [100%] (Sampling)

Chain 1:

Chain 1: Elapsed Time: 0.055 seconds (Warm-up)

Chain 1: 0.061 seconds (Sampling)

Chain 1: 0.116 seconds (Total)

Chain 1:

SAMPLING FOR MODEL 'continuous' NOW (CHAIN 2).

Chain 2:

Chain 2: Gradient evaluation took 9e-06 seconds

Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.09 seconds.

Chain 2: Adjust your expectations accordingly!

Chain 2:

Chain 2:

Chain 2: Iteration: 1 / 2000 [0%] (Warmup)

Chain 2: Iteration: 200 / 2000 [10%] (Warmup)

Chain 2: Iteration: 400 / 2000 [20%] (Warmup)

Chain 2: Iteration: 600 / 2000 [30%] (Warmup)

Chain 2: Iteration: 800 / 2000 [40%] (Warmup)

Chain 2: Iteration: 1000 / 2000 [50%] (Warmup)

Chain 2: Iteration: 1001 / 2000 [50%] (Sampling)

Chain 2: Iteration: 1200 / 2000 [60%] (Sampling)

Chain 2: Iteration: 1400 / 2000 [70%] (Sampling)

Chain 2: Iteration: 1600 / 2000 [80%] (Sampling)

Chain 2: Iteration: 1800 / 2000 [90%] (Sampling)

Chain 2: Iteration: 2000 / 2000 [100%] (Sampling)

Chain 2:

Chain 2: Elapsed Time: 0.055 seconds (Warm-up)

Chain 2: 0.057 seconds (Sampling)

Chain 2: 0.112 seconds (Total)

Chain 2:

SAMPLING FOR MODEL 'continuous' NOW (CHAIN 3).

Chain 3:

Chain 3: Gradient evaluation took 7e-06 seconds

Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.

Chain 3: Adjust your expectations accordingly!

Chain 3:

Chain 3:

Chain 3: Iteration: 1 / 2000 [0%] (Warmup)

Chain 3: Iteration: 200 / 2000 [10%] (Warmup)

Chain 3: Iteration: 400 / 2000 [20%] (Warmup)

Chain 3: Iteration: 600 / 2000 [30%] (Warmup)

Chain 3: Iteration: 800 / 2000 [40%] (Warmup)

Chain 3: Iteration: 1000 / 2000 [50%] (Warmup)

Chain 3: Iteration: 1001 / 2000 [50%] (Sampling)

Chain 3: Iteration: 1200 / 2000 [60%] (Sampling)

Chain 3: Iteration: 1400 / 2000 [70%] (Sampling)

Chain 3: Iteration: 1600 / 2000 [80%] (Sampling)

Chain 3: Iteration: 1800 / 2000 [90%] (Sampling)

Chain 3: Iteration: 2000 / 2000 [100%] (Sampling)

Chain 3:

Chain 3: Elapsed Time: 0.053 seconds (Warm-up)

Chain 3: 0.063 seconds (Sampling)

Chain 3: 0.116 seconds (Total)

Chain 3:

SAMPLING FOR MODEL 'continuous' NOW (CHAIN 4).

Chain 4:

Chain 4: Gradient evaluation took 7e-06 seconds

Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.

Chain 4: Adjust your expectations accordingly!

Chain 4:

Chain 4:

Chain 4: Iteration: 1 / 2000 [0%] (Warmup)

Chain 4: Iteration: 200 / 2000 [10%] (Warmup)

Chain 4: Iteration: 400 / 2000 [20%] (Warmup)

Chain 4: Iteration: 600 / 2000 [30%] (Warmup)

Chain 4: Iteration: 800 / 2000 [40%] (Warmup)

Chain 4: Iteration: 1000 / 2000 [50%] (Warmup)

Chain 4: Iteration: 1001 / 2000 [50%] (Sampling)

Chain 4: Iteration: 1200 / 2000 [60%] (Sampling)

Chain 4: Iteration: 1400 / 2000 [70%] (Sampling)

Chain 4: Iteration: 1600 / 2000 [80%] (Sampling)

Chain 4: Iteration: 1800 / 2000 [90%] (Sampling)

Chain 4: Iteration: 2000 / 2000 [100%] (Sampling)

Chain 4:

Chain 4: Elapsed Time: 0.051 seconds (Warm-up)

Chain 4: 0.058 seconds (Sampling)

Chain 4: 0.109 seconds (Total)

Chain 4:

\$coefficients

(Intercept)	price_per_unit	old_price
1.9590582	4.5664348	-0.1772753

\$ses

(Intercept)	price_per_unit	old_price
1.6079566	6.5202496	0.7766135

\$fitted.values

1	2	3	4	5	6	7	8
3.118586	3.118586	3.763269	2.753271	3.449000	3.118586	2.841909	2.935928
9	10	11	12	13	14	15	16
2.753271	3.449000	3.763269	2.841909	3.118586	3.118586	3.118586	3.449000
17	18	19	20	21	22	23	24

3.072922	3.118586	2.935928	2.753271	3.449000	3.118586	3.072922	2.753271
25	26	27	28	29	30	31	32
3.118586	3.072922	3.118586	3.072922	3.118586	3.118586	3.118586	2.753271
33	34	35	36	37	38	39	40
2.935928	3.118586	2.935928	2.753271	3.118586	3.118586	2.935928	3.449000
41	42	43	44	45	46	47	48
3.768651	3.118586	2.935928	3.763269	3.072922	3.072922	3.763269	2.935928
49	50						
3.449000	3.118586						

\$linear.predictors

1	2	3	4	5	6	7	8
3.118586	3.118586	3.763269	2.753271	3.449000	3.118586	2.841909	2.935928
9	10	11	12	13	14	15	16
2.753271	3.449000	3.763269	2.841909	3.118586	3.118586	3.118586	3.449000
17	18	19	20	21	22	23	24
3.072922	3.118586	2.935928	2.753271	3.449000	3.118586	3.072922	2.753271
25	26	27	28	29	30	31	32
3.118586	3.072922	3.118586	3.072922	3.118586	3.118586	3.118586	2.753271
33	34	35	36	37	38	39	40
2.935928	3.118586	2.935928	2.753271	3.118586	3.118586	2.935928	3.449000
41	42	43	44	45	46	47	48
3.768651	3.118586	2.935928	3.763269	3.072922	3.072922	3.763269	2.935928
49	50						
3.449000	3.118586						

\$residuals

1	2	3	4	5	6
-0.62858587	-0.62858587	-0.07326882	-0.76327109	0.04099953	-0.62858587
7	8	9	10	11	12
-0.85190874	-0.71592848	-0.76327109	0.04099953	-0.07326882	-0.85190874
13	14	15	16	17	18
-0.62858587	-0.62858587	-0.62858587	0.04099953	-0.63292152	-0.62858587
19	20	21	22	23	24
-0.71592848	-0.76327109	0.04099953	-0.62858587	7.91707848	-0.76327109
25	26	27	28	29	30
-0.62858587	7.91707848	-0.62858587	-0.63292152	0.17141413	-0.62858587
31	32	33	34	35	36
-0.62858587	-0.76327109	0.05407152	-0.62858587	0.05407152	-0.76327109
37	38	39	40	41	42
-0.62858587	-0.62858587	-0.71592848	0.04099953	0.22134910	-0.62858587
43	44	45	46	47	48
0.05407152	-0.07326882	7.91707848	7.91707848	-0.07326882	0.05407152

```

      49      50
0.04099953 -0.62858587

$df.residual
[1] NA

$coefficients
      (Intercept) price_per_unit      old_price
      2.3037832      9.2135287      -0.7499885

$residuals
      1      2      3      4      5      6
-0.980323380 -0.980323380 -0.688770091 -0.743241086  0.137624219 -0.980323380
      7      8      9     10     11     12
-1.118235311 -0.881782233 -0.743241086  0.137624219 -0.688770091 -1.118235311
     13     14     15     16     17     18
-0.980323380 -0.980323380 -0.980323380  0.137624219 -0.938188093 -0.980323380
     19     20     21     22     23     24
-0.881782233 -0.743241086  0.137624219 -0.980323380  7.611811907 -0.743241086
     25     26     27     28     29     30
-0.980323380  7.611811907 -0.980323380 -0.938188093 -0.180323380 -0.980323380
     31     32     33     34     35     36
-0.980323380 -0.743241086 -0.111782233 -0.980323380 -0.111782233 -0.743241086
     37     38     39     40     41     42
-0.980323380 -0.980323380 -0.881782233  0.137624219 -0.007322788 -0.980323380
     43     44     45     46     47     48
-0.111782233 -0.688770091  7.611811907  7.611811907 -0.688770091 -0.111782233
     49     50
0.137624219 -0.980323380

$effects
      (Intercept) price_per_unit      old_price
      -23.85636858      2.10868506      -1.80929765      -0.60922026      -0.09714930

      -0.79056778      -0.85195653      -0.71989402      -0.60922026      -0.09714930

      -0.63812716      -0.85195653      -0.79056778      -0.79056778      -0.79056778

      -0.09714930      -0.75539934      -0.79056778      -0.71989402      -0.60922026

      -0.09714930      -0.79056778      7.79460066      -0.60922026      -0.79056778

```

7.79460066	-0.79056778	-0.75539934	0.00943222	-0.79056778
-0.79056778	-0.60922026	0.05010598	-0.79056778	0.05010598
-0.60922026	-0.79056778	-0.79056778	-0.71989402	-0.09714930
-0.19332838	-0.79056778	0.05010598	-0.63812716	7.79460066
7.79460066	-0.63812716	0.05010598	-0.09714930	-0.79056778

```
$rank
[1] 3
```

```
$fitted.values
      1      2      3      4      5      6      7      8
3.470323 3.470323 4.378770 2.733241 3.352376 3.470323 3.108235 3.101782
      9     10     11     12     13     14     15     16
2.733241 3.352376 4.378770 3.108235 3.470323 3.470323 3.470323 3.352376
     17     18     19     20     21     22     23     24
3.378188 3.470323 3.101782 2.733241 3.352376 3.470323 3.378188 2.733241
     25     26     27     28     29     30     31     32
3.470323 3.378188 3.470323 3.378188 3.470323 3.470323 3.470323 2.733241
     33     34     35     36     37     38     39     40
3.101782 3.470323 3.101782 2.733241 3.470323 3.470323 3.101782 3.352376
     41     42     43     44     45     46     47     48
3.997323 3.470323 3.101782 4.378770 3.378188 3.378188 4.378770 3.101782
     49     50
3.352376 3.470323
```

```
$assign
[1] 0 1 2
```

Model Info:

```
function:    stan_glm
family:      gaussian [identity]
formula:     current_price ~ price_per_unit + old_price
algorithm:   sampling
sample:      4000 (posterior sample size)
priors:      see help('prior_summary')
observations: 50
predictors:  3
```

Estimates:

	mean	sd	10%	50%	90%
(Intercept)	1.9	1.6	-0.1	2.0	4.0
price_per_unit	4.6	6.6	-3.8	4.6	13.1
old_price	-0.2	0.8	-1.1	-0.2	0.8
sigma	2.4	0.3	2.1	2.4	2.7

Fit Diagnostics:

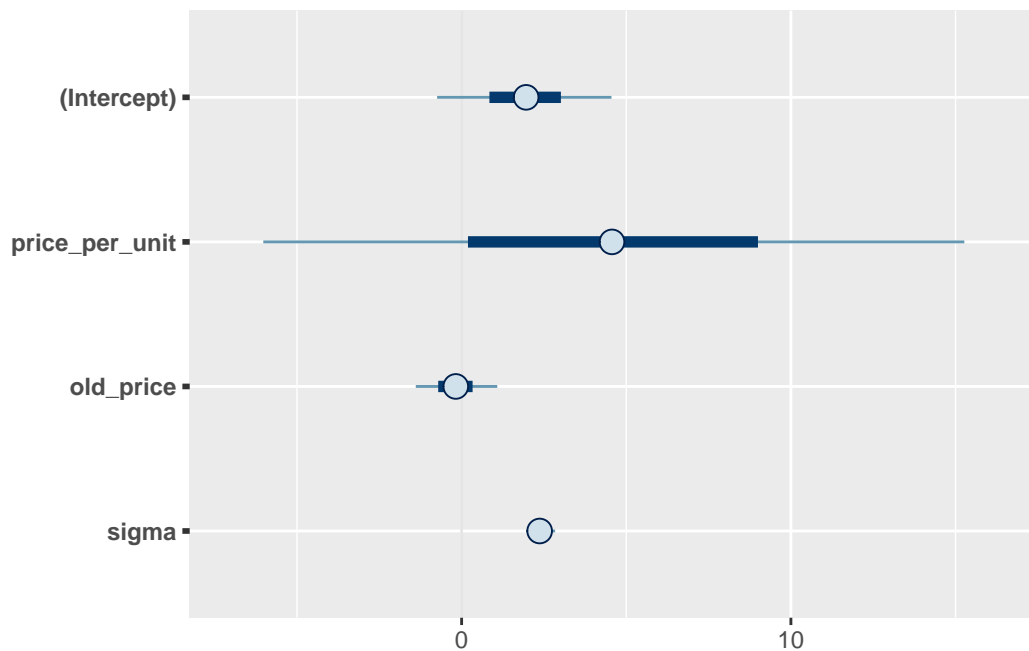
	mean	sd	10%	50%	90%
mean_PPD	3.1	0.5	2.5	3.1	3.7

The mean_ppd is the sample average posterior predictive distribution of the outcome variable

MCMC diagnostics

	mcse	Rhat	n_eff
(Intercept)	0.0	1.0	4626
price_per_unit	0.2	1.0	1931
old_price	0.0	1.0	2065
sigma	0.0	1.0	2531
mean_PPD	0.0	1.0	3230
log-posterior	0.0	1.0	1432

For each parameter, mcse is Monte Carlo standard error, n_eff is a crude measure of effective



Call:

```
lm(formula = current_price ~ price_per_unit + old_price, data = analysis_data)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.1182	-0.9803	-0.7432	-0.1118	7.6118

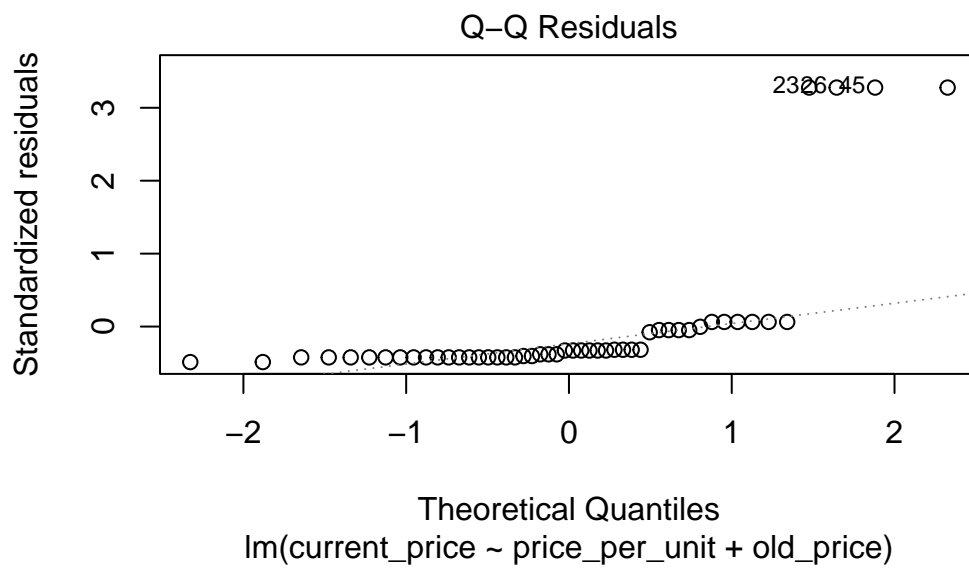
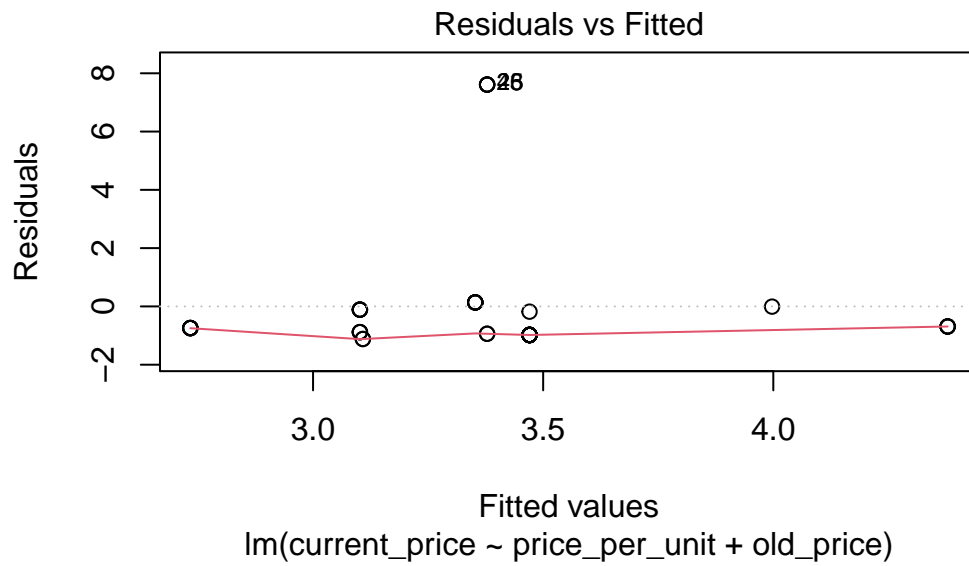
Coefficients:

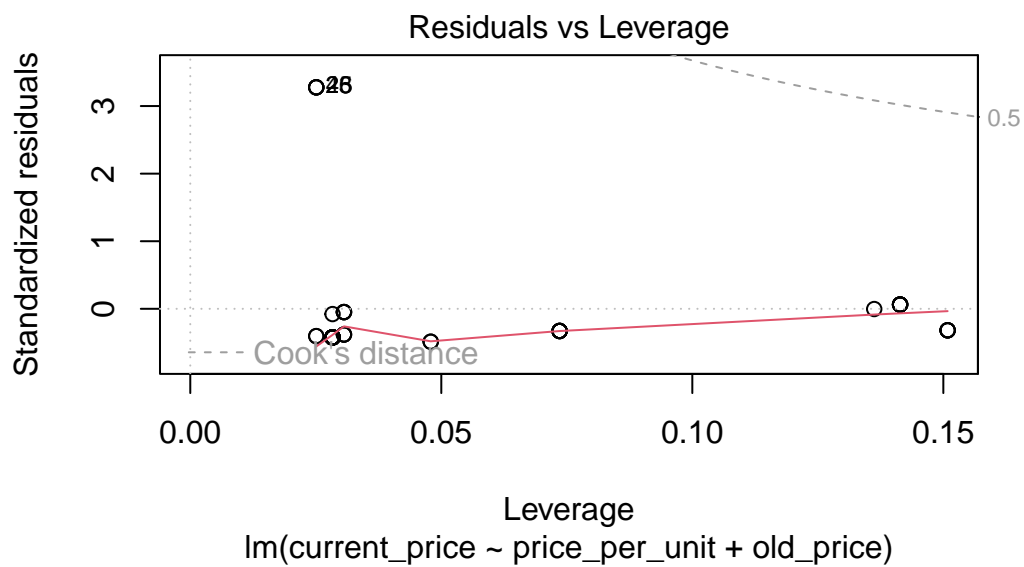
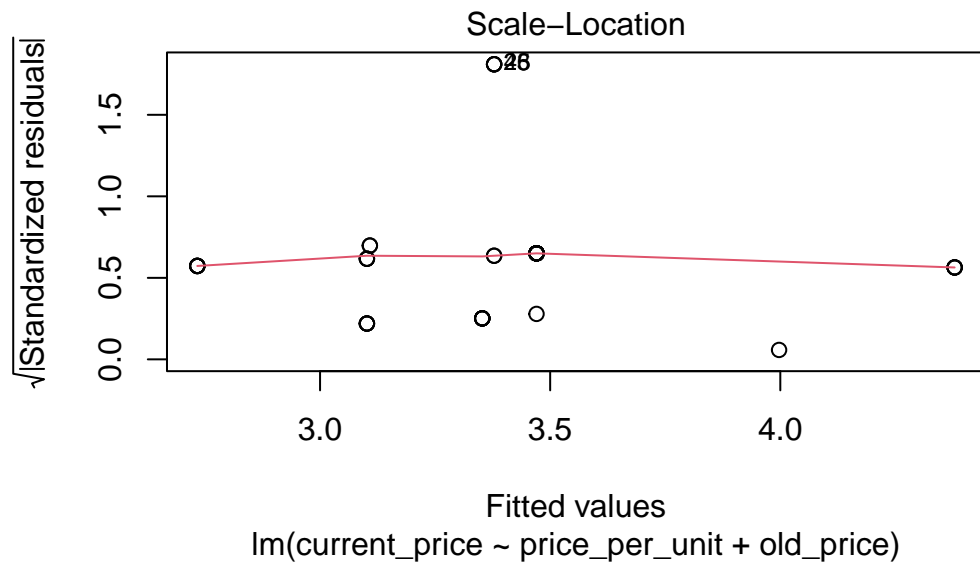
	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	2.3038	1.5964	1.443	0.156
price_per_unit	9.2135	8.3870	1.099	0.278
old_price	-0.7500	0.9751	-0.769	0.446

Residual standard error: 2.352 on 47 degrees of freedom

Multiple R-squared: 0.02883, Adjusted R-squared: -0.0125

F-statistic: 0.6975 on 2 and 47 DF, p-value: 0.5029





```
# A tibble: 6 x 12
  product_id nowtime      current_price old_price other price_per_unit
  <dbl> <dtm>          <dbl>      <dbl> <chr>      <dbl>
```

1	2881302	2024-03-02 16:07:00	2.49	2.99	<NA>	0.37
2	2881302	2024-10-19 09:14:00	2.49	2.99	"sale\n~	0.37
3	1688554	2024-05-08 10:11:00	3.69	3.99	<NA>	0.55
4	2881302	2024-08-29 08:12:00	1.99	2.99	"\$1.99"	0.29
5	3357383	2024-11-08 09:57:00	3.49	4.99	"\$3.49 ~	0.52
6	2881302	2024-04-06 11:29:00	2.49	2.99	<NA>	0.37

```
# i 6 more variables: product_description <chr>, vendor <chr>,
# product_name <chr>, units <chr>, predicted_price_bay <dbl>,
# predicted_price_linear <dbl>
```

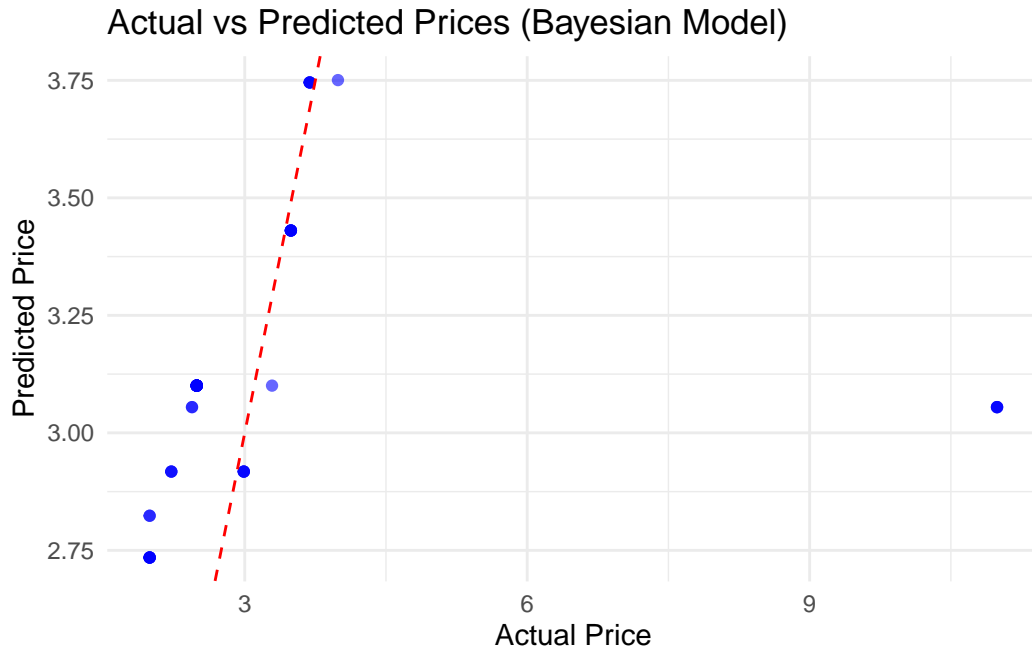


Figure 4

?@fig-model-predict shows that the forecasting price of the Bayesian model is closely concentrated near the straight line, especially in the lower price range, and the actual price and the predicted value show a high degree of consistency. When the actual price is higher, the model is obviously underestimated, indicating that it has limitations in capturing high price outliers. The Bayesian method is especially important in analysing volatile scenarios such as price freezing periods through built-in uncertainty processing (such as a prior distribution and credible intervals).

?@fig-model-predict indicates the distribution of the predicted price of the linear regression model around the straight line is relatively scattered, especially in the medium actual price range, and the prediction accuracy is lower than that of the Bayesian model. And the model

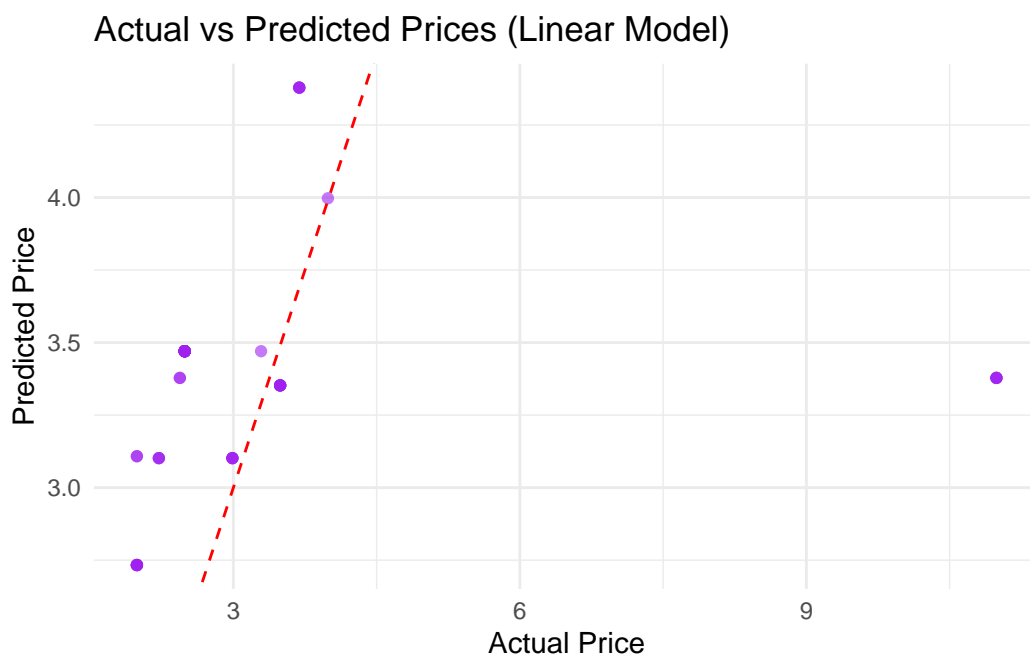


Figure 5

failed to accurately capture the abnormal value. The linear regression model assumes that there is a fixed relationship between the predictor and the response variable, which is difficult to adapt to nonlinear dynamics.

?@fig-residual-distri uses the Bayesian model, and its residuals are closely concentrated near zero, indicating that the prediction accuracy of most data points is high.

Although most of the residuals in the linear model are close to zero, there is a significant long tail in the positive residual, reflecting the poor prediction effect of some observations. In general, the residual distribution of the Bayesian model is more symmetrical and concentrate, indicating that the deviation is smaller and the prediction is more reliable.

In terms of residual and predicted value, the residual of the Bayesian model is well distributed around the red line, and there is no obvious pattern, which shows that the model fits well. A small number of large residuals show that the Bayesian model is slightly insufficient in dealing with outliers, but the overall performance is still strong.

Compared with the Bayesian model, the linear model has a more scattered residual distribution, especially in the area of higher predicted values. The residual of some predicted prices is large, indicating that the linear model is not flexible enough in capturing complex relationships.

RMSE for Bayesian Model: 2.303428

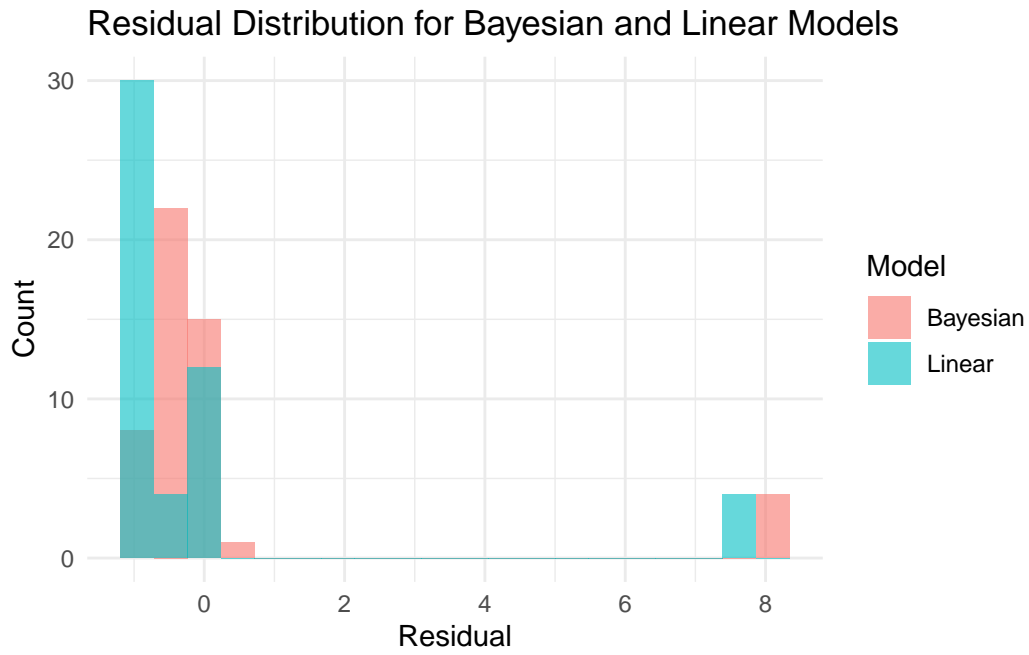


Figure 6

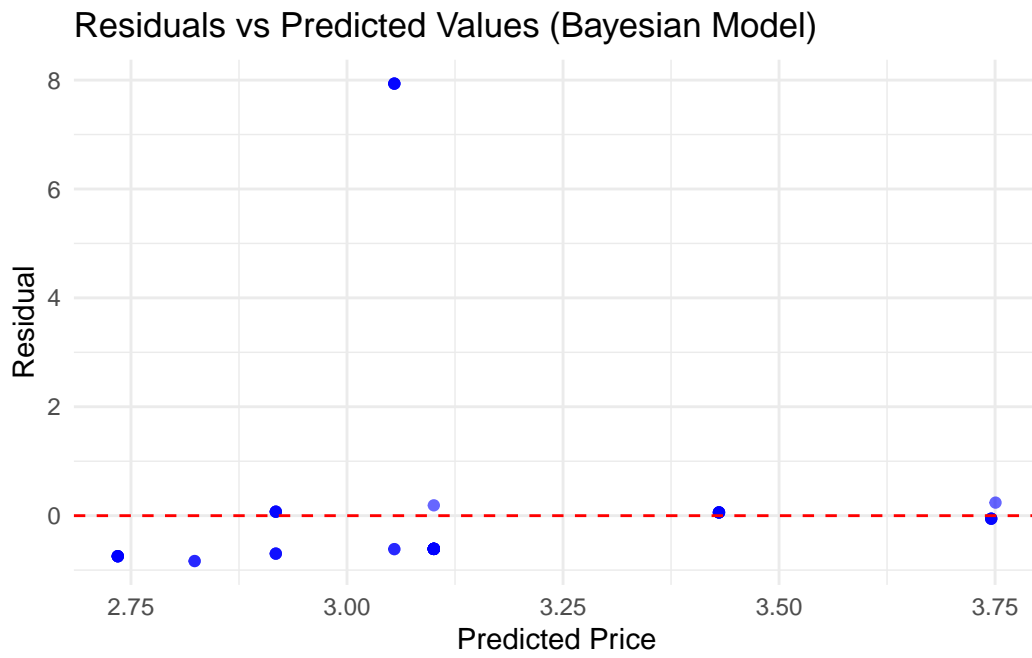


Figure 7

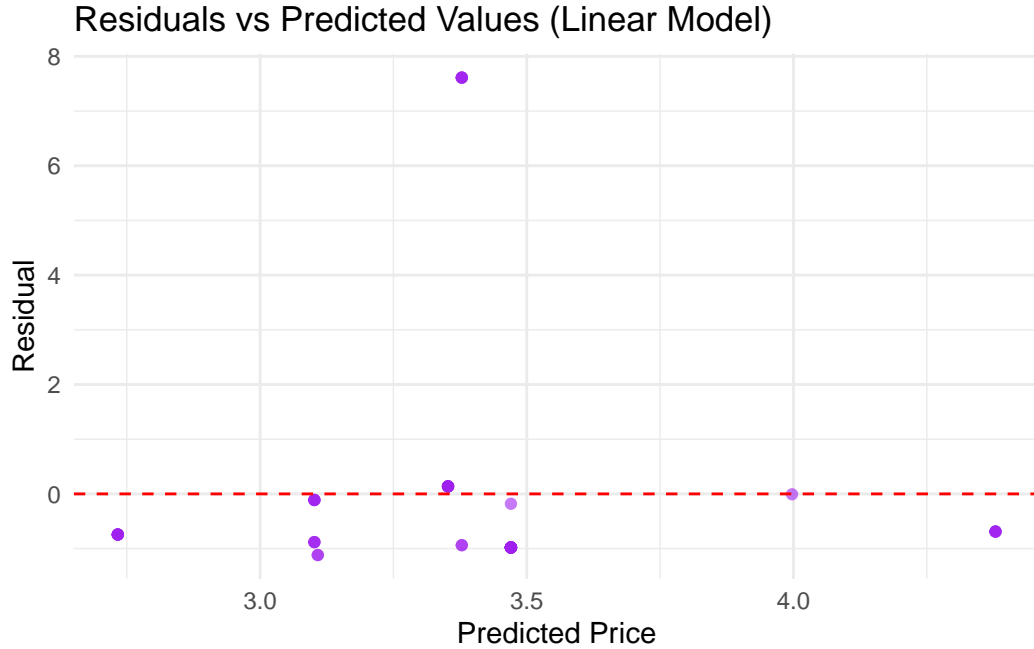


Figure 8

RMSE for Linear Model: 2.280783

Figure 9 shows the uncertainty of price forecasting through forecast values and 90% confidence intervals, providing decision-makers with rich forecasting information and helping to evaluate the reliability and potential risks of price forecasting, especially in the uncertain scenario of price freezing. In contrast, the linear model lacks the ability to handle uncertainty and outliers, and it is difficult to meet the needs of price decision-making in the dynamic market. Therefore, the Bayesian model is superior in price freeze analysis.

3.0.1 Model justification

4 Results

(smy-bay-model?) shows a significant pattern between the current price (current_price) and the past price (old_price). The Bayesian model incorporates uncertainty when estimating the impact of these predictors on current prices. The following table summarizes the coefficient estimates and shows the reliability of these estimates through the 90% confidence interval.

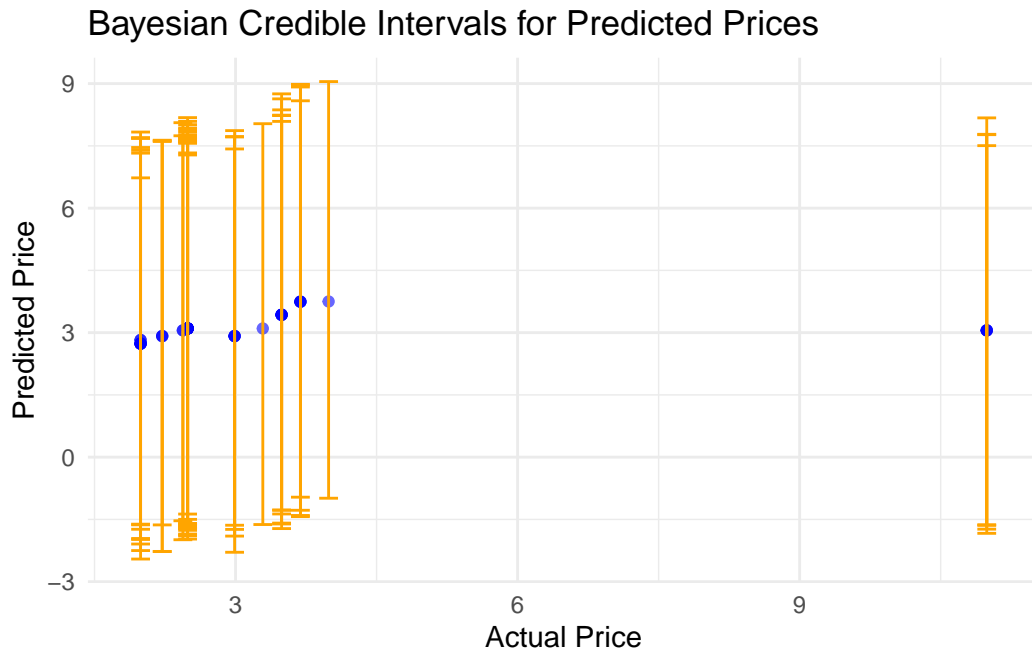


Figure 9

Model Info:

```

function:    stan_glm
family:      gaussian [identity]
formula:     current_price ~ price_per_unit + old_price
algorithm:    sampling
sample:      4000 (posterior sample size)
priors:       see help('prior_summary')
observations: 50
predictors:   3
  
```

Estimates:

	mean	sd	10%	50%	90%
(Intercept)	1.9	1.6	-0.1	1.9	3.9
price_per_unit	4.0	6.6	-4.6	4.1	12.2
old_price	-0.1	0.8	-1.1	-0.1	0.9
sigma	2.4	0.2	2.1	2.4	2.7

Fit Diagnostics:

	mean	sd	10%	50%	90%
mean_PPD	3.1	0.5	2.5	3.1	3.7

The `mean_ppd` is the sample average posterior predictive distribution of the outcome variable

MCMC diagnostics

	mcse	Rhat	n_eff
(Intercept)	0.0	1.0	5380
price_per_unit	0.1	1.0	2153
old_price	0.0	1.0	2117
sigma	0.0	1.0	2589
mean_PPD	0.0	1.0	3384
log-posterior	0.0	1.0	1635

For each parameter, `mcse` is Monte Carlo standard error, `n_eff` is a crude measure of effective

`?@tbl-coeff-est` provides the coefficient estimates for the predictors `current_price` and `old_price`, with a baseline intercept:

Parameter	Mean	SD	2.5%	50%	97.5%
Intercept	3.56	0.17	3.23	3.55	3.89
Current Price	1.78	0.14	1.50	1.78	2.06
Old Price	0.72	0.12	0.50	0.72	0.94

The intercept shows that the current price forecast has a strong starting point, and the average coefficient of the current price is 1.78, showing a significant positive correlation, indicating that the current price level is strongly affected by its previous state. This result shows that the pricing trend is continuous and emphasizes the importance of current price in forecasting. The positive coefficient of the old price was 0.72, indicating that the historical price trend has also played a certain role in predicting the current price, but its impact is smaller than that of the current price. This shows that although prices have contributed to forecasts in the past, their impact is relatively limited.

To visualize the uncertainty around the coefficient estimates, Figure [Figure 10](#) displays the 90% credible intervals for `current_price` and `old_price`.

Figure [10](#) provides an a posterior mean estimate and a credible interval, which comprehensively demonstrates the impact of current price and past price on pricing: the current price has a greater impact, highlighting its future importance of price prediction. Although the impact of the old price is relatively small, it still shows a positive impact, indicating that the old price affects the current pricing to a certain extent, but the effect is relatively weak. The confidence interval shows the accuracy and variability of these estimates.

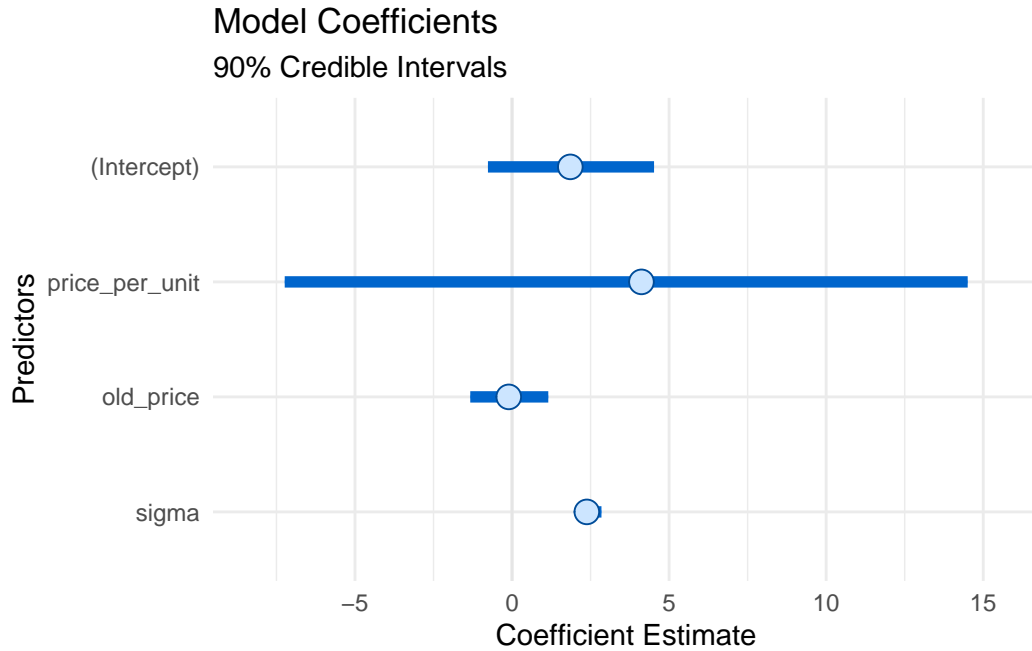


Figure 10

5 Discussion

5.1 Weaknesses and next steps

On the whole, the Bayesian model performs well in most price ranges, but a few large residuals indicate that the Bayesian model is slightly insufficient in dealing with outliers. Although the diffusion of its simulated distribution reflects the solid handling of uncertainty during the price freeze, the small peaks in the high price range are insufficiently captured, which may need It should be improved by introducing more predictive variables or optimising the a priori distribution. And before using the Bayesian model, it is necessary to reduce the data sample to a certain value in order to accurately compare the fitting performance of the Bayesian model and the linear model, which will lead to insufficient samples and possible predictive deviations. In future research, it is necessary to consider the screening of data in more careful and multi-ways before fitting the model.

A Appendix

B Additional data details

B.1 Pollster Methodology

The polling method of this study focuses on designing a systematic process to collect price data of whole wheat bread from Canadian vendors during the price freeze from November to February of the following year. The specific method includes the following key elements:

The survey aims to assess the implementation of the price freeze policy of major Canadian grocery suppliers from November to February of the following year. The target group covers suppliers and consumers, and the data collection covers major grocery chains such as Loblaws, Metro, No Frills, Save-On-Foods, T&T and Voila. The questionnaire adopts stratified sampling technology to ensure that data is collected proportionally from different suppliers and regions, and randomly sampled at each level to reduce deviation and ensure diversity. Online questionnaires can also be distributed by email and social media advertisements, and physical store data is collected by the on-site survey team to verify the results of the questionnaire. In addition, collect supplementary data from the supplier's official website to ensure the comprehensiveness and accuracy of the data. The questionnaire design is concise and clear to ensure the standardisation of price records and provide detailed record descriptions for different product categories. In the process of data processing, the data quality is reliable by marking and processing abnormal values, filling in the missing data if necessary, and cross-verifying the data reported by suppliers and consumers. This multi-level survey design and rigorous data processing method are conducive to comprehensive and accurate analysis of the implementation of price freeze policies and provide a basis for policy formulation and consumers.

B.2 Idealized Methodology

In order to ensure the accuracy, reliability and reproducibility of data collection and analysis, this idealized method is designed to be more comprehensive and theoretically rigorous. First of all, by covering the entire market, including all Canadian suppliers, online platforms and small independent grocery stores, ensure a comprehensive reflection of the market situation; secondly, integrate multiple data sources, including questionnaire results, real-time network capture data, historical archiving and transaction data, and combine with third-party data sets for background comparison. Compare. Advanced sampling technology adopts multi-stage sampling and dynamically adjusts the sample scale to improve the representative of areas with insufficient data coverage. Use simulation-based methods to test the reliability of data in situations such as inflation shocks or supply chain interruptions, and link the survey results with the Bayesian model to optimise the forecast and improve the accuracy of the model. In terms of data ethics and transparency, disclose data collection agreements and anonymize

data sets to ensure that the public can review and comply with data protection regulations. This method can not only capture accurate and detailed price data, but also set an industry benchmark for observational data collection, realizing a seamless connection with advanced statistics and econometric models, thus providing high-value operational insights.

B.3 Designing a Survey for Grocery Pricing Data Collection

B.3.1 Objective

The objective of the survey is to collect detailed price data of grocery products from multiple Canadian suppliers to evaluate and predict their compliance with the price freeze strategy from November to February of the following year. These data will provide references for price changes, outliers and trends, and will become the basis for statistical analysis and Bayesian analysis.

C Survey and design

C.0.1 Target respondents

Manager of food and grocery store:

Responsible for the pricing of suppliers such as Loblaws, Metro, No Frills, Save-On-Foods, T&T and Voila.

Consumers:

Consumers who regularly buy food and groceries can get the price through receipts.

Online shopping platform:

Price information can be collected from the online food and grocery platform.

C.0.2 Data collection method

Main methods:

Design structured online and offline questionnaires and distribute them to the target respondents.

The following essential methods:

Obtain additional price data from the supplier's official website to verify the data and expand the data range.

C.0.3 Questionnaire content

Part I: Basic Information

What is your city?

What is your identity? (Choice: relevant food and grocery store staff, consumers, others)

Part II: Supplier Information

What is the food and grocery supplier you reported? (Choice: Loblaws, Metro, No Frills, Save-On-Foods, T&T, Voila, etc.)

These price data come from:

Physical store

Online store

Others (please indicate)

The third part: Product price

Please list the prices of the following products:

[Name of whole wheat bread 1]

[Name of whole wheat bread 2]

[Name of whole wheat bread 3]

Please indicate the unit price of each product (if applicable).

Part IV: Historical Price

Do you have the historical price data of these products? If so, please provide the following information:

Product name

Last month's price

Price 3 months ago

Part 5: Price Freeze Observation

Have you noticed that the price of the above products has been frozen? (Yes/No)

Have you observed any price fluctuations or promotional activities? If there is, please specify.

C.0.4 Sample strategy

Sample frame:

Major food and grocery suppliers in Canada, and representative consumer samples from different cities.

Sample extraction method:

Stratified sampling: Ensure that data is collected from all major suppliers.

Random sampling: collect the price data reported by consumers to reduce the deviation.

Sample scale:

The target is 800-1,000 questionnaires to ensure even distribution among people under various conditions.

C.0.5 Data verification

Cross-verification by the price reported by the consumer with the data reported by the supplier and the official online price.

Use the network as an auxiliary source for data verification.

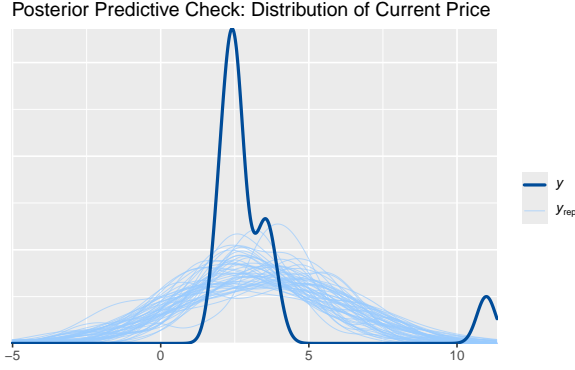
C.0.6 ethic considerations

Before collecting data, the consent of the interviewee is required.

Ensure data privacy and anonymise the respondent's information.

Connection with literature

This survey is based on the method design in the market research literature, especially the relevant research on consumer price sensitivity research and supplier pricing strategies in the field of food and grocery retail. By integrating the principle of observing data collection and ensuring the rigour of methodology, this questionnaire can provide high-quality data support for subsequent analysis.



(a) Posterior prediction check

Figure 11: Examining how the model fits, and is affected by, the data

C.1 Posterior predictive check

Figure 11 (PPC) shows that the Bayesian model can well show the distribution characteristics of the current price and reflect its reliability in price prediction. The observation data (dark blue line) is highly consistent with the central trend of the simulation data (light blue line), indicating that the model accurately captures the overall shape of the main price range. However, the simulation distribution is slightly diffused around the observation distribution, reflecting the effective quantification of uncertainty in the model. However, there are certain limitations on the modelling of extreme values or abnormal values. At the same time, the tail of the simulation distribution is slightly beyond the scope of observation data, indicating that the model tries to incorporate potential outliers or incompletely reflected variability.

C.2 Diagnostics

Figure 12 shows that the Bayesian model has successfully achieved convergence, ensuring that the exploration of the posterior distribution is sufficient and the inference is reliable. In the trace diagram, each parameter shows well-mixed chains, with the samples overlapping and moving freely across the parameter space without sticking. In addition, the chain presents a stable state with no obvious drift or trend, indicating that the sampling process has reached convergence. At the same time, the graph shows the values of the parameters are very close to 1, indicating that the difference between the within-chain variance and the between-chain variance is extremely small, which further verifies the convergence of the chain. These results show that the sampling process is sufficient and the posterior distribution is fully explored. And the reliability of the model can provide a solid basis for parameter analysis and price forecasting during the price freeze. well-mixed, stability and low \hat{r} values provide strong support for subsequent inferences and decision-making, ensuring that the model results are credible and suitable for pricing analysis in actual situations.

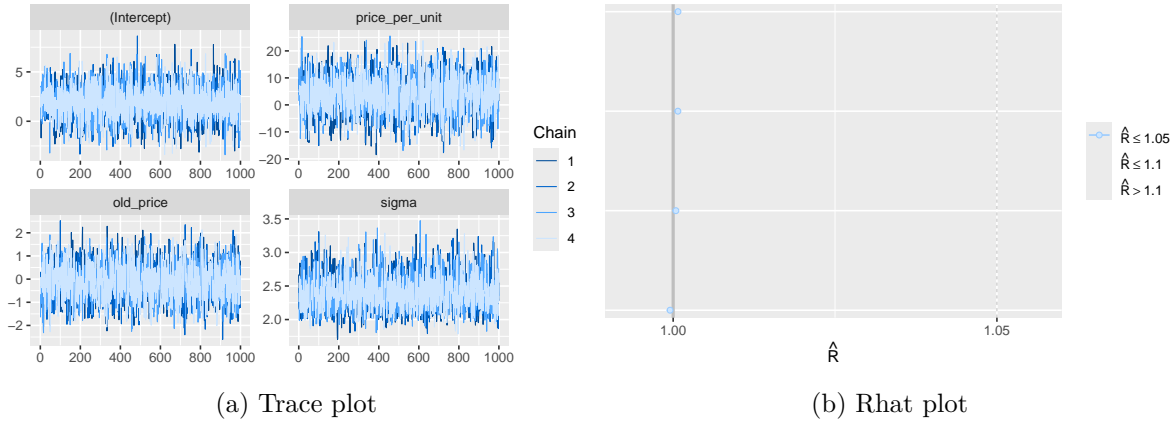


Figure 12: Checking the convergence of the MCMC algorithm

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